

course: [CSC 135-01 - Computing Theory and Programming Languages](#)

instructor: [Ted Krovetz](#)

related notes: [2022-05-10](#)

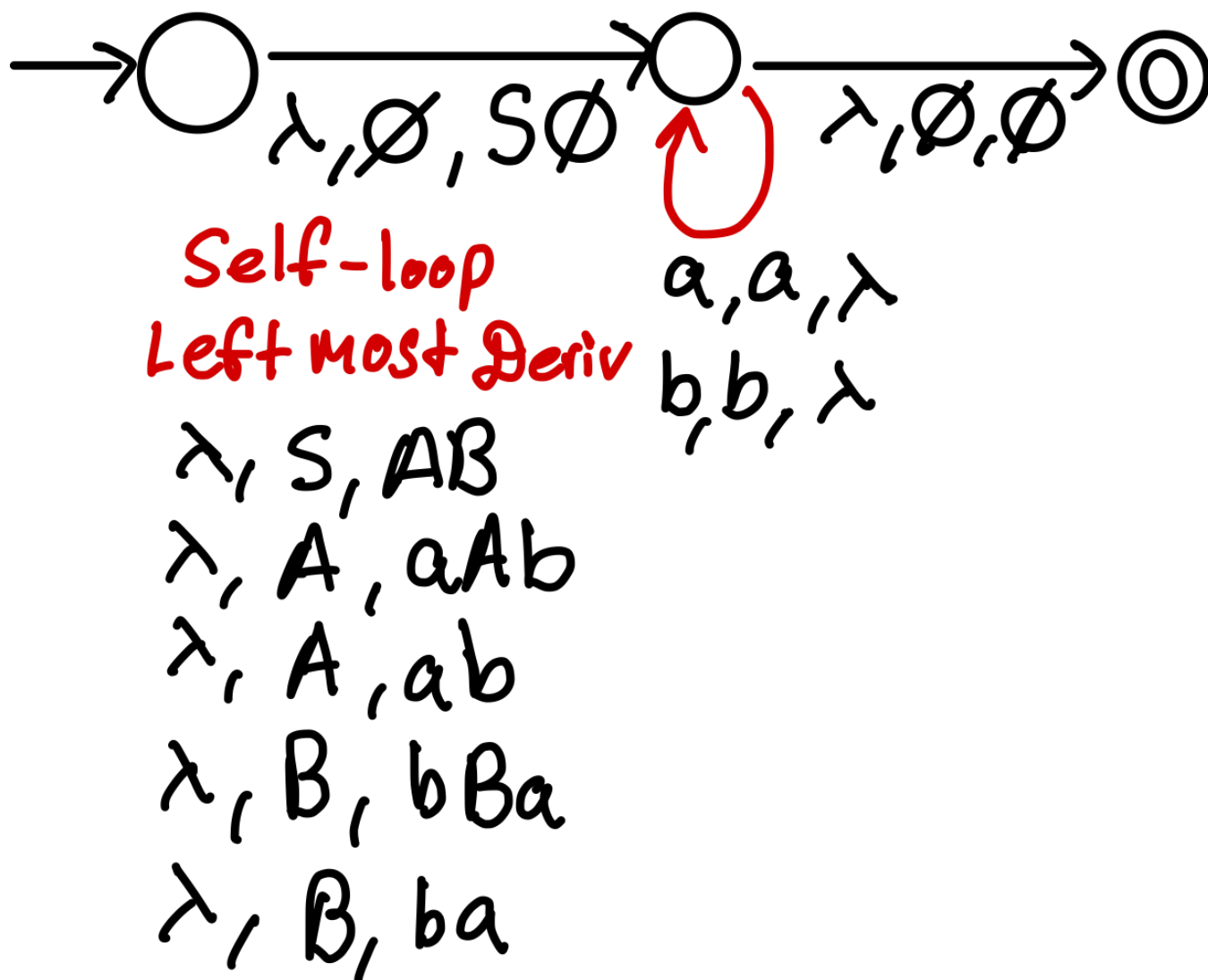
Review

W19.2 | Tuesday, May 10, 2022 | 09:02 AM

Context Free Grammar (CFG)

