

**Linear Spectroscopic Studies of Semiconductor Quantum  
Wells**

by

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Linear Spectroscopic Studies of Semiconductor Quantum Wells  
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Linear Spectroscopic Studies of Semiconductor Quantum Wells

Thesis directed by Prof. Steven Cundiff

Manufacturing processes unintentionally introduce fluctuations in the width of semiconductor quantum wells. These fluctuations subtly modulate the optical emission energies of excitons confined within the quantum well layer. It is therefore imperative to quantify these width fluctuations so their effect on exciton confinement potentials can be accounted for in ultrafast spectroscopic studies of semiconductor quantum wells. The use of microphotoluminescence spectroscopy makes quantifying this disorder possible. I present microphotoluminescence spectroscopy work taken in pursuit of an Honors' thesis.

## Dedication

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## Acknowledgements

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## Contents

Chapter	
<b>1</b>	<b>Introduction</b> <span style="float: right;">1</span>
<b>2</b>	<b>Theory and Background</b> <span style="float: right;">4</span>
2.1	The Semiconductor Quantum Well . . . . . 4
2.1.1	Bandgap . . . . . 4
2.1.2	Confinement . . . . . 7
2.1.3	The Exciton . . . . . 11
2.2	Quantum Well Disorder . . . . . 13
2.3	Microphotoluminescence Spectroscopy . . . . . 16
2.4	Exciton Coupling in Asymmetric Double Quantum Wells . . . . . 19
2.5	Photoluminescence Excitation Spectroscopy . . . . . 19
<b>3</b>	<b>Experimental Methods</b> <span style="float: right;">20</span>
3.1	The Light Source . . . . . 20
3.2	Optical Components and Optical Path Configuration for $\mu$ PL Experiments . 22
3.2.1	Manufacturing the SIL . . . . . 22
3.2.2	Manufacturing the Cryostat Optics Mount . . . . . 24
3.2.3	Experimental Optical Path Configuration . . . . . 25
3.3	$\mu$ PL Data Collection . . . . . 28
3.3.1	Optical Alignment Considerations . . . . . 28

3.3.2	Data Collection Process . . . . .	29
3.4	Optical Components and Optical Path Configuration for PLE Experiments .	30
3.4.1	Optical Path Configuration and Alignment . . . . .	30
3.4.2	Data Collection for Photoluminescence Excitation Spectroscopy . . .	31
4	Experimental Results	33
4.1	$\mu$ PL Results and Analysis . . . . .	33
4.2	PLE Results and Analysis . . . . .	33

## Figures

### Figure

- |     |   |    |
|-----|---|----|
| 2.1 | A typical dispersion curve minima for a direct-gap semiconductor. An optical transition is illustrated at $k = 0$ , where an electron is absorbing a photon resulting in a transition from the conduction band to the valance band. . . .   | 6  |
| 2.2 | The band structure of GaAs, the allowed states are the thick horizontal curves, and the boxed region is the direct-gap region, in which electrons can be make direct transitions across the bandgap. Note, the minima of this region look like the dispersion curve in figure 2.1 CITE Davies. . . . .  | 7  |
| 2.3 | A graphical representation of the one-dimensional infinite potential well of width $L$ . . . . .  | 8  |
| 2.4 | An example of the semiconductor quantum well. These layers can be repeated arbitrarily many times. . . . .  | 10 |
| 2.5 | A simple model for the behavior of an exciton in a quantum well, suitable for the work completed herein. . . . .  | 14 |
| 2.6 | An STM picture of the GaAs growth front, stopped mid-growth, of a 110 oriented sample. The shown defect size is roughly representative of disorder in modern GaAs samples grown by molecular beam epitaxy. However, defect size and shape is highly sample dependent, so disorder varies widely from one QW structure to the next. Note, the disorder terraces are on the order of 100nm across. Taken from CITE Yoshita Terrace. . . . . | 15 |



2.7	In a), the energy of a ground state exciton located in a portion of the QW of average thickness, the blue line in b) depicts the ground state energy of an exciton located in a slightly thinner than average portion of the QW, and in c), the blue line depicts the ground state energy of an exciton located in a slightly thicker than average portion of the QW. In both b) and c), the average exciton ground state energy is depicted by the maroon dashed line. .	15
2.8	A representation of a confocal optical geometry used to collect the PL from the QW sample. The PL image is being collected from a small region of the QW sample, magnified, and then collimated by the two lenses. . . . .	17
2.9	A representation of the principle of our specific $\mu$ PL experiment. The PL image leaves the SIL normal to the hemispheric surface, so it just increases $n$ and lowers the diffraction limit. . . . .	18
3.1	A depiction of the modified mount: the actuator arm fits into a sleeve attached by a pivot to the rotating filter mount. A spring attached to both the rotating mount and aluminum block holds the sleeve to the actuator and ensures smooth rotation in either direction. . . . .	21
3.2	A depiction of the modified mount: the actuator arm fits into a sleeve attached by a pivot to the rotating filter mount. A spring attached to both the rotating mount and aluminum block holds the sleeve to the actuator and ensures smooth rotation in either direction. . . . .	22
3.3	A depiction of the lapp. The orange casing is copper while the grey lining is lead solder. The cavity left by the ball bearing was smooth enough to polish the relatively soft ZnSe hemispheres to an optical quality finish. . . . .	23
3.4	A depiction of the polishing setup in the lathe. The off-center placement of the lapp and lapp pin allowed the lapp to rotate and move slightly to randomize the SIL polishing. . . . .	24

3.5	A diagram of the experimental components. The second telescope was an optional feature, its use doubled the system magnification. The light pink beam is the PL signal, while the red beam is the excitation laser. . . . .	27
3.6	A depiction of the PL spot on the spectrometer slit. The spot translates across the slit as we move the lens on the translation stage, allowing us to take vertical slices of the image as it translates across the slit. . . . .	28
3.7	A flowchart depicting the LabView code processing sequence. Each set of $\mu$ PL data was acquired using this process, where $s_s$ was the lens step size and $i_0$ was the number of data collection steps to be run. . . . .	30
3.8	A diagrammatic representation of the PLE experiment. The red beam is the excitation laser while the pink beam is the PL signal. We used a long pass filter (LPF) to cut out any light with wavelength lower than 800nm, as we suspected some of the pump scatter (green) was making it to the sample, reducing our ability to control the excitation wavelength. . . . .	31
3.9	A flowchart depicting the LabView code processing sequence for the PLE experiments. Each set of PLE data was acquired using this process, where $\lambda_{step}$ was the wavelength step size and $i_0$ was the number of data collection steps to be run. . . . .	32

## Chapter 1

### Introduction

Recent advances in nanoscale semiconductor manufacturing techniques allow for the realization of unique nanostructures ideally suited for a broad range of optical and electronic devices. Precise control of material geometry and immense parametric freedom during device fabrication makes tailoring semiconductor nanostructures to their applications relatively easy. With these processes, confining charge carriers on the scale of their de Broglie wavelengths becomes possible. Nanostructures employing confinement on such small scales have proven to be especially useful. A particularly useful subset of these structures, known as quantum wells, confine their charge carriers in just one dimension. It is therefore possible to create such useful devices as highly efficient photo- and laser diodes. Additionally quantum wells (QWs) have shown particular promise in such diverse areas as quantum information processing CITE QI REVIEW, as low noise transistors, and as saturable absorbers in mode-locked lasers. In addition to their applications, QWs have proven useful as a testbed for studying the quantum interactions between light and matter CITE Steve Review.

Despite immense progress in the growth of quantum wells, manufacturing processes still unintentionally introduce inhomogeneities to the layer thickness during crystal deposition. This translates to an uneven interface between two different materials on the scale of a few crystal monolayers. What this means for a quantum well structure is that small fluctuations in interface flatness translate to small fluctuations in well width as these happen at both interfaces of the quantum well and barrier layers. These small width fluctuations are known

as structural disorder.

Disorder affects charge carrier mobility within QWs, which can affect device efficiency and optical activity. Because of the ubiquity of QW structures, it is important to characterize disorder. Being able to quantitatively map structural disorder within QWs can help manufacturers improve the uniformity of their QWs, and in turn the quality and efficiency of their devices. For use of QWs in optical experiments, quantifying the spatial distribution of disorder is important because complete information concerning inhomogeneous contributions to the overall spectral response of QWs can help us enrich our understanding of many-body physics of excitons within quantum wells.

