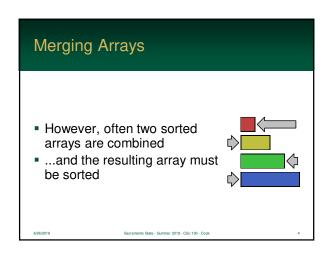


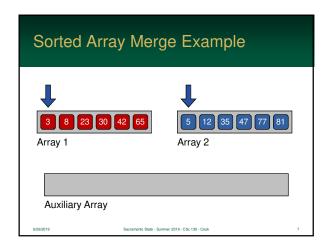
It is a common task in Computer Science to combine two different arrays into one If both arrays are unsorted... the task is fairly simple O(n) just add one onto the end of the other

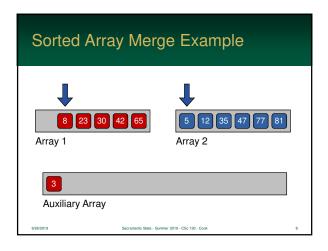


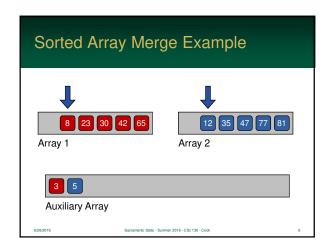
The algorithm for merging two sorted arrays is very simple The resulting time complexity is O(n) However, it requires auxiliary storage of O(n)

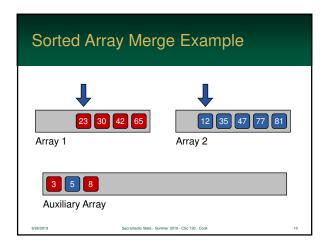
Merging Arrays

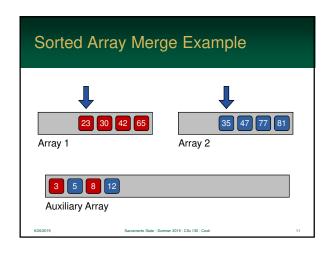
Keep two counters – one for each array Loop while both arrays have data take the smaller element and put it in the auxiliary array increment the array's counter (which just lost an element) After the loop one array will still have elements append them to the auxiliary array

