Good morning !!!

SOLVING PROBLEMS BY SEARCHING

Outline

- Problem-solving agents
- Problem formulation
- Example problems
- Uninformed search algorithms

Problem solving agent

- Particular type of goal-based agent
 - Goal-based agents act to <u>achieve their goals</u>
- Problem-solving agents use atomic representation
 - states of the world have <u>no internal structure</u> visible to the problem-solving algorithm

Solution: fixed sequence of actions (in this chapter)

Problem solving agent

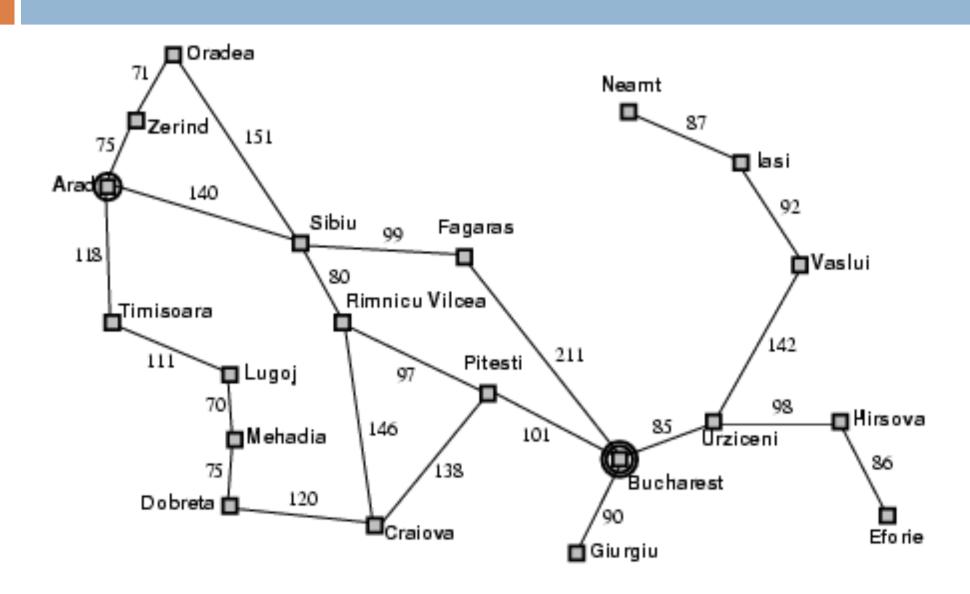
Intelligent agents are supposed to <u>maximize</u> their performance measure

Achieving this is sometimes **simplified**if the <u>agent</u> can **select a goal** and aim at **satisfying it**

Example: Romania

- On road trip in Romania. Currently in Arad
- Flight back leaves tomorrow from Bucharest
- Formulate goal
 - Be in Bucharest
- Formulate problem
 - states: various cities
 - actions: drive between cities
- □ Find solution
 - sequence of cities (e.g., Arad, Sibiu, Fagaras, Bucharest)

Example: Romania



Formulate, search and execute

- □ If the environment is:
 - observable (the agent always knows the current state)
 - known (the agent knows which states are reached by each action)
 - deterministic (each action has exactly one outcome)
 - a solution to a problem is a <u>fixed sequence of actions</u>
- Search: process of looking for such a sequence
- Search algorithm:
 - □ input: problem
 - output: an action sequence
- The sequence in output can then be executed

Problem-solving agent

return action

Goal formulation based on the current situation and the agent's performance measure

```
function SIMPLE-PROBLEM-SOLVING-AGENT (percept) returns an action static: seq, an action sequence, initially empty

state, some description of the current world state

goal, a goal, initially null

problem, a problem formulation

state \( \text{UPDATE-STATE}(state, percept) \)

if seq is empty then do

goal \( \text{FORMULATE-GOAL}(state) \)

problem \( \text{FORMULATE-PROBLEM}(state, goal) \)

seq \( \text{SEARCH}(problem) \)

action \( \text{FIRST}(seq) \)

seq \( \text{REST}(seq) \)
```

Problem formulation: what **states and actions** to consider given the goal

Search: Decide **what to do next** by <u>exploring consequences</u> <u>of actions</u> in the future and if they lead to the goal