The local thickness of a QW structure can be optically determined: simply by spectrally resolving the total emission signal from a photo-excited QW, allows one to determine the average thickness of a QW layer CITE Gileo. Structural QW disorder modifies the thickness on the well at nanometer scale and therefore slightly modulates the energies of the emitted photons as a function of position within the QW system. Therefore, disorder can be experimentally quantified. By obtaining a spatial map of QW emission energies with sufficient resolution spatial and spectral resolution, we can determine the local well thickness and therefore obtain a quantitative picture of disorder within a QW. By optically exciting a QW sample and spectrally imaging the emitted light, a linear spectroscopic technique known as micro-photoluminescence spectroscopy, we recover a spatially resolved map of emission energies, and thereby quantify QW structural disorder CITE Yoshita SIL/QW paper.

In addition to studying quantum well disorder, linear spectroscopy is useful for characterizing the energy profile of electron states in matter. For example, we can use linear spectroscopy to study exciton states and incoherent coupling in the asymmetric double quantum well (AQW). These systems are great testbeds for various quantum coupling phenomena CITE AQW Review, and understanding incoherent coupling between exciton states in asymmetric double quantum wells allows us to fulfill two important experimental goals: we obtain a better understanding of the exact absorption energies of the various exciton states. Ad-

ditionally, we can explore incoherent coupling mechanisms between exciton states in each of the wells. Particularly, we can explore the temperature and barrier width dependence of coupling between excitons in adjacent wells.

In this thesis, I present the development of a high-resolution micro-photoluminescence spectroscopy ( $\mu$ -PL) experiment to quantify QW disorder. Furthermore, I translate this spatial picture into a quantitative measurement of disorder on three different types of QW structures: a periodic ten-quantum well structure, a periodic four-quantum well structure, and an interfacial quantum dot ensemble. In addition to  $\mu$ -PL experiments, I present the development of Photoluminescence Excitation Spectroscopy (PLE) to study the incoherent coupling between exciton states in GaAs/InGaAs AQW structures. I will then use our PLE characterization of exciton states in AQWs to comment on and add to the relative paucity of information on thermal and barrier width mediation of coupling between exciton states in the stokes and anti-stokes directions.

This thesis is structured such that Chapter 2 is a theoretical introduction to the physical concepts necessary to understand our  $\mu$ -PL and PLE experiments. Chapter 3 will be a description of our experimental methods, while results of our experiments will be presented in Chapter 4. Chapter 5 will conclude this thesis with our experimental interpretations and a discussion of possible experimental directions for the future.

## Chapter 2

### Theory and Background

In this chapter, I will provide the theoretical background necessary to understand the work presented in this thesis. The first section will deal with the definition and importance of the bandgap of a material, the second will introduce the effects of confinement on electrons within semiconductors, leading to a discussion of experimental confinement within the semiconductor quantum well. The third section will introduce the concept of semiconductor quantum well disorder, and the fourth will motivate the study of semiconductor quantum well disorder with micro photoluminescence spectroscopy. Finally, I will discuss the optical properties of asymmetric double quantum wells and how to use photoluminescence excitation spectroscopy to investigate incoherent coupling between excitons in the asymmetric double quantum wells.

#### 2.1 The Semiconductor Quantum Well

This section will broadly lay out band theory of electron states in solids. I will then discuss interband absorption by electrons in direct-gap semiconductors.

##### 2.1.1 Bandgap

In order to understand how electrons behave in a crystalline solid, one must first understand how bound electrons act when arbitrarily many atoms are brought together in a lattice structure. Consider a collection of  $N$  atoms sufficiently far apart such that interactions

between atoms can be neglected. In this limit, electrons in an atom such as Hydrogen occupy *discreet* energy levels. For instance: suppose all  $N$  of our atoms are monatomic hydrogen atoms. In our system, an electron behaves according to the following Hamiltonian:

$$\hat{H} = -\frac{\hbar^2}{2m} \nabla^2 - \frac{e^2}{2\pi\epsilon_0 r}. \quad (2.1)$$

We can find the electron wavefunctions  $\psi(x)$  by solving the time independent Shrödinger equation,

$$\hat{H}\psi(x) = E_n\psi(x) \quad (2.2)$$

where  $E_n$  is the energy of the  $n^{th}$  energy level. This equation can be solved using the usual methods CITE Griffiths, but doing so here would be a diversion, so I'll just skip to the crucial points: evidently, the  $n = 2$  electron wavefunction (again neglecting interactions between atoms and ground state perturbations) is

$$\psi(x) = Y_l^m \frac{1}{\sqrt{2}} a_0^{-3/2} \left(1 - \frac{r}{2a_0}\right) \exp(-r/2a_0) \quad (2.3)$$

where  $a_0$  is the Bohr radius,  $Y_l^m$  is either the  $l = 0, m = 0$ , the  $l = 1, m = 1$ , or the  $l = 1, m = 1$  spherical harmonic. Note: each  $n = 2$  energy level in this system is  $N$ -fold degenerate, as there are  $N$  orbitals with the same energy. Considering just the  $n = 2$  states and neglecting perturbations, electrons in these states evidently all have energy

$$E_2 = \frac{-13.6eV}{n^2} = \frac{-13.6eV}{4}. \quad (2.4)$$

In the limit that many atoms are brought together such that interactions can no longer be neglected, two things happen: each  $N$ -fold degenerate electron energy level will split into  $N$  components, and these levels will become so close that they will smear into allowed and disallowed energy densities of state CITE Indonesi, Siradesh, Grif, Davies. Roughly speaking, the occupied states are known as the “valance band” states, and the unoccupied states are known as the “conduction band states”. The energy difference between the valance band and conduction band is called the bandgap, and its importance will be illuminated momentarily.

These band states are simultaneous eigenstates of both the Hamiltonian and the crystal momentum CITE Davies(?). This means that bands can be easily depicted in  $k$ -space using dispersion curves. Dispersion curves map out allowed band energies in  $k$ -space, and their full functional shape is dependent on the types and arrangement of constituent atoms. Solids can be broadly organized into three categories based upon the  $k$ -space arrangement of their electron bands. In metals, the conduction band energies are below the highest energy valence band states and thus some conduction band states are occupied. In insulators, the bandgap is relatively large (about 10eV) CITE Mark Fox. By contrast in semiconductors, the bandgap is roughly 1eV and can therefore be optically accessed. Sometimes, as in the case of GaAs crystals, a local valence band minima and conduction band maxima occur for the same value of  $k$  in  $k$ -space. Semiconductors with this sort of bandstructure are known as direct-gap semiconductors. Around this value of  $k$ , electrons can absorb a photon with enough energy to undergo a direct transition from the valence band to the conduction band CITE Iandonesi, Galan thesis. This fact forms the basis of linear and nonlinear optical studies of semiconductor nanostructures (CITE Steve review), photonic devices, and certain types of theoretical quantum information processing schemes (CITE Nature Review of QI).

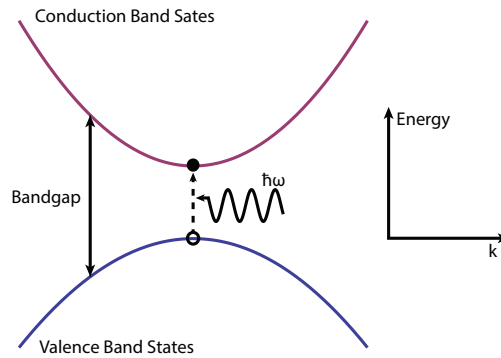


Figure 2.1: A typical dispersion curve minima for a direct-gap semiconductor. An optical transition is illustrated at  $k = 0$ , where an electron is absorbing a photon resulting in a transition from the conduction band to the valence band.



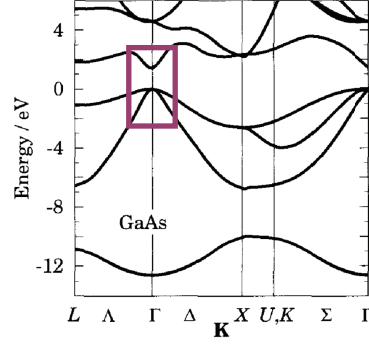


Figure 2.2: The band structure of GaAs, the allowed states are the thick horizontal curves, and the boxed region is the direct-gap region, in which electrons can be make direct transitions across the bandgap. Note, the minima of this region look like the dispersion curve in figure 2.1 CITE Davies.

