

Binary Searching

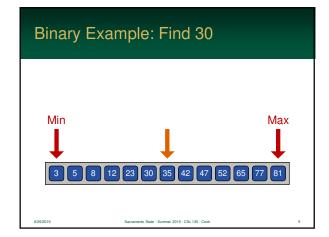
- A binary search is an fast and efficient way to search an
- Algorithm works like the classic "secret number game"
- Requires that the array is sorted before the search

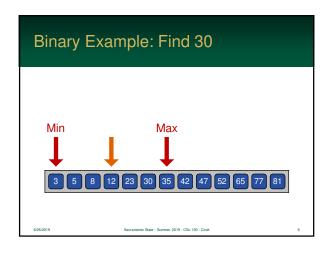


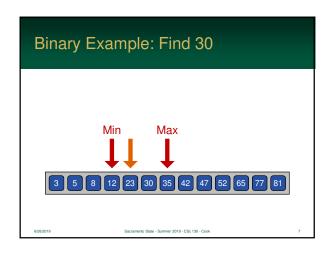


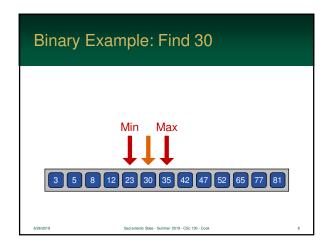
How it Works

- Starts knowing the max & min values
 - in the case of arrays, this is the min and max index
 - in the number game, it is the min and max value
- Algorithm continues
 - it looks at the midpoint between the first and last
 - if the value > target, the max is set to the midpoint
 - if the value < target, the min is set to the midpoint
 - this eliminates half of the numbers each iteration









Benefits

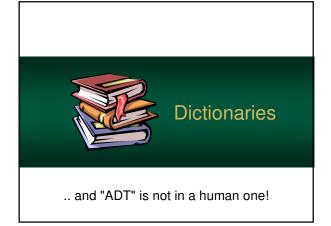
- The binary search is incredibly efficient and <u>absolutely necessary</u> for large arrays
- Any item can be found only log₂(n) searches!
- However, since array must be sorted, sorting algorithms are equally vital

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Maximum # of Searches

Array Size	Sequential Search	Binary Search
10	10	4
100	100	7
1,000	1,000	10
10,000	10,000	14
100,000	100,000	17
1,000,000	1,000,000	20
10,000,000	10,000,000	24
100,000,000	100,000,000	27
1,000,000,000	1,000,000,000	30



Moving Past Arrays....

- A collection is general term for an group of data items
- So, this can include arrays, linked lists, stacks, queues, and much more
- So far, we have just used arrays – which are indexed by an integer

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Moving Past Arrays....

- Are there are other ways to index data?
- Yes.
 - any object can be used as an index
 - e.g. strings, integers, pictures, etc...

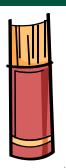


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Dictionaries

- Collections of objects indexed by other objects are called dictionaries
- They have a few alternative names...
 - keyed tables
 - symbol tables
 - maps

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Dictionary Terminology

- The objects that are used for indices are called keys
- The objects that are accessed using the key are called values



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Databases vs. Dictionaries

- Dictionaries...
 - · have a single key
 - · that key is the only way to access data
 - key returns a single value
- Databases...
 - may have multiple keys
 - information can be accessed using other fields (e.g. SSN, name, age, etc...)
- may return multiple objects e.g. all the students taking CSc 130

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Implementing Dictionaries

- There are numerous approaches to implementing dictionaries
- Typically, it uses a keyedvalue structure
 - a class stores a key object and data object
 - this can be stored in any data structure we have covered

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Implementing Dictionaries

- Using a linked list
 - adding takes O(1)
 - access is O(n)
- Unsorted array
 - add is O(n) have to resize
 - access is O(n)
- Sorted array
 - add is O(n) have to resize
 - access is O(log n)

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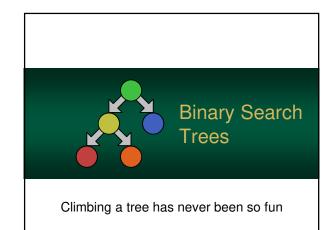


This Ain't So Good

- So, adding in to an array is O(n)!
- Arrays seem like a poor approach
- Is there a better way to store dictionary data? Keeping adding close to O(1)?
- ... and keep access at O(log n)
- Perhaps, we will learn that soon....

