

1. (1 point)

Write the augmented matrix of the system

$$\begin{cases} 20x + 87z = -33 \\ 1x - 7y - 87z = -8 \\ 60x + 90y = 5 \end{cases}$$

$$\left[ \begin{array}{ccc|c} \_ & \_ & \_ & \_ \\ \_ & \_ & \_ & \_ \\ \_ & \_ & \_ & \_ \end{array} \right]$$

Answer(s) submitted:

- 20
- 0
- 87
- -33
- 1
- -7
- -87
- -8
- 60
- 90
- 0
- 5

(correct)

2. (1 point) Convert the augmented matrix

$$\left[ \begin{array}{cccc} 5 & 1 & 5 & -4 \\ 0 & 2 & -5 & 5 \end{array} \right]$$

to the equivalent linear system. Use **x1**, **x2**, and **x3** to enter the variables  $x_1$ ,  $x_2$ , and  $x_3$ .

$$\_ = \_$$

$$\_ = \_$$

Answer(s) submitted:

- $5x_1 + x_2 + 5x_3$
- -4
- $0x_1 + 2x_2 - 5x_3$
- 5

(correct)

3. (1 point) Determine which of the points  $(-6, 3, -2)$ ,  $(-4, -5, -4)$ , and  $(-4, 6, -2)$  satisfy the linear system

$$\begin{aligned} 5x_1 + 3x_2 - 4x_3 &= -13 \\ 2x_1 - 2x_2 + 5x_3 &= -28 \end{aligned}$$

Answer: \_\_\_\_\_

Answer(s) submitted:

- $(-6, 3, 2)$

(incorrect)

4. (1 point) Solve the system using elimination.

$$\begin{cases} -4x + 2y + 5z = -29 \\ 5x - 2y + 2z = -5 \\ -5x - 5y + 6z = -35 \end{cases}$$

$$x = \_$$

$$y = \_$$

$$z = \_$$

Answer(s) submitted:

- 1
- 0
- -5

(correct)

5. (1 point) Solve the system using any method

$$-x + y + z = -7$$

$$4x - 3y - z = 18$$

$$x + y + z = -5$$

Your answer is

$$x = \_$$

$$y = \_$$

$$z = \_$$

Answer(s) submitted:

- 1
- -4
- -2

(correct)

6. (1 point)

Solve the system using matrices (row operations)

$$\begin{cases} 2x - 5y + 3z = -13 \\ x + 2y - 4z = 19 \\ -4x - 3y - 4z = -6 \end{cases}$$

How many solutions are there to this system?

- A. None
- B. Exactly 1
- C. Exactly 2
- D. Exactly 3
- E. Infinitely many
- F. None of the above

If there is one solution, give its coordinates in the answer spaces below.

If there are infinitely many solutions, enter  $z$  in the answer blank for  $z$ , enter a formula for  $y$  in terms of  $z$  in the answer blank for  $y$  and enter a formula for  $x$  in terms of  $z$  in the answer blank for  $x$ .

If there are no solutions, leave the answer blanks for  $x$ ,  $y$  and  $z$  empty.

$x =$  \_\_\_\_\_

$y =$  \_\_\_\_\_

$z =$  \_\_\_\_\_

Answer(s) submitted:

- B
- 3
- 2
- -3

(correct)

### 7. (1 point)

The reduced row echelon form of a system of linear equations in  $x$  and  $y$  or in  $x$ ,  $y$  and  $z$  is given. For each system, determine whether it has a unique solution (in this case, find the solution), infinitely many solutions, or no solutions.

