

Institute of Informatics – Institute of Neuroinformatics

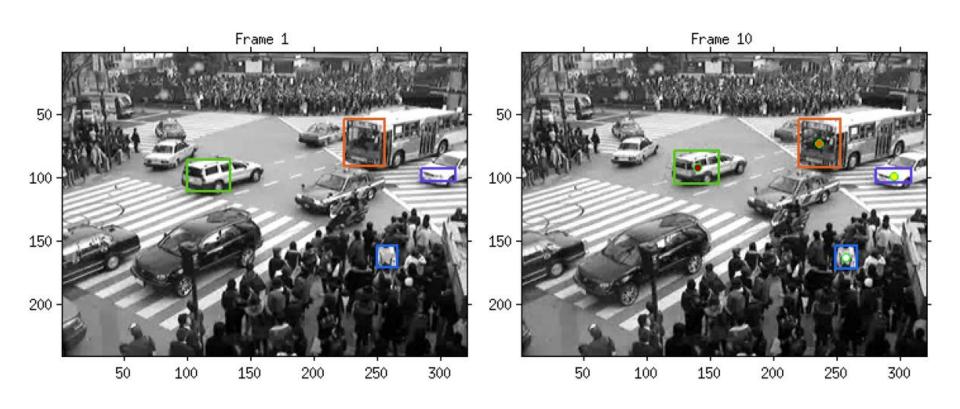


Lecture 11 Tracking

Davide Scaramuzza

Lab Exercise 7 - Today

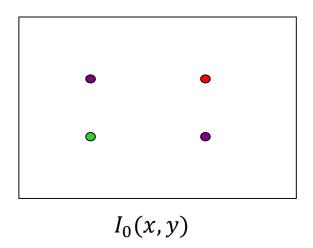
- > Room ETH HG E 1.1 from 13:15 to 15:00
- Work description: Lucas-Kanade template tracking



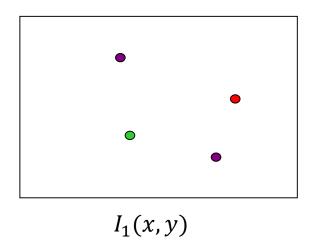
Outline

- Point tracking
- Template tracking
- Tracking by detection of local image features

• **Problem:** given two images, estimate the motion of a pixel point from image I_0 to image I_1



• **Problem:** given two images, estimate the motion of a pixel point from image I_0 to image I_1



Template tracking

• **Problem:** given two images, estimate the warping that defines the motion and/or the distortion of a template from image I_0 to image I_1

Template image

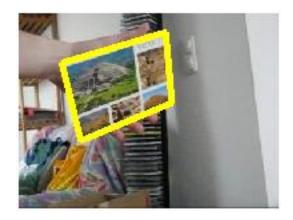




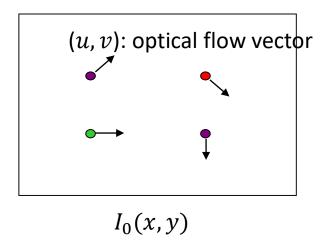






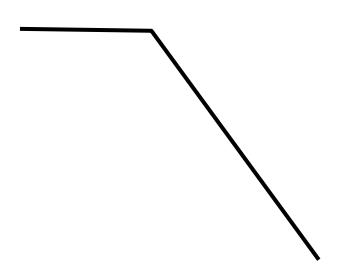


• **Problem:** given two images, estimate the motion of a pixel point from image I_0 to image I_1

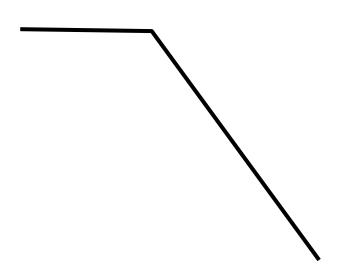


- Two approaches exist, depending on the amount of motion between the frames
 - Block-based methods
 - Differential methods

Consider the motion of the following corner

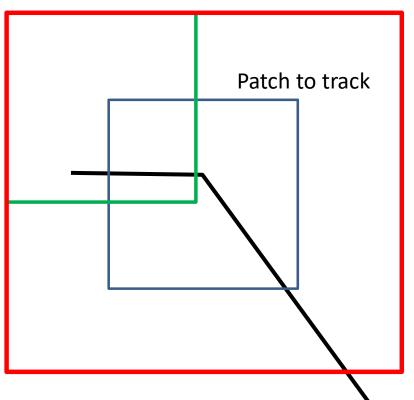


Consider the motion of the following corner



Point Tracking with Block Matching

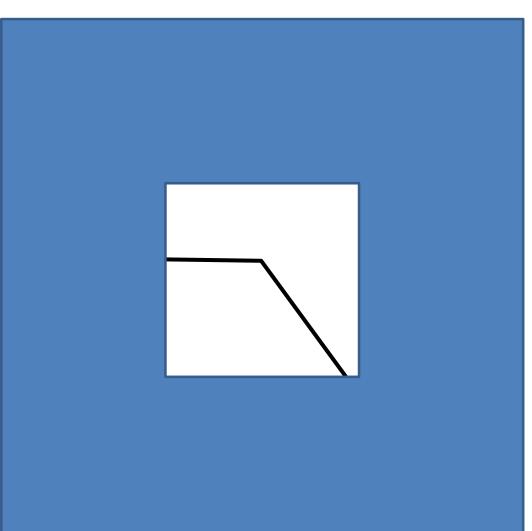
- Search for the corresponding patch in a neighborhood around the point.
- Use SSD, SAD, or NCC to search for corresponding patches in a local neighborhood of the point. The search region is usually a $D \times D$ squared patch.



Search region

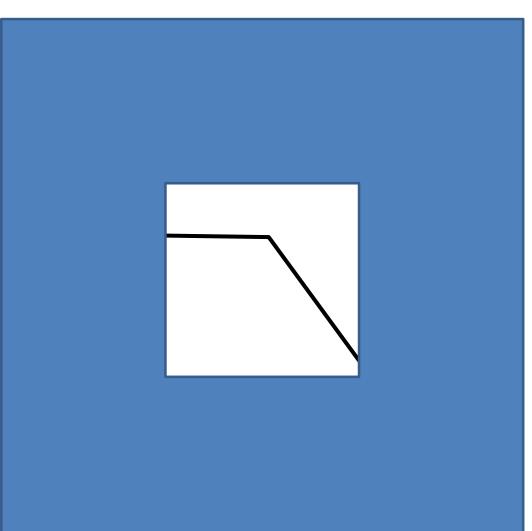
Point Tracking with Differential Methods

• Looks at the local brightness changes at the **same** location. **No patch shift** is performed!



Point Tracking with Differential Methods

• Looks at the local brightness changes at the **same** location. **No patch shift** is performed!



