

Please show and explain your work where necessary. Good luck!!

1. (8 points) For each of the following differential equations, determine whether it is exact or not. (Use math to justify your answer.)

a. (2 pts) $x dx - y dy = 0 \rightarrow x dx + (-y) dy = 0$

$M(x,y) = x$

$N(x,y) = -y$

$\frac{d}{dx} M = \frac{d}{dx}(x) = 1x^0 = 1$

$\frac{d}{dy} N = \frac{d}{dy}(-y) = -1y^0 = -1$

Not
same
Not exact

b. (3 pts) $y dx + x dy = 0$

$M(x,y) = y \rightarrow \frac{d}{dx}(y) = 1$

$N(x,y) = x \rightarrow \frac{d}{dy}(x) = 1$

Exact

c. (3 pts) $(y - x) dx + (x - y) dy = 0$

$M(x,y) = (y-x) \rightarrow \frac{d}{dx}(y-x) \rightarrow \frac{d}{dx}(y) - \frac{d}{dx}(x) \rightarrow 0 - 1 = -1$

$N(x,y) = (x-y) \rightarrow \frac{d}{dy}(x-y) \rightarrow \frac{d}{dy}(x) - \frac{d}{dy}(y) \rightarrow 0 - 1 = -1$

Exact

2. (2 points) Compute the integrating factor for the differential equation $xy' = 5 - 2y$.

Need to review this.

Section More...