Info

$$\begin{aligned} S &\rightarrow AB \\ A &\rightarrow aAB \mid ab \\ B &\rightarrow bBa \mid ba \end{aligned}$$



CFG to Pushdown Automata

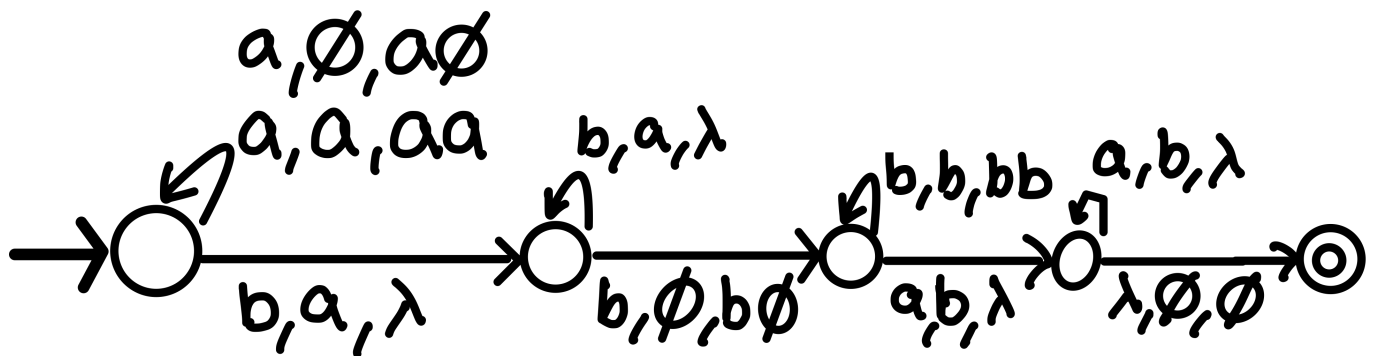
Info

$$\{a^i b^j a^k \mid i + k = j\}$$

If you had a stack how would you fit a string in language

aaabbb|bbaa

1. Consume and Push a 's
2. Consume b 's and Pop a 's
3. Consume and Push b 's
4. Consume a 's and Push b 's



Is Suitable For Recursion?

1. No left recursion
2. Not ambiguous
3. No prediction table conflicts
 1. Fails because both have first of a
 1. $A \rightarrow aAB \mid ab$
 2. $B \rightarrow bBa \mid ba$

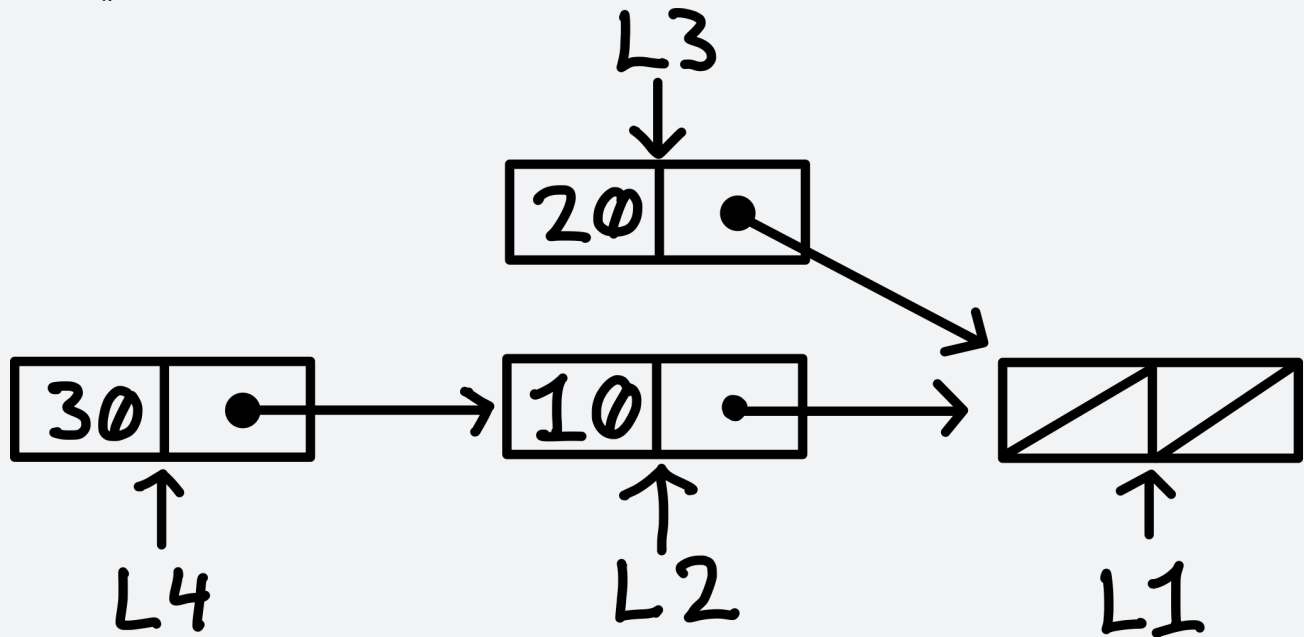
Persistent Structures (**list135**) - Everything is $O(1)$