Applying the Spatial Coherency

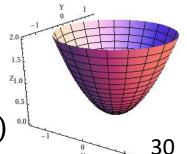
- Assume that all the pixels in the patch undergo the same motion (same u and v) (usually, a square patch of $n \times n$ pixels is used)
- Also, assume that the time interval between the two images I_0 , I_1 is small
- We want to find the motion vector (u, v) that minimizes the Sum of Squared Differences (SSD):

$$SSD = \sum (I_0(x, y) - I_1(x + u, y + v))^2$$

$$\cong \sum (I_0(x, y) - I_1(x, y) - I_x u - I_y v)^2$$

$$= \sum (\Delta I - I_x u - I_y v)^2$$

This is a simple quadratic function in two variables (u, v)



Computing the Motion Vector

$$E=SSD=\sum (\Delta I - I_x u - I_y v)^2$$

• To minimize the E, we differentiate E with respect to (u,v) and equate it to zero

$$\frac{\partial E}{\partial u} = 0$$
 , $\frac{\partial E}{\partial v} = 0$

$$\frac{\partial E}{\partial u} = 0 \implies -2\sum_{x} I_{x}(\Delta I - I_{x}u - I_{y}v) = 0$$

$$\frac{\partial E}{\partial v} = 0 \implies -2\sum_{x} I_{y} (\Delta I - I_{x} u - I_{y} v) = 0$$

Computing the Motion Vector

$$\frac{\partial E}{\partial u} = 0 \implies -2\sum_{x} I_{x}(\Delta I - I_{x}u - I_{y}v) = 0$$

$$\frac{\partial E}{\partial v} = 0 \implies -2\sum_{x} I_{y}(\Delta I - I_{x}u - I_{y}v) = 0$$

- Linear system of two equations in two unknowns
- We can write them in matrix form:

$$\begin{bmatrix} \sum I_{x}I_{x} & \sum I_{x}I_{y} \\ \sum I_{x}I_{y} & \sum I_{y}I_{y} \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = \begin{bmatrix} \sum I_{x}\Delta I \\ \sum I_{y}\Delta I \end{bmatrix}$$

Ve can write them in matrix form:
$$\begin{bmatrix} \sum I_x I_x & \sum I_x I_y \\ \sum I_x I_y & \sum I_y I_y \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = \begin{bmatrix} \sum I_x \Delta I \\ \sum I_y \Delta I \end{bmatrix}$$

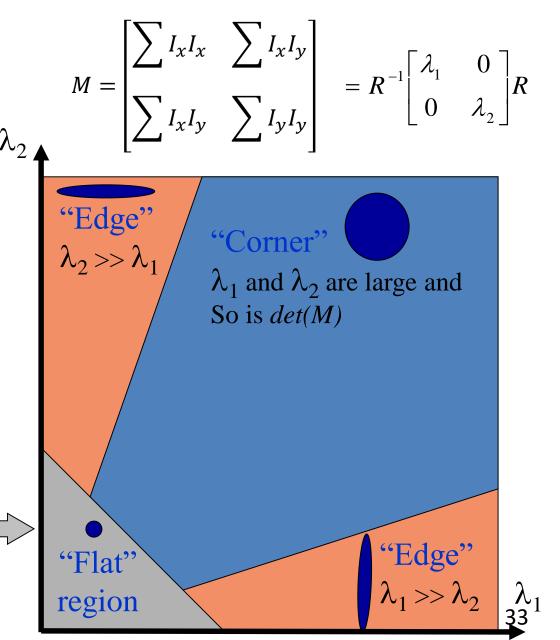
$$\Rightarrow \begin{bmatrix} u \\ v \end{bmatrix} = \begin{bmatrix} \sum I_x I_x & \sum I_x I_y \\ \sum I_y \Delta I \end{bmatrix}$$

M matrix Haven't we seen this matrix already?

For M to be invertible, its determinant has to be non zero

 In practice, det(M) should be non zero, which means that its eigenvalues should be large (i.e., not a flat region, not an edge) -> in practice, it should be a corner or more generally contain texture!

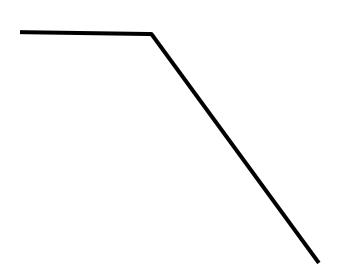
 λ_1 and λ_2 are small



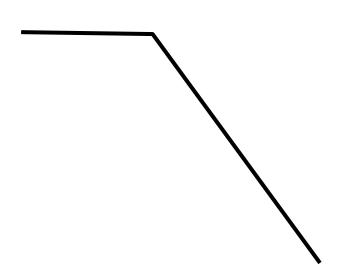
Point Tracking Edge – Low texture – High texture



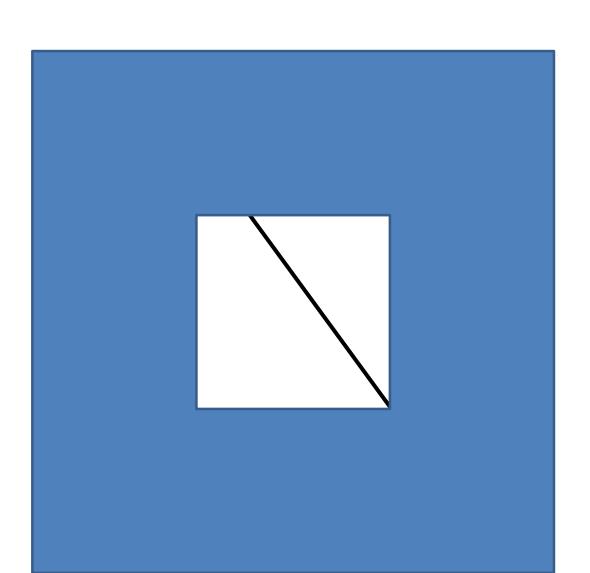
Consider the motion of the following corner



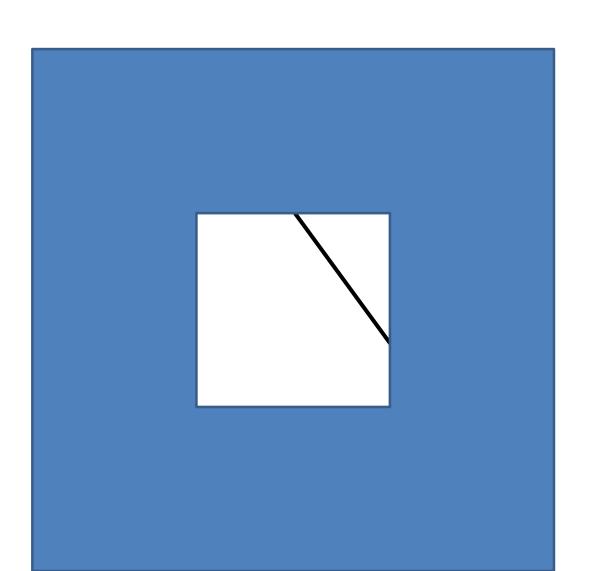
Consider the motion of the following corner



Now, look at the local brightness changes through a small aperture



Now, look at the local brightness changes through a small aperture

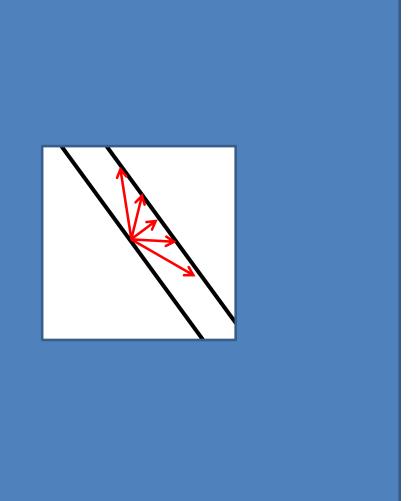


Now, look at the local brightness changes through a small aperture

We cannot always determine the motion direction -> Infinite motion

solutions may exist!

Solution?

