

Mining Unstructured Data

6. Constituent parsing



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Outline

Syntactic
parsing

Trees and
Grammars

Constituent
Parsing

- 1 Syntactic parsing
 - Goal and motivation

- 2 Trees and Grammars

- 3 Constituent Parsing
 - Background
 - Chart-based methods
 - CKY Algorithm

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Goal and motivation

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Goal and motivation

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- Syntax studies the combination of words in a sentence.
- Syntactic parsing provides information of the combination of words in a sentence (the syntactic structure).
- Syntactic information is relevant for many NLP applications:
 - Authorship recognition
 - Grammar checking
 - Ex: 3th-Singular-noun + basic-verb \implies error
 - Machine Translation
 - Ex: [es] NN+JJ \implies [en] JJ+NN
 - Information Extraction
 - Ex: $X - [subj] \rightarrow \text{visited} \leftarrow [dobj] - Y \implies \text{visit}(X,Y)$
 - ...
- **Goal:** find the syntactic structure associated to a sentence.

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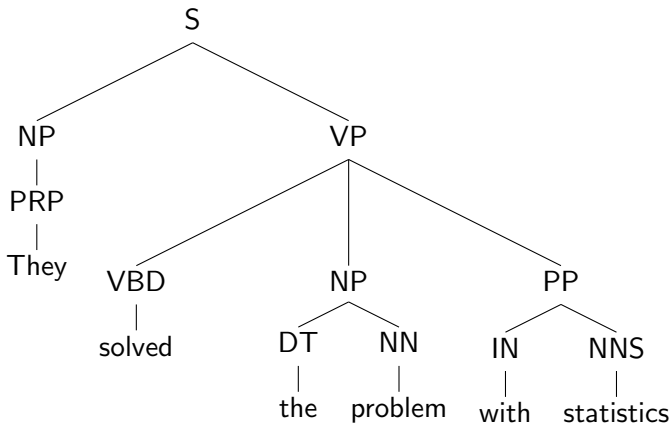
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A Syntactic Tree

Syntactic
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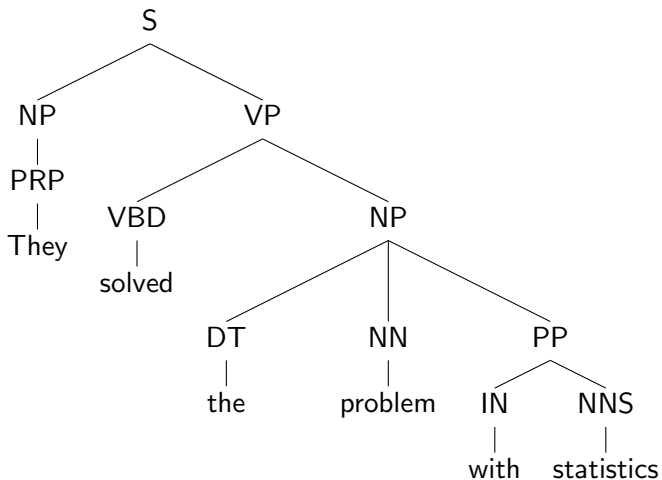


Another Syntactic Tree

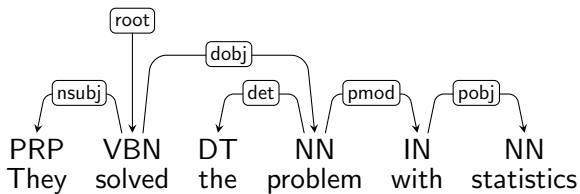
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Dependency Trees



