

We have  $y = Cx^2$  is a 1-parameter family of solutions for the differential equation  $y'x - 2y = 0$ . Which of the following is a solution for the initial value problem consisting of the differential equation  $y'x - 2y = 0$  and initial condition  $y(2) = 12$ .

- A.  $y = 12x^2$
- B.  $y = 3x^2$
- C.  $y = Cx^2$
- D.  $y = 2x^2$

2. (1 point) Consider the initial value problem

$$2ty' = 4y, \quad y(-2) = 4.$$

Find the value of the constant  $C$  and the exponent  $r$  so that  $y = Ct^r$  is the solution of this initial value problem.  
 $y =$  \_\_\_\_\_ help (formulas)

3. (1 point) Suppose  $y' = f(x, y) = \frac{xy}{\cos(x)}$ .

(1)  $\frac{\partial f}{\partial y} =$  \_\_\_\_\_ help (formulas)

(2) Since the function  $f(x, y)$  is

- Choose
- continuous
- not continuous

at the point  $(0, 0)$ , the partial derivative  $\frac{\partial f}{\partial y}$

- Choose
- exists
- does not exist

and is

- Choose
- continuous
- not continuous

at and near the point  $(0, 0)$ , the solution to  $y' = f(x, y)$

- Choose
- exists and is unique
- does not exist

near  $y(0) = 0$

4. (1 point) For the differential equations  $\frac{dy}{dx} = \sqrt{y^2 - 16}$  does the existence/uniqueness theorem guarantee that there is a solution to this equation through the point

☐ 1.  $(-1, 4)$ ?

☐ 2.  $(-4, 19)$ ?

☐ 3.  $(1, 25)$ ?

☐ 4.  $(3, -4)$ ?

Note: To answer this question, compute the partial derivative of  $f(x, y) = \sqrt{y^2 - 16}$  with respect to  $y$  and check if  $f(x, y)$  and  $\frac{\partial f}{\partial y}$  exists at the given points. If they do, then the conditions of the theorem are satisfied at the given points.

5. (1 point)

Enter a value for  $\pi$