

Please show and explain your work where necessary. Good luck!!

1. (5 points) For each of the following,  
Circle all of the following expression which are differential equations.

(i)  $g'(x) + g(x) = 0$

(ii)  $\left(\frac{d}{dt}\right)^5 f(t) + \frac{d}{dt}f(t) + f(t) = 0$

(iii)  $\sin(x) \frac{d^2 f}{dx^2} + \frac{df}{dx} + e^x = \frac{d^3 f}{dx^3}$

(iv)  ~~$y''' + y' + x$~~  Not an equation

(v)  $f'(x) = f(x)$

(vi)  $y^2 x = x^2$

(vii)  $\csc(y'') + \sin(x) - y = 0$

(viii)  $x^2 \frac{\partial^2 y}{\partial t^2} + y^2 \frac{\partial x}{\partial s} = s + t$

(ix)  $e^{y''} + e^x = 3y$

(x)  $x \frac{\partial^2 y}{\partial t^2} = y \frac{\partial x}{\partial s}$

2. (3 points) For the following equations, provide the *dependent variable*.

a. (1 pt)  $f'(x) - f(x) = 0$   $f(x)$

b. (1 pt)  $\frac{d^2 g}{dt^2} - e^t g(t) = 3$   $g$

c. (1 pt)  $\sin(x)y' + y = 0$   $y?$

$\frac{dx}{dt}$  &  $\frac{dy}{dt}$  Dependent  
 $\frac{dt}{dt}$  Independent

3. (2 points) Consider the function  $y = x^3$ .

- a. (1 pt) Compute  $y'$  and  $y''$ .

$[x^3]' = 3x^2, [x^3]'' \rightarrow [3x^2]' = 6x$

- b. (1 pt) Does  $y$  satisfy the differential equation  $x^2 y'' - 5y = 0$ ? Justify your answer.

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