

Introduction to Trees

- In computer science, a tree is an abstract model of a hierarchical structure
- A tree consists of nodes with a parent-child relationship to zero or more nodes



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Some Applications

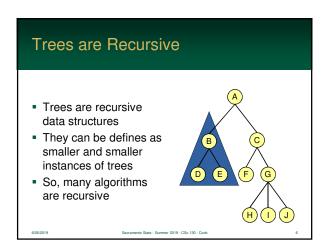
- Organizational charts
- Class hierarchy
- Disk directory and subdirectories
- Structure of a program



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Linked Lists vs. Trees

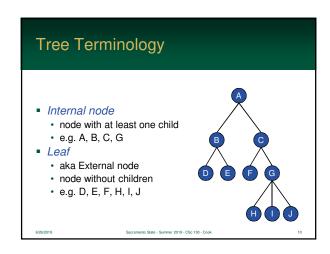
- Linked Lists
 - linear accessing all elements is O(n)
 - nodes can only have one predecessor and/or one successor node
- Trees
 - · nonlinear and hierarchical
 - nodes can have multiple successors but only one predecessor

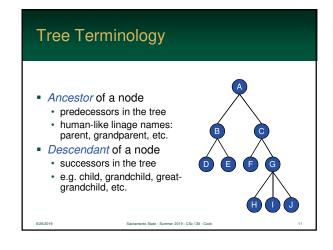
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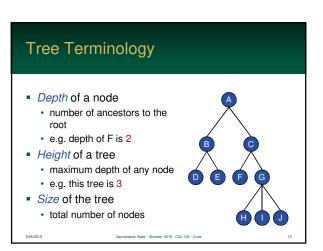
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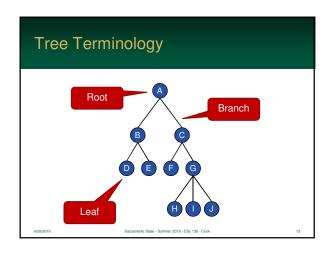
■ Node • just like in linked lists, the units of linked data are called nodes • nodes usually contain data ■ Root • starting point of the tree • no nodes link to it • e.g. A

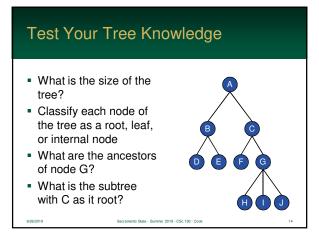
Branch links between tree nodes often unidirectional Branching-factor the max number branches any node can have it can be anything from 2 to infinity

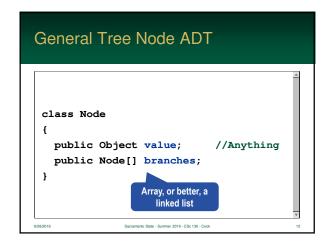


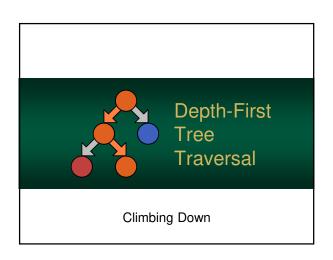








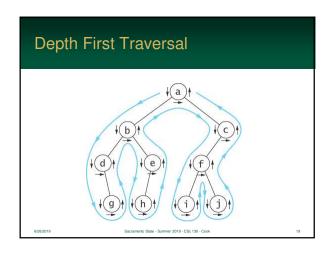


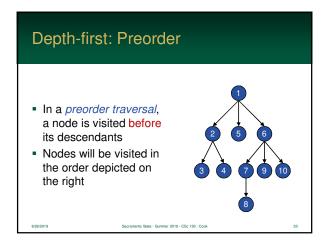


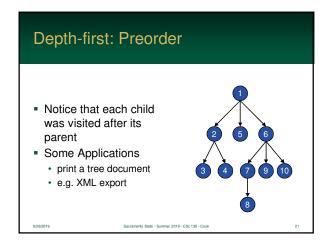
A tree traversal visits the nodes of a tree in a systematic manner Given that trees can be defined into smaller and smaller subtrees, recursion is an eloquent solution When a node is "visited", it contents are analyzed This can before or after its children are visited

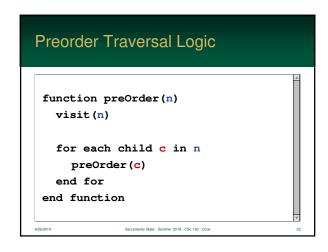
In depth-first transversal, the algorithm travels down the tree So, the algorithm looks at a child and it looks at its children This approach lends itself to recursion There are several approaches of when a node is "visited"