### 2.1.2 Confinement

It is well known that nanometer scale confinement of particles results in quantized energy states CITE Griffiths. In the previous section, I briefly introduced the bandgap, and its important physical properties. In this section, I'll illustrate an interesting application of band theory: the semiconductor quantum well (QW). First, it is important to understand what we mean by confinement, and how quantized energy levels arise for confined particles. I will draw an analogy to a familiar physical situation, the particle confined within an infinite potential. I will then use this analogy to construct a physical picture for QWs, and then I will discuss the formation of excitons and a simple physical model of their behavior, sufficient for understanding the spectroscopy conducted in this thesis.

Perhaps the simplest problem in quantum mechanics is the of confinement of a particle in an infinite, one dimensional potential well. I will sketch a derivation of the wave function of a particle trapped in such a well, and use this derivation as the basis for exploring the physics of the QW exciton. We will begin by considering an arbitrary particle confined in a one dimensional infinite potential well. The potential that our arbitrary particle feels is:

$$V(x) = \begin{cases} 0 & 0 < x < L \\ \infty & |x| > 0 \end{cases}$$

where  $L$  is the length of the potential well. Graphically, the potential the particle feels looks like 2.1.2.

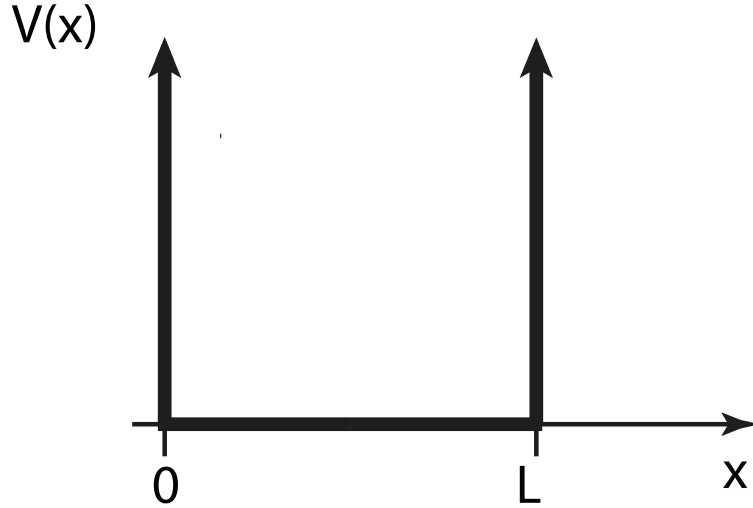


Figure 2.3: A graphical representation of the one-dimensional infinite potential well of width  $L$ .

Our task is to solve the time independent Schrödinger equation to show how quantized bound states arise for one-dimensional confinement. The time independent Schrödinger equation reads:

$$\hat{H}\psi(x) = E\psi(x) \quad (2.5)$$

where  $E$  is the energy of the particle, and  $\psi(x)$  is the particle's wavefunction. The particle will evidently be confined to the well, so our Hamiltonian inside the well is just

$$\hat{H} = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \quad (2.6)$$

where  $m$  is the particle's mass, and  $E$  is the particle's total energy. The time independent Schrödinger equation now reads:

$$\frac{\partial^2}{\partial x^2}\psi(x) = -\alpha\psi(x) \quad (2.7)$$

where we define

$$\alpha = \frac{2mE}{\hbar^2}. \quad (2.8)$$

Now, eq. 2.7 looks like the familiar simple harmonic oscillator equation from classical mechanics. Because the wave function must be continuous at  $x = L$  and  $x = 0$ , i.e. it vanishes at those locations, and the potential is odd about the origin, solutions to eq. 2.7 have the form:

$$\psi(x) = A\sin(kx) \quad (2.9)$$

where  $k$  contains  $E$  and is determined by our boundary conditions. Now we want  $\psi(L)$  to vanish, but we can't have  $A = 0$ , because that is the trivial solution to eq. 2.7. Therefore, because we want  $\psi(L) = A\sin(kL) = 0$ , we must have  $ka = \pm n\pi$  where  $n \in \mathbb{N}$ . Now, we can absorb all of the negative combinations of  $kL$  into our normalization constant,  $A$ , and we have, then, that

$$k_n L = n\pi \quad (2.10)$$

where the subscript denotes the fact that we now have infinitely many, *discreet* solutions to eq. 2.5. Evidently

$$k_n = \frac{n\pi}{L} \quad (2.11)$$

and therefore

$$\psi(x) = A\sin\left(\frac{n\pi x}{L}\right). \quad (2.12)$$

Now, if we let  $k_n = \alpha$  and solve for  $E$ , we obtain

$$E = \frac{n^2\pi^2\hbar^2}{2mL^2}. \quad (2.13)$$

It will do us no good to normalize the wavefunctions we found, as their use for our purposes is minimal. The important part is that confinement in one dimension resulted in our particle occupying *discrete* energy levels whose energy depends on the size of the confinement potential.

Using layers of semiconductors, one can generate similar one-dimensional confinement effects for electrons. A simple way this can be done is by sandwiching a layer of low-bandgap semiconductor material in between two layers of higher bandgap materials (CITE Davies). One period of this structure is shown in figure 2.4. If the well material is a direct-gap semiconductor, then simple optical transitions (i.e. not mediated by phonons) across the bandgap can be made, as the transition illustrated in figure 2.1. Figure 2.5 is the band structure for GaAs, the chosen well material for the studies of growth disorder. Annotated on the figure is the direct-gap transition zone of interest. The potential well created by the semiconductor sandwich leads to quantization of electron states within the well layer CITE Miller, Davies, Steve Review. We can access each of these states optically, making the QW a great testbed for exploring electron dynamics within a simple and well-known potential CITE Steve Review.

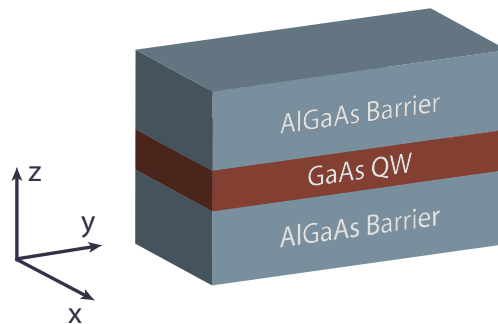


Figure 2.4: An example of the semiconductor quantum well. These layers can be repeated arbitrarily many times.

### 2.1.3 The Exciton

The simple picture presented above doesn't quite adequately represent the physics of an electron within a quantum well, however. After an excited electron moves from the valence band to the conduction band, it will leave behind a vacancy, or "hole", around its parent atom CITE Miller, Davies. The electron feels a *screened* Coulomb potential from this vacancy, as the vacancy is positively charged. I'll briefly sketch why this potential arises and then introduce the key concept of this section: the exciton. Imagine a number of electrons have been excited within the QW. Now, spatially, one will have a quasi-neutral distribution of electrons and holes in the well layer: an electron-hole plasma. I will assume that the holes are stationary relative to the electrons in the well, and that the excitation density is relatively low. These assumptions are *a priori* unphysical, but they immensely simplify the derivation of the electric potential QW electrons feel, and preserve the important physical results.

