

Please show and explain your work where necessary. Good luck!!

1. (5 points) For each of the following,
Circle all of the following expression which are differential equations.

(i) $g'(x) + g(x) = 0$

(vi) $y^2x = x^2$

(ii) $\left(\frac{d}{dt}\right)^5 f(t) + \frac{d}{dt}f(t) + f(t) = 0$

(vii) $\csc(y'') + \sin(x) - y = 0$

(iii) $\sin(x)\frac{d^2f}{dx^2} + \frac{df}{dx} + e^x = \frac{d^3f}{dx^3}$

(viii) $x^2\frac{\partial^2y}{\partial t^2} + y^2\frac{\partial x}{\partial s} = s + t$

(iv) $y''' + y' + x$

(ix) $ey'' + e^x = 3y$

(v) $f'(x) = f(x)$

(x) $x\frac{\partial^2y}{\partial t^2} = y\frac{\partial x}{\partial s}$

2. (3 points) For the following equations, provide the *dependent variable*.

a. (1 pt) $f'(x) - f(x) = 0$

b. (1 pt) $\frac{d^2g}{dt^2} - e^tg(t) = 3$

c. (1 pt) $\sin(x)y' + y = 0$

3. (2 points) Consider the function $y = x^3$.

a. (1 pt) Compute y' and y'' .

b. (1 pt) Does y satisfy the differential equation $x^2y'' - 5y = 0$? Justify your answer.