1.

$$\left[ \begin{array}{ccc|c} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & 2 \end{array} \right]$$

- A. Unique solution:  $x = 1, y = 2, z = 2$
- B. No solutions
- C. Unique solution:  $x = 1, y = 2, z = 0$
- D. Unique solution:  $x = 1, y = 2$
- E. Infinitely many solutions
- F. None of the above

2.

$$\left[ \begin{array}{ccc|c} 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

- A. Infinitely many solutions
- B. Unique solution:  $x = -1, y = -1$
- C. Unique solution:  $x = 0, y = 0, z = 0$
- D. Unique solution:  $x = -1, y = -1$
- E. No solutions
- F. None of the above

3.

$$\left[ \begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & -2 \end{array} \right]$$

- A. Unique solution:  $x = 2, y = -2$
- B. Unique solution:  $x = 0, y = 2, z = -2$
- C. Unique solution:  $x = 0, y = 2$
- D. Infinitely many solutions

- E. No solutions
- F. None of the above

4.

$$\left[ \begin{array}{cc|c} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{array} \right]$$

- A. Unique solution:  $x = 1, y = 1, z = 0$
- B. Unique solution:  $x = 0, y = 0, z = 0$
- C. No solutions
- D. Infinitely many solutions
- E. Unique solution:  $x = 0, y = 0$
- F. None of the above

Answer(s) submitted:

- B
- A
- B
- E

(correct)

8. (1 point) Determine whether the following system has no solution, an infinite number of solutions or a unique solution.

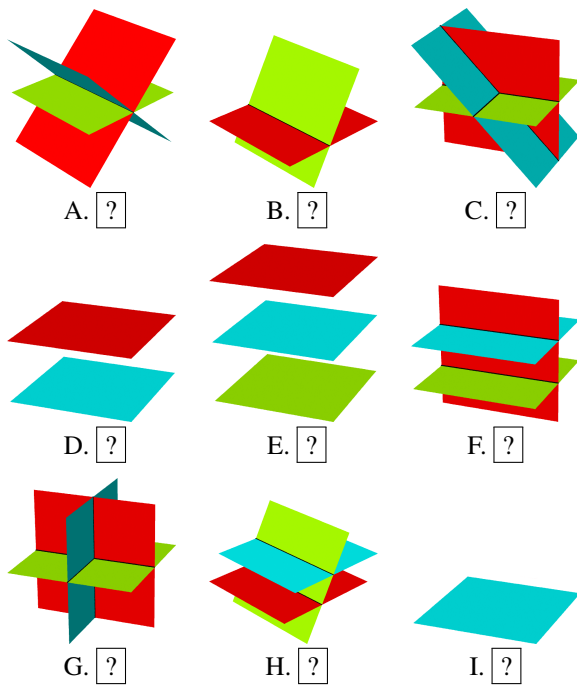
$$\begin{aligned} \boxed{?}1. & \begin{cases} -10x + 10y - 6z = 10 \\ 20x - 20y + 12z = -20 \\ -30x + 30y - 18z = 30 \end{cases} \\ \boxed{?}2. & \begin{cases} -4x - 16y - 61z = 6 \\ 4x + 17y + 63z = 10 \\ x + 4y + 15z = 0 \end{cases} \\ \boxed{?}3. & \begin{cases} 3x + 3y - 3z = -5 \\ -3x + 5y + 5z = -3 \\ 9x + 25y - 5z = -28 \end{cases} \\ \boxed{?}4. & \begin{cases} 3x + 3y - 3z = -5 \\ -3x + 5y + 5z = -3 \\ 9x + 25y - 5z = -31 \end{cases} \end{aligned}$$

Answer(s) submitted:

- Infinite Solutions
- Unique Solution
- No Solution
- Infinite Solutions

(correct)

9. (1 point) Each graph below is the graph of a system of three linear equations in three unknowns. Determine which systems are consistent and inconsistent.



(Click on a graph to enlarge it.)

Answer(s) submitted:

- consistent
- inconsistent
- consistent
- inconsistent
- inconsistent
- inconsistent
- consistent
- inconsistent
- consistent

(correct)

**10.** (1 point) Consider a linear system whose augmented matrix is

$$\left[ \begin{array}{ccc|c} 1 & 1 & 5 & -3 \\ 1 & 2 & -4 & 1 \\ 7 & 17 & k & 20 \end{array} \right]$$

For what value of  $k$  will the system have no solutions?

$k =$  \_\_\_\_\_

Answer(s) submitted:

- -55

(correct)