Let's explore the local behavior of an excited electron due to a single adjacent hole in the QW. Note that in this picture, electrons everywhere in the QW feel a Coulomb attraction to the hole, but the electrons adjacent to the hole *screen* its effects from charges far away. This phenomenon, known in plasma physics as Debye shielding CITE Chen and in quantum mechanics as electron screening CITE Griffiths, modifies the pure Coulomb potential one would expect a single electron-hole pair to experience. We will assume that the electrons in the plasma obey a Maxwellian density distribution. Now, the local density of electrons around the hole is

$$n_e = n_0 \exp\left[\frac{e\phi}{kT}\right] \quad (2.14)$$

where  $n_0$  is the electron density far away,  $e$  is the electron charge,  $\phi$  is the local electromagnetic potential, and  $T$  is the electron temperature. A complete derivation for this electron number density in an arbitrary plasma can be found in CITE Chen. This is the local electron

distribution, and we can assume  $e\phi \ll kT$  because the potential an electron feels due to one hole can be considered small relative to its thermal energy. Taylor expanding to first order, we find that

$$n_e \approx n_0 \left[ \frac{e\phi}{kT} \right]. \quad (2.15)$$

Now, our local charge density is

$$\rho(r) = e \left[ \delta(r) - n_0 \left( \frac{e\phi}{kT} \right) \right] \quad (2.16)$$

where we've assumed that the hole has positive charge magnitude  $e$ , is infinitely small, and situated at the origin. The Poisson equation reads

$$\epsilon_0 \nabla^2 \phi(r) = -e \left[ \delta(r) + n_0 \left( \frac{e\phi}{kT} \right) \right]. \quad (2.17)$$

We can define a constant,

$$k^2 = \frac{n_0 e \phi}{\epsilon_0 kT} \quad (2.18)$$

and now the Poisson equation is

$$(\nabla^2 - k^2)\phi = -\frac{e\delta(r)}{\epsilon_0}. \quad (2.19)$$

This is known as the screened Poisson equation, and its solution is

$$\phi(r) = -\frac{e}{4\pi\epsilon_0 r} e^{-kr}. \quad (2.20)$$

Now,  $\phi(r)$ , functionally, *exactly* the correct result (albeit with a different  $k$ ) had we proceeded under the Thomas-Fermi approximation, assuming only that the potential is weak and varies smoothly and slowly over a distance around the hole equivalent to  $\frac{1}{k_f}$ . This turns out to be a very good approximation for the local potential an electron feels relatively close to a hole CITE Patterson. The single-particle hamilltonian for an electron in the QW is now:

$$\hat{H} = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} - \frac{e}{4\pi\epsilon_0 r} e^{-k_0 r} \quad (2.21)$$

where  $k_0^2 = \frac{n_0 e \phi}{k T_f}$  is the “corrected”  $k$  for the same potential derived under the Thomas-Fermi approximation CITE Patterson.

Note that if the potential electrons feel was exactly Coulombic in nature, then any bound state between an electron and a hole would be hydrogenic CITE Griffiths. This potential, however, is *not* exactly Coulombic in nature, so the bound states between the electrons and holes can’t be described by hydrogenic wavefunctions. Nevertheless, bound states between an excited electron and an adjacent hole do exist, and when an electron and hole occupy these states, they form a quasiparticle called an “exciton”, and they can be treated as a single particle with an effective mass CITE Davies, Iandonesi, Rogers.

The subtleties of the wave function are treated in CITE Rogers, exploring their exact functional form and corresponding density of exciton states in the QW will not be of use to us here. Only energy levels of the QW exciton are discretized by its confinement, those of excitons created in the bulk are not. A final important note: in both my derivation and those proceeding under the Thomas-Fermi approximation, the hole is assumed to be a *stationary* point particle. This is emphatically *not* true, but the physics doesn’t change that much if we assume both charge carriers are mobile. Excitons can still be treated as a single particle even removing this assumption. Figure 2.5 depicts a simple physical picture for excitons: the electron and hole excited energy levels can be thought of as the ground state of a particle trapped in a finite potential.

## 2.2 Quantum Well Disorder

When an exciton is optically created, in a direct gap semiconductor such as GaAs, the charge carriers can recombine from the either exciton “ground” state ( $n = 1$ ), or “excited” states ( $n > 1$ ) and emit a photon at the exciton binding energy CITE Gilleo. Since I am only interested in linear, long-timescale exciton physics, we can treat QW excitons as an approximately two-level system, only looking at ground state recombination. The emission energies for QW excitons will be dependent on well depth, a function of the barrier composition, and

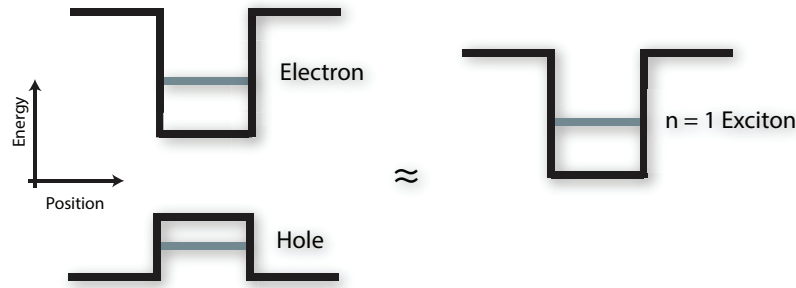


Figure 2.5: A simple model for the behavior of an exciton in a quantum well, suitable for the work completed herein.

well width. Control of QW layer thickness has improved immensely, as QW structures can be made to precise specifications with modern molecular beam epitaxial growth methods CITE Davies. However, imperfections of layer width on the order of a crystal monolayer occur unavoidably at the interface between the well and barrier materials during the QW manufacturing process CITE Yoshita Terrace paper (find better). In figure 2.6, an AFM picture of imperfections of a GaAs surface are shown. These defects, known as structural disorder, slightly change the width of the well layer and thus subtly modulate exciton emission energies, an illustration of which is shown in figure 2.7. By analogy to eq. 2.11, excitons localized in slightly thinner than average sections of the QW will emit at slightly higher energies than average. Conversely, excitons localized in thicker than average sections of the QW will emit at slightly lower energies than average. Thus, structural disorder is the main contribution to inhomogeneous broadening in the QW coherent optical response CITE Bristow.



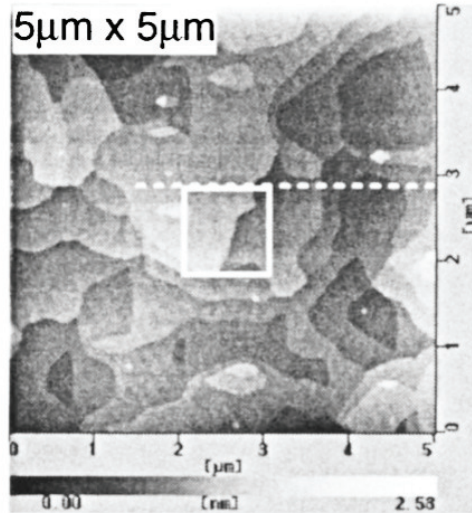


Figure 2.6: An STM picture of the GaAs growth front, stopped mid-growth, of a 110 oriented sample. The shown defect size is roughly representative of disorder in modern GaAs samples grown by molecular beam epitaxy. However, defect size and shape is highly sample dependent, so disorder varies widely from one QW structure to the next. Note, the disorder terraces are on the order of 100nm across. Taken from CITE Yoshita Terrace.

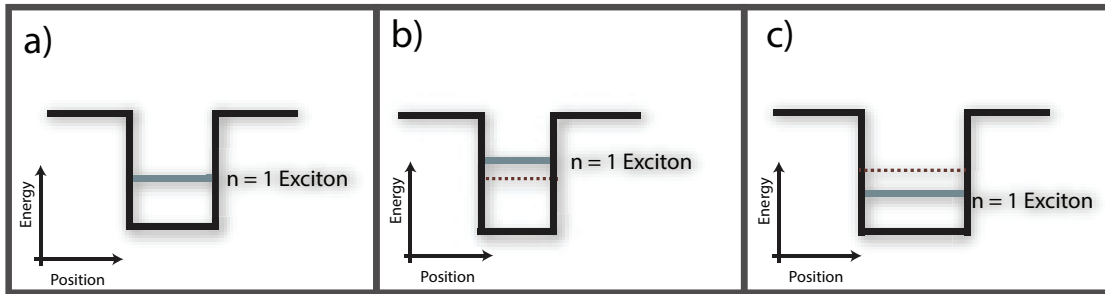


Figure 2.7: In a), the energy of a ground state exciton located in a portion of the QW of average thickness, the blue line in b) depicts the ground state energy of an exciton located in a slightly thinner than average portion of the QW, and in c), the blue line depicts the ground state energy of an exciton located in a slightly thicker than average portion of the QW. In both b) and c), the average exciton ground state energy is depicted by the maroon dashed line.