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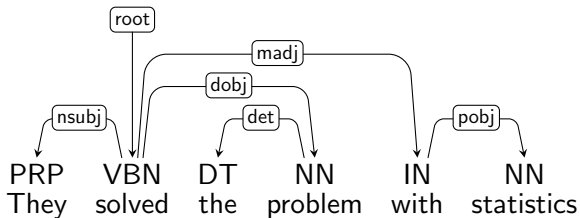
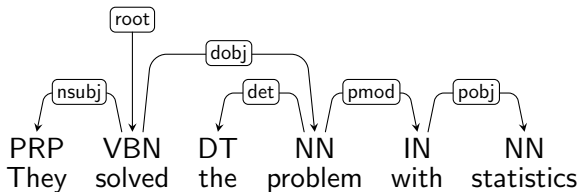
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Dependency Trees

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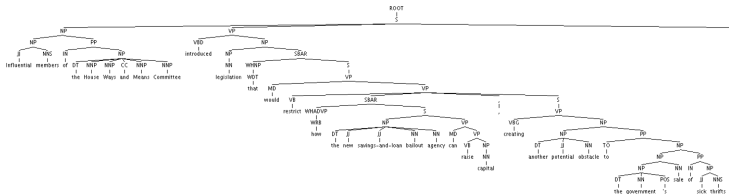


A “real” sentence

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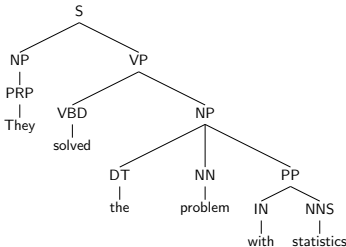
Constituent
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Influential members of the House Ways and Means Committee
introduced legislation that would restrict how the new
savings-and-loan bailout agency can raise capital, creating another
potential obstacle to the government's sale of sick thrifts.

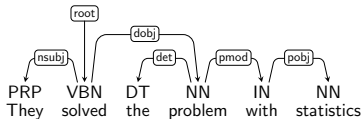
Theories of Syntactic Structure

Constituent Trees



- Main element: constituents (or phrases, or bracketings)
- Constituents = abstract linguistic units
- Results in nested trees

Dependency Trees



- Main element: dependency
- Focus on relations between words
- Handles *free word order* nicely.

Context Free Grammars (CFGs)

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A context-free grammar is defined as a tuple $G = \langle N, \Sigma, R, S \rangle$ where:

- N is a set of non-terminal symbols
- $S \in N$ is a distinguished start symbol
- Σ is a set of terminal symbols
- R is a set of rules of the form $X \rightarrow Y_1 Y_2 \dots Y_n$ where $n \geq 0$, $X \in N$, $Y_i \in N \cup \Sigma$

Context Free Grammars, Example

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$$N = \{S, VP, NP, PP, DT, Vi, Vt, NN, IN\}^1$$

$$S = \{S\}$$

$$\Sigma = \{\text{sleeps, saw, man, woman, telescope, the, with, in}\}$$

$$R = \left\{ \begin{array}{ll} S \rightarrow NP VP & Vi \rightarrow \text{sleeps} \\ S \rightarrow NP Vi & Vt \rightarrow \text{saw} \\ NP \rightarrow DT NN & NN \rightarrow \text{man} \\ NP \rightarrow NP PP & NN \rightarrow \text{woman} \\ PP \rightarrow IN NP & NN \rightarrow \text{telescope} \\ VP \rightarrow Vt NP & DT \rightarrow \text{the} \\ VP \rightarrow VP PP & IN \rightarrow \text{with} \\ VP \rightarrow Vi PP & IN \rightarrow \text{in} \end{array} \right\}$$

¹S=sentence, VP=verb phrase, NP=noun phrase, PP=prepositional phrase, DT=determiner, Vi=intransitive verb, Vt=transitive verb, NN=noun, IN=preposition

Properties of CFGs

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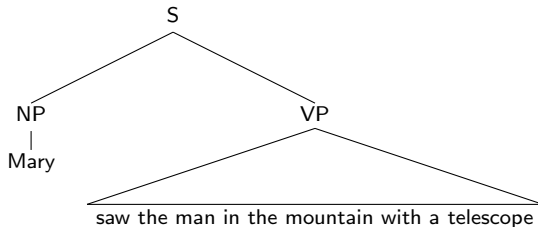
- A CFG defines a set of possible *derivations* (i.e. unique trees)
- A sequence of terminals $s \in \Sigma^*$ is *generated* by the CFG (or *recognized* by it, or *belongs* to the language defined by it) if there is at least a derivation that produces s .
- Some sequences of terminals generated by the CFG may have more than one derivation (*ambiguity*).