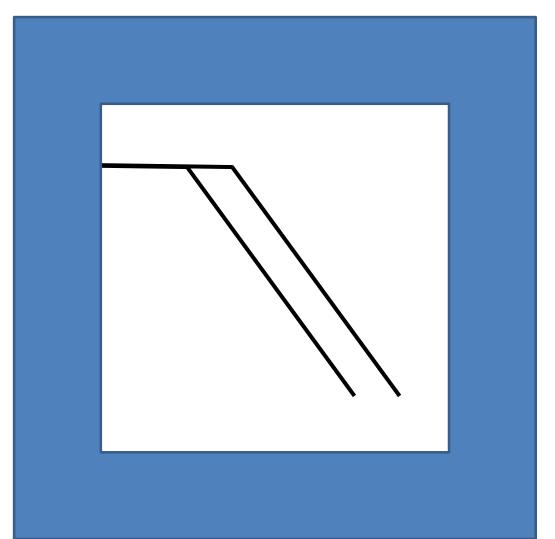


Now, look at the local brightness changes through a small aperture

We cannot always determine the motion direction -> Infinite motion

solutions may exist!

Solution? Increase aperture size!

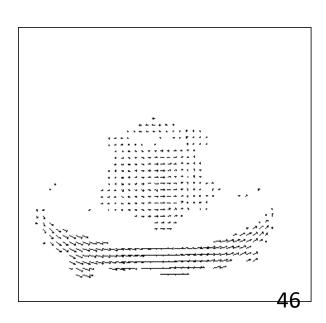


Application of Differential Methods: Optical Flow

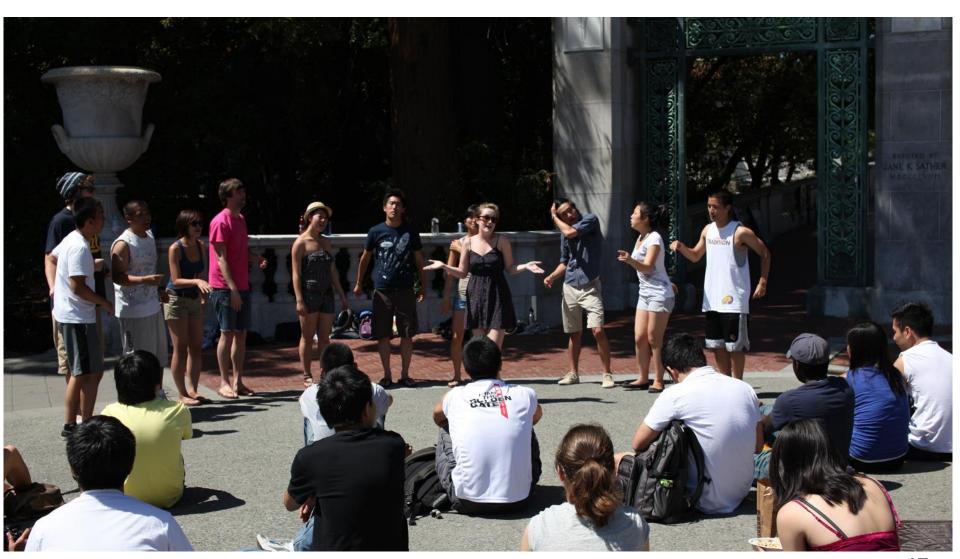
- Optical flow or optic flow is the pattern of apparent motion of objects in a visual scene caused by the relative motion between the observer (an eye or a camera) and the scene
- Tracks the motion of every pixels (or a grid of pixels) between two consecutive frames
- For each pixel, a motion vector is computed:
 - Vector direction represents motion direction
 - Vector length represents the amount of movement





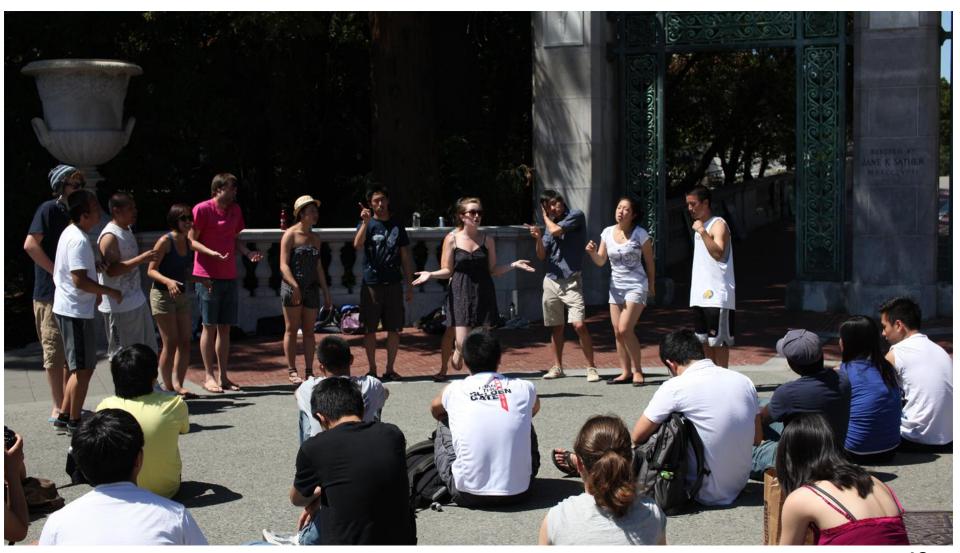


Optical Flow



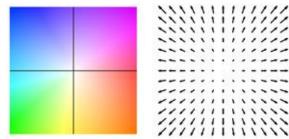
[Tao et al., Eurographics 2012]

Optical Flow



[Tao et al., Eurographics 2012]

Optical Flow





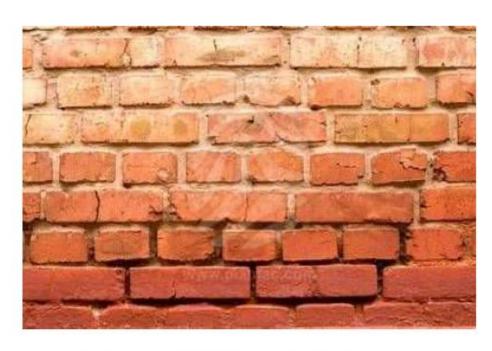
Optical Flow example



Optical flow issue: choosing the right patch size









Application to Corner Tracking

Color encodes motion direction



Block-based vs. Differential methods

• Block-based methods: search for the corresponding patch in a neighborhood of the point to be tracked. The search region is usually a square of $n \times n$ pixels.



Robust to large motions



Can be **computationally expensive** ($n \times n$ validations need to be made for a single point to track)

Differential methods:



Works only for **small motions** (e.g., high frame rate). For larger motion, multiscale implementations are used but are more expensive

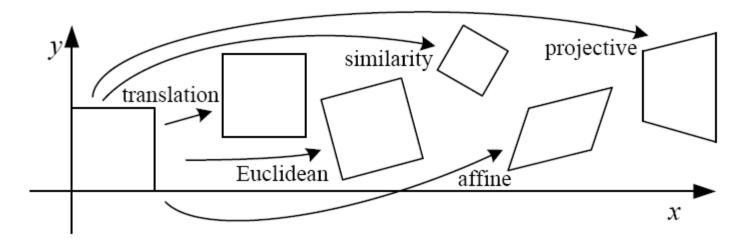


Much more **efficient** than block-based methods. Thus, can be used to track the motion of every pixel in the image (i.e., optical flow). It avoids searching in the neighborhood of the point by analyzing the **local intensity changes** (i.e., differences) of an image patch at a **specific location** (i.e., no search is performed).