Problem-solving agents

This simple problem-solving agent

- 1. Formulates a goal and a problem
- 2. Searches for a sequence of actions that would solve the problem
- 3. Executes the actions one at a time

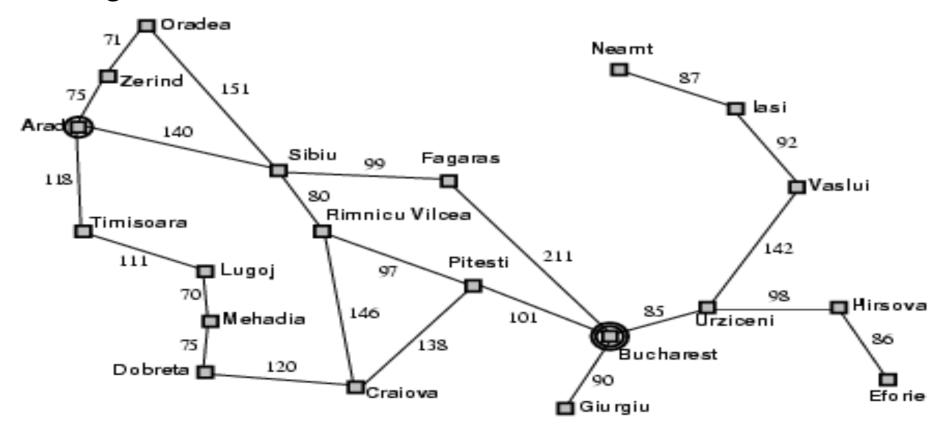
When this is complete, it formulates **another goal** and **starts over**

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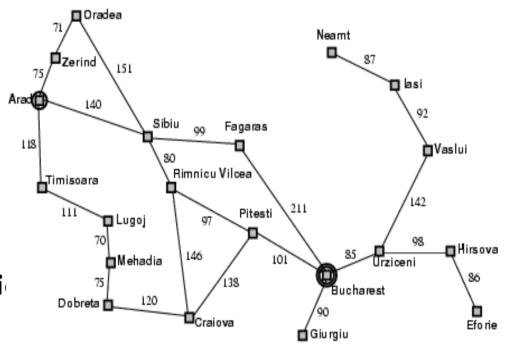
Example: Romania

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Example: Romania

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- □ Find solution
 - sequence of cities (e.g., Arad, Sibiu, Fagaras, Bucharest)

A problem can be defined formally by:

- Initial state
- Actions
- Transition model
- Goal test
- Path cost

Solution: sequence of actions (path) leading

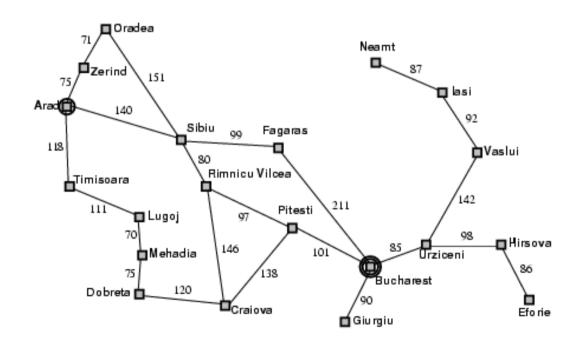
from the <u>initial state</u> to a <u>goal state</u>

Optimal solution: a solution with minimal path-cost

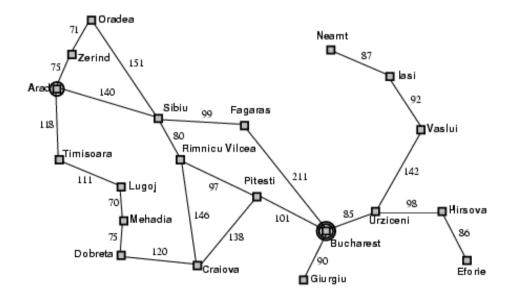
A problem can be defined formally by:

Initial state that the agent starts in

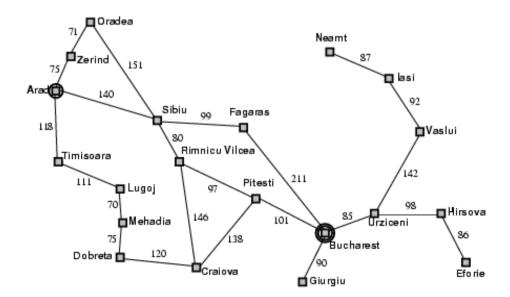
Example: In(Arad)



- Actions available to the agent
 - □ Given a state s, ACTIONS(s) returns the set of actions that can be executed in s
 - We say that each of these actions is applicable in s
 - Example: from the state In(Arad), the applicable actions are {Go(Sibiu), Go(Timisoara), Go(Zerind)}.