### 2.3 Microphotoluminescence Spectroscopy

Because local QW thickness determines exciton emission energy, a spatial picture of disorder is possible through spectral imaging. By using a continuous wave (CW) excitation source to create a population of QW excitons and monitoring the emission energy as a function of sample position, one can extract the local QW width. With sufficiently high resolution, obtaining a map of emission energies for a representative portion of a QW sample is possible. In order to obtain a map of emission energies, one must monitor the photoluminescence (PL) energies as a function of position CITE Steve's theory recommendation. In a PL experiment, light of sufficiently high energy is shown on a sample, exciting a large number of charge carriers to the conduction band. During this process, electrons fall back into holes in the valance band, emitting a photon equivalent to the lost energy CITE Davies. If a QW exciton recombines, it will emit a photon equivalent the energy difference between the valance band and one of the quantized exciton states. If we regard the exciton as a two level system, by exciting QW excitons near-resonantly, the energy of the emitted photon will be equivalent to the energy difference between the valance band and the exciton ground state.

In order to obtain an image of PL, we must collect the signal carefully. More precisely, if we are to obtain a spatial picture of QW disorder, we must collect and spectrally resolve a PL image. The PL will be emitted from the exciton population over a  $4\pi$  solid angle, so we must place the QW directly at the focus of our imaging system in order to form a clear PL image. Furthermore, since the scale of the disorder is on the order of 100nm CITE Yoshita Terrace paper, we must have comparable resolution for the PL image. Measuring a PL image is fairly easy, one must place the QW at the focus of a pair of lenses in a confocal optical geometry. Figure 2.8 is a diagram of this setup, and the magnification of the PL image is set by the ratio of the lens focal lengths. Namely,

$$M = \frac{f_1}{f_2} \tag{2.22}$$

where  $f_2$  and  $f_1$  are the focal lengths of the short focal length lens and the long focal length lens respectively, and  $M$  is the image magnification factor. A PL experiment with sub-micron resolution which is capable of spectrally resolving a PL image is known as a “microphotoluminescence spectroscopy” experiment, or  $\mu$ PL.

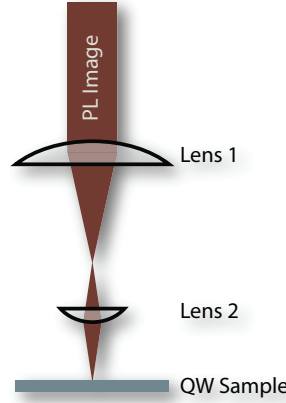


Figure 2.8: A representation of a confocal optical geometry used to collect the PL from the QW sample. The PL image is being collected from a small region of the QW sample, magnified, and then collimated by the two lenses.

As simple as the PL image collection is, it is difficult to obtain the requisite image resolution because the PL is around 750-800nm wavelength, but as I’ve asserted above, the islands can be smaller than this. What this means is that if we were able to image at the Abbe diffraction limit of our optical geometry, we still wouldn’t have the resolution necessary to resolve adjacent disorder sites. The Abbe diffraction limit is

$$d = \frac{\lambda}{2nNA} \quad (2.23)$$

where  $\lambda$  is the wavelength of the PL image,  $n$  is the index of refraction in the intermediate space between the sample and lens 2 (the imaging lens) in figure 2.8, and  $NA$  is the numerical aperture of lens 2. Note that  $NA = f/D$  where  $f$  is the focal length of the imaging lens and  $D$  is its diameter. In our case,  $d \approx 500nm$  for  $\lambda \approx 780nm$ ,  $n = 1$  in vacuum, and we pick

$NA = .83$ , as that was the NA of the lens in our experimental setup.

In order to get around this limit, we either need to resort to exotic microscopic techniques, or we can employ a fairly simple trick. It has been shown that by increasing the index of refraction ( $n$ ) with a solid immersion lens (SIL), the Abbe diffraction limit can be substantially reduced CITE Yoshita Application paper, and broad SIL paper. In order to do this, one simply places a hemisphere of sufficiently high  $n$  material between the sample and the imaging lens. Figure 2.9 is a diagrammatic representation of this improvement. Note, I'll use SIL and hemisphere interchangeably from here on out, though they aren't necessarily interchangeable, as "SIL" refers to a truncated sphere of some degree.

In my experimental setup, I used a Zinc Selenide (ZnSe) SIL, for which  $n = 2.4$  at  $\lambda = 780nm$ . This improvement decreases the diffraction limit from  $d \approx 500nm$  to  $d \approx 185nm$ , roughly sufficient resolution for our purposes. I'll expand on the precise setup in the next chapter, but the experiment will be very similar to what I've just described.

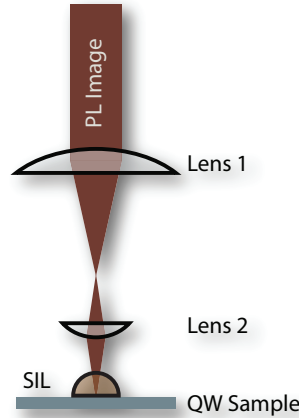


Figure 2.9: A representation of the principle of our specific  $\mu$ PL experiment. The PL image leaves the SIL normal to the hemispheric surface, so it just increases  $n$  and lowers the diffraction limit.

## 2.4 Exciton Coupling in Asymmetric Double Quantum Wells

(Summary, flesh out)

Quantum coupling between excitons occurs when multiple quantum wells get close enough so that the exciton wavefunction can tunnel slightly into other wells CITE Griff, Davies (?). In order to study quantum coupling between states in adjacent QWs, however, it is not simply enough to grow multiple quantum well layers fairly close to one another. Evidently, if each of the wells is of identical thickness, then QW PL from one well will be spectrally indistinguishable from another CITE Thomas. Indeed, it is necessary to grow wells of varying thickness when studying coupling in multiple quantum wells CITE Heagarty. In this thesis, I will only discuss incoherent coupling of exciton states in various asymmetric double quantum well (AQW) samples.

## 2.5 Photoluminescence Excitation Spectroscopy

(PLE Papers from my lit. review, Chris', suggestions from Steve. In lib1, Zotero)

## Chapter 3

### Experimental Methods

In this chapter I will describe the experiments I conducted for this thesis. The first section will deal cover the configuration and customization of the continuous wave (CW) Titanium Sapphire laser I used as an excitation source for conducting both PLE and  $\mu$ PL experiments. Section two will cover the design and construction of the in-cryostat optic mount for the  $\mu$ PL experiment as well as the optical configuration for data collection. Section three will illustrate the data collection procedure used in  $\mu$ PL experiments, as well as the function and implementation of LabView code I wrote for hardware control and data acquisition. In section four, I will lay out the optical design of our PLE experiments and in section five, I will discuss the experimental data collection process and signal optimization routines.

#### 3.1 The Light Source

The PLE and  $\mu$ PL experiments required a CW laser light source with a few properties: the laser must be a stable and fairly high-power light source with narrow line-width. For  $\mu$ PL, it was important that we have a fairly Gaussian and symmetric beam so we could obtain the desired spot-size and resolution at the sample. Additionally, conducting PLE scans required that we have the ability to computer control the laser wavelength over a fairly broad range of wavelengths, roughly a spectral region from  $\lambda = 780\text{nm}$  to  $\lambda = 850\text{nm}$ . The laser we chose for this task was a Schwartz Electro Optics Titan-CW Titanium Sapphire

(Ti:Sapph) laser. Its specifications were fairly close to our needs, as its specified operating power is 500mW with a tunable range from roughly 700-820nm CITE Titan manual.

The laser cavity can be configured for either CW or pulsed operation. In CW operation a 532nm pump beam, 5W of power, enters the cavity through a series of steering mirrors. After entering, the pump passes through a lens to focus the pump on the Ti:Sapph crystal. After the gain medium, the remaining pump light passes through the end mirror and terminates at the back of the laser enclosure. The laser configuration is shown in figure 3.1.