Ambiguity

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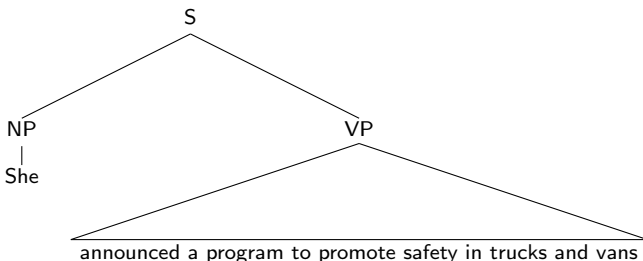
Trees and
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- *Mary used a telescope to see a man who was in the mountain*
- *Mary saw a man who was in the mountain and carried a telescope*
- *Mary was in the mountain and used a telescope to see a man*
- *Mary was in the mountain that has a telescope and saw a man*
- *Mary saw a man who was in the mountain that has a telescope*
- *Mary was in the mountain and saw a man carrying a telescope*

Ambiguity



- *She announced a program aimed to make trucks and vans safer*
- *She used trucks and vans to announce a program aimed to promote safety*
- *She announced a program aimed to make trucks safer. She also announced vans*
- *She used trucks to announce a program aimed to promote safety. She also announced vans*
- *She announced a program. She did so in order to promote safety in trucks and vans*
- *She used trucks and vans to announce a program. She did so in order to promote safety*
- ...

Ambiguity

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Some trees are more likely than others...

Ambiguity

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Some trees are more likely than others...

Can we model that?

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Probabilistic Context Free Grammar (PCFGs)

A context-free grammar is defined as a tuple $G = \langle N, \Sigma, R, S \rangle$ where:

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- R is a set of rules of the form $X \rightarrow Y_1 Y_2 \dots Y_n$ where $n \geq 0$, $X \in N$, $Y_i \in N \cup \Sigma$
- q is a set of non-negative parameters, one for each rule $X \rightarrow \alpha \in R$ such that, for any $X \in N$,

$$\sum_{(X \rightarrow \alpha) \in R} q(X \rightarrow \alpha) = 1$$

Context Free Grammars, Example

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¹S=sentence, VP=verb phrase, NP=noun phrase, PP=prepositional phrase, DT=determiner, Vi=intransitive verb, Vt=transitive verb, NN=noun, IN=preposition

Probabilistic Context Free Grammars, Example

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$$S = \{S\}$$

$$\Sigma = \{\text{sleeps, saw, man, woman, telescope, the, with, in}\}$$

$$R = \left\{ \begin{array}{ll} S \rightarrow NP VP & 0.5 \\ S \rightarrow NP Vi & 0.5 \\ NP \rightarrow DT NN & 0.4 \\ NP \rightarrow NP PP & 0.6 \\ PP \rightarrow IN NP & 1.0 \\ VP \rightarrow Vt NP & 0.4 \\ VP \rightarrow VP PP & 0.1 \\ VP \rightarrow Vi PP & 0.5 \end{array} \quad \begin{array}{ll} Vi \rightarrow \text{sleeps} & 1.0 \\ Vt \rightarrow \text{saw} & 1.0 \\ NN \rightarrow \text{man} & 0.7 \\ NN \rightarrow \text{woman} & 0.2 \\ NN \rightarrow \text{telescope} & 0.1 \\ DT \rightarrow \text{the} & 1.0 \\ IN \rightarrow \text{with} & 0.5 \\ IN \rightarrow \text{in} & 0.5 \end{array} \right\}$$

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Properties of PCFGs

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- The probability of a parse tree $t \in \mathcal{T}_G$ is computed as:

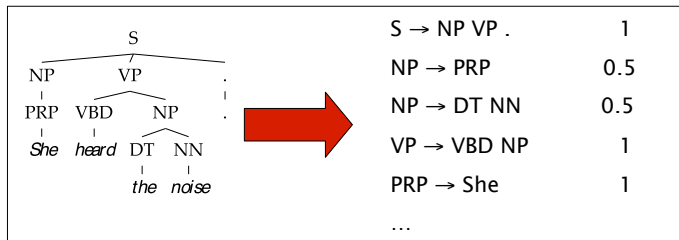
$$p(t) = \prod_{r \in t} q(r)$$

- If there is more than one tree for a sentence, we can rank them by probability.
- The most likely tree for a sentence s is:

$$\arg \max_{t \in \mathcal{T}(s)} p(t)$$

Learning Treebank Grammars

- Read the grammar rules from a treebank



- Set rule weights by maximum likelihood

$$q(\alpha \rightarrow \beta) = \frac{\text{Count}(\alpha \rightarrow \beta)}{\text{Count}(\alpha)}$$

- Smoothing issues apply
- Having the appropriate CFG is critical to success

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Parsing Natural Language Sentences

Possible goals of a parser:

Find all possible trees

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Parsing Natural Language Sentences

Possible goals of a parser:

Find all possible trees, maybe ranked by probability

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Parsing Natural Language Sentences

Possible goals of a parser:

Find all possible trees, maybe ranked by probability or find the most likely tree.

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Parsing Natural Language Sentences

Possible goals of a parser:

Find all possible trees, maybe ranked by probability or find the most likely tree.

Parsing performance depends on many aspects:

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- Grammar expressivity (combination of symbols)

Parsing Natural Language Sentences

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Parsing Natural Language Sentences

Possible goals of a parser:

Find all possible trees, maybe ranked by probability or find the most likely tree.

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- Coverage (words)
- Parsing strategy (bottom-up, top-down)

Parsing Natural Language Sentences

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Parsing Natural Language Sentences

Possible goals of a parser:

Find all possible trees, maybe ranked by probability or find the most likely tree.

Parsing performance depends on many aspects:

- Grammar expressivity (combination of symbols)
- Coverage (words)
- Parsing strategy (bottom-up, top-down)
- Rule application order (largest rule, most likely rule) *heuristics*
largest rule = more specific rule
- Ambiguity management (keep all, select one - probabilities, semantics, pragmatics)
- ...

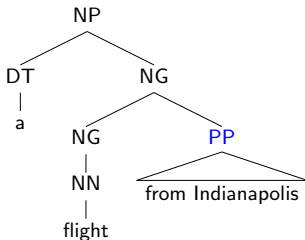
The problem of repeating derivations

- Top-down and bottom-up strategies both lead to repeated derivations when using backtracking

Ex: "a flight from Indianapolis to Houston [on TWA...]"

NG \rightarrow NN

NG \rightarrow NG PP



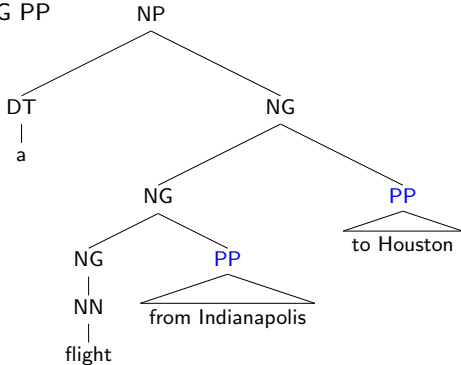
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Chart-based methods

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Properties

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Chart-based methods

- They avoid re-doing derivations using dynamic programming.
- They represent derivations as a directed graph named **chart**.
- They use a dynamic programming table to build the chart.