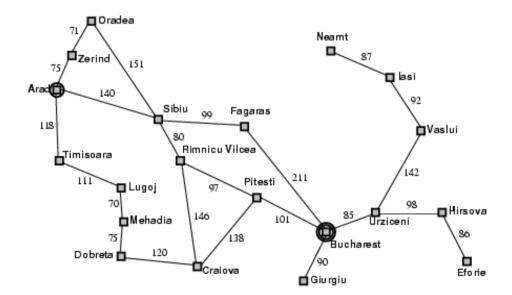


- □ Transition model:
 - RESULT(s,a) returns the <u>state</u> obtained from doing action a in state s
 - Successor: any state reachable from a given state by a single action
 - **Example: RESULT** (In(Arad), Go(Zerind)) = In(Zerind)



- □ Problem state space = (initial state, actions, transition model)
- State space = the set of <u>all states reachable</u> from <u>the initial</u> state by any sequence of actions
- The state space can be depicted as a directed graph:
 nodes → states
 edges → actions
 path → sequence of states connected by a sequence of actions

- □ Goal test: allows to check if a state is a goal
 - **Example:** The agent's goal in Romania is the singleton set { In(Bucharest) }



The **state space** can be depicted as a **directed graph**:

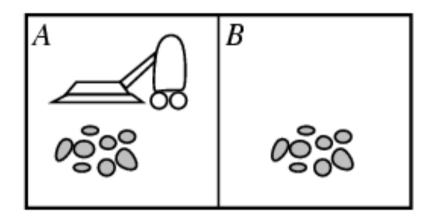
```
    nodes → states
    edges → actions
    path → sequence of states connected by a sequence of actions
```

Path cost: numeric value associated to each path reflecting the desired performance measure

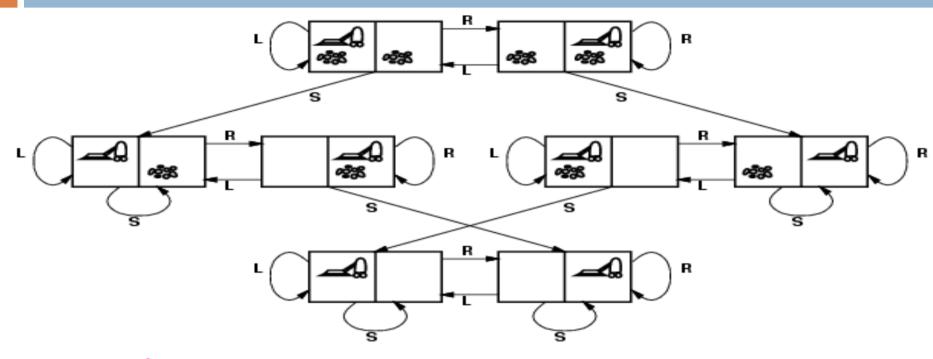
- e.g., sum of distances, number of actions executed, etc.
- c(x,a,y) is the step cost, for going from state x to state y by performing action a
- \square assumed to be ≥ 0
- We assume path costs to be additive: sum of step costs

- Solution: a sequence of actions (path) leading from the <u>initial state</u> to <u>a goal state</u>
- Optimal solution: a solution with minimal path-cost

Example: Vacuum-cleaner world

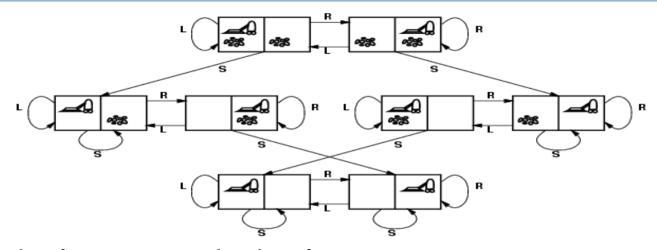


Example: Vacuum world



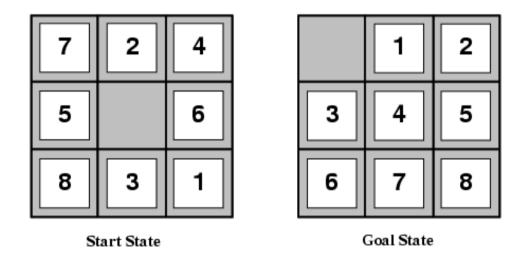
- □ states?
- □ initial state?
- □ actions?
- <u>transition model?</u>
- □ goal test?
- □ path cost?

