

# MICROELECTRONIC TECHNOLOGIES

## EXAMS NOTES

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*...Scooby-doo?...*



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# Chapter 1

## Exams notes

### 1.1 Ion implant range and +1 model

Given an implant of an element with a dose  $Q$  and an energy  $E$  we can find from tables the values of

- $R_p$  the projected range of our implant that is the maximum of our gaussian distribution that we expect
- $\Delta R_p$  the standard deviation of our gaussian distribution

So we will have a distribution like

$$C(x) = C_p \exp\left(-\frac{(x - R_p)^2}{2\Delta R_p^2}\right) \quad (1.1)$$

where  $C_p$  is the concentration at the peak of our distribution.

The total dose implanted will be  $Q = \sqrt{2\pi\Delta R_p^2} C_p$  and so  $C_p = \frac{Q}{\sqrt{2\pi\Delta R_p^2}}$  doing so we can write

$$C(x) = \frac{Q}{\sqrt{2\pi\Delta R_p^2}} \exp\left(-\frac{(x - R_p)^2}{2\Delta R_p^2}\right) \quad (1.2)$$

If we want to know the dose that is present after a certain depth  $x$

$$Q_{imp} = \int_x^{+\infty} C_p \exp\left(-\frac{(x - R_p)^2}{2\Delta R_p^2}\right) dx \quad (1.3)$$

That becomes

$$Q_{imp} = \frac{Q}{2} \operatorname{erfc}\left(\frac{x - R_p}{\sqrt{2}\Delta R_p}\right) \quad (1.4)$$

The function  $\operatorname{erfc}$  has the following proprieties

- $\text{erfc}(x)=1-\text{erf}(x)$  if  $x > 0$
- $\text{erfc}(x)=1+\text{erf}(x)$  if  $x < 0$

If we want to estimate the amount of interstitial caused by an implant using the +1 model we can say that the concentration of interstitial is equal to the dose Q implanted in silicon. If the silicon is fully amorphised and then re-crystallized there are no interstitial due to ion implantation since in an amorphous crystal do not exist interstitials or defects.

## 1.2 Ion implant and dopant diffusion

After an implant (with a certain dose Q and having also  $R_p$  and  $\Delta R_p$ ) there will always be a thermal annealing process for a certain time t at a temperature T. The profile of the doping will be a gaussian with the standard deviation modified by the diffusion due to thermal treatment so like

$$C(x) = \frac{Q_i}{\sqrt{2\pi(\Delta R_p^2 + 2Dt)}} \exp\left(-\frac{(x - R_p)^2}{2(\Delta R_p^2 + 2Dt)}\right) \quad (1.5)$$

From this we can know the concentration of dopants for all x. Beware to correctly set Q depending on the symmetry of the system.

## 1.3 CZ-growth

CZ growth of silicon gives different doping concentrations for the wafers depending on the distance from the top of the ingot.

The parameters that we need to have the doping concentration at a certain value x are the segregation coefficient k and the initial dose of doping  $C_0$

$$C = C_0 k (1 - f)^{k-1} \quad (1.6)$$

where f is the % of the ingot where we are.

From the concentration we can derive the resistivity of the wafer as

$$\rho = \frac{1}{q\mu C} \quad (1.7)$$

## 1.4 Deal-Grove model

Using the correct table parameters we can derive the coefficients B and B/A for wet or dry oxidation through their Arrhenius form

$$B = C_1 \cdot \exp\left(-\frac{E_1}{kT}\right) \quad B/A = C_2 \cdot \exp\left(-\frac{E_2}{kT}\right) \quad (1.8)$$

remember that

- B is related to the transport through the present oxide so it isn't dependent on crystal orientation.
- B/A is related to the interaction with the surface its activation energy it's  $\simeq 2eV$  that is the energy to break one Si-Si bond and it's strongly dependent on crystal orientation in fact

$$\left(\frac{B}{A}\right)_{\langle 111 \rangle} = 1.68 \left(\frac{B}{A}\right)_{\langle 100 \rangle} \quad (1.9)$$

Notice that none of the mentioned parameters depends on pressure.

The model gives us the following expression

$$\frac{x^2}{B} + \frac{x}{B/A} = t + \tau \quad (1.10)$$

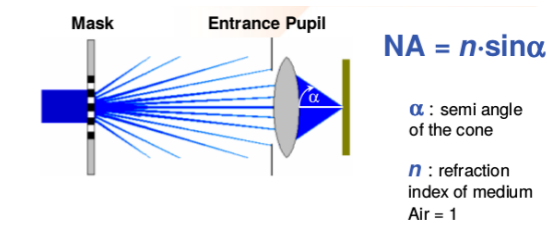
The boundary between the 2 regimes ,parabolic and linear, is given by the following thickness

$$x_b = \frac{B}{2B/A} \quad (1.11)$$

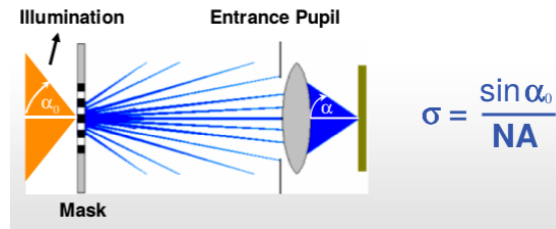
Beware that 46% of the  $SiO_2$  grows inside the silicon and the other 56% over it.

## 1.5 Lito resoution limit

Defining some parameters of our lito tool as:



NA determines the maximum number of diffraction orders that can be captured by projection lens and thus the quality of the reconstructed image.



It defines the illumination of the mask, depends from source extension. For  $\sigma = 0$  we have coherent illumination  $\sigma = 1$  incoherent illumination.

For a coherent illumination that means a light perpendicular to the mask we have that the minimum resolution is

$$R = \frac{1}{2} \frac{\lambda}{NA} \quad (1.12)$$

For a partially coherent illumination that means a light tilted by an angle  $\theta$  the resolution is

$$R = \frac{1}{2} \frac{\lambda}{(1 + \sigma)NA} \quad (1.13)$$

## 1.6 Technology scaling; propagation delay

Propagation delay of a metal wire can be modelled as

$$\tau \simeq 0.89 \cdot \varepsilon_{oxide} \varepsilon_0 \rho \frac{A}{F_{min}^2} \quad (1.14)$$