## **1.** (1 point) Let

$$A = \left[ \begin{array}{ccc} 8 & -3 & -4 \\ -7 & 5 & 4 \end{array} \right].$$

Define the linear transformation  $T: \mathbb{R}^3 \to \mathbb{R}^2$  by  $T(\vec{x}) = A\vec{x}$ .

Find the images of  $\vec{u} = \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix}$  and  $\vec{v} = \begin{bmatrix} a \\ b \\ c \end{bmatrix}$  under T.

$$T(\vec{u}) = \begin{bmatrix} & - & \\ & - & \end{bmatrix}$$
 $T(\vec{v}) = \begin{bmatrix} & - & \\ & - & \end{bmatrix}$ 

Answer(s) submitted:

- −2.6
- 8a-3b-4c

(correct)

**2.** (1 point) Consider a linear transformation T from  $\mathbb{R}^3$  to  $\mathbb{R}^3$  for which

$$T\left(\left[\begin{array}{c}1\\0\\0\end{array}\right]\right)=\left[\begin{array}{c}-5\\3\\-5\end{array}\right],\ T\left(\left[\begin{array}{c}0\\1\\0\end{array}\right]\right)=\left[\begin{array}{c}5\\-2\\2\end{array}\right],\ T\left(\left[\begin{array}{c}0\\0\\1\end{array}\right]$$

Find the matrix A of T

$$A = \begin{bmatrix} - & - & - \\ - & - & - \\ - & - & - \end{bmatrix}$$

Answer(s) submitted:

• -5

(correct)

**3.** (1 point) Let  $T: \mathbb{R}^2 \to \mathbb{R}^4$  be the linear transformation defined by

$$T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} 5x - 9y \\ 3y - 7x \\ x - 2y \\ 6y - 4x \end{bmatrix}.$$

Find its standard matrix A.

Answer(s) submitted:

• 5

(correct)

## **4.** (1 point)

Let  $T: \mathbb{R}^2 \to \mathbb{R}^2$  be the linear transformation that first reflects points through the *x*-axis and then then reflects points through the line y = -x. Find the standard matrix A for T.

$$A = \begin{bmatrix} --- \\ --- \end{bmatrix}.$$
Answer(s) submitted:

• 0

(correct)

## **5.** (1 point)

Let  $T: \mathbb{R}^2 \to \mathbb{R}^2$  be the linear transformation that first rotates points clockwise through  $120^\circ$  ( $2\pi/3$  radians) and then reflects points through the line y = x. Find the standard matrix A for T.

$$A = \left[ \begin{array}{cc} - & - \\ - & - \end{array} \right].$$

Answer(s) submittea:

• -((sqrt(3))/2)

(correct)

here is an associated  $2 \times 2$  matrix. Match the following linear transformations with their associated matrix.

- \_\_\_1. Reflection about the line y=x
- 2. Clockwise rotation by  $\pi/2$  radians
- \_\_\_\_3. Reflection about the y-axis
- --4. The projection onto the x-axis given by T(x,y)=(x,0)
- \_\_\_5. Counter-clockwise rotation by  $\pi/2$  radians
- \_\_\_\_6. Reflection about the x-axis

A. 
$$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

B. 
$$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$

C. 
$$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$$

D. 
$$\begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$$

E. 
$$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$$

F. 
$$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

G. None of the above

Answer(s) submitted:

- 1
- e
- C
- d

- b
- a

(correct)

7. (1 point) Let  $T: \mathbb{R}^2 \to \mathbb{R}^2$  be the linear transformation defined by

$$T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} -5x - 15y \\ 5x + 15y \end{bmatrix}$$

Find a vector  $\vec{w}$  that is **not** in the range of T.

$$\vec{w} = \begin{bmatrix} & -- \\ & -- \end{bmatrix}$$
.

Answer(s) submitted:

• 5

(correct)

**8.** (1 point) Let  $T: \mathbb{R}^2 \to \mathbb{R}^3$  be the linear transformation defined by

$$T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} -2x - 2y \\ -4x - 4y \\ 3x - 4y \end{bmatrix}.$$

Find a vector  $\vec{w}$  that is **not** in the range of T.

$$\vec{w} = \begin{bmatrix} -- \\ -- \end{bmatrix}$$
.

Answer(s) submitted:

• 1

(correct)

**9.** (1 point) Let T be an linear transformation from  $\mathbb{R}^r$  to  $\mathbb{R}^s$ . Let A be the matrix associated to T.

Fill in the correct answer for each of the following situations.

\_\_\_1. The row-echelon form of *A* has a column corresponding to a free variable.

- \_\_\_\_2. Every column in the row-echelon form of *A* is a pivot
- \_\_\_\_3. The row-echelon form of *A* has no column corresponding to a free variable.
- \_\_\_\_4. Two columns in the row-echelon form of *A* are not pivot columns.
  - A. T is not one-to-one
  - B. T is one-to-one
- C. There is not enough information to tell.

Answer(s) submitted:

- a
- b
- b

• 6

(correct)

**10.** (1 point) Let T be an linear transformation from  $\mathbb{R}^r$  to  $\mathbb{R}^s$ . Let A be the matrix associated to T.

Fill in the correct answer for each of the following situations.

- \_\_\_1. Every row in the row-echelon form of A has a pivot.
- \_\_\_\_2. Two rows in the row-echelon form of A do not have pivots.
- \_\_\_\_3. The row-echelon form of *A* has a pivot in every column.
- \_\_\_4. The row-echelon form of *A* has a row of zeros.
  - A. T is onto
  - B. T is not onto
  - C. There is not enough information to tell.

Answer(s) submitted:

- a
- b
- C
- b

(correct)

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