Example: Vacuum world



- states? dirt locations and robot location
- □ <u>initial state?</u> any state
- actions? Left, Right, Suck
- Trasition model? The actions have the expected effects, except that moving Left in the leftmost square, moving Right in the rightmost square, and Sucking in a clean square have no effect
- goal test? no dirt at all locations
- \square path cost? Each step costs 1 \rightarrow path cost is the number of steps in the path

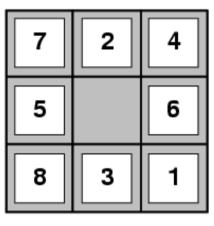
Example: The 8-puzzle



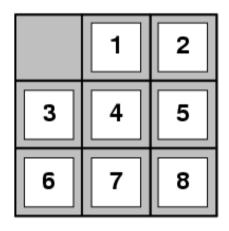
The 8-puzzle

- A 3 × 3 board with eight numbered tiles and a blank space
- A tile adjacent to the blank space can slide into that space
- Object: to reach a specified goal state such as the one shown on the right of the figure

Example: The 8-puzzle



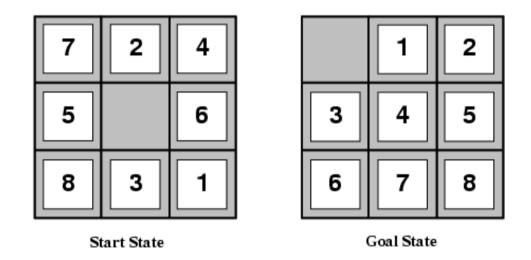




Goal State

- □ states?
- □ <u>initial state?</u>
- □ actions?
- transition model?
- □ goal test?
- □ path cost?

Example: The 8-puzzle



- states? <u>locations</u> of eight <u>tiles</u> and the <u>blank</u> in one of the nine squares
- initial state? any
- <u>actions?</u> move blank left, right, up, down
- <u>transition model?</u> Given a state and an action, it returns the resulting state (that is, the puzzle configuration <u>after moving the blank</u>)
- goal test? goal state (given)
- path cost? Each step cost 1 per move, path cost is the number of steps in the path

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Review: Problem-solving agent

This simple problem-solving agent

- 1. Formulates a goal and a problem
- 2. Searches for a sequence of actions that would solve the problem
- 3. Executes the actions one at a time

When this is complete, it formulates another goal and starts over

Review: Problem formulation

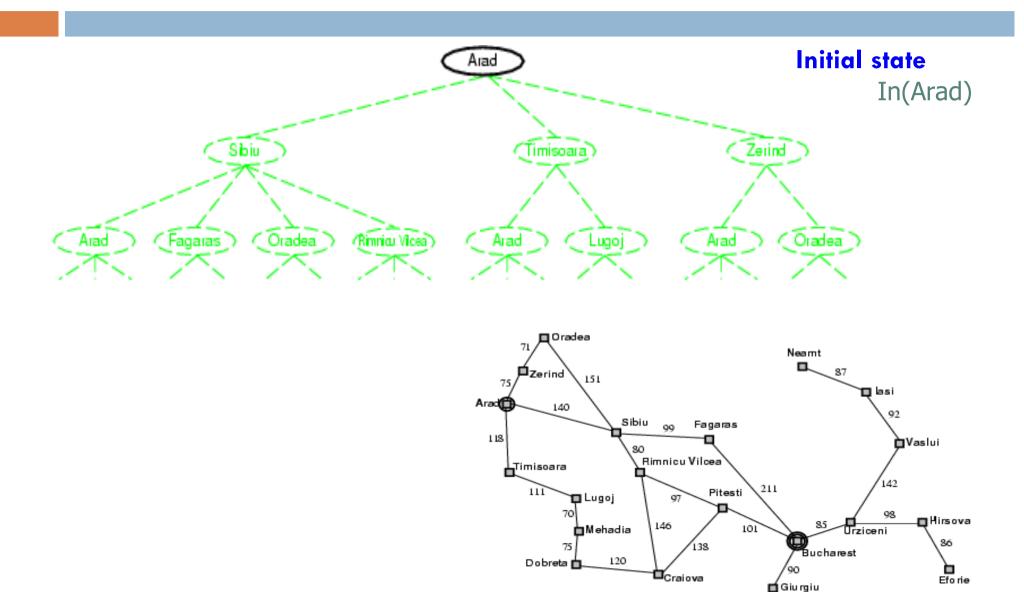
A problem can be defined formally by:

- Initial state that the agent starts in
- Actions available to the agent
- Transition model: A description of what each action does
- Goal test: Determines whether a given state is a goal state
- Path cost: Numeric value associated to each path reflecting the desired performance measure

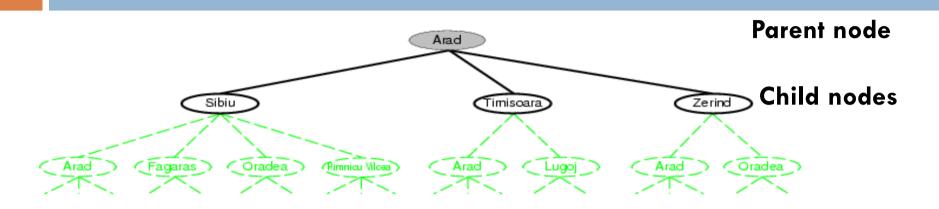
The Search Tree from the initial state to a goal state

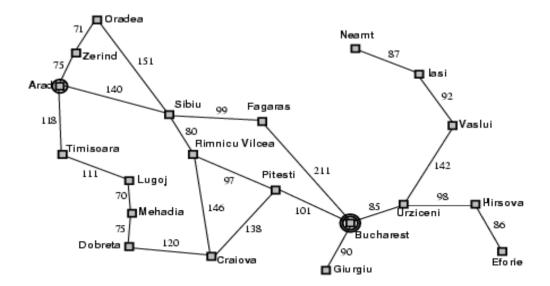
Solution: a **sequence of actions** (path) leading from the initial state to a goal state

- Search algorithms consider possible sequences of actions
- Possible <u>sequences of actions</u> from initial state form a <u>search tree</u>
 - \square Root \rightarrow initial state
 - Nodes → states
 - Branches → actions
 - The same state can appear multiple time
 - Outgoing edges from a node -> all possible actions available in the state represented by the node

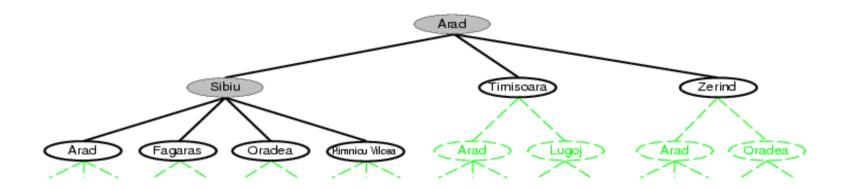


After expanding Arad





After expanding Sibiu

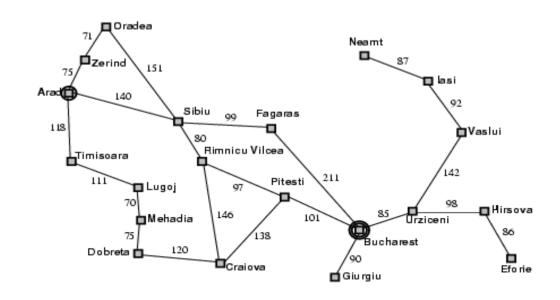


Leaf node:

a node with no children in the tree

Frontier:

The set of **all leaf nodes** available **for expansion** at any given point



Tree search algorithm

function TREE-SEARCH(problem) returns a solution, or failure

initialize the frontier using the initial state of problem

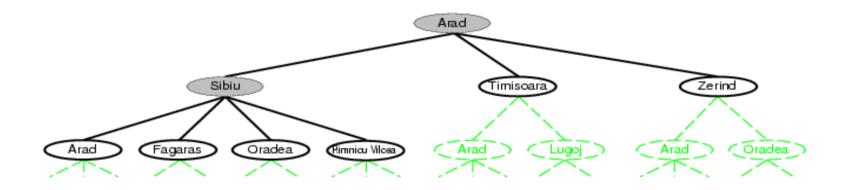
loop do

if the frontier is empty then return failure

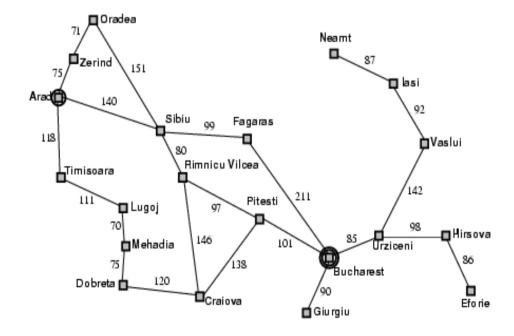
choose a leaf node and remove it from the frontier

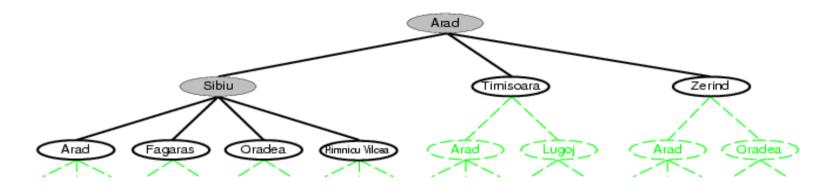
if the node contains a goal state then return the corresponding solution

expand the chosen node, adding the resulting nodes to the frontier



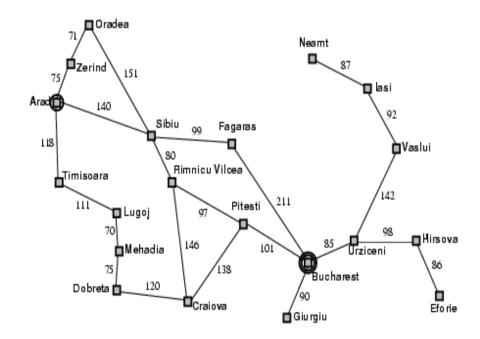
- The search tree includes the path from Arad to Sibiu and back to Arad again!
- The state In(Arad) is a repeated state generated by a loopy path

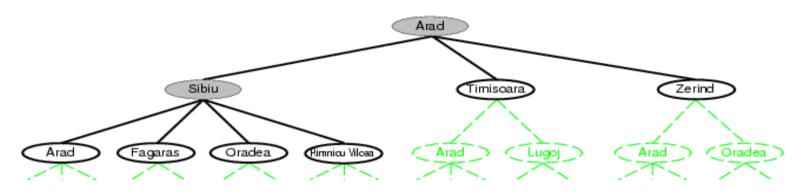




 Loopy paths: special case of redundant paths

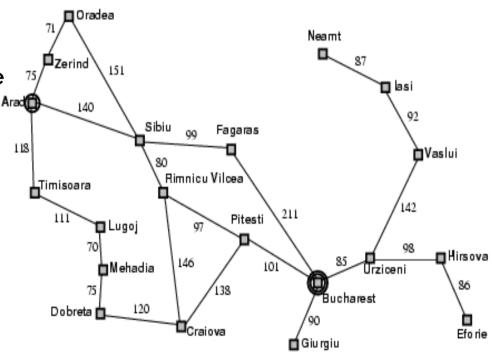
Redundant paths: exist whenever there
is more than one way to get from one
state to another