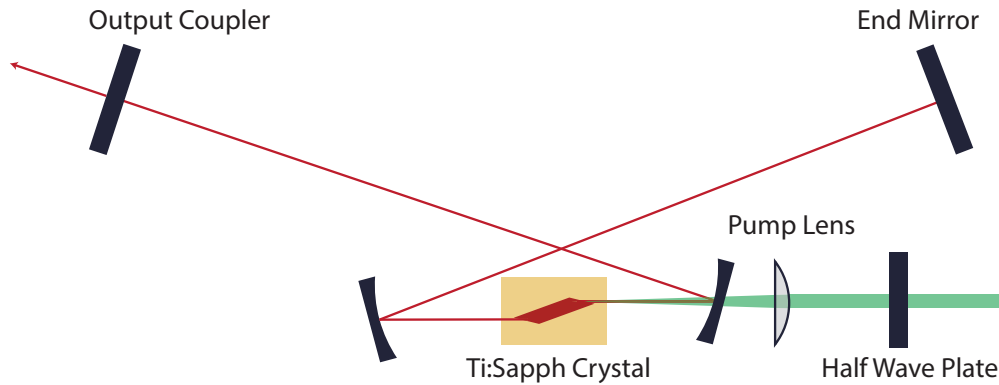


Figure 3.1: A depiction of the modified mount: the actuator arm fits into a sleeve attached by a pivot to the rotating filter mount. A spring attached to both the rotating mount and aluminum block holds the sleeve to the actuator and ensures smooth rotation in either direction.

Though the Ti:Sapph laser nearly met our specifications, it required two modifications to be operable in our experiments. First, we needed to add a computer controlled actuator to rotate the the birefringent tuner in order to allow for increased tenability and repeatability relative to a manually actuated micrometer. We modified the rotation mount for the birefringent filter (BRF) to accommodate a Newport TRB25 linear actuator. The linear actuator pushed a spring-loaded arm to rotate the BRF to a specified angle and select our desired wavelength. Figure 3.2 depicts the modified BRF mount with the actuator attached.

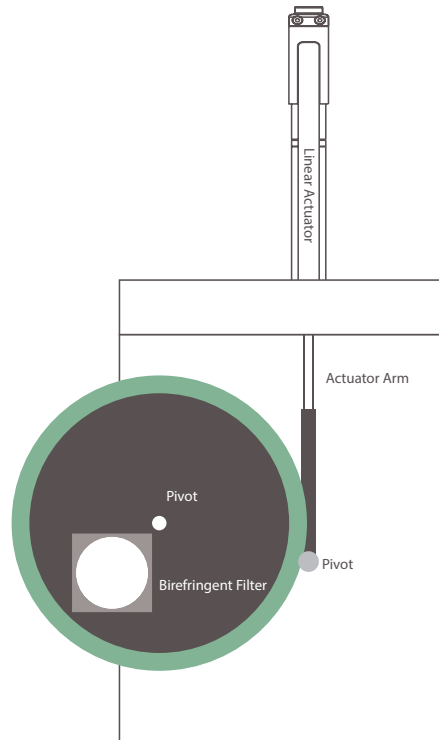


Figure 3.2: A depiction of the modified mount: the actuator arm fits into a sleeve attached by a pivot to the rotating filter mount. A spring attached to both the rotating mount and aluminum block holds the sleeve to the actuator and ensures smooth rotation in either direction.

## 3.2 Optical Components and Optical Path Configuration for $\mu$ PL Experiments

### 3.2.1 Manufacturing the SIL

In order to obtain the resolution necessary to image disorder, the experiment employed a solid immersion lens (SIL) at the surface of the sample to increase the index of refraction at the imaging plane. I chose ZnSe as the SIL material, as its index of refraction at 780nm is  $n=2.53$  CITE website. However, ZnSe SILs are not commercially available, so I resorted



to manufacturing SILs from a stock ZnSe window. The window measured 2.54cm diameter by 1cm thickness, and our goal was to manufacture SILs of roughly 3mm in radius. To begin, we used a core drill, diameter 6.35mm, to cut out a cylindrical chunk of ZnSe. I then centered and glued the cylindrical stock material to a brass dowel, 2mm in radius. After the ZnSe was glued to the rod, the SIL shaping began. I put the brass dowel in a power drill used 200 grit sandpaper to shape the ZnSe cylinder roughly into a hemisphere.

When the SIL was in the roughly correct shape, we lapped and polished the hemispherical surface until the SIL was the correct size. Additionally, since the experiment required optical quality surfaces, this was a careful and fairly lengthy process. I made the polishing lapps by machining a 2.54cm diameter copper rod to roughly 2cm in diameter with a 1.8cm wide by 1cm deep cavity. Then, I melted lead solder into the cavity, let it harden, and machined the face of the copper and solder until they were flush and machine-smooth. Then, I pressed a cleaned, 6.35mm diameter ball bearing halfway into the solder. Figure 3.3 depicts what a finished lapp looked like before it was used to grind and polish the SIL.

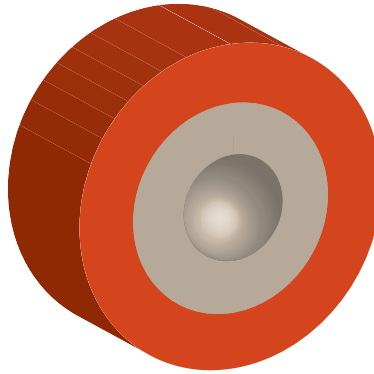


Figure 3.3: A depiction of the lapp. The orange casing is copper while the grey lining is lead solder. The cavity left by the ball bearing was smooth enough to polish the relatively soft ZnSe hemispheres to an optical quality finish.

After the lapp was made, we mounted the dowel with the SIL attached to a glass-working lathe. As the lathe rotated, we placed the lapp with a mixture of glass polishing

solution of various grit and mineral oil onto the SIL and held it in place with a sharpened wire. The wire and Lapp were set off-center relative to the SIL so the friction of the rotating SIL would randomly move the lapp so as to evenly polish the surface of the hemisphere. A depiction of this setup is in figure 3.4. (GET GRIT SIZE INFO) We iterated polishing runs from grit size ?? to ?? to ??, changing the lapp for each different grit size. After the polishing process finished, the SIL was removed from the dowel and the flat surface was polished with a colloidal silicon mixture. When the SIL was finished, we had a hemispherical (to within 1%) ZnSe SIL.

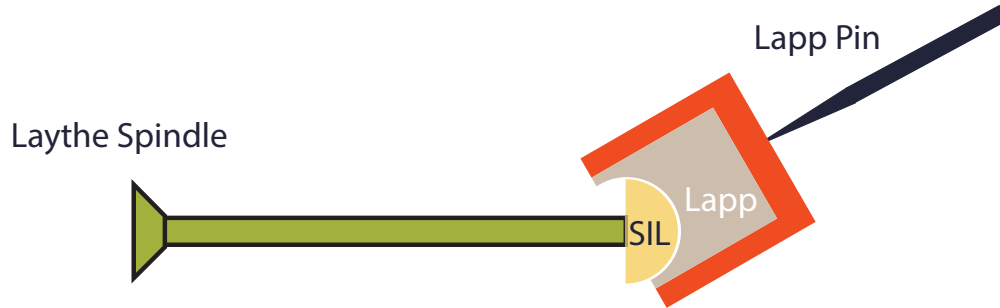


Figure 3.4: A depiction of the polishing setup in the lathe. The off-center placement of the lapp and lapp pin allowed the lapp to rotate and move slightly to randomize the SIL polishing.

### 3.2.2 Manufacturing the Cryostat Optics Mount

In order to achieve the desired imaging resolution, our chosen optical geometry (refer to 2.3) required a high-NA lens as the imaging lens. We therefore chose an Edmund Optics 0.83NA, 9mm effective focal length aspheric lens. Together with our ZnSe SIL, this gave us an Abbe diffraction limit of  $d = 185.05\text{nm}$  for PL centered around  $\lambda = 780\text{nm}$ . This diffraction limit is less than our goal of  $d = 200\text{nm}$ . As our experiment required cooling to cryogenic temperatures, we had to build a mechanically and thermally stable optics platform to hold the lenses and QW sample together in the correct configuration. Therefore, working

with our machinists, I designed the optics mount in Figure ??(MAKE). The optics mount stands vertically in our Cryo-Con 8CN bath cryostat. Therefore, since the excitation laser enters the cryostat vertically, we designed the optics mount to be held to a mirror which filled the entire optics mount and was positioned at a 45 degree angle so as to direct the laser to the sample and capture the total PL image. The mirror was ground by taking a stock Thor Labs 2.54cm diameter mirror, protecting the silvered face with weak glass tape, cutting the mirror to 3mm thick, and securing the mirror to an aluminum rod of 15mm diameter (the same diameter as the inside of the optic mount). The end of the rod was bevelled at 45 degrees, and the mirror and rod combination was spun by hand on the side of a glass cutting saw blade. This process ensured that, when the glass was cut flush with the edge of the rod, the mirror was the correct elliptical shape and diameter to fit in the optics mount. The mirror was then secured to a roughly .5mm thick sheet of indium which was epoxied to the mirror mount.