....

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Binary Search Trees

- Binary Search Tree, or BST for short, is a special type of binary tree that sorts nodes by value
- Basically.
 - all the nodes on the <u>left</u> branch are <u>less than</u> the current node
 - all the nodes on the <u>right</u> branch are greater than the current node



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Searching the Tree

- Since the tree divides the problem progressively by two, the time complexity is only O(log n)
- Which gives that all the benefits of a sorted array
- Worst case is O(n) if the tree is a list-like chain



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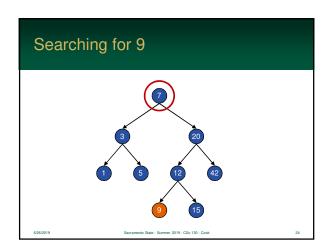
Search logic (looking for S)

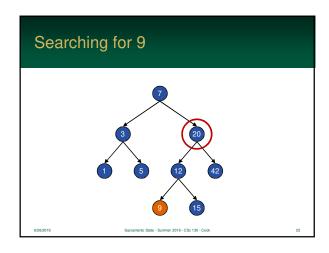
- If S is equal to the current node, you found it
- If S is smaller than the current node, take the left branch
- If S is bigger than the current node, take the right branch
- If there are no branches, S was not found

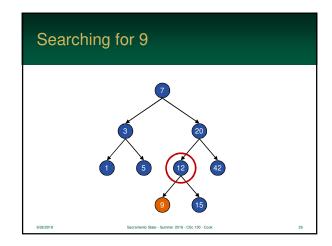


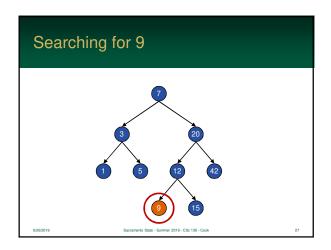
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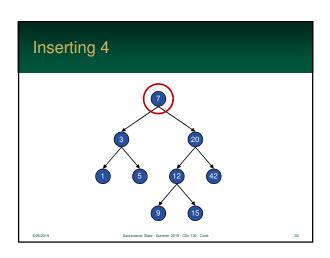


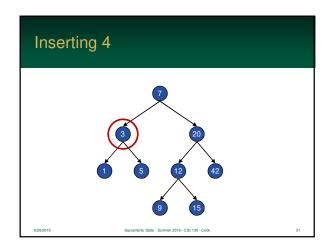
When data is inserted in a Binary Search Tree traverses down the tree until it finds the correct location it then add itself there and restructures the tree hence, the tree remains sorted as new data is added it requires only O(log n) When data is inserted in an Array it must be expanded when new elements are added ...and compacted when elements are removed these requires O(n)

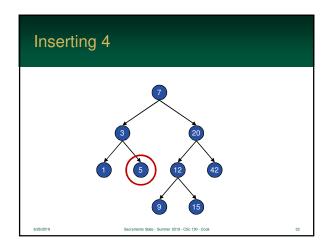
Inserting into the Tree

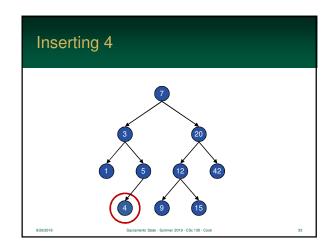
- Inserting is handled exactly like a search
- The only difference is that if the item is not found, the node is added
- If the item is not found,
 - we are already at the max-depth of the tree
 - we are at the node that needs to be changed
 - so, add a left or right node (based on value)
 - · ... wow, this is easy!