Code

```
L1 = list135()
L2 = L1.cons(10)
L3 = L1.cons(20)
L4 = L2.cons(30)
```

```
L.is_empty: L.next == None
L.first(): L.first_element
```

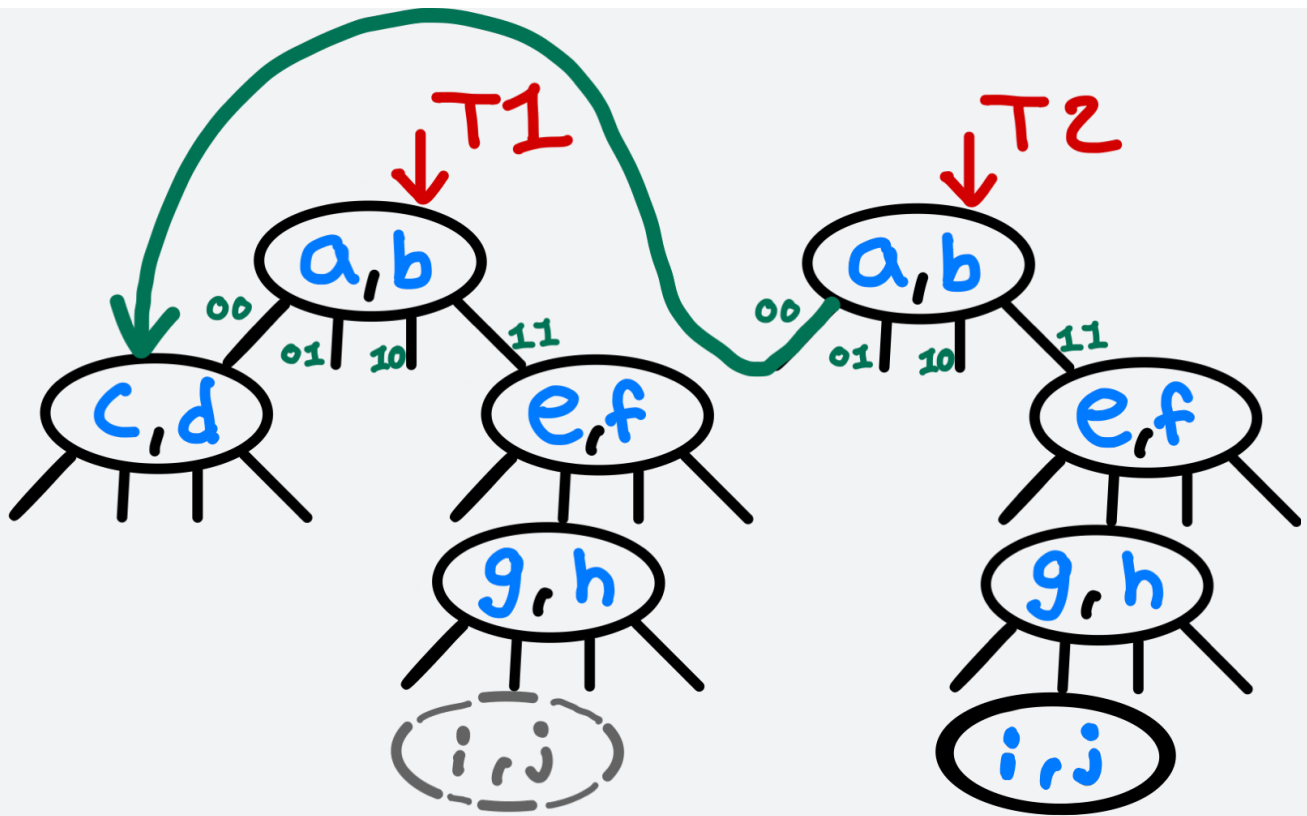
L.rest(): L.rest_of_list



Hash Array Mapped Trie (HAMT)

Code

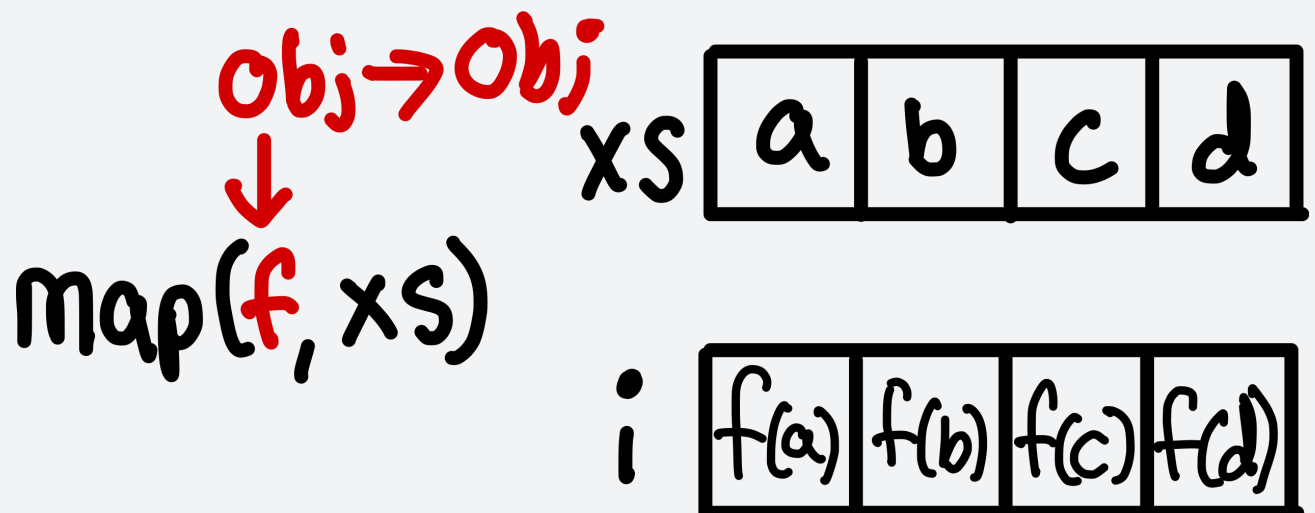
```
T1 = hamt(a, b)
T2 = T1.set(i, j)
hash(i) = ... 010111
```



Higher Order Functions: `map`, `filter`, `reduce`; `lambda`

map()

