

1. (1 point)

Write the augmented matrix of the system

$$\begin{cases} 20x + 87z = -33 \\ 1x - 7y - 87z = -8 \\ 60x + 90y = 5 \end{cases}$$

$$\left[\begin{array}{ccc|c} _ & _ & _ & _ \\ _ & _ & _ & _ \\ _ & _ & _ & _ \end{array} \right]$$

2. (1 point) Convert the augmented matrix

$$\left[\begin{array}{cccc} 5 & 1 & 5 & -4 \\ 0 & 2 & -5 & 5 \end{array} \right]$$

to the equivalent linear system. Use **x1**, **x2**, and **x3** to enter the variables x_1 , x_2 , and x_3 .

$$_ = _$$

$$_ = _$$

3. (1 point) Determine which of the points $(-6, 3, -2)$, $(-4, -5, -4)$, and $(-4, 6, -2)$ satisfy the linear system

$$\begin{aligned} 5x_1 + 3x_2 - 4x_3 &= -13 \\ 2x_1 - 2x_2 + 5x_3 &= -28 \end{aligned}$$

Answer: $_$

4. (1 point) Solve the system using elimination.

$$\begin{cases} -4x + 2y + 5z = -29 \\ 5x - 2y + 2z = -5 \\ -5x - 5y + 6z = -35 \end{cases}$$

$$x = _$$

$$y = _$$

$$z = _$$

5. (1 point) Solve the system using any method

$$\begin{aligned} -x + y + z &= -7 \\ 4x - 3y - z &= 18 \\ x + y + z &= -5 \end{aligned}$$

Your answer is

$$x = _$$

$$y = _$$

$$z = _$$

6. (1 point)

Solve the system using matrices (row operations)

$$\begin{cases} 2x - 5y + 3z = -13 \\ x + 2y - 4z = 19 \\ -4x - 3y - 4z = -6 \end{cases}$$

How many solutions are there to this system?

- A. None
- B. Exactly 1
- C. Exactly 2
- D. Exactly 3
- E. Infinitely many
- F. None of the above

If there is one solution, give its coordinates in the answer spaces below.

If there are infinitely many solutions, enter z in the answer blank for z , enter a formula for y in terms of z in the answer blank for y and enter a formula for x in terms of z in the answer blank for x .

If there are no solutions, leave the answer blanks for x , y and z empty.

$$x = _$$

$$y = _$$

$$z = _$$

7. (1 point)

The reduced row echelon form of a system of linear equations in x and y or in x , y and z is given. For each system, determine whether it has a unique solution (in this case, find the solution), infinitely many solutions, or no solutions.

1.

$$\left[\begin{array}{ccc|c} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & 2 \end{array} \right]$$

- A. Unique solution: $x = 1, y = 2, z = 2$
- B. No solutions
- C. Unique solution: $x = 1, y = 2, z = 0$
- D. Unique solution: $x = 1, y = 2$
- E. Infinitely many solutions
- F. None of the above

2.

$$\left[\begin{array}{ccc|c} 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

- A. Infinitely many solutions
- B. Unique solution: $x = -1, y = -1$
- C. Unique solution: $x = 0, y = 0, z = 0$
- D. Unique solution: $x = -1, y = -1$
- E. No solutions
- F. None of the above

3.

$$\left[\begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & -2 \end{array} \right]$$

- A. Unique solution: $x = 2, y = -2$
- B. Unique solution: $x = 0, y = 2, z = -2$
- C. Unique solution: $x = 0, y = 2$
- D. Infinitely many solutions
- E. No solutions
- F. None of the above

4.

$$\left[\begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

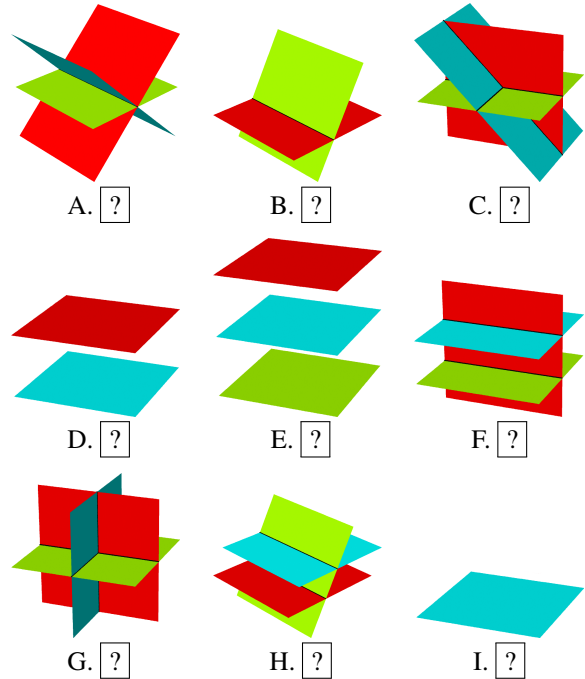
- A. Unique solution: $x = 1, y = 1, z = 0$
- B. Unique solution: $x = 0, y = 0, z = 0$
- C. No solutions
- D. Infinitely many solutions
- E. Unique solution: $x = 0, y = 0$
- F. None of the above

8. (1 point) Determine whether the following system has no solution, an infinite number of solutions or a unique solution.

$$\begin{aligned} & \boxed{?} 1. \begin{cases} -10x + 10y - 6z = 10 \\ 20x - 20y + 12z = -20 \\ -30x + 30y - 18z = 30 \end{cases} \\ & \boxed{?} 2. \begin{cases} -4x - 16y - 61z = 6 \\ 4x + 17y + 63z = 10 \\ x + 4y + 15z = 0 \end{cases} \\ & \boxed{?} 3. \begin{cases} 3x + 3y - 3z = -5 \\ -3x + 5y + 5z = -3 \\ 9x + 25y - 5z = -28 \end{cases} \end{aligned}$$

$$\boxed{?} 4. \begin{cases} 3x + 3y - 3z = -5 \\ -3x + 5y + 5z = -3 \\ 9x + 25y - 5z = -31 \end{cases}$$

9. (1 point) Each graph below is the graph of a system of three linear equations in three unknowns. Determine which systems are consistent and inconsistent.



(Click on a graph to enlarge it.)

10. (1 point) Consider a linear system whose augmented matrix is

$$\left[\begin{array}{ccc|c} 1 & 1 & 5 & -3 \\ 1 & 2 & -4 & 1 \\ 7 & 17 & k & 20 \end{array} \right]$$

For what value of k will the system have no solutions?

$k =$ _____