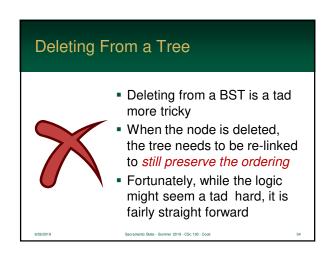
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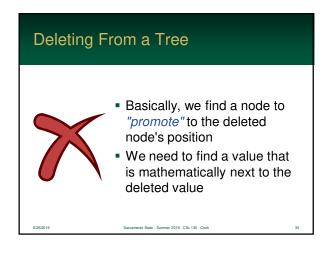




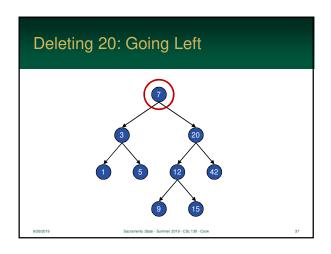


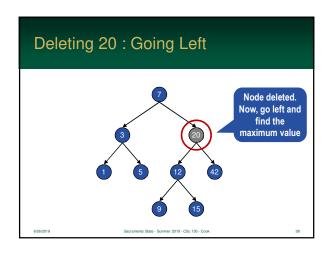


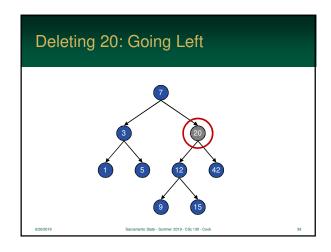


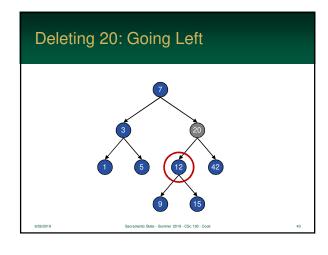


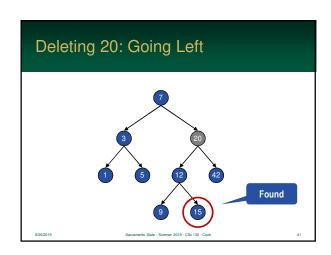


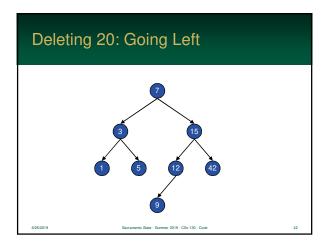


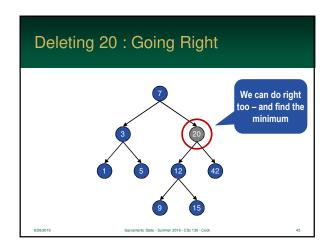


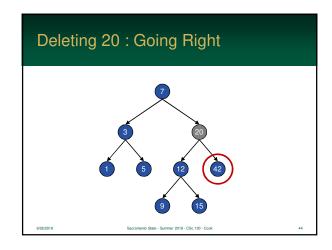


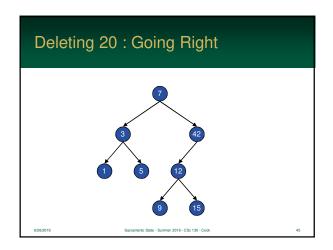












Internal nodes don't really change – but have a profound affect on the rest of the tree There are cases where the tree is unbalanced – one particular path contains all the data In this case, the time complexity slowly deteriorates to O(n)

Sort in a Binary Search Tree? Unfortunately, while this might seem like a good idea, this is not a great solution Binary Search Trees can deteriorate into linked lists So... O(log n) search can quickly deteriorate to O(n) ...and O(n log n) sort can deteriorate to O(n²)