Outline

- What is Tracking?
- Point tracking
- Review of 2D image transformations and Jacobians
- Template tracking
- Tracking by detection of local image features

Transformations – 2D



Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$egin{bmatrix} ig[egin{array}{c c} I & t \end{bmatrix}_{2 imes 3} \end{array}$	2	orientation $+ \cdots$	
rigid (Euclidean)	$\left[egin{array}{c c} R & t\end{array} ight]_{2 imes 3}$	3	lengths + · · ·	\Diamond
similarity	$\left[\begin{array}{c c} sR \mid t\end{array}\right]_{2 imes 3}$	4	angles +···	\Diamond
affine	$\left[egin{array}{c} oldsymbol{A} \end{array} ight]_{2 imes 3}$	6	parallelism + · · ·	
projective	$\left[egin{array}{c} ilde{m{H}} \end{array} ight]_{3 imes 3}$	8	straight lines	

Summary of displacement models (2D transformations)

• Translation
$$x' = x + a_1$$

 $y' = y + a_2$

• Euclidean
$$x' = xcos(a_3) - ysin(a_3) + a_1$$
$$y' = xsin(a_3) + ycos(a_3) + a_2$$

• Affine
$$x' = a_1 x + a_3 y + a_5$$

$$y' = a_2 x + a_4 y + a_6$$

• Projective (homography)
$$x' = \frac{a_1x + a_2y + a_3}{a_7x + a_8y + 1}$$
$$y' = \frac{a_4x + a_5y + a_6}{a_7x + a_8y + 1}$$

Summary of displacement models (2D transformations)

We call the transformation Warping W(\mathbf{x} , \mathbf{p}) and \mathbf{p} the set of parameters $p = (a_1, a_2, ..., a_n)$

• Translation
$$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} x + a_1 \\ y + a_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & a_1 \\ 0 & 1 & a_2 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
 Homogeneous coordinates

• Euclidean
$$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} x\cos(a_3) - y\sin(a_3) + a_1 \\ x\sin(a_3) + y\cos(a_3) + a_2 \end{bmatrix} = \begin{bmatrix} ca_3 & -sa_3 & a_1 \\ sa_3 & ca_3 & a_2 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

• Affine
$$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} a_1 x + a_3 y + a_5 \\ a_2 x + a_4 y + a_6 \end{bmatrix} = \begin{bmatrix} a_1 & a_3 & a_5 \\ a_2 & a_4 & a_6 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

• Projective
$$W(\widetilde{\mathbf{x}}, \mathbf{p}) = \begin{bmatrix} a_1 & a_2 & a_3 \\ a_4 & a_5 & a_6 \\ a_7 & a_8 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Summary of displacement models (2D transformations)

Name	Matrix	# D.O.F.	Preserves:	Icon	
translation	$ig[egin{array}{c c} I & t \end{bmatrix}_{2 imes 3}$	2	orientation + · · ·		$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} 1 & 0 & a_1 \\ 0 & 1 & a_2 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$
rigid (Euclidean)	$\left[egin{array}{c c} R & t\end{array} ight]_{2 imes 3}$	3	lengths + · · ·	\Diamond	$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} ca_3 & -sa_3 & a_1 \\ sa_3 & ca_3 & a_2 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \\ Tx \end{bmatrix}$
similarity	$\begin{bmatrix} sR \mid t \end{bmatrix}_{2 \times 3}$		angles +···	\Diamond	$W(\mathbf{x}, \mathbf{p}) = \lambda \begin{bmatrix} ca_3 & -sa_3 & a_1 \\ sa_3 & ca_3 & a_2 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$
affine	$\left[egin{array}{c} A \end{array} ight]_{2 imes 3}$	6	parallelism + · · ·		$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} a_1 & a_3 & a_5 \\ a_2 & a_4 & a_6 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$
projective	$\left[egin{array}{c} ilde{m{H}} \end{array} ight]_{3 imes 3}$	8	straight lines		$ W(\widetilde{\mathbf{x}}, \mathbf{p}) = \begin{bmatrix} a_1 & a_2 & a_3 \\ a_4 & a_5 & a_6 \\ a_7 & a_8 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} $

Derivative and gradient

- Function: f(x)
- Derivative: $f'(x) = \frac{df}{dx}$, where x is a scalar

- Function: $f(x_1, x_2, ..., x_n)$
- Gradient: $\nabla f(x_1, x_2, ..., x_n) = \left(\frac{\partial f}{\partial x_1}, \frac{\partial f}{\partial x_2}, ..., \frac{\partial f}{\partial x_n}\right)$

Jacobian

•
$$F(x_1, x_2, ..., x_n) = \begin{bmatrix} f_1(x_1, x_2, ..., x_n) \\ \vdots \\ f_m(x_1, x_2, ..., x_n) \end{bmatrix}$$

Vector-valued function

Derivative?

$$J(F) = \nabla F = \begin{bmatrix} \frac{\partial f_1}{\partial x_1}, \dots, \frac{\partial f_1}{\partial x_n} \\ \vdots \\ \frac{\partial f_m}{\partial x_1}, \dots, \frac{\partial f_m}{\partial x_n} \end{bmatrix}$$



Carl Gustav Jacob (1804-1851)

Displacement-model Jacobians

$$\nabla W_p$$

$$p = (a_1, a_2, \dots, a_n)$$

Translation

$$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} x + a_1 \\ y + a_2 \end{bmatrix} \quad \nabla W_p = \begin{bmatrix} \frac{\partial W_1}{\partial a_1} & \frac{\partial W_1}{\partial a_2} \\ \frac{\partial W_2}{\partial a_1} & \frac{\partial W_2}{\partial a_2} \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

Euclidean

$$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} x\cos(a_3) - y\sin(a_3) + a_1 \\ x\sin(a_3) + y\cos(a_3) + a_2 \end{bmatrix} \quad \forall W_p = \begin{bmatrix} 1 & 0 & -x\sin(a_3) - y\cos(a_3) \\ 0 & 1 & x\cos(a_3) - y\sin(a_3) \end{bmatrix}$$

Affine

$$W(\mathbf{x}, \mathbf{p}) = \begin{bmatrix} a_1 x + a_3 y + a_5 \\ a_2 x + a_4 y + a_6 \end{bmatrix} \qquad \nabla W_p = \begin{bmatrix} x & 0 & y & 0 & 1 & 0 \\ 0 & x & 0 & y & 0 & 1 \end{bmatrix}$$

Outline

- What is Tracking?
- Point tracking
- Review of 2D image transformations and Jacobians
- Template tracking: Lucas-Kanade algorithm
- Tracking by detection of local image features

