

1. (1 point)

- (1) Find a particular solution to the nonhomogeneous differential equation $y'' + 4y' + 4y = 8x^2 + 4x + 8$. (Note: it might be better to first do part (b) before part (a).)

$y_p =$ _____ help (formulas)

- (2) Find the most general solution to the associated homogeneous differential equation. Use c_1 and c_2 in your answer to denote arbitrary constants, and enter them as c_1 and c_2 .

$y_c =$ _____ help (formulas)

- (3) Find the most general solution to the original nonhomogeneous differential equation. Use c_1 and c_2 in your answer to denote arbitrary constants.

$y =$ _____ help (formulas)

Correct Answers:

- $2x^2 - 3x + 4$
- $c_1 e^{-2x} + c_2 x e^{-2x}$
- $2x^2 - 3x + 4 + c_1 e^{-2x} + c_2 x e^{-2x}$

2. (1 point)

- (1) Find a particular solution to the nonhomogeneous differential equation $y'' - y' = -5$. (Note: it might be better to first do part (b) before part (a).)

$y_p =$ _____ help (formulas)

- (2) Find the most general solution to the associated homogeneous differential equation. Use c_1 and c_2 in your answer to denote arbitrary constants, and enter them as c_1 and c_2 .

$y_c =$ _____ help (formulas)

- (3) Find the most general solution to the original nonhomogeneous differential equation. Use c_1 and c_2 in your answer to denote arbitrary constants.

$y =$ _____ help (formulas)

Correct Answers:

- $5x$
- $c_1 + c_2 e^x$
- $5x + c_1 + c_2 e^x$

- 3. (1 point)** Solve the following differential equation by variation of parameters. Fully evaluate all integrals.

$$y'' + 9y = \sec(3x).$$

- (1) Find the most general solution to the associated homogeneous differential equation. Use c_1 and c_2 in your answer to denote arbitrary constants, and enter them as c_1 and c_2 .

$y_c =$ _____ help (formulas)

- (2) Find a particular solution to the nonhomogeneous differential equation $y'' + 9y = \sec(3x)$.

$y_p =$ _____ help (formulas)

- (3) Find the most general solution to the original nonhomogeneous differential equation. Use c_1 and c_2 in your answer to denote arbitrary constants.

$y =$

_____ help (formulas)

Correct Answers:

- $c_1 \cos(3x) + c_2 \sin(3x)$
- $a \cos(3x) + b \sin(3x) + 1/3 x \sin(3x) + 1/9 \cos(3x) \ln|\cos(3x)|$
- $c_1 \cos(3x) + c_2 \sin(3x) + 1/3 x \sin(3x) + 1/9 \cos(3x) \ln|\cos(3x)|$

- 4. (1 point)** Solve the following differential equation by variation of parameters. Fully evaluate all integrals.

$$y'' - 4y = x e^{2x}.$$

- (1) Find the most general solution to the associated homogeneous differential equation. Use c_1 and c_2 in your answer to denote arbitrary constants, and enter them as c_1 and c_2 .

$y_c =$ _____ help (formulas)

- (2) Find a particular solution to the nonhomogeneous differential equation $y'' - 4y = x e^{2x}$.

$y_p =$ _____ help (formulas)

- (3) Find the most general solution to the original nonhomogeneous differential equation. Use c_1 and c_2 in your answer to denote arbitrary constants.

$y =$

_____ [help \(formulas\)](#)

Correct Answers:

- $c_1 e^{(2x)} + c_2 e^{(-2x)}$
- $a e^{(2x)} + b e^{(-2x)} + \frac{1}{8} x^2 e^{(2x)} - \frac{1}{16} x e^{(2x)}$
- $c_1 e^{(2x)} + c_2 e^{(-2x)} + \frac{1}{8} x^2 e^{(2x)} - \frac{1}{16} x e^{(2x)}$