



Hashing

- Array elements can be accessed in O(1)
- Why?
 - the memory address of any element can be calculated mathematically
 - however, this doesn't work for dictionary keys

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Hashing

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Hashing

- What if we come up with a "magic function"?
- So....
 - given a key specific key the function would compute the exact location the element is stored
 - this would given dictionaries O(1) access

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Hash Mathematics

- This function is called a *hash function*
- It takes a key object as an argument and returns a numeric value
- We use this value to store data into a parent array
- Since the value is unique...
 - access is O(1)
 - at least ideally that is what we want....

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- Use hash function to map keys into positions in a hash table
- With element e has key k and h is hash function
 - then e is stored in position h(k) of table
 - To search for e, compute h(k) to locate position
 - If no element, dictionary does not contain e

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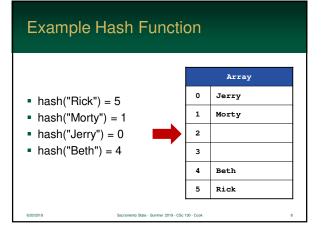
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Using the Function

- Put key/value pairs into the table
- Key is used to find the index
- Value holds the information about the object

Index	Key	Data
0	cat	cat info
1		
2	chicken	chicken info
3	dog	dog info
4		
5		

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But, There are Problems

- Simple hash functions
 - · work for implementing dictionaries
 - but most applications have key ranges that are too large for 1-1 mapping between hashes and keys
- Example:
 - key range from 0 to 65,535
 - collection will have no more than 100 items at any given time
 - impractical to use a hash table with 65,536 slots!

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Finding the Hash Function

- There is no such magic function
 - only in rare cases, with a limited key range, a perfect function can exist
 - however, for real World cases, there is no function possible
- So, we can take a different approach
 - · don't use the hash value as a finishing point
 - use it as a location to start looking

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Example Hash Function

- hash("Isaac") = 5
- hash("Mercer") = 1
- hash("Bortus") = 0
- hash("Yaphet") = 4
- hash("Grayson") = 1



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Collisions

- When two keys hash to the same array location, this is called a collision
- What do we do?
 - normally collisions are treated as "first come, first serve"
 - the first key that hashes to the location gets it
 - so, we need to decide what do with the second item that hash to the same location
 - there are <u>two</u> solutions

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Collision Solution: Closed Hashing

- With closed hashing, we use the existing array and search for a empty position
- Use the hash value as start position – we start searching here



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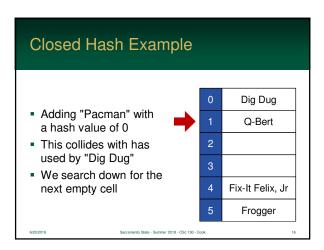
Collision Solution: Closed Hashing

- If the array element is a occupied...
 - search down the array and look for an empty array element
 - the search must also wrap-around to the top
 - and be aware if the search cycles through the entire array – we ran out of space



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Closed Hash Example O Dig Dug Adding "Pacman" with a hash value of 0 This collides with has used by "Dig Dug" We search down for the next empty cell This collides with has used by "Dig Dug" Fix-It Felix, Jr Frogger



Closed Hash Example Adding "Pacman" with a hash value of 0 This collides with has used by "Dig Dug" We search down for the next empty cell Fix-It Felix, Jr Frogger

Closed Hashing Clustering One problem with the closed hashing is the tendency to form clusters A cluster is a group of continuous used cells – with no open slots What happens? the bigger a cluster gets, the more likely it is that new keys will hash into it it then grows larger and larger clusters will eventually degrade the hash to O(n)

Efficiency of Closed Hashing

- Hash tables are surprisingly efficient
- Although collisions cause searching, tables, items can found near O(1)
- Even if the table is nearly full (leading to long searches), efficiency is still quite high



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Closed Hashing Pitfalls



- Closed hashing is not the best solution
- It requires a static array
 - the array cannot be increased at runtime (or the hash fails)
 - as a result, the array can fill up
- Clustering causes O(n) degradation

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Closed Hashing Pitfalls



- You cannot delete items
 - it will create empty slots in clusters!
 - this can prevent an item, added in a cluster, from being found below the gap
 - there are work-rounds, but it gets convoluted

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Closed Delete Problem

- "Dig Dug" and "Pacman" have the same hash value of 0
- When "Pacman" was added, "Dig Dug" caused "Pacman to be stored at 2

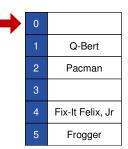
0 Dig Dug
1 Q-Bert
2 Pacman
3
4 Fix-It Felix, Jr
5 Frogger

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Closed Delete Problem

- If "Dig Dug" is deleted, the array element is empty
- If there is a search for "Pacman", it will hash to 0 and it won't be found



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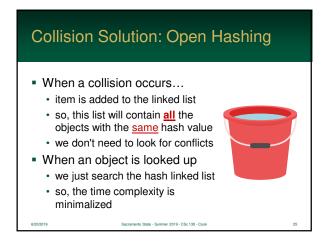
Collision Solution: Open Hashing

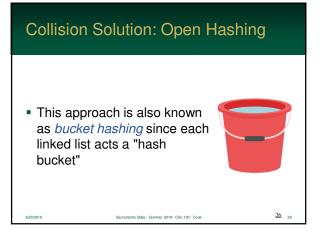
- With open hashing, we don't store individual objects in each array cell
- Instead, each array element is a linked list

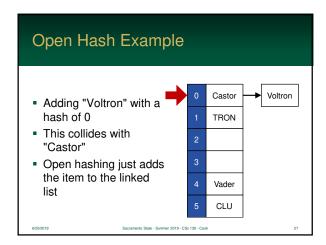


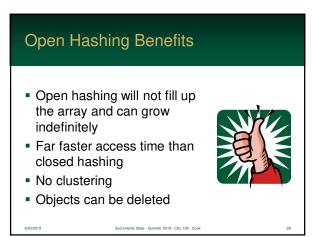
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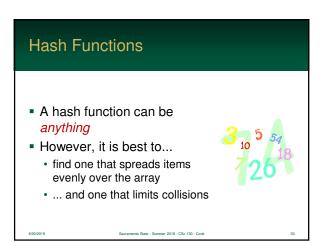












Random Hashing

- Most hashing algorithms use a pseudorandom number generator
- This essentially scatters the items "randomly" throughout the hash table
- ... but there is no real "random" numbers in computers – only chaotic series

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Popular Algorithm: Division

- Uses the formula: $h(k) = k \mod N$
 - *k* is a raw key value produced by some internal function
 - for all purpose, we don't care "how" this was produced
 - N is the size of the array
- Selecting N
 - table size N is usually chosen as a prime number
 - it prevents patterns which can cause collisions

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Popular Algorithm: MAD

- Based on multiply, add, and divide (MAD)
- Uses the formula: $h(k) = (a * k + b) \mod N$
 - a and b are both constants
 - eliminates patterns provided $a \mod N \neq 0$
 - this is the same formula used to create (pseudo) random number generators

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