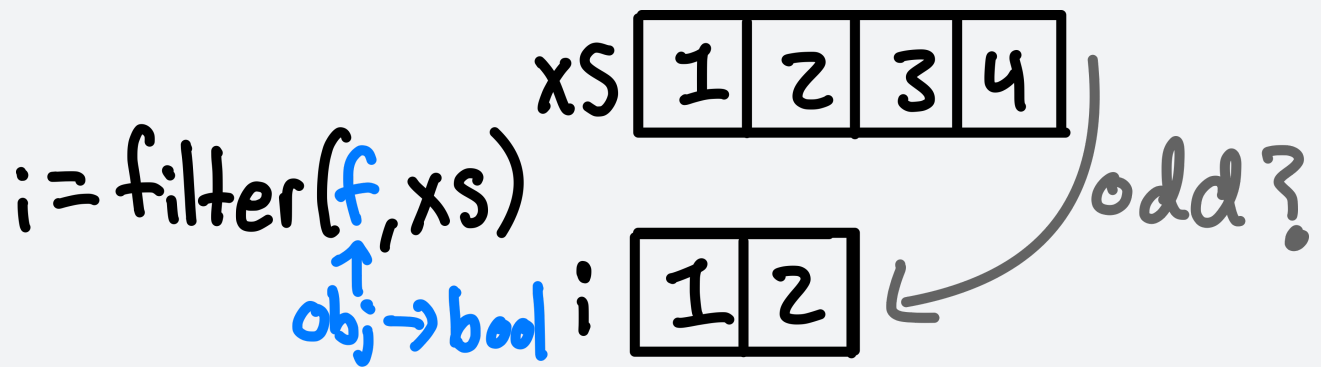
```
i = map(f, xs)
L = list(i)
```





filter()

