

Part 2

The Evaluation of Programs

Structure vs. Evaluation

- The data model describes the structure

`23 + 4.5` \longrightarrow `BinOp('+', Integer(23), Float(4.5))`

- Evaluation is about how a program executes
- Semantics

Your Intuitions

- You, as a programmer, have certain intuitions about how programs actually work
- At least I hope so...
- We'll start with that
- Will dig deeper later

Literal Values

- Literals

2
2.3
'c'

- Literals just "are"
- They don't do anything other than exist.

Expressions

- Example: A binary operator (+)

left + right

- You evaluate each side first, then add together

The diagram illustrates the evaluation of the expression $(2*3) + (4*5)$ through four stages, connected by downward arrows:

- Stage 1: $(2*3) + (4*5)$
- Stage 2: $6 + (4*5)$ (The $2*3$ part is evaluated to 6)
- Stage 3: $6 + 20$ (The $4*5$ part is evaluated to 20)
- Stage 4: 26 (The final result of the addition)

- It's a recursive process ("show your work!")
- The final result is a value.

Names/Variables

- Names refer to objects in an environment

```
const pi = 3.14159;  
var r float = 2.0;  
var a = pi * r * r;
```

```
{  
    'pi': 3.14159,  
    'r': 2.0,  
    'a': 12.56636  
}
```

- An environment is a place to store things
- Two core operations: load/store

```
a = 2.0 * pi;           // Loads from "pi". Stores to "a"
```

Statements

- Statements execute one after another

```
result = result * n;  
n = n - 1;  
print result;
```

- Each statement causes some kind of change in the environment (note: includes I/O).
- "Imperative programming"

Conditionals

- if-statement presents two evaluation routes

```
if a < b {  
    max = b;  
} else {  
    max = a;  
}
```

- You evaluate the test first ($a < b$)
- Then, only one branch executes

Loops

- Repeated evaluation of statements

```
while n > 0 {  
    result = result * n;  
    n = n - 1;  
}
```

- You evaluate the test first ($n > 0$)
- If true, evaluate the body and repeat.

Functions

- Consider a function

```
func sum_squares(x int, y int) int {  
    return x*x + y*y;  
}
```

- You evaluate arguments first. Then the body

sum_squares(2+3, 4+5)
↓
sum_squares(5, 4+5)
↓
sum_squares(5, 9)
↓ ↓
5*5 + 9*9
↓ ↓
25 + 9*9
↓ ↓
25 + 81
↓
106

Note: This is not the only way to do it, but most "normal" programming languages work like this.

"Applicative Order"

- Terminology: "Function Application"

Scoping

- Environments are nested/linked

```
const pi = 3.14159;  
  
func area(r float) float {  
    a = pi * r * r;  
    return a;  
}  
  
print area(4.0);
```

Functions can see variables defined in the surrounding definition context.

(lexical scoping)

Globals

```
{  
  'pi': 3.14159,  
  'area': <function>  
}
```

Locals (area)

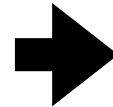
```
{  
  'r': 4.0,  
  'a': 50.26544  
}
```



Structures

- A structure is a container of data

```
struct Point {  
    x int;  
    y int;  
}
```



```
{  
    'x': 2,  
    'y': 3  
}
```

```
p = Point(2, 3);
```

- An instance holds values for all fields
- They're all together in one object
- Precise representation details vary.

Moving Beyond Intuition

- Yes, we have intuitions about how things "work" when we write programs
- Question: How do you turn this into a more formal specification?
- To write a compiler, you need a precise definition of how everything actually works.
- At a fine level of detail (i.e., language lawyer).

Formalizing Semantics

- One approach : Write an interpreter
- Example: Write a program that takes the data model and actually executes it.
- Sole focus: "What does the program do?"
- Sometimes known as a "definitional interpreter."

Definitional Interpreter

```
class BinOp(Expression):  
    def __init__(self, op, left, right):  
        self.op = op  
        self.left = left  
        self.right = right
```

(Model)



(Interpreter)

```
def interpret_binop(node, env):  
    leftval = interpret(node.left, env)  
    rightval = interpret(node.right, env)  
    assert type(leftval) == type(rightval)  
    if node.op == '+':  
        return leftval + rightval  
    elif node.op == '*':  
        return leftval * rightval  
    ...
```

Operational Semantics

- Writing a "definitional interpreter" is an approach taken by language designers and compiler writers in the real world
- They just don't use Python (not usually)
- There is also a mathematical notational that gets used for a similar purpose

Example:

- Semantics of a conditional

(E-IFTRUE) `if true then t2 else t3 \mapsto t2`

(E-IFFALSE) `if false then t2 else t3 \mapsto t3`

(E-IF)
$$\frac{t_1 \mapsto t_1'}{\text{if } t_1 \text{ then } t_2 \text{ else } t_3 \mapsto \text{if } t_1' \text{ then } t_2 \text{ else } t_3}$$

- This is defining "small steps"
- Think of it as defining substitutions.

Example: Wasm



Introduction

Structure

Validation

Execution

- Conventions
- Runtime Structure
- Numerics
- Instructions
- Modules

Binary Format

if blocktype instr₁^{} else instr₂^{*} end*

1. Assert: due to *validation*, $\text{expand}_F(\text{blocktype})$ is defined.
2. Let $[t_1^m] \rightarrow [t_2^n]$ be the function type $\text{expand}_F(\text{blocktype})$.
3. Let L be the label whose arity is n and whose continuation is the end of the *if* instruction.
4. Assert: due to *validation*, a value of *value type i32* is on the top of the stack.
5. Pop the value *i32.const c* from the stack.
6. Assert: due to *validation*, there are at least m values on the top of the stack.
7. Pop the values val^m from the stack.
8. If c is non-zero, then:

a. Enter the block $\text{val}^m \text{instr}_1^*$ with label L .

9. Else:

a. Enter the block $\text{val}^m \text{instr}_2^*$ with label L .

$F; \text{val}^m (\text{i32.const } c) \text{ if } bt \text{ instr}_1^* \text{ else instr}_2^* \text{ end} \hookrightarrow F; \text{label}_n\{\epsilon\} \text{ val}^m \text{ instr}_1^* \text{ end} \quad (\text{if } c \neq 0 \wedge \text{expand}_F(bt) = [t_1^m] \rightarrow [t_2^n])$
 $F; \text{val}^m (\text{i32.const } c) \text{ if } bt \text{ instr}_1^* \text{ else instr}_2^* \text{ end} \hookrightarrow F; \text{label}_n\{\epsilon\} \text{ val}^m \text{ instr}_2^* \text{ end} \quad (\text{if } c = 0 \wedge \text{expand}_F(bt) = [t_1^m] \rightarrow [t_2^n])$

- All of this can be very difficult to read (to me)
- Big Picture: it's describing an interpreter

Project

- Find the file `wabbit/interp.py`
- Follow instructions inside.
- Goal: Can we more precisely define/understand the semantics of Wabbit by writing an interpreter that runs programs directly from the data model?