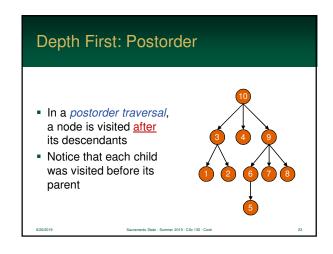
Depth-First Transversal

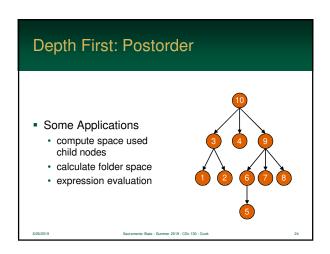




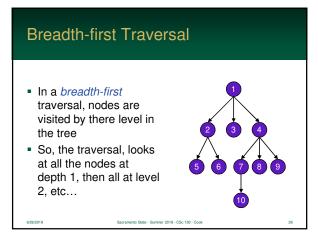


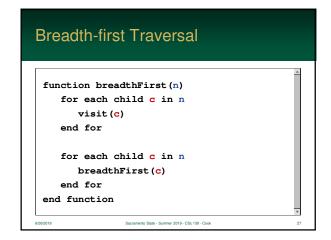


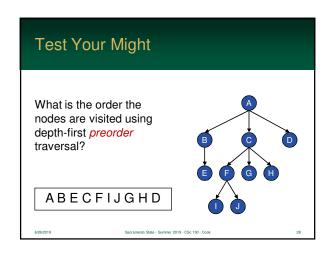


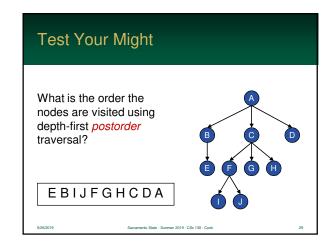


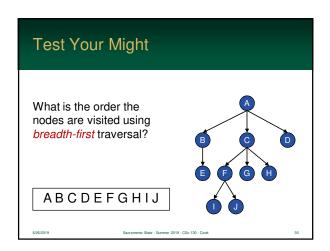
function postOrder(n) for each child c in n postOrder(c) end for visit(n) end function

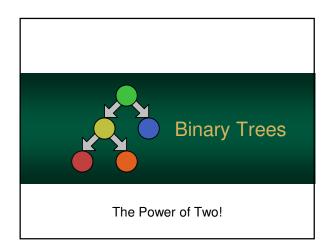


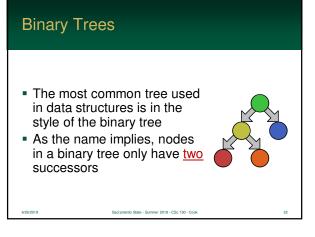










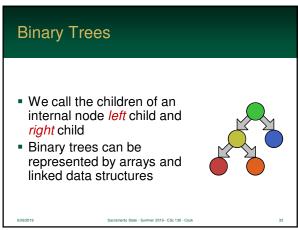


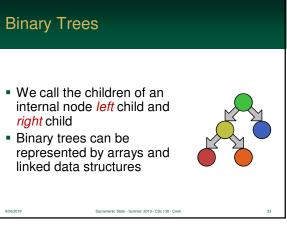
Binary Trees

structures

Applications:

· searching sorting





Boolean Decision Tree Binary tree can be used for decision branching • internal nodes: questions with yes/no answer leaves: decisions Slytherin Gryffindorr Ravenclaw

```
Binary Tree Node
 class Node
   public Object value; //Can be anything
   public Node left;
```

Branches are much simpler

• Binary Trees are extremely useful in data

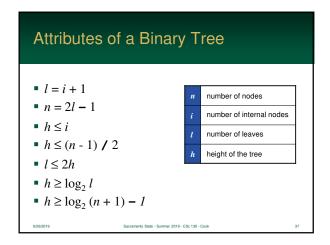
and is ideal for binary operations

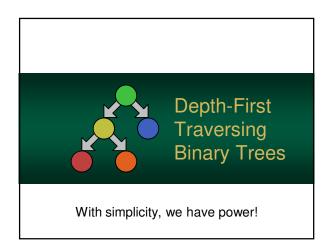
· storing arithmetic expressions

decision processes

public Node right;

The two branches allow for efficient branching







- Because of the simplicity of binary trees, we have a very useful structure for tree traversal
- We can only traverse left and right
- This gives three possibilities for a depth first search

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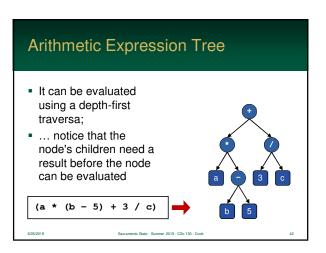
Postorder Depth-first Traversal

- In an postorder traversal a node is evaluated <u>after</u> its left branch and <u>after</u> its right branch
- In other words: recurse left, recurse right, then do something

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Arithmetic Expression Tree Expressions can be represented with a tree How? internal nodes: operators leaves: operand (a * (b - 5) + 3 / c) b 5



Postorder: Evaluate Expressions

- A postorder traversal can be used to evaluate the tree
- Each recursive call (left, right) returns a value – the result of its calculation
- The node that applies the operator to the two returned values

....

```
function evaluate (Node n)
  if n is a leaf
    return n.value
  else
    x ← evaluate(n.left)
    y ← evaluate(n.right)
    ◊ ← operator stored at n
    return x ◊ y
  end if
end function
```

Inorder Depth-first Traversal

- In an inorder traversal a node is evaluated after its left branch and before its right branch
- In other words: recurse left, do something, then recurse right



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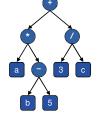
Some Inorder Applications Draw a binary tree Heap sorting Binary tree searching – O(log n) when sorted

Depth First: Inorder

function inOrder(n)
 inorder(n.left)
 visit(n)
 inorder(n.right)
end function

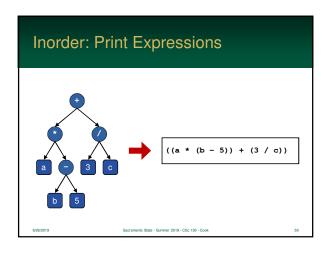
Inorder: Print Expressions

- Inorder can be used to easily print an expression stored in a tree
- Print....
 - "(" before traversing left
 - · the node's operator
 - ")" after traversing right



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function print (Node n) if n is a leaf write n.value else write "(" print(n.left) write n.operator print(n.right) write ")" end if end function



When a preorder depth-first traversal is performed, the node is evaluated before the right or left child This is useful for copying a tree, but not much more