

You must show and explain your work! The following formulas may, or may not, be useful.

**1.** (10 points)

**a.** (2 pts) Circle all of the following expression which are **linear** differential equations.

(i)  $y''' - y'' + y = 0$

(iii)  $\ln(y') - y = x \cos(x)$

(ii)  $(y')^3 = y^2$

(iv)  $e^x y^{(7)} - (x^2 - 3)y = \sin(x^2)$

**b.** (2 pts) Circle all of the following expression which are linear **nonhomogeneous** differential equations.

(i)  $y''' - y'' = y - x^2 \sin(x)$

(iii)  $y^{(3)} - \sec(x)y' - y = e^x$

(ii)  $t^2 \frac{d^3 f}{dt^3} + t \frac{df}{dt} + t^5 = t^5$

(iv)  $y^{(3)} - x^5 y' - 2x^2 = 0$

**c.** (3 pts) Compute  $\mathcal{L}\{e^{5t} \sin(3t)\}$ .

**d.** (3 pts) Compute  $\mathcal{L}^{-1}\left\{\frac{9}{s+2} + \frac{3}{s^2+16}\right\}$ .

**2.** (10 points) Solve the following differential equations.

**a.** (5 pts)  $e^y dx + (2y + xe^y) dy = 0$

**b.** (5 pts)  $y' - \frac{3}{x+1}y = (x+1)^4$

**3.** (*20 points*) Solve the following differential equations. Your answers should be written as real general solutions.

**a.** (*5 pts*)  $y'' - 4y' + 13y = 0$

**b.** (*5 pts*)  $x^2y'' + 5xy' + 4y = 0$

**c.** (10 pts)  $y'' - 8y' + 15y = 8 \cos(x) - 14 \sin(x)$

**4.** (*10 points*) Use the Laplace Transform to solve the initial value problem  $y'' = 2 + 3t$  with initial conditions  $y(0) = 0$ ,  $y'(0) = 0$ . (You must use the method of Laplace Transform for credit.)