

1. (1 point) Select the following which are differential equations.

☒ A. $y = x$ is an equation, but not a differential equation

☒ B. $y'' + 3$ is not an equation

☐ C. $s^{(2)} = 5$ is a second order

☐ D. $x'' - 2x' + 3x = 0$ $n=2, a_0=1, a_1=-2$ and $a_2=3$

☒ E. $y^3 - y^2 + y = 0$ is not a DE (y^2 is $y \cdot y$)

☐ F. $y'y = 2$

☐ G. $\ln(y'') + \sin(y') = e^y$

☐ H. $\frac{d^2y}{dx^2} - e^x \frac{dy}{dx} + \sin(x) = 2$

☐ I. $y' = 2y$ $\frac{dy}{dx} - 2y = 0, n=1, a_0(x)=1,$ and $a_1(x)=-2$

☐ J. None of the above

2. (1 point)

$\frac{dx}{dt}$ $\frac{dy}{dt}$ Dependent
at at Independent

State what the independent and dependent variables are in the differential equation $y'' + yx = 2x$.

Independent variable: x

Dependent variable: y

State what the independent and dependent variables are in the differential equation $\frac{d^2x}{dy^2} = 15$.

Independent variable: y

Dependent variable: x

Which of the following is NOT a correct partial derivative of the 4-variable function $g(x, y, z, w) = x^6 \ln(4y) e^{7z} \cos(4w)$.

☐ A. $\frac{\partial g}{\partial x} = 6x^5 \ln(4y) e^{7z} \cos(4w)$

☐ B. $\frac{\partial g}{\partial w} = -4x^6 \ln(4y) e^{7z} \sin(4w)$

☐ C. $\frac{\partial g}{\partial y} = \frac{x^6 e^{7z} \cos(4w)}{y}$

☐ D. $\frac{\partial g}{\partial z} = -7x^6 \ln(4y) e^{7z} \sin(4w)$

4. (1 point)

Find the partial derivatives $\frac{\partial f}{\partial x}$ and $\frac{\partial f}{\partial y}$ for the function $f(x, y) = \sin(x^9 y^6)$.

$\frac{\partial f}{\partial x} =$ _____ help (formulas)

$\cos(x^9 y^6) 9x^8 y^6$

$\frac{\partial f}{\partial y} =$ _____ help (formulas)

$\cos(x^9 y^6) x^9 6y^5$

5. (1 point) Select the following which are ordinary differential equations.

☐ A. $\frac{d^3y}{dx^3} - \sin(x) \frac{d^2y}{dx^2} + \ln(x) = \pi$

☐ B. $y' - 2y = 3$

☐ C. $\ln(y'') + e^{y'} = e^y$

☐ D. $(y')^2 = y$

☒ E. $\frac{\partial h}{\partial r} + \frac{\partial h}{\partial s} = 5$ Different Independent variables

☐ F. $x^{(57)} - 2x''' + 3x = 0$

☒ G. $\frac{\partial^2 f}{\partial x^2} - \frac{\partial f}{\partial y} = 0$

Different Independent variables

L = Linear, NL = Non-Linear, O = Ordinary, P = Partial

X H. $y''' + x$ Not An Equation

• I. $y^5 + y' = y$

• J. $\frac{df}{dx} + \frac{dg}{dx} = 0$

• K. None of the above

6. (1 point) Select the following which are linear differential equations.

• A. $x^{(57)} - 2x''' + 3x = 0$

• B. $\ln(y'') + e^{y'} = e^y$

• C. $\frac{df}{dx} + \frac{dg}{dx} = 0$

• D. $\frac{\partial^2 f}{\partial x^2} - \frac{\partial f}{\partial y} = 0$

• E. $\frac{d^3 y}{dx^3} - \sin(x) \frac{d^2 y}{dx^2} + \ln(x) = \pi$

• F. $y^5 + y' = y$

• G. $y''' + x$

• H. $y' - 2y = 3$

• I. $(y')^2 = y$

• J. $\frac{\partial h}{\partial r} + \frac{\partial h}{\partial s} = 5$

• K. $\frac{\partial h}{\partial r} + \left(\frac{\partial h}{\partial s}\right)^4 = 5$

• L. None of the above

7. (1 point)

7. (1 point) Differential equation with order

$(1-x)y'' - 4xy' + 5y = \cos(x)$ is a **L** ☐ **O** ☐ **2** differential equation with

$x \frac{d^3 y}{dx^3} - \left(\frac{dy}{dx}\right)^4 = 0$ is a **NL** ☐ **O** ☐ **3** differential equation with

$\frac{\partial^2 z}{\partial x^2} + \frac{\partial z}{\partial y} + y = \cos(x+y)$ is a **L** ☐ **P** ☐ **2** differential equation with

$\frac{d^2 y}{dx^2} = \sqrt{1 + \left(\frac{dy}{dx}\right)^2}$ is a **NL** ☐ **O** ☐ **2** differential equation with

$\frac{dy}{dx} = \frac{\cos(y)}{y}$ is a **NL** ☐ **O** ☐ **1** differential equation with

$\frac{\partial^2 z}{\partial x \partial y} + (xy)^2 = 0$ is a **L** ☐ **P** ☐ **2** differential equation with

$y'(1-4t)y + 5y = t$ is a **NL** ☐ **O** ☐ **1** differential equation with

$y' - (1-y'')y' = t^3 - t$ is a **NL** ☐ **O** ☐ **2** differential equation with

8. (1 point)

State the order of the given differential equations below.

$x^2 \frac{dy}{dx} = 9x$ has order: **1**

$\frac{\partial^4 g}{\partial r^4} - e^{r^2 r^3} \frac{\partial^3 g}{\partial y^3} = rt$ has order: **4**

$\sin(y^{(7)}) + y' - 3x = 0$ has order: **7**

$x^{(6)} = x$ has order: **6**

9. (1 point)

Determine if the following differential equations are in differential form, normal form, or standard form.

(a) The equation $e^{rs} dr - s ds = 0$ is in

- Choose
- differential
- normal
- standard form.

(b) The equation $\frac{d^4 f}{dx^4} - e^x \frac{d^2 f}{dx^2} - x = 0$ is in

- Choose
- differential
- normal
- standard form.

(c) The equation $y' = y - 3$ is in

- Choose
- differential
- normal
- standard form.

(d) The equation $x''' - t^2 x' + x = 0$ is in

- Choose
 - differential
 - normal
 - standard
- form.

(e) The equation $\frac{dg}{ds} = \cos(s)g + s^2$ is in

- Choose
- differential
- normal
- standard

form.

(f) The equation $x^2 dx + y^2 dy = 0$ is in

- Choose
- differential
- normal
- standard

form.

10. (1 point)

Enter a value for π

Pi