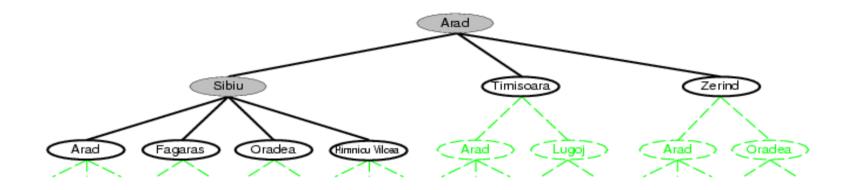




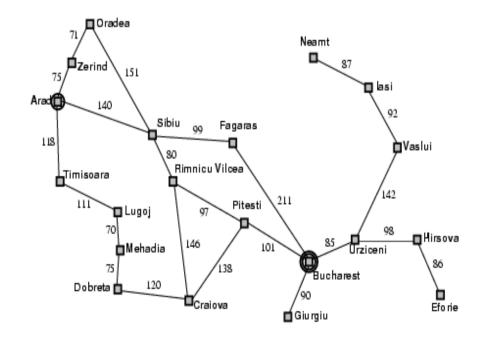
 Redundant paths: exist whenever there is more than one way to get from one state to another

- **Example:** Consider the path
 - Arad–Sibiu (140)
 - Arad-Zerind-Oradea-Sibiu (297)
 - the second path is redundant—it's just a
 worse way to get to the same state





To avoid exploring redundant paths
TREE-SEARCH algorithm is
augmented with explored set that
remembers every expanded node



Graph search algorithm

function GRAPH-SEARCH(problem) returns a solution, or failure

initialize the frontier using the initial state of problem initialize the explored set to be empty

loop do

if the frontier is empty then return failure

choose a leaf node and remove it from the frontier

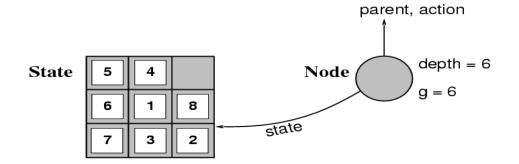
if the node contains a goal state then return the corresponding solution

add the node to the explored set

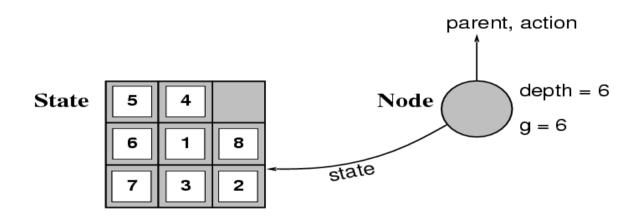
expand the chosen node, <u>adding</u> the resulting nodes to the frontier only if not in the frontier or explored set

Infrastructure for search algorithms

- Search algorithms require a data structure to keep track of the search tree
- □ For each node n of the tree, we have a structure with:
 - n.STATE: the state in the state space to which the node corresponds
 - n.PARENT: the node in the search tree that generated this node
 - n.ACTION: the action that was applied to the parent to generate the node
 - n.PATH-COST: the cost, traditionally denoted by g(n), of the path from the <u>initial state</u> to <u>the node</u>, as indicated by the parent pointers



Infrastructure for search algorithms



- A state corresponds to a configuration of the world
- A node is a data structure used to represent the search tree

Frontier: The set of all leaf nodes available for expansion at any given point

Infrastructure for search algorithms

- Frontier needs to be stored in such a way that the search algorithm can easily choose the next node to expand
 - The appropriate data structure for this is a queue

Operations on a queue:

- EMPTY?(queue) returns true only if there are no more elements in the queue
- POP(queue) removes the first element of the queue and returns it
- INSERT(element, queue) inserts an element and returns the resulting queue

Infrastructure for search algorithms

Queues are characterized by the order in which they
 store the inserted nodes

Three common variants:

- □ FIFO queue
 - which pops the oldest element of the queue
- □ LIFO queue
 - which pops the newest element of the queue
- Priority queue
 - which pops the element of the queue with the *highest* priority according to some ordering function

Search strategies

- □ A search strategy is defined by picking the order of node expansion
- Strategies are evaluated along the following dimensions:
 - completeness: does it always find a solution if one exists?
 - time complexity: number of <u>nodes generated</u>
 - space complexity: maximum number of <u>nodes in memory</u>
 - optimality: does it always find a least-cost solution?

Search strategies

- □ Time and space complexity are measured in terms of
 - b: branching factor of the search tree
 (i.e., <u>maximum</u> number of <u>successors</u> of any node)
 - d: depth of the least-cost solution
 - m: the maximum depth of the state space

Uninformed search strategies

- Uninformed strategies use only the information available in the problem definition
 - generate successors
 - distinguish goal
 - Breadth-first search
 - Uniform-cost search
 - Depth-first search
 - Depth-limited search
 - Iterative deepening search