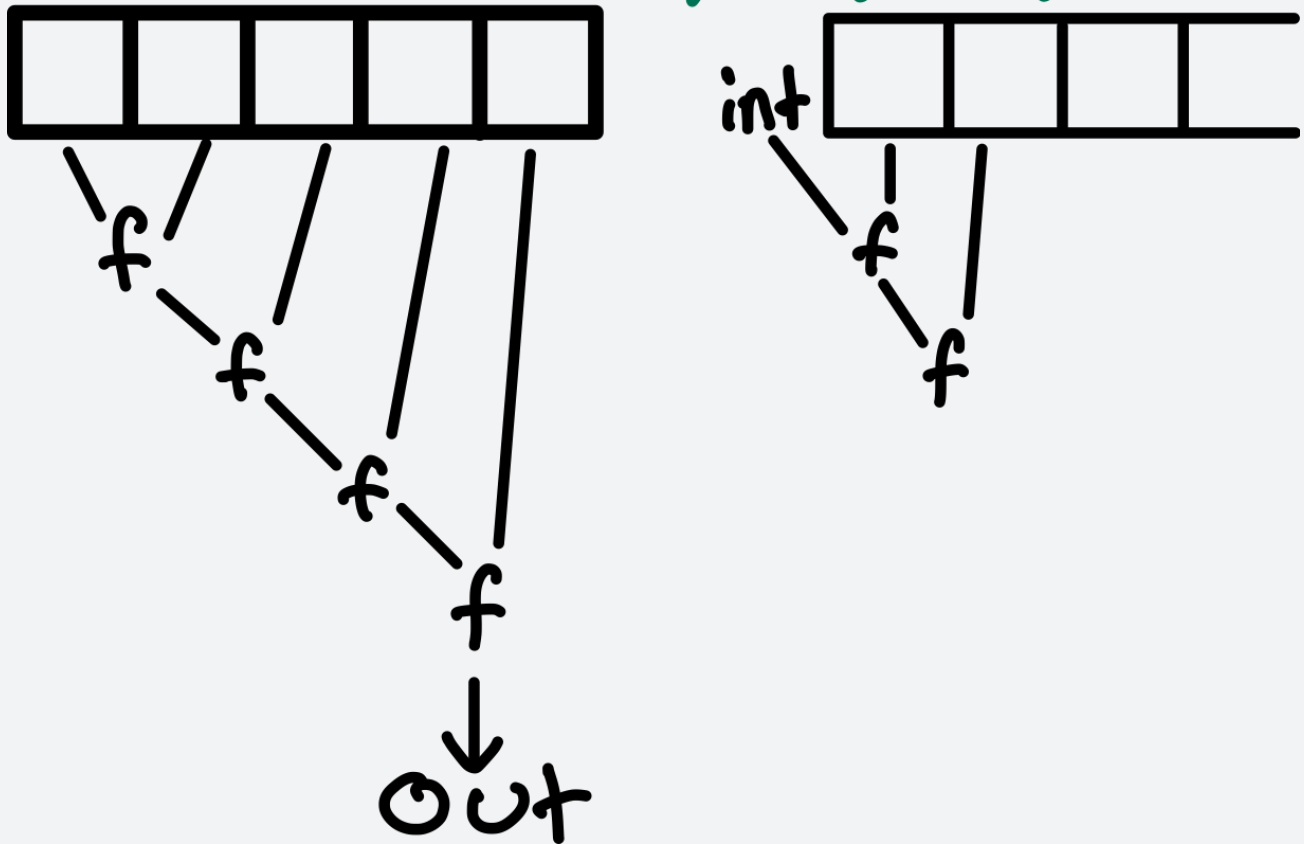
```
i = filter(f, xs)
```



reduce()

```
from functools import reduce  
r = reduce(f, xs, [int])
```

$\text{reduce}(f, xs, [\text{int}])$
 $\uparrow \text{Obj} \times \text{Obj} \rightarrow \text{Obj}$



Higher Order Functions Challenge

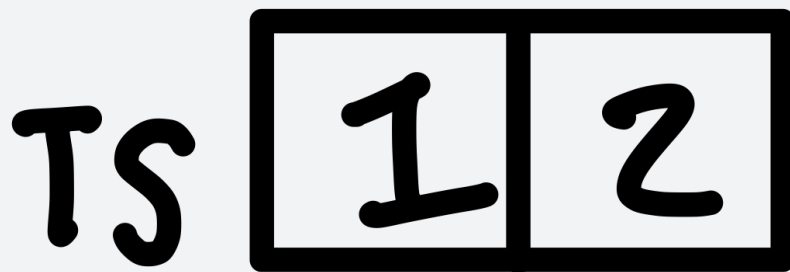
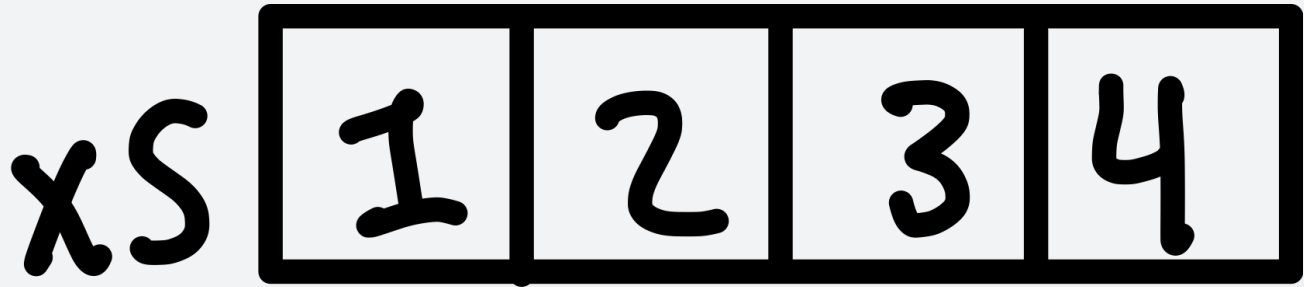
? Question

Given list of non-negative integers
return largest odd one or zero if none.



Idea

Filter to keep odds, reduce to find max.



```
TS = filter(lambda x: x % 2 != 0, XS)
```

```
def is_odd(x):  
    return x % 2 != 0
```

```
# Is the same as the anonymous function
```

```
lambda: x % 2 != 0
```

Python Ternary Statement: `x if bool else y`

- Similar to C/C++ Ternary: `(bool ? x : y)`

```
# Solution
```

```
res = reduce(lambda a, b: a if a > b and a % 2 != 0 else b, TS, 0)`
```