Template tracking

Definition: follow a template image in a video sequence by estimating the warp

Template image

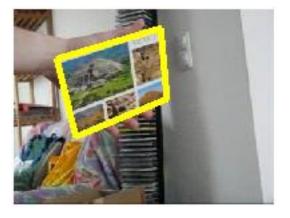




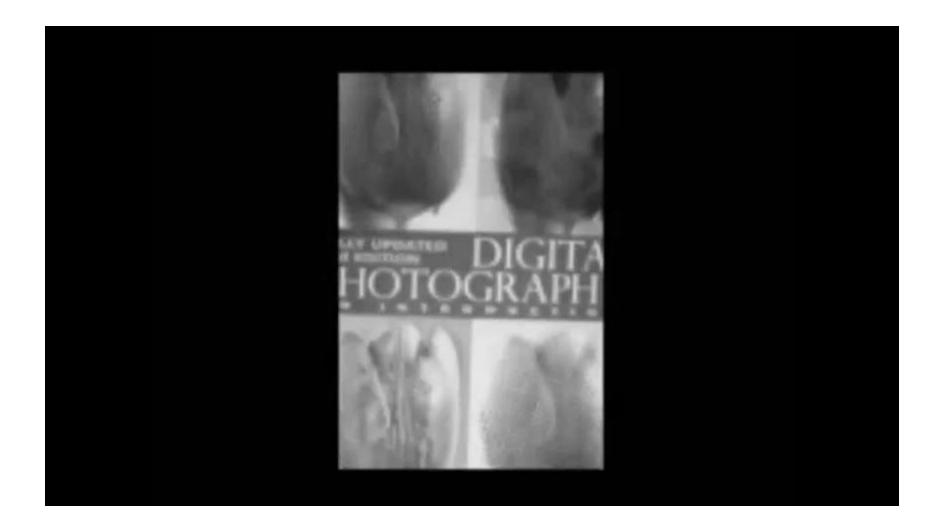








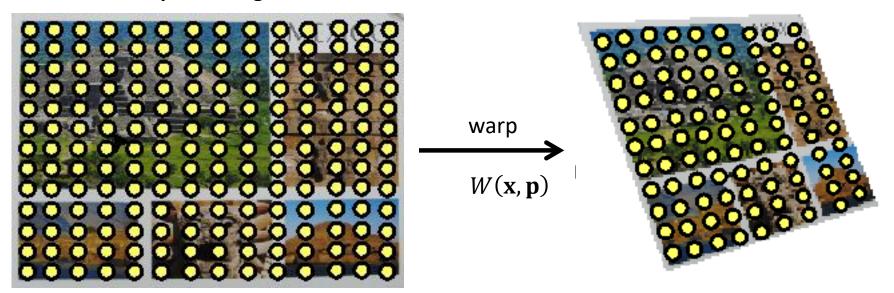
The Lucas-Kanade tracker



Template warping

- Given the template image $T(\mathbf{x})$
- Take all pixels from the template image $T(\mathbf{x})$ and warp them using the function $W(\mathbf{x}, \mathbf{p})$ parameterized in terms of parameters \mathbf{p}

Template image



 $T(\mathbf{x})$

 $I(\tilde{x})$

Template Tracking: Problem Formulation

The goal of template-based tracking is to find the set of warp parameters
 p such that:

$$I(W(\mathbf{x}, \mathbf{p})) = T(\mathbf{x})$$

This is solved by determining **p** that minimizes the Sum of Squared Differences

$$E = SSD = \sum_{\mathbf{x} \in \mathbf{T}} [I(W(\mathbf{x}, \mathbf{p})) - T(\mathbf{x})]^{2}$$

Assumptions

- No errors in the template image boundaries: only the appearance of the object to be tracked appears in the template image
- No occlusion: the entire template is visible in the input image
- Brightness constancy assumption: the intensity of the object appearance is always the same across different views







The Lucas-Kanade tracker

- Uses the Gauss-Newton method for minimization, that is:
 - Applies a first-order approximation of the warp
 - Attempts to minimize the SSD iteratively

$$E = \sum_{\mathbf{x} \in \mathbf{T}} [I(W(\mathbf{x}, \mathbf{p})) - T(\mathbf{x})]^{2}$$

How do I get the initial estimate?

Assume that an initial estimate of ${f p}$ is known. Then, we want to find the increment $\Delta {f p}$ that minimizes

$$\sum_{\mathbf{x} \in \mathbf{T}} \left[I(W(\mathbf{x}, \mathbf{p} + \Delta \mathbf{p})) - T(\mathbf{x}) \right]^{2}$$

• First-order Taylor approximation of $I(W(\mathbf{x}, \mathbf{p} + \Delta \mathbf{p}))$ yelds to:

$$I(W(\mathbf{x}, \mathbf{p} + \Delta \mathbf{p})) \cong I(W(\mathbf{x}, \mathbf{p})) + \nabla I \frac{\partial W}{\partial \mathbf{p}} \Delta \mathbf{p}$$

 $\nabla I = [I_x, I_y] = \text{Image gradient evaluated at } W(\mathbf{x}, \mathbf{p})$ Jacobian of the warp $W(\mathbf{x}, \mathbf{p})$

$$E = \sum_{\mathbf{x} \in \mathbf{T}} [I(W(\mathbf{x}, \mathbf{p} + \Delta \mathbf{p})) - T(\mathbf{x})]^{2}$$

• By replacing $I(W(\mathbf{x}, \mathbf{p} + \Delta \mathbf{p}))$ with its 1st order approximation, we get

$$E = \sum_{\mathbf{x} \in \mathbf{T}} \left[I(W(\mathbf{x}, \mathbf{p})) + \nabla I \frac{\partial W}{\partial \mathbf{p}} \Delta \mathbf{p} - T(\mathbf{x}) \right]^{2}$$

- How do we minimize it?
- We differentiate E with respect to $\Delta {f p}$ and we equate it to zero, i.e.,

$$\frac{\partial E}{\partial \Delta \mathbf{p}} = 0$$

$$E = \sum_{\mathbf{x} \in \mathbf{T}} \left[I(W(\mathbf{x}, \mathbf{p})) + \nabla I \frac{\partial W}{\partial \mathbf{p}} \Delta \mathbf{p} - T(\mathbf{x}) \right]^{2}$$

$$\frac{\partial E}{\partial \Delta \mathbf{p}} = 2 \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathrm{T}} \left[I(W(\mathbf{x}, \mathbf{p})) + \nabla I \frac{\partial W}{\partial \mathbf{p}} \Delta \mathbf{p} - T(\mathbf{x}) \right]$$

$$\frac{\partial E}{\partial \Delta \mathbf{p}} = 0$$

$$2\sum_{\mathbf{r}\in\mathbf{T}}\left[\nabla I\frac{\partial W}{\partial \mathbf{p}}\right]^{\mathrm{T}}\left[I(W(\mathbf{x},\mathbf{p}))+\nabla I\frac{\partial W}{\partial \mathbf{p}}\Delta\mathbf{p}-T(\mathbf{x})\right]=0 \Rightarrow$$

$$\Rightarrow \Delta \mathbf{p} = H^{-1} \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathrm{T}} \left[T(\mathbf{x}) - I(W(\mathbf{x}, \mathbf{p})) \right] =$$

$$H = \sum_{\mathbf{v} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathrm{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]$$

Second moment matrix (Hessian) of the warped image

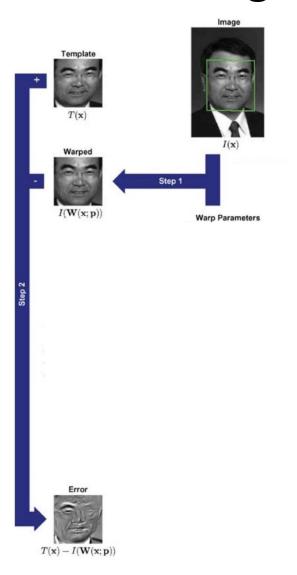
What does H look like when the warp is a pure translation?

