1. (1 point) Let

$$A = \left[\begin{array}{ccc} 8 & -3 & -4 \\ -7 & 5 & 4 \end{array} \right].$$

Define the linear transformation $T: \mathbb{R}^3 \to \mathbb{R}^2$ by $T(\vec{x}) = A\vec{x}$.

Find the images of $\vec{u} = \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix}$ and $\vec{v} = \begin{bmatrix} a \\ b \\ c \end{bmatrix}$ under T.

$$T(\vec{u}) = \begin{bmatrix} & & & \\ & & & \end{bmatrix}$$
 $T(\vec{v}) = \begin{bmatrix} & & & \\ & & & \end{bmatrix}$

2. (1 point) Consider a linear transformation T from \mathbb{R}^3 to

$$T\begin{pmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \end{pmatrix} = \begin{bmatrix} -5 \\ 3 \\ -5 \end{bmatrix}, T\begin{pmatrix} \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \end{pmatrix} = \begin{bmatrix} 5 \\ -2 \\ 2 \end{bmatrix}, T\begin{pmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \end{pmatrix} = \begin{bmatrix} B. \begin{pmatrix} 0 & -1 \\ 1 & 0 \\ 0 & 1 \end{bmatrix} \\ C. \begin{pmatrix} 1 \\ -1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$A = \left[\begin{array}{ccc} -- & - & - \\ -- & - & - \\ -- & - & - \end{array} \right].$$

3. (1 point) Let $T: \mathbb{R}^2 \to \mathbb{R}^4$ be the linear transformation defined by

$$T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} 5x - 9y \\ 3y - 7x \\ x - 2y \\ 6y - 4x \end{bmatrix}.$$

Find its standard matrix A.

$$A = \left[\begin{array}{cc} - & - \\ - & - \\ - & - \end{array} \right]$$

4. (1 point)

Let $T: \mathbb{R}^2 \to \mathbb{R}^2$ be the linear transformation that first reflects points through the x-axis and then then reflects points through the line y = -x. Find the standard matrix A for T.

$$A = \begin{bmatrix} --- \\ -- \end{bmatrix}$$
.

Let $T: \mathbb{R}^2 \to \mathbb{R}^2$ be the linear transformation that first rotates points clockwise through 120° ($2\pi/3$ radians) and then reflects points through the line y = x. Find the standard matrix A for T.

$$A = \begin{bmatrix} ---- \\ --- \end{bmatrix}$$
.

6. (1 point) To every linear transformation T from \mathbb{R}^2 to \mathbb{R}^2 , there is an associated 2×2 matrix. Match the following linear transformations with their associated matrix.

- ___1. Reflection about the line y=x
- 2. Clockwise rotation by $\pi/2$ radians
- ____3. Reflection about the y-axis
- --4. The projection onto the x-axis given by T(x,y)=(x,0)
- ___5. Counter-clockwise rotation by $\pi/2$ radians
- ____6. Reflection about the x-axis

$$A. \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$B. \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$

$$C. \begin{pmatrix} 1 \\ -1 \\ 0 \end{pmatrix}$$

$$D. \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

- G. None of the above

7. (1 point) Let $T: \mathbb{R}^2 \to \mathbb{R}^2$ be the linear transformation defined by

$$T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} -5x - 15y \\ 5x + 15y \end{bmatrix}.$$

Find a vector \vec{w} that is **not** in the range of T.

$$\vec{w} = \left[\begin{array}{c} - - \\ - - \end{array} \right].$$

8. (1 point) Let $T: \mathbb{R}^2 \to \mathbb{R}^3$ be the linear transformation defined by

$$T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} -2x - 2y \\ -4x - 4y \\ 3x - 4y \end{bmatrix}.$$

Find a vector \vec{w} that is **not** in the range of T.

$$\vec{w} = \begin{bmatrix} --- \\ --- \end{bmatrix}$$

9. (1 point) Let T be an linear transformation from \mathbb{R}^r to \mathbb{R}^s . C. There is not enough information to tell. Let A be the matrix associated to T. **10.** (1 point) Let T be an linear transformation from \mathbb{R}^r to \mathbb{R}^s . Let *A* be the matrix associated to *T*. Fill in the correct answer for each of the following situations. ___1. The row-echelon form of A has a column corresponding Fill in the correct answer for each of the following situations. to a free variable. ___1. Every row in the row-echelon form of A has a pivot. _2. Every column in the row-echelon form of A is a pivot __2. Two rows in the row-echelon form of A do not have pivots. _3. The row-echelon form of A has no column correspond-____3. The row-echelon form of *A* has a pivot in every column. ing to a free variable. ___4. The row-echelon form of *A* has a row of zeros. ___4. Two columns in the row-echelon form of A are not pivot A. T is onto columns. B. T is not onto A. T is not one-to-one C. There is not enough information to tell.

B. T is one-to-one

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