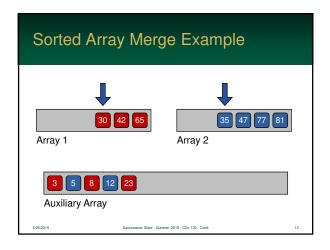


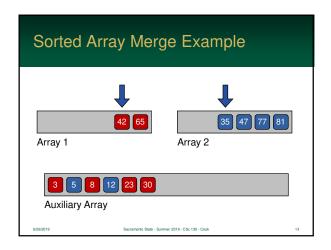


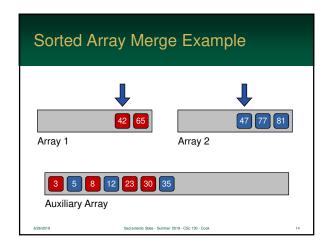


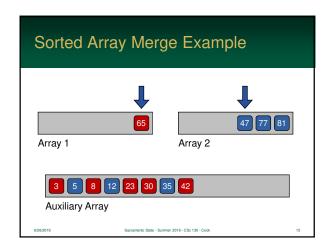


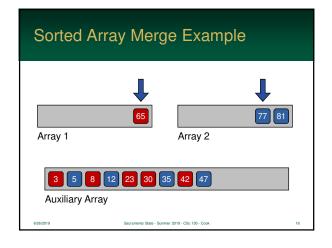


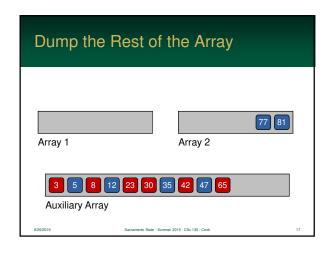


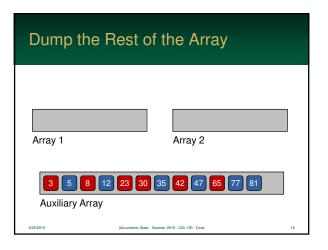


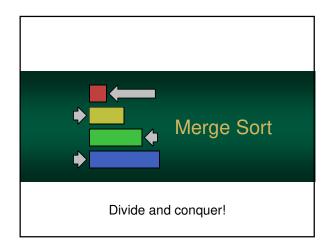


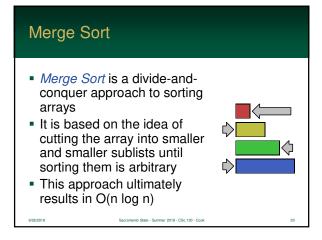












Merge Sort

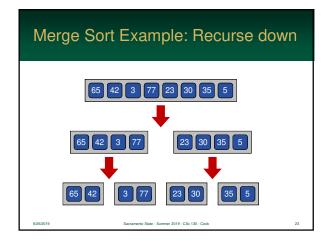
- Because Merge-Sort defines a dividing the list into a list into smaller instances of itself, it naturally is solved using recursion
- Each recursive step cuts the lists into 2 until the list is either 1 element – which is, well, obviously sorted

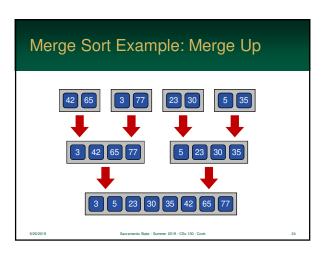
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Merge Sort

- As the recursion bubbles up, each sub list is merged using the algorithm we just discussed
- Since an auxiliary array is required for the merge process, Merge-Sort, while fast, has O(n) auxiliary storage requirements

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Merge Sort Summary Merge Sort Time Average O(n log n) Time Best O(n log n) Time Worst O(n log n) Auxiliary space O(n) Stable Yes - Equal element order preserved Online? Yes - New data → new sublist



Quick Sort

- Quick-Sort is a divide-andconquer algorithm that rotates values around a pivot
- Even faster than both Merge Sort and Heap Sort
- ... but does have its weaknesses



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How it Works

- Like Merge-Sort, the array is broken down into smaller and smaller sub-lists
- However, before recursion
 - an value p is chosen in the sub-list as the pivot value
 - smaller items are moved before it
 - · larger items are moved after it

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Choosing a Pivot

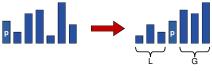
- The pivot can be <u>any</u> element in the sub-list
 we just need one real value to compare
- This value is used to partition the values
- Different versions use different pivots
 - · first item in the sub-list
 - · end item in the sub-list
 - the midpoint of the sub-list
 - · random value in the sub-list

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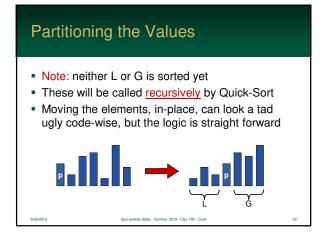
Partitioning the Values

- After the pivot is selected, all elements are moved
- Two loops move through the elements swapping elements less than/greater than the pivot



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Partitioning the Values The result is... • sub-list L that contains items less than P and • sub-list G that contains items greater than P • The sub-lists are stored in the original data array



Partition Algorithm

- The algorithm maintains two pointers
 - first moves left to right and keeps track of the values that are too big
 - second moves right to left and keeps track of the values that are too little
- Each moves independently

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Partition Algorithm

- First move the Too Big pointer until a value is found that is bigger than the pivot
- Then move the Too Little pointer until a value is found that is smaller than Pivot
- Then, these values are swapped
- When the two pointers collide, we are done

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Example Partition

- In this example, we pivot at the <u>start</u> of the array
- Any value can be used...
 - but it will have to be swapped to the start before the algorithm runs
 - · this "saves" the pivot for later



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```
while (tooBig < tooSmall)
{
   while (array[tooBig] <= array[pivot])
   {
      tooSig++;
   }
   while (array[tooSmall] > array[pivot])
   {
      tooSmall---;
   }
   if (tooBig < tooSmall)
   {
      //swap array[tooBig] and array[tooSmall]
   }
   //swap array[tooSmall] and array[pivot]
   //Recurse QuickSort on both L and G</pre>
```