### 3.2.3 Experimental Optical Path Configuration

Our aim was to characterize disorder over an area roughly  $200\mu\text{m}$  in diameter. In order to do so, we needed the laser spotsize to be  $200\mu\text{m}$  in diameter or larger. Additionally, to obtain clear images, the excitation spot needed to be monotonic, symmetric, and preferably Gaussian in shape. To this end, I characterized the laser spot size and found it to be  $1.6 \pm .1\text{mm}$  FWHM diameter, roughly Gaussian and symmetric to within 20%. In order to obtain the requisite beam diameter at the sample, it was necessary to resize the beam going into the cryostat. In order to do so, we used a succession of four lenses to resize the beam. The first two lenses, one of focal length 60mm and the other of focal length 25.4mm, shrunk our beam from 1.6mm to 0.68mm. The second lens in the second pair of lenses was the in-cryostat asphere, and in combination with the lens outside the cryostat, focal length 30mm, resized our beam to  $203\mu\text{m}$  in diameter. After the beam hit the sample, the PL signal travelled through the asphere and out of the cryostat. We placed a 90%

reflective non-polarizing beamsplitter (NPBS) outside the cryostat to pick off the PL signal. The beamsplitter sent the PL signal through an achromatic, 20cm focal length lens, and a polarizer to filter out the laser. Finally, the signal focused onto the slit of a Horiba iHR550 imaging spectrometer. The 20cm lens was 50.4cm in diameter and mounted to a linear translation stage. Its function was to focus the PL spot on the spectrometer slit and translate the image across the spectrometer slit, as in Figure 3.6. The PL image was roughly 9mm in radius at the lens, so since the lens was relatively large compared to the image, spherical image aberrations during image translation were negligible.

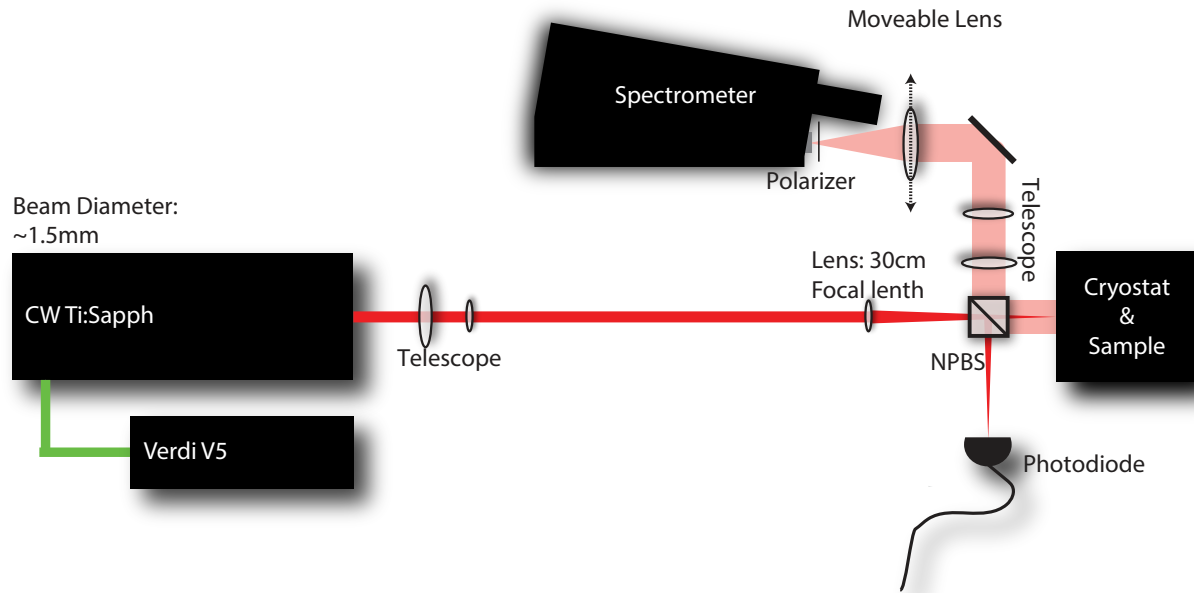


Figure 3.5: A diagram of the experimental components. The second telescope was an optional feature, its use doubled the system magnification. The light pink beam is the PL signal, while the red beam is the excitation laser.

We monitored the laser power with a photodiode, using the light that was dumped out of the experiment by the NPBS. Additionally, between the NPBS and the moveable lens, we had the option to add a telescope to improve the magnification of the system further. The use of the telescope depended on the intensity of the signal. If the signal was vanishingly small, the telescope made it nearly unreadable. Therefore, in cases where less signal reached the spectrometer, the telescope became impractical.

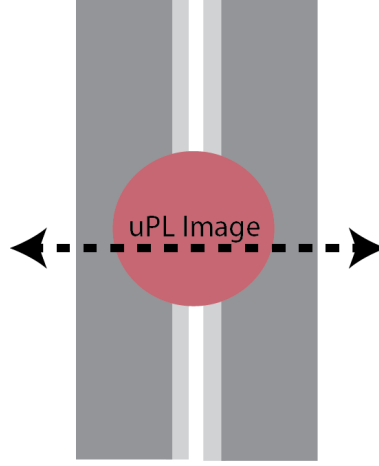


Figure 3.6: A depiction of the PL spot on the spectrometer slit. The spot translates across the slit as we move the lens on the translation stage, allowing us to take vertical slices of the image as it translates across the slit.

### 3.3 $\mu$ PL Data Collection

#### 3.3.1 Optical Alignment Considerations

When the optical components were roughly in the configuration seen in Figure 3.5, we cooled the sample to  $10 \pm 1\text{K}$  and adjusted the laser power to  $100 \pm 1\text{mW}$  so that the laser power at the sample was roughly  $1\text{mW}$  at the sample (because the NPBS dumped 90% of the power we fed into it). We identified the PL signal using a polarization filter, as it was the only signal left after the filter was rotated such that its polarization was orthogonal to that of the beam reflected from the sample. We set the position of the 30cm lens by maximizing the size of the PL image while monitoring it with an IR viewer as we adjusted the position of the lens. Then, we experimentally adjusted the focus of the moveable lens to maximize the spatial differences seen in PL amplitude on the CCD. Finally, we put the polarizer just in front of the spectrometer slit and rotated it to cut out as much laser scatter from the signal as possible.

### 3.3.2 Data Collection Process

The data collection process was fairly simple. The spectrometer CCD recorded an intensity image 1024x2048 pixels large. The vertical pixel dimension corresponded to vertical spatial dimension on the sample, while the horizontal pixel dimension corresponded to PL emission wavelength and both axes could be calibrated such that we could read peak emission wavelength as a function of vertical sample position. Each image we recorded was effectively a vertical slice of the larger two dimensional PL image. If we step-translated the PL image across the spectrometer slit and took an image at each lens position, we could recover both PL intensity and PL energy as a function of position. This is exactly the information required to reconstruct a spatial map of QW disorder.

The computer control of the experiment involved five pieces of hardware: two linear actuators, a photodiode, the spectrometer and the imaging CCD. The photodiode was read by the analog-to-digital converter of a Stanford SRS 810 lock-in amplifier using General Purpose Interface Bus (GPIB) protocol. The lens translation stage was actuated by a Newport TRB12 linear actuator, and it was controlled (along with the laser wavelength adjustment) by a Newport ESP300 motion controller interfaced through GPIB. Both the Horiba spectrometer and CCD interfaced over USB. The manufacturers of each of the above devices wrote LabView interface code which I incorporated into my overall experimental control code. The experimental control and data acquisition process proceeded according to the flowchart in Figure 3.7. The collected images and photodiode readings were handled and analyzed with MATLAB code that I wrote, included in Appendix A.

