

# Artificial Intelligence

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Grupo de Inteligencia Artificial

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## Probabilistic Reasoning – Exercises

## Exercise 1: full joint distribution

A dentist registered the following information for a total of 1000 patients. These data relates toothache, cavity and catch (the dentist's nasty steel probe catches in the tooth)

	toothache		$\neg$ toothache	
	catch	$\neg$ catch	catch	$\neg$ catch
cavity	108	12	72	8
$\neg$ cavity	16	64	144	576

- What is the full joint distribution?
- What is the probability that a patient has a cavity,  $P(\text{cavity})$ ?
- What is the probability of a catch and the patient has not toothache,  $P(\neg\text{toothache}, \text{catch})$ ?
- We know a patient has toothache. What is the probability of cavity?

## Exercise 2:

- After your yearly checkup, the doctor has bad news and good news. The bad news is that you tested positive for a serious disease and that the test is 99% accurate (i.e., the probability of testing positive when you do have the disease is 0.99, as is the probability of testing negative when you don't have the disease). The good news is that this is a rare disease, striking only 1 in 10,000 people of your age. Why is it good news that the disease is rare? What are the chances that you actually have the disease?

## Exercise 3:

- In Barcelona, 51 % of the adults are males. (It doesn't take too much advanced mathematics to deduce that the other 49 % are females.) One adult is randomly selected for a survey involving credit card usage.
  - ① Find the prior probability that the selected person is a male.
  - ② It is later learned that the selected survey subject was smoking a cigar. Also, 9.5 % of males smoke cigars, whereas 1.7 % of females smoke cigars (based on data from the Substance Abuse and Mental Health Services Administration). Use this additional information to find the probability that the selected subject is a male.

## Exercise 4

- ▶ Company A makes 80 % of a product, the Company B makes 15 % of them, and Company C makes the other 5 %. The products made by Company A have a 4 % rate of defects, the Company B products have a 6 % rate of defects, and the Company C products have a 9 % rate of defects (which helps to explain why Company C has the lowest market share).
  - ❶ If a product is randomly selected from the general population of all products, find the probability that it was made by the Company A.
  - ❷ If a randomly selected product is then tested and is found to be defective, find the probability that it was made by the Company A.

## Exercise 5

- ▶ A couple has four children. The general probability of having a male child is 50 %.
  - ① What is the probability that the four children are the same sex?
  - ② What is the probability that only two children are men?
  - ③ What is the probability that at least two children are male?