1. (1 point) Find the dot product of

$$\vec{x} = \begin{bmatrix} 1 \\ 7 \end{bmatrix} \text{ and } \vec{y} = \begin{bmatrix} 8 \\ -4 \end{bmatrix}.$$

$\vec{x} \cdot \vec{y} =$ ____.

Correct Answers:

- `1*8+7*-4`

2. (1 point) Find the dot product of

$$\vec{x} = \begin{bmatrix} -4 \\ 5 \\ 1 \end{bmatrix} \text{ and } \vec{y} = \begin{bmatrix} 5 \\ 2 \\ 2 \end{bmatrix}.$$

$\vec{x} \cdot \vec{y} =$ ________.

Correct Answers:

- `-8`

3. (1 point) Find the length of the vector $\vec{x} = \begin{bmatrix} -4 \\ -6 \\ -3 \end{bmatrix}$.

$||\vec{x}|| =$ ________.

Correct Answers:

- `sqrt((-4)^2+(-6)^2+(-3)^2)`

4. (1 point) Find the length of $\vec{x}$ and the unit vector $\vec{u}$ in the direction of $\vec{x}$ if

$$\vec{x} = \begin{bmatrix} 3 \\ 1 \\ -1 \\ 3 \end{bmatrix}.$$

$||\vec{x}|| =$ ________,

$$\vec{u} = \begin{bmatrix} \_\_ \\ \_\_ \\ \_\_ \\ \_\_ \end{bmatrix}$$

Correct Answers:

- `sqrt(20)`
- $$\begin{bmatrix} 0.67082 \\ 0.223607 \\ -0.223607 \\ 0.67082 \end{bmatrix}$$

5. (1 point)

Suppose $\vec{u} = \langle -2, -6, -3 \rangle$. Mark each vector below with a "**T**" if it is orthogonal to $\vec{u}$, and an "**F**" if it is not orthogonal to $\vec{u}$:

___ 1. $\langle -2, 5, 3 \rangle$
___ 2. $\langle -3, -16, 34 \rangle$
___ 3. $\langle 1, 5, -5 \rangle$
___ 4. $\langle -3, 1, 0 \rangle$

Correct Answers:

- `F`
- `T`
- `F`
- `T`

6. (1 point)

Find the value of k for which the vectors

$$\begin{bmatrix} -4 \\ 0 \\ 4 \\ 4 \end{bmatrix} \text{ and } \begin{bmatrix} -1 \\ 4 \\ 4 \\ k \end{bmatrix}$$

are orthogonal.

$k =$ ____.

Correct Answers:

- `-20/4`

7. (1 point) Find a non-zero vector $\vec{v}$ orthogonal to the vector $\vec{u} = \begin{bmatrix} 8 \\ -1 \end{bmatrix}$.

$\vec{v} = \begin{bmatrix} \_\_ \\ \_\_ \end{bmatrix}$

Correct Answers:

- $$\begin{bmatrix} 1 \\ 8 \end{bmatrix}$$

8. (1 point) Find the angle α between the vectors

$$\begin{bmatrix} -4 \\ 1 \\ 4 \end{bmatrix} \text{ and } \begin{bmatrix} 4 \\ 5 \\ 2 \end{bmatrix}.$$

Please give your answer in radians.

$\alpha =$ ____________.

Correct Answers:

- `acos(-0.0778499)`

9. (1 point) Let L be the line in $\mathbb{R}^3$ that consists of all scalar multiples of the vector $\begin{bmatrix} -1 \\ 2 \\ -2 \end{bmatrix}$. Find the orthogonal projection of the vector $\vec{x} = \begin{bmatrix} 9 \\ 3 \\ 1 \end{bmatrix}$ onto L.

$\text{proj}_L \vec{x} = \begin{bmatrix} \_\_ \\ \_\_ \\ \_\_ \end{bmatrix}$

Correct Answers:

- $\begin{bmatrix} 0.555556 \\ -1.11111 \\ 1.11111 \end{bmatrix}$

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10. (1 point) Compute the orthogonal projection of $\vec{v} = \begin{bmatrix} -5 \\ 7 \\ 6 \end{bmatrix}$ onto the line L through $\begin{bmatrix} -7 \\ 6 \\ -4 \end{bmatrix}$ and the origin.

$\text{proj}_L(\vec{v}) = \begin{bmatrix} \_\_\_\_ \\ \_\_\_ \\ \_\_\_ \end{bmatrix}$.

Correct Answers:

- $\begin{bmatrix} -3.67327 \\ 3.14851 \\ -2.09901 \end{bmatrix}$

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11. (1 point) Find the orthogonal projection of

$$\vec{v} = \begin{bmatrix} -20 \\ -10 \\ 4 \end{bmatrix}$$

onto the subspace W of $\mathbb{R}^3$ spanned by

$$\begin{bmatrix} -7 \\ 4 \\ -2 \end{bmatrix} \text{ and } \begin{bmatrix} 2 \\ -4 \\ -15 \end{bmatrix}.$$

$\text{proj}_W(\vec{v}) = \begin{bmatrix} \_\_\_\_ \\ \_\_\_ \\ \_\_\_ \end{bmatrix}$

Correct Answers:

- $\begin{bmatrix} -9.82313 \\ 6.31293 \\ 1.0068 \end{bmatrix}$

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12. (1 point) Find the orthogonal projection of

$$\vec{v} = \begin{bmatrix} -20 \\ -16 \\ 8 \\ 3 \end{bmatrix}$$

onto the subspace W of $\mathbb{R}^4$ spanned by

$$\begin{bmatrix} -2 \\ 4 \\ 2 \\ 1 \end{bmatrix} \text{ and } \begin{bmatrix} 4 \\ 5 \\ -6 \\ 0 \end{bmatrix}.$$

$\text{proj}_W(\vec{v}) = \begin{bmatrix} \_\_\_\_ \\ \_\_\_ \\ \_\_\_ \\ \_\_\_ \end{bmatrix}$

Correct Answers:

- $\begin{bmatrix} -10.4052 \\ -14.3065 \\ 15.8078 \\ -0.2 \end{bmatrix}$

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13. (1 point) Find the least-squares solution $\hat{\mathbf{x}}$ of the system

$$\begin{bmatrix} 2 & -2 \\ -2 & 2 \\ 3 & 3 \end{bmatrix} \mathbf{x} = \begin{bmatrix} 14 \\ -2 \\ 6 \end{bmatrix}.$$

$\hat{\mathbf{x}} = \begin{bmatrix} \_\_\_ \\ \_\_ \end{bmatrix}$

Correct Answers:

- $\begin{bmatrix} 3 \\ -1 \end{bmatrix}$

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14. (1 point) Find the least-squares solution $\hat{\mathbf{x}}$ of the system

$$\begin{bmatrix} 1 & -1 & 1 \\ 1 & 1 & 1 \\ 1 & -1 & -1 \\ 1 & 1 & -1 \end{bmatrix} \mathbf{x} = \begin{bmatrix} -10 \\ -4 \\ 6 \\ 0 \end{bmatrix}.$$

$\hat{\mathbf{x}} = \begin{bmatrix} \_\_\_ \\ \_\_ \\ \_\_ \end{bmatrix}$

Correct Answers:

- $\begin{bmatrix} -2 \\ 0 \\ -5 \end{bmatrix}$

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15. (1 point) Fit a quadratic function of the form $f(t) = c_0 + c_1 t + c_2 t^2$ to the data points $(0,-8)$, $(1,-11)$, $(2,-8)$, $(3,-19)$, using least squares.

$f(t) =$ ________

Correct Answers:

- `3*t-9-2*t^2`