

1. (1 point)

Calculate the 3x3 determinant:

$$\begin{vmatrix} 4 & 4 & 0 \\ -4 & -5 & 7 \\ -3 & 5 & 6 \end{vmatrix} = \underline{\hspace{2cm}}$$

2. (1 point) Evaluate the following  $3 \times 3$  determinant.

$$\begin{vmatrix} 9 & 0 & -8 \\ -1 & 0 & -3 \\ -7 & 0 & 2 \end{vmatrix}$$

Answer:                     

3. (1 point)

Find the determinant of the matrix

$$M = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 6 & 2 \\ 0 & 0 & -3 \end{bmatrix}.$$

$\det(M) = \underline{\hspace{2cm}}$ .

4. (1 point) Compute the determinant of the following  $3 \times 3$  matrix:

$$\begin{bmatrix} 4 & 3 & 1 \\ -1 & -1 & -1 \\ -3 & 2 & -3 \end{bmatrix}$$

The determinant is                     

5. (1 point) Evaluate the following  $4 \times 4$  determinant.

$$\begin{vmatrix} 4 & 10 & -1 & -1 \\ 5 & 2 & 6 & 1 \\ 0 & 0 & 1 & 0 \\ 12 & 2 & 5 & -10 \end{vmatrix}$$

Answer:                     

6. (1 point)

The determinant of the matrix

$$A = \begin{bmatrix} 0 & 7 & -3 & 0 & 0 \\ -5 & 9 & -6 & 0 & 0 \\ 0 & -8 & 0 & 0 & 0 \\ -7 & -5 & 2 & 4 & -1 \\ -1 & 8 & 1 & 0 & -3 \end{bmatrix}$$

is                     .

**Hint:** Find a good row or column for cofactor expansion.

7. (1 point)

If  $A$  and  $B$  are  $3 \times 3$  matrices,  $\det(A) = 4$ ,  $\det(B) = -9$ , then

$\det(AB) = \underline{\hspace{2cm}}$ ,

$\det(-2A) = \underline{\hspace{2cm}}$ ,

$\det(A^T) = \underline{\hspace{2cm}}$ ,

$\det(B^{-1}) = \underline{\hspace{2cm}}$ ,

$\det(B^2) = \underline{\hspace{2cm}}$ .

8. (1 point)

$$\text{If } B = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & -1 \\ 2 & 1 & -1 \end{bmatrix}$$

then  $\det(B^5) = \underline{\hspace{2cm}}$

9. (1 point)

If the determinant of a  $4 \times 4$  matrix  $A$  is  $\det(A) = 5$ , and the matrix  $C$  is obtained from  $A$  by swapping the third and fourth rows, then

$\det(C) = \underline{\hspace{2cm}}$ .

10. (1 point)

If the determinant of a  $5 \times 5$  matrix  $A$  is  $\det(A) = 6$ , and the matrix  $D$  is obtained from  $A$  by adding 3 times the third row to the second, then

$\det(D) = \underline{\hspace{2cm}}$ .

11. (1 point) Given the matrix

$$\begin{bmatrix} -3 & -1 & 4 \\ 5 & 0 & 3 \\ 0 & 4 & 3 \end{bmatrix}$$

(a) find its determinant;

Your answer is :                     

(b) does the matrix have an inverse?

Your answer is (input Yes or No) :                     

12. (1 point)

$$\text{If } A = \begin{bmatrix} -5 & 2 & -1 \\ -4 & 1 & 3 \\ 3 & 2 & -3 \end{bmatrix}, \text{ then } \det(A) = \underline{\hspace{2cm}}$$

Is  $A$  invertible?

- A. Yes
- B. No