Lucas-Kanade algorithm

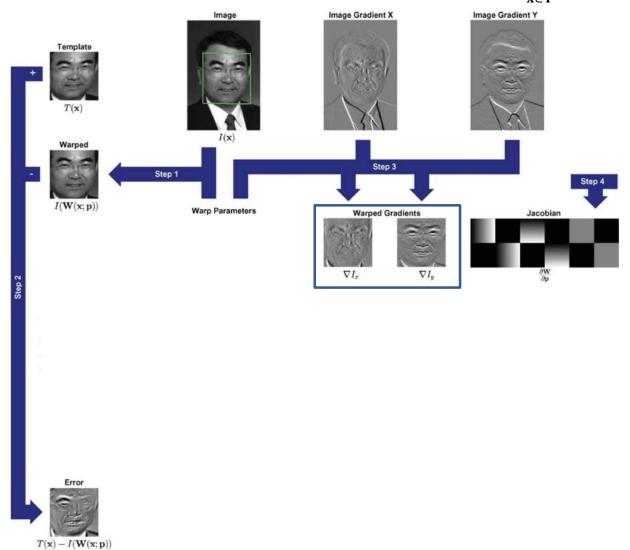
$$\Rightarrow \Delta \mathbf{p} = H^{-1} \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathrm{T}} \left[T(\mathbf{x}) - I(W(\mathbf{x}, \mathbf{p})) \right]$$

- 1. Warp $I(\mathbf{x})$ with $W(\mathbf{x}, \mathbf{p}) \rightarrow I(W(\mathbf{x}, \mathbf{p}))$
- 2. Compute the error: subtract $I(W(\mathbf{x}, \mathbf{p}))$ from $T(\mathbf{x})$
- 3. Compute warped gradients: $\nabla I = [I_x, I_y]$, evaluated at $W(\mathbf{x}, \mathbf{p})$
- 4. Evaluate the Jacobian of the warping: $\frac{\partial W}{\partial \mathbf{p}}$
- 5. Compute steepest descent: $\nabla I \frac{\partial W}{\partial \mathbf{p}}$
- 6. Compute Inverse Hessian: $H^{-1} = \left[\sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathrm{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right] \right]^{-1}$
- 7. Multiply steepest descend with error: $\sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathsf{T}} \left[T(\mathbf{x}) I(W(\mathbf{x}, \mathbf{p})) \right]$
- 8. Compute $\Delta \mathbf{p}$
- 9. Update parameters: $\mathbf{p} \leftarrow \mathbf{p} + \Delta \mathbf{p}$
- 10. Repeat until $\Delta \mathbf{p} < \boldsymbol{\varepsilon}$

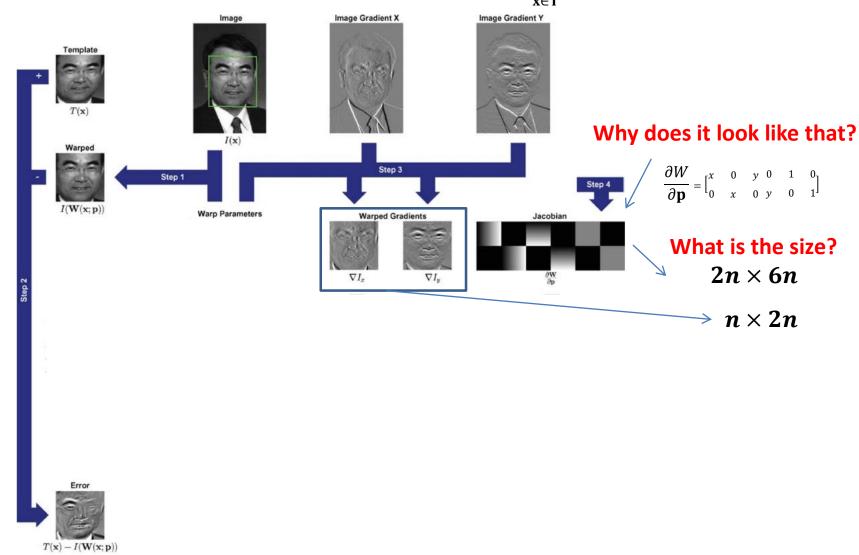
$$\Delta \mathbf{p} = H^{-1} \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{1} \left[T(\mathbf{x}) - I(W(\mathbf{x}, \mathbf{p})) \right]$$



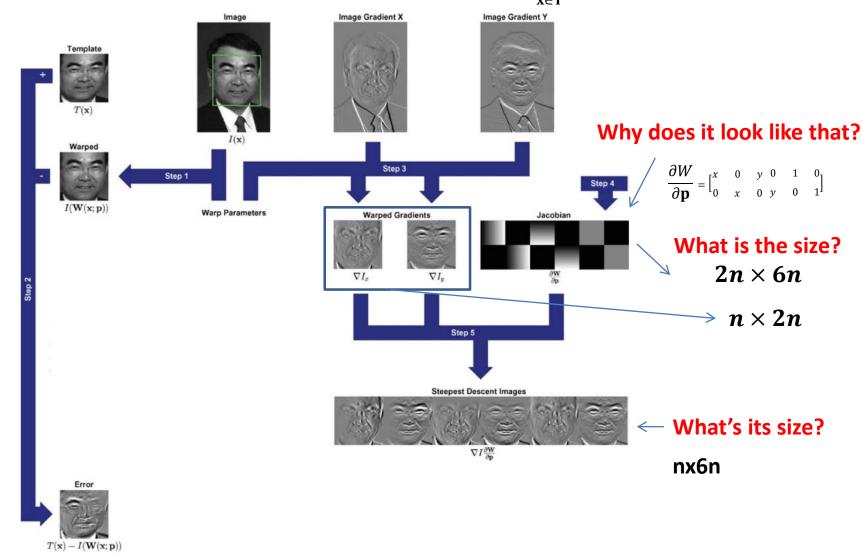
$$\Delta \mathbf{p} = H^{-1} \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{1} \left[T(\mathbf{x}) - I(W(\mathbf{x}, \mathbf{p})) \right]$$



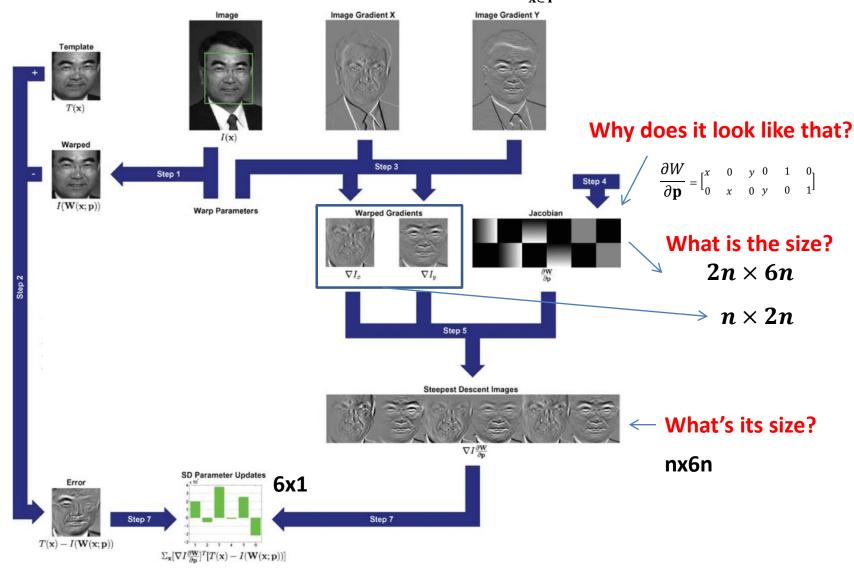
$$\Delta \mathbf{p} = H^{-1} \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{1} \left[T(\mathbf{x}) - I(W(\mathbf{x}, \mathbf{p})) \right]$$