Chart

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Chart-based methods

- Nodes: positions between words of the input sentence
- Edges: **dotted rules** subsuming a sequence of words of the input sentence
- Dotted rules represent rules states:
 - Passive rules: $A \rightarrow B_1 \dots B_k \bullet$ **e' finita**
 - Active rules: $A \rightarrow B_1 \dots B_i \bullet B_{i+1} \dots B_k$ **e' ancora in corso, sto aspettando per dei pezzi per finire la regola**

Ex:

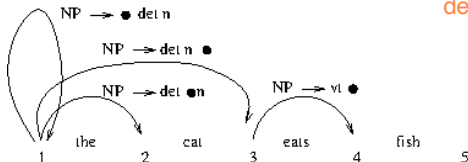
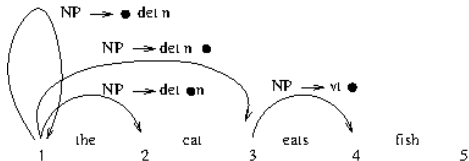


Chart as a dynamic programming table



					[1,5]
				[1,4]	[2,5]
		[1,3] $NP \rightarrow \text{ det } n \bullet$	[2,4]	[3,5]	
	[1,2] $NP \rightarrow \text{ det } \bullet n$	[2,3]	[3,4] $VP \rightarrow v_i \bullet$	[4,5]	
[1,1] $NP \rightarrow \bullet \text{ det } n$	[2,2]	[3,3]	[4,4]	[5,5]	
1	2	3	4	5	
the	cat	eats	fish		

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Chart-based methods

Popular chart-based algorithms

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Chart-based methods

- CKY algorithm
 - introduced dynamic programming
 - limited to CFGs in Chomsky Normal Form
 - passive bottom-up chart parser (only passive rules)
 - straightforward probabilistic version
- Earley algorithm
 - any CFG
 - active top-down parser (active/passive rules)
 - non-straightforward probabilistic version
- Generalized chart parsing

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CKY Algorithm properties

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CKY Algorithm

- Bottom-up
- Requires a grammar in Chomsky Normal Form (CNF).
- Dynamic programming: Store partial results that can be reused in different candidate solutions.
- Analogous to Viterbi in HMMs.
- Intermediate results stored in a *chart* structure.

Chomsky Normal Form (CNF)

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CKY Algorithm

A CFG $G = (N, \Sigma, R, S)$ expressed in CNF is as follows:

- N is a set of non-terminal symbols
- Σ is a set of terminal symbols
- R is a set of rules which take one of two forms:
 - $X \rightarrow Y_1 Y_2$ for $X, Y_1, Y_2 \in N$
 - $X \rightarrow \alpha$ for $X \in N$ and $\alpha \in \Sigma$
- $S \in N$ is a start symbol

Any CFG can be converted into CNF

CNF conversion

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- 1 Convert Hybrid rules: replace terminals with new non-terminals

$$\text{Ex: } INF_VP \rightarrow to\ VP\ (p_1) \implies \begin{array}{l} INF_VP \rightarrow TO\ VP\ (p_1) \\ TO \rightarrow to\ (1.0) \end{array}$$

- 2 Convert non-binary rules:

$$\text{Ex: } S \rightarrow VP\ NP\ PP\ (p_1) \implies \begin{array}{l} S \rightarrow VP\ X\ (p_1) \\ X \rightarrow NP\ PP\ (1.0) \end{array}$$

- 3 Convert unit productions: $A \rightarrow^* B$ and $B \rightarrow \alpha \implies A \rightarrow \alpha$

$$\text{Ex: } \begin{array}{l} NP \rightarrow N\ (p_1) \\ N \rightarrow dog\ (p_2) \end{array} \implies NP \rightarrow dog\ (p_1 * p_2)$$

Exercise

Convert the following PCFG to CNF

1 $S \rightarrow NP VP$ (1.0)

2 $NP \rightarrow det n$ (0.6)

3 $NP \rightarrow n$ (0.4)

4 $VP \rightarrow vt NP PP$ (0.7)

5 $VP \rightarrow vi$ (0.3)

