

1. (1 point) Are the following functions homogeneous? (You have only one attempt! Submit all answers at the same time)

(a)

- Choose
- Homogeneous
- Not Homogeneous

$$f(x, y) = x^3 y^5.$$

(b)

- Choose
- Homogeneous
- Not Homogeneous

$$f(x, y) = x \sin(y).$$

(c)

- Choose
- Homogeneous
- Not Homogeneous

$$f(x, y) = x + y^2.$$

2. (1 point)

Determine whether the differential equation is homogeneous or not. If it is homogeneous, provide the degree of  $x^2 y^4$  and  $x^6 + y^6$ . If it is not homogeneous, put  $-1$  as the degree. (Note: This is the first definition of homogeneous DE we saw!)

$$(x^2 y^4) dx + (x^6 + y^6) dy = 0$$

(a) The degree is \_\_\_\_.

(b) The equation is

- Choose
- Homogeneous
- Not Homogeneous

3. (1 point) Use substitution to find the general solution of the differential equation  $(7x - y) dx + x dy = 0$ .

(Use  $C$  to denote the arbitrary constant and  $\ln|$  input | if using  $\ln$ .)

$y =$  \_\_\_\_\_ help (formulas)

$$\text{Solve the differential equation } (y^2 + xy) dx - x^2 dy = 0.$$

- A.  $y = \frac{x}{xC + \ln|x|}$

- B.  $y = C - \ln|x|$

- C.  $y = \frac{x}{C - \ln|x|}$

- D.  $y = C + \ln|x|$

Solve the homogeneous differential equation  $-y dx + (x + \sqrt{xy}) dy = 0$ . (Note: Some algebraic manipulation goes into putting your answer into the form below.)

- A.  $y = x(\ln|x| - C)^2$

- B.  $y(\ln|y| - C)^2 = 4x$

- C.  $\sqrt{yx} \ln|y| = C\sqrt{x}$

Which of the following is a solution to the IVP consisting of the homogeneous differential equation  $-y dx + (x + \sqrt{xy}) dy = 0$  with the initial condition  $y(4) = 1$ . (Note: Some algebraic manipulation goes into putting your answer into the form below.)

- A.  $\sqrt{yx} \ln|y| = 4\sqrt{x}$

- B.  $y = x(\ln|x| + 4)^2$

- C.  $y(\ln|y| + 4)^2 = 4x$

7. (1 point) Note that  $y = c_1 e^{4x} + c_2 e^{-x}$  is a general solution for the second-order differential equation  $y'' - 3y' - 4y = 0$  on the interval  $(-\infty, \infty)$ . Find values  $c_1$  and  $c_2$  so that  $y$  is a solution to the second-order IVP consisting of the differential equation  $y'' - 3y' - 4y = 0$  and the initial condition  $y(0) = 3$ ,  $y'(0) = 7$ . The values are  $c_1 =$  \_\_\_\_\_ and  $c_2 =$  \_\_\_\_\_.

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8. (1 point) Note that  $y = c_1x + c_2x\ln(x)$  is a general solution for the second-order differential equation  $x^2y'' - xy' + y = 0$  on the interval  $(0, \infty)$ . Find values  $c_1$  and  $c_2$  so that  $y$  is a solution to the second-order IVP consisting of the differential equation  $x^2y'' - xy' + y = 0$  and the initial condition  $y(1) = 2, y'(1) = 7$ . The values are  $c_1 = \underline{\hspace{1cm}}$  and  $c_2 = \underline{\hspace{1cm}}$ .

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We have that  $y = c_1 + c_2x^2$  is a two-parameter family of solutions for the differential equation  $xy'' - y' = 0$  on the interval  $(-\infty, \infty)$ . Does there exist values  $c_1$  and  $c_2$  so that  $y$  satisfies the initial conditions  $y(0) = 0$  and  $y'(0) = 1$ ?

- A. No
- B. Yes

Why does your answer above not violate the theorem in class concerning the existence of a unique solution?

- A. The coefficients are continuous on the interval.

- B. The highest order derivative is two.
- C. The coefficient of the  $y''$  term is 0.
- D. The differential equation is linear.

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Consider the initial value problem  $(x - 8)y'' + 3y = x$  with initial conditions  $y(0) = 3$  and  $y'(0) = 1$ . Which of the following is an interval containing 0 for which this IVP has a unique solution on?

- A.  $(-\infty, 8)$
- B.  $(-8, \infty)$
- C.  $(-\infty, -8)$
- D.  $(-\infty, 3)$