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Please show and explain your work where necessary. Good luck!!

- 1. (8 points) For each of the following differential equations, determine whether it is exact or not. (Use math to justify your answer.)
 - a. (2 pts) $x dx y dy = 0 \rightarrow x dx + (-y) dy = 0$

$$M(x,y) = x$$

$$N(x,y) = -y$$

$$\frac{d}{dx} M = \frac{d}{dx} (x) = 1x^0 = 1$$

$$\frac{dy}{dy}N = \frac{dy}{dy}(-y) = -1y^{0} = -1$$

$$M(x,y) = y \rightarrow \frac{d}{dx}(y) = I$$

$$N(x,y)=x \rightarrow \frac{d}{dy}(x)=I$$

c. (3 pts)
$$(y-x) dx + (x-y) dy =$$

$$N(x,y) = y + \frac{1}{4x}(y) = 1$$

$$N(x,y) = x + \frac{1}{4x}(y) = 1$$

$$N(x,y) = (y-x) dx + (x-y) dy = 0$$

$$N(x,y) = (y-x) + \frac{1}{4x}(y-x) + \frac{1}{4x}(y) - \frac{1}{4x}(x) + 0 - 1 = 1$$

$$N(x,y) = (x-y) + \frac{1}{4x}(y-x) + \frac{1}{4x}(y) - \frac{1}{4x}(x) + 0 - 1 = 1$$

$$(2 \text{ points}) \text{ Compute the integrating factor for the differential equation } xy' = 5 - 2y.$$

$$N(x,y) = (x-y)^{-1} \frac{dy}{dy}(x-y)^{-2} \frac{dy}{dy}(x) - \frac{dy}{dy}(y) \rightarrow 0 - 1 = 0$$

2. (2 points) Compute the integrating factor for the differential equation xy' = 5 - 2y.