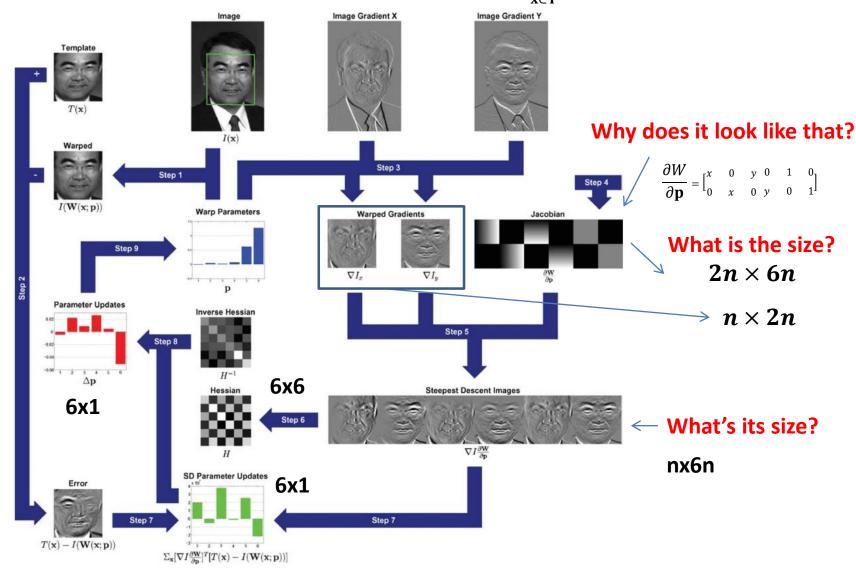
$$\Delta \mathbf{p} = H^{-1} \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathrm{T}} \left[T(\mathbf{x}) - I(W(\mathbf{x}, \mathbf{p})) \right]$$



$$\Delta \mathbf{p} = H^{-1} \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathrm{T}} \left[T(\mathbf{x}) - I(W(\mathbf{x}, \mathbf{p})) \right]$$



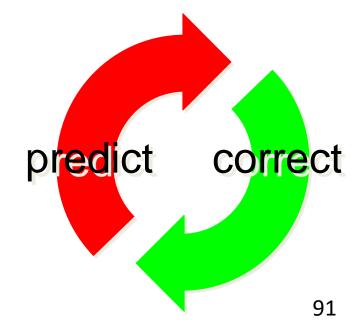
$$\Delta \mathbf{p} = H^{-1} \sum_{\mathbf{x} \in \mathbf{T}} \left[\nabla I \frac{\partial W}{\partial \mathbf{p}} \right]^{\mathrm{T}} \left[T(\mathbf{x}) - I(W(\mathbf{x}, \mathbf{p})) \right]$$



Lucas-Kanade algorithm: Discussion

Lucas-Kanade follows a *predict-correct* cycle

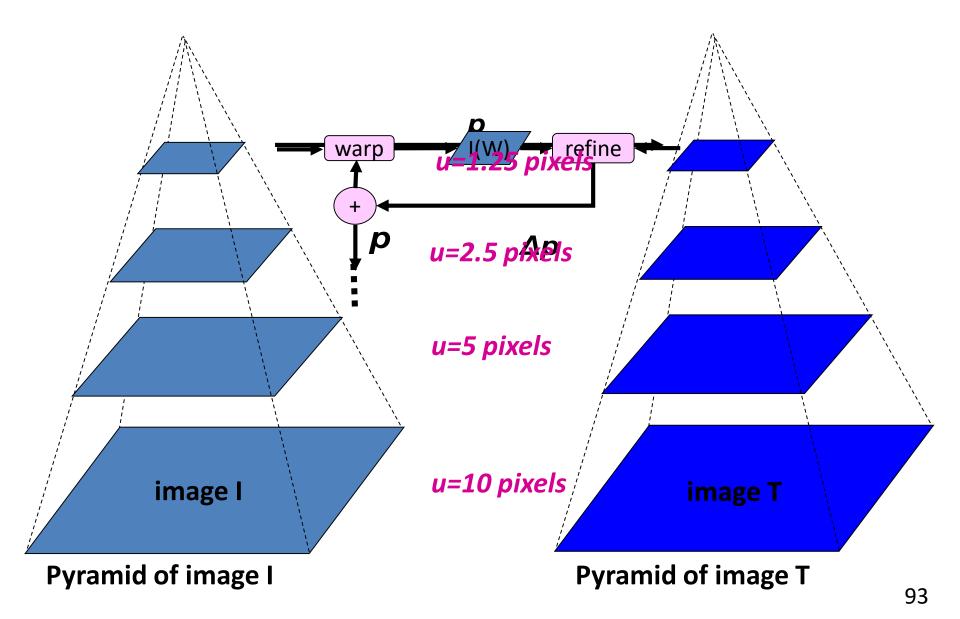
- A prediction $I(W(\mathbf{x}, \mathbf{p}))$ of the warped image is computed from an initial estimate
- The *correction* parameter $\Delta \mathbf{p}$ is computed as a function of the error $T(\mathbf{x})$
 - $-I(W(\mathbf{x},\mathbf{p}))$ between the prediction and the template
- The larger this error, the larger the correction applied



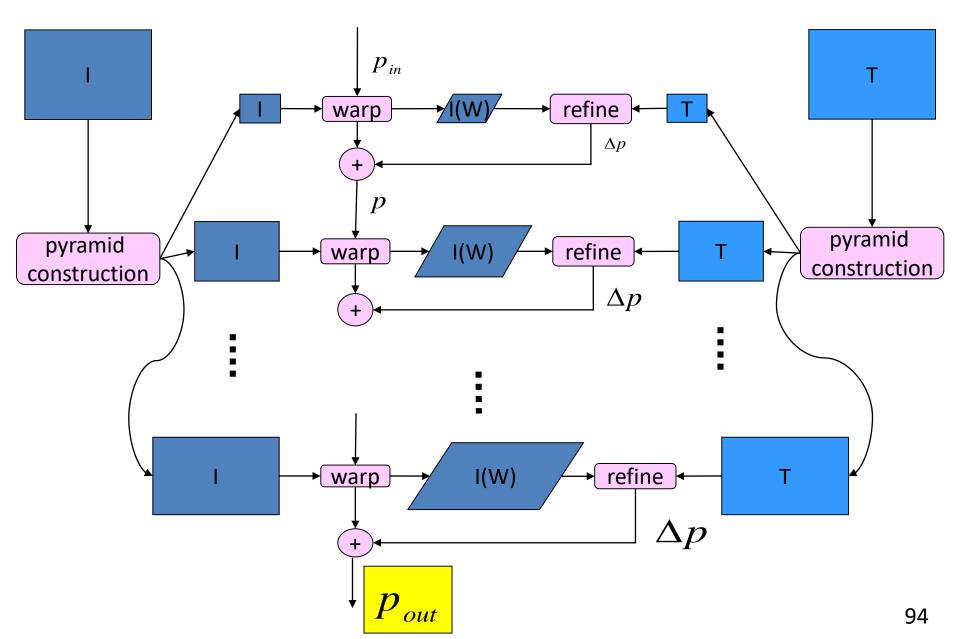
Lucas-Kanade algorithm: Discussion

- How to get the initial estimate p?
- When does the Lucas-Kanade fail?
 - If the initial estimate is too far, then the linear approximation does not longer hold -> solution?
 - Pyramidal implementations (see next slide)
- Other problems:
 - Deviations from the mathematical model: object deformations, illumination changes, etc.
 - Occlusions
 - Due to these reasons, tracking may drift -> solution?
 - Update the template with the last image

Coarse-to-fine estimation



Coarse-to-fine estimation



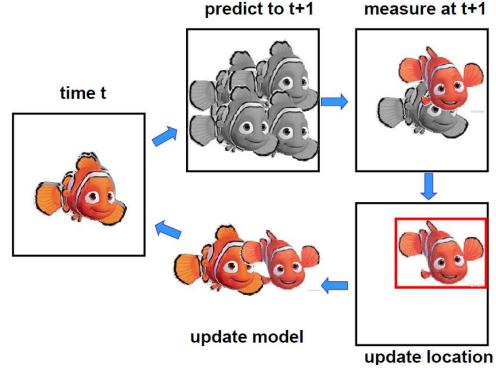
Generalization of Lucas-Kanade

 The same concept (predict/correct) can be applied to tracking of 3D object (in this case, what is the transformation to etimate? What is the template?)



