

We have $y = Cx^2$ is a 1-parameter family of solutions for the differential equation $y'x - 2y = 0$. Which of the following is a solution for the initial value problem consisting of the differential equation $y'x - 2y = 0$ and initial condition $y(2) = 12$.

- A. $y = 12x^2$
- B. $y = 3x^2$
- C. $y = Cx^2$
- D. $y = 2x^2$

Solution:

SOLUTION:

The correct answer is B.

Correct Answers:

- B

2. (1 point) Consider the initial value problem

$$2ty' = 4y, \quad y(-2) = 4.$$

Find the value of the constant C and the exponent r so that $y = Ct^r$ is the solution of this initial value problem.

$y = \underline{\hspace{2cm}}$ help (formulas)

Solution: The answer is $y = 1t^2$.

Correct Answers:

- $1t^2$

3. (1 point) Suppose $y' = f(x, y) = \frac{xy}{\cos(x)}$.

(1) $\frac{\partial f}{\partial y} = \underline{\hspace{2cm}}$ help (formulas)

(2) Since the function $f(x, y)$ is

- Choose
- continuous
- not continuous

at the point $(0, 0)$, the partial derivative $\frac{\partial f}{\partial y}$

- Choose
- exists
- does not exist

and is

- Choose
- continuous
- not continuous

at and near the point $(0, 0)$, the solution to $y' = f(x, y)$

- Choose
- exists and is unique
- does not exist

near $y(0) = 0$

Correct Answers:

- $x \cos(x) / (\cos(x))^2$
- continuous
- exists
- continuous
- exists and is unique

4. (1 point) For the differential equations $\frac{dy}{dx} = \sqrt{y^2 - 16}$ does the existence/uniqueness theorem guarantee that there is a solution to this equation through the point

? 1. $(-1, 4)$?

? 2. $(-4, 19)$?

? 3. $(1, 25)$?

? 4. $(3, -4)$?

Note: To answer this question, compute the partial derivative of $f(x, y) = \sqrt{y^2 - 16}$ with respect to y and check if $f(x, y)$ and $\frac{\partial f}{\partial y}$ exists at the given points. If they do, then the conditions of the theorem are satisfied at the given points.

Correct Answers:

- FALSE
- TRUE
- TRUE
- FALSE

5. (1 point)

Enter a value for π

Correct Answers:

- 3.14159