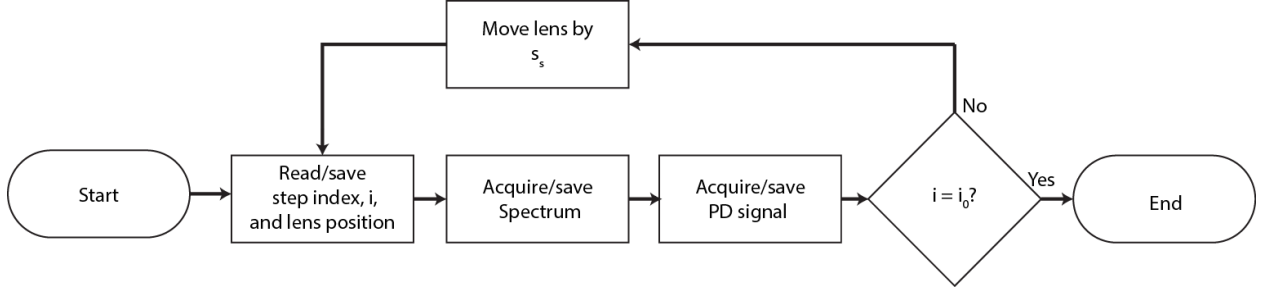


Figure 3.7: A flowchart depicting the LabView code processing sequence. Each set of  $\mu$ PL data was acquired using this process, where  $s_s$  was the lens step size and  $i_0$  was the number of data collection steps to be run.

### 3.4 Optical Components and Optical Path Configuration for PLE Experiments

#### 3.4.1 Optical Path Configuration and Alignment

Because we didn't need to image the PL from the QW sample in PLE experiments, the optical configuration simplified immensely. The laser first went into an NPBS where about 10% of its power was directed at a photodiode to monitor the laser power during acquisition. From there, the laser travelled to a 7.5cm focusing lens. The lens focused the laser onto our InGaAs/GaAs QW samples, which were rotated at 45 degrees with respect to the laser path to minimize reflected laser light arriving at the spectrometer. The sample was kept in a Janis FIND OUT MODEL helium vapor flow cryostat with tunable temperature control. The PL signal was collected by the same 7.5cm focusing lens, and then sent through a polarizing beam splitter whose polarization was orthogonal to the laser's. Following the beamsplitter, the PL signal was sent to the same achromatic 20cm focal length lens used as the moveable lens in the  $\mu$ PL experiments. After the lens, the PL signal passed through another polarizer rotated orthogonally to the laser polarization to minimize the laser light entering the spectrometer. The signal then passed into the spectrometer where it was collected as a spectral trace instead of a spectral image. We took data over an area of the CCD which measured 100x2048 pixels.



We then integrated over the vertical pixels and recorded spectra which were intensity vs. horizontal pixel number which we calibrated to wavelength. Figure 3.8 is a diagram of the experimental setup. Note, we modified the laser slightly by replacing the output coupler with one coated to work at wavelengths longer than 800nm so we could sweep the laser wavelength out to 850 or 860nm during PLE runs. Only negligible changes to the beams size and output power resulted from this change.

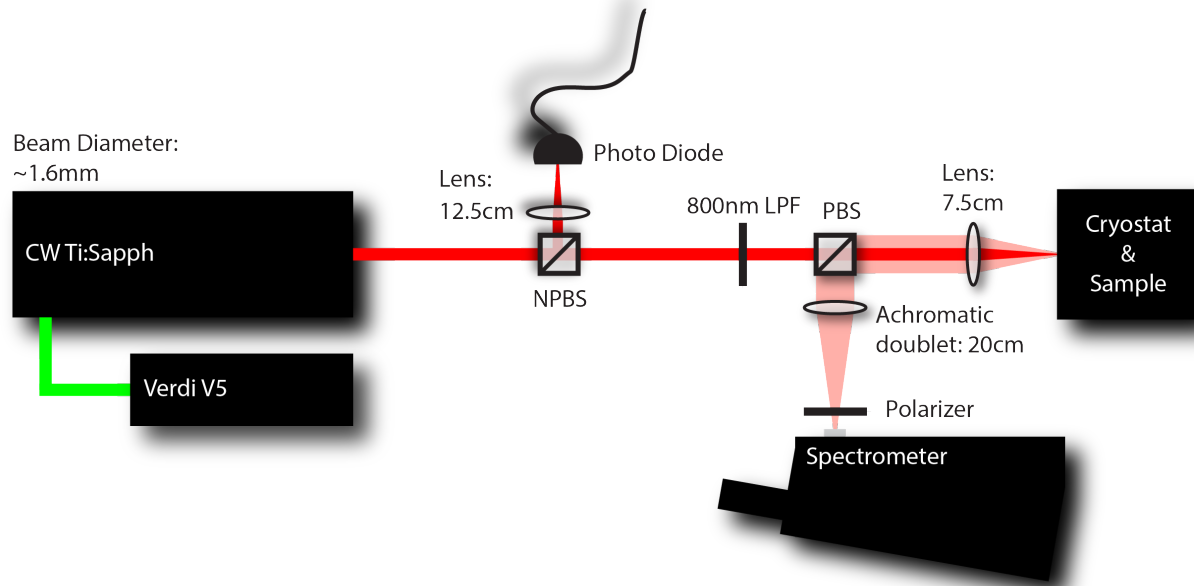


Figure 3.8: A diagrammatic representation of the PLE experiment. The red beam is the excitation laser while the pink beam is the PL signal. We used a long pass filter (LPF) to cut out any light with wavelength lower than 800nm, as we suspected some of the pump scatter (green) was making it to the sample, reducing our ability to control the excitation wavelength.

### 3.4.2 Data Collection for Photoluminescence Excitation Spectroscopy

The PLE data runs were fairly similar to those used for taking  $\mu$ PL data. The computer interfaced with the spectrometer, the photodiode, and the laser wavelength actuation in the

same way. During the data collection process, we monitored spectral response as a function of wavelength, recorded these spectra, and then changed the excitation wavelength of the laser. The sets of PLE spectra, BRF actuator position, and PD signal were collected and processed using MATLAB and Igor. Figure 3.9 is a flowchart representing the LabView code I wrote for the data collection process.

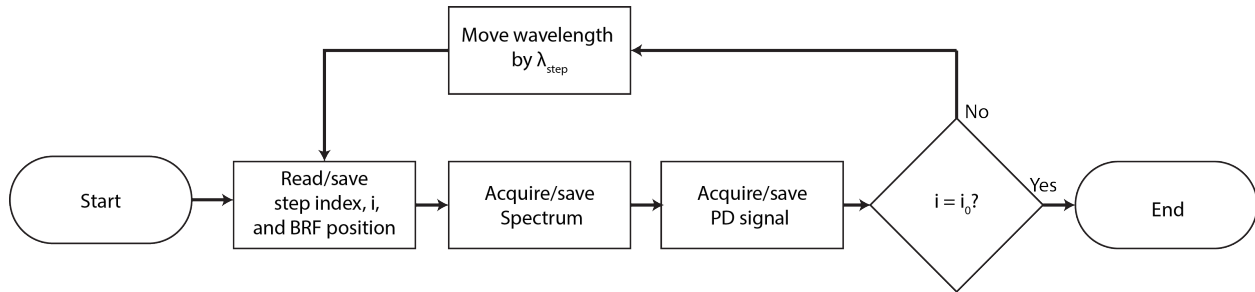


Figure 3.9: A flowchart depicting the LabView code processing sequence for the PLE experiments. Each set of PLE data was acquired using this process, where  $\lambda_{step}$  was the wavelength step size and  $i_0$  was the number of data collection steps to be run.

## Chapter 4

### Experimental Results

#### 4.1 $\mu$ PL Results and Analysis

- 10QW experiments

PL image and raw img, PL deviation small. Estimate smoothing, estimate resolution, comment on disorder agreement with thry.

- 4QW experiment

PL image and raw img, PL deviation slightly larger, but still small estimate, estimate rez, comment on disorder agreement with thry.

- IQD experiment

Introduce IQD, talk about disorder in IQD, show raw image, explain difference btwn IQD, MQW, estimate rez, comment on agreement with thry.

#### 4.2 PLE Results and Analysis

- PLE curve analysis

show stock PLE curve, show slices, say what they mean, show peaks, say what peaks mean

- PLE anti-stokes. show anti-stokes t dep. curves

show anti-stokes pow-dep curves, talk about linearity or no, comment on CCD bs., compare with thry, talk about mechanisms. well width dep

- PLE stokes peak

show stokes pow-dep curves, talk about linearity or no, comment on CCD bs.,  
compare with thry, talk about well width dep, say mechanisms understood(?) point  
to lit chris and I found