Generalization of Lucas-Kanade

- The same concept (predict/correct) can be applied to tracking of 3D object (in this case, what is the transformation to etimate? What is the template?)
- In order to deal with wrong prediction, it can be implemented in a Particle-Filter fashion (using multiple hipotheses that need to be validated)

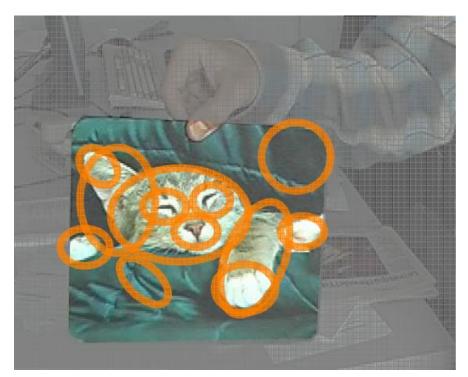


Outline

- Point tracking
- Template tracking
- Tracking by detection of local image features

Step 1: Keypoint detection and matching

invariant to scale, rotation, or perspective



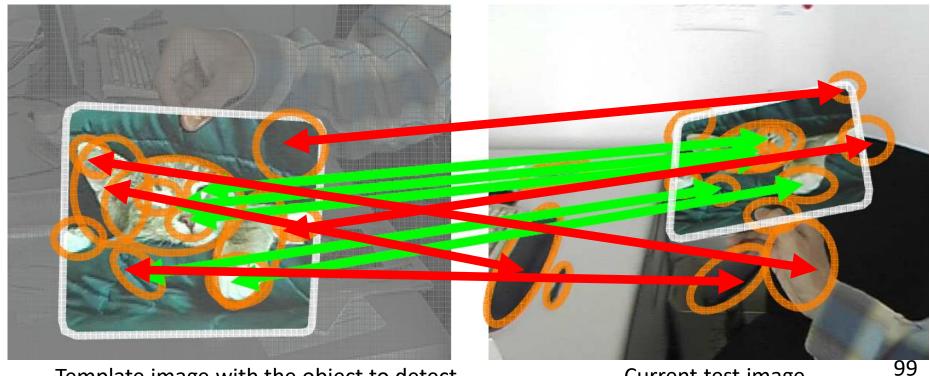
Template image with the object to detect



Current test image

Step 1: Keypoint detection and matching

invariant to scale, rotation, or perspective



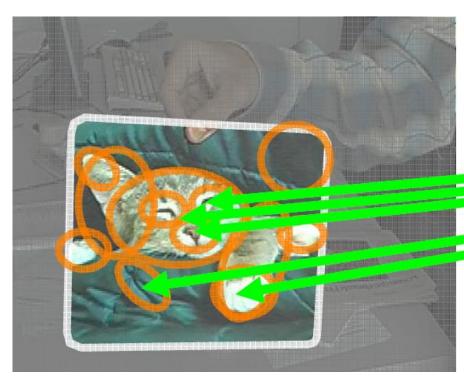
Template image with the object to detect

Current test image

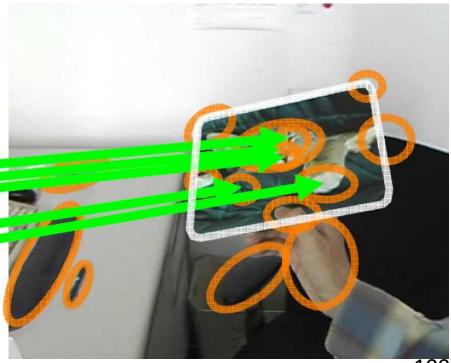
Step 1: Keypoint detection and matching

invariant to scale, rotation, or perspective

Step 2: Geometric verification (RANSAC)

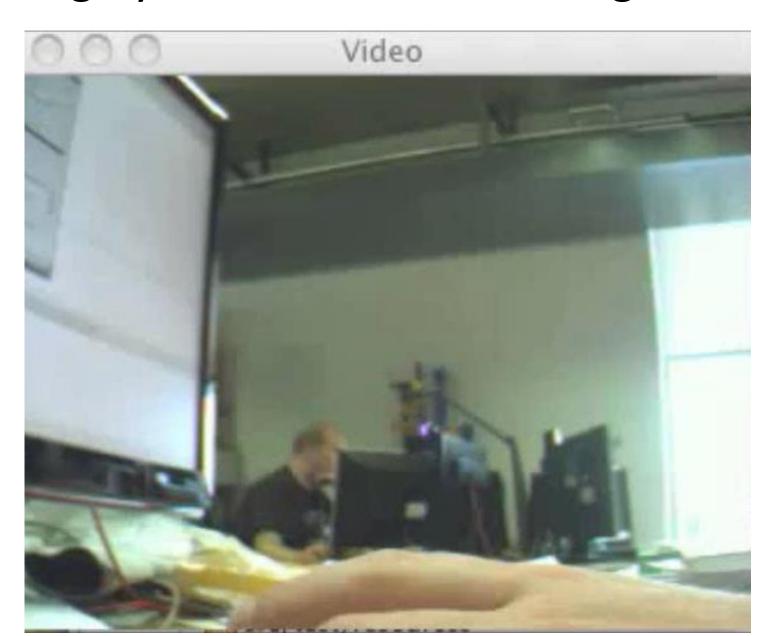


Template image with the object to detect



Current test image

100



Tracking issues

How to segment the object to track from background?



- How to initialize the warping?
- How to handle occlusions



How to handle illumination changes and non modeled effects?

References

- Chapter 8 of Szeliski's book
- Original paper: B. D. Lucas and T. Kanade (1981), <u>An iterative image</u>
 registration technique with an application to stereo vision. Proceedings of
 Imaging Understanding Workshop, pages 121—130
- Baker, Matthews, "<u>Lucas-Kanade 20 Years On: A Unifying Framework</u>", IJCV, 2004.

Implementations

OpenCV implementation :

http://docs.opencv.org/modules/video/doc/motion analysis and object tracking.html?highlight=lucas%20kanade

Some Matlab implementations:

- Lucas Kanade with Pyramid
 http://www.mathworks.com/matlabcentral/fileexchange/30822
- Affine tracking:

http://www.mathworks.com/matlabcentral/fileexchange/24677-lucas-kanade-affine-template-tracking
http://vision.eecs.ucf.edu/Code/Optical Flow/Lucas%20Kanade.zip