

1. (1 point)

Calculate the 3x3 determinant:

$$\begin{vmatrix} 4 & 4 & 0 \\ -4 & -5 & 7 \\ -3 & 5 & 6 \end{vmatrix} = \underline{\hspace{2cm}}$$

2. (1 point) Evaluate the following 3×3 determinant.

$$\begin{vmatrix} 9 & 0 & -8 \\ -1 & 0 & -3 \\ -7 & 0 & 2 \end{vmatrix}$$

Answer:

3. (1 point)

Find the determinant of the matrix

$$M = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 6 & 2 \\ 0 & 0 & -3 \end{bmatrix}.$$

$\det(M) = \underline{\hspace{2cm}}$.

4. (1 point) Compute the determinant of the following 3×3 matrix:

$$\begin{bmatrix} 4 & 3 & 1 \\ -1 & -1 & -1 \\ -3 & 2 & -3 \end{bmatrix}$$

The determinant is

5. (1 point) Evaluate the following 4×4 determinant.

$$\begin{vmatrix} 4 & 10 & -1 & -1 \\ 5 & 2 & 6 & 1 \\ 0 & 0 & 1 & 0 \\ 12 & 2 & 5 & -10 \end{vmatrix}$$

Answer:

6. (1 point)

The determinant of the matrix

$$A = \begin{bmatrix} 0 & 7 & -3 & 0 & 0 \\ -5 & 9 & -6 & 0 & 0 \\ 0 & -8 & 0 & 0 & 0 \\ -7 & -5 & 2 & 4 & -1 \\ -1 & 8 & 1 & 0 & -3 \end{bmatrix}$$

is .

Hint: Find a good row or column for cofactor expansion.

7. (1 point)

If A and B are 3×3 matrices, $\det(A) = 4$, $\det(B) = -9$, then

$\det(AB) = \underline{\hspace{2cm}}$,

$\det(-2A) = \underline{\hspace{2cm}}$,

$\det(A^T) = \underline{\hspace{2cm}}$,

$\det(B^{-1}) = \underline{\hspace{2cm}}$,

$\det(B^2) = \underline{\hspace{2cm}}$.

8. (1 point)

$$\text{If } B = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & -1 \\ 2 & 1 & -1 \end{bmatrix}$$

then $\det(B^5) = \underline{\hspace{2cm}}$

9. (1 point)

If the determinant of a 4×4 matrix A is $\det(A) = 5$, and the matrix C is obtained from A by swapping the third and fourth rows, then

$\det(C) = \underline{\hspace{2cm}}$.

10. (1 point)

If the determinant of a 5×5 matrix A is $\det(A) = 6$, and the matrix D is obtained from A by adding 3 times the third row to the second, then

$\det(D) = \underline{\hspace{2cm}}$.

11. (1 point) Given the matrix

$$\begin{bmatrix} -3 & -1 & 4 \\ 5 & 0 & 3 \\ 0 & 4 & 3 \end{bmatrix}$$

(a) find its determinant;

Your answer is :

(b) does the matrix have an inverse?

Your answer is (input Yes or No) :

12. (1 point)

$$\text{If } A = \begin{bmatrix} -5 & 2 & -1 \\ -4 & 1 & 3 \\ 3 & 2 & -3 \end{bmatrix}, \text{ then } \det(A) = \underline{\hspace{2cm}}$$

Is A invertible?

- A. Yes
- B. No