6 $PP \rightarrow with NP$ (1.0)

7 $det \rightarrow the|a$ (0.6|0.4)

8 $n \rightarrow cat|fish|knife$ (0.3|0.5|0.2)

9 $vt \rightarrow eats$ (1.0)

10 $vi \rightarrow eats$ (1.0)

CKY Algorithm

Chart content:

- Maximum probability of a subtree with root X spanning words $i \dots j$:

$$\pi(i, j, X)$$

- Backpath to recover which rules produced the maximum probability tree:

$$\psi(i, j, X)$$

The goal is to compute:

- $\max_{t \in \mathcal{T}(s)} p(t) = \pi(1, n, S)$
- $\psi(1, n, S)$
- It is possible to use it without probabilities to get all parse trees (with higher complexity)

CKY Algorithm

Base case: Tree leaves

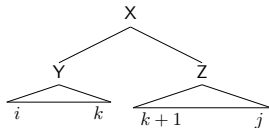
$$\blacksquare \forall i = 1 \dots n, \forall X \rightarrow w_i \in R, \pi(i, i, X) = q(X \rightarrow w_i)$$

Recursive case: Non-terminal nodes

$$\blacksquare \forall i = 1 \dots n, \forall j = (i + 1) \dots n, \forall X \in N$$

$$\pi(i, j, X) = \max_{\substack{X \rightarrow YZ \in R \\ k: i \leq k < j}} q(X \rightarrow YZ) \times \pi(i, k, Y) \times \pi(k + 1, j, Z)$$

$$\psi(i, j, X) = \arg \max_{\substack{X \rightarrow YZ \in R \\ k: i \leq k < j}} q(X \rightarrow YZ) \times \pi(i, k, Y) \times \pi(k + 1, j, Z)$$



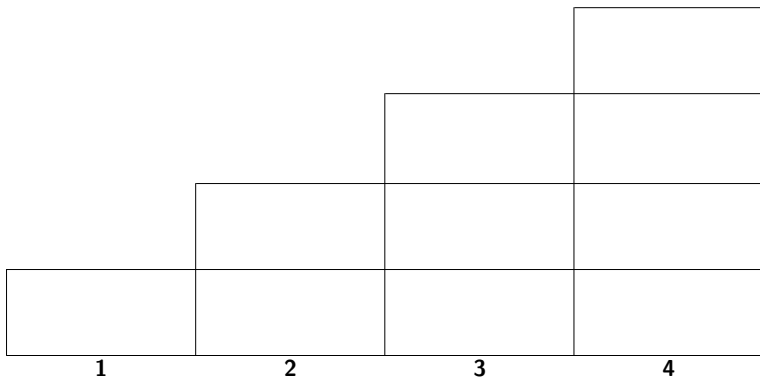
Output:

$$\blacksquare \text{Return } \pi(1, n, S) \text{ and recover backpath through } \psi(1, n, S)$$

CKY Algorithm

Suppose $s = w_1 w_2 w_3 w_4$ and $G = \langle N, \Sigma, S, R, q \rangle$ a PCFG

$$R = \{X_k \rightarrow Y_s Z_t\} \cup \{X_k \rightarrow \alpha\}$$



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Base case:

\forall_k shot $\{X_k \rightarrow w_i\}$ to compute $\pi(i, i, X_k)$

11 $\{X_k \rightarrow w_1\}_k$	22 $\{X_k \rightarrow w_2\}_k$	33 $\{X_k \rightarrow w_3\}_k$	44 $\{X_k \rightarrow w_4\}_k$	
1	2	3	4	

CKY Algorithm

Suppose $s = w_1 w_2 w_3 w_4$ and $G = \langle N, \Sigma, S, R, q \rangle$ a PCFG

$$R = \{X_k \rightarrow Y_s Z_t\} \cup \{X_k \rightarrow \alpha\}$$

Recursive case:

\forall_k shot $\{X_k \rightarrow Y_s Z_t\}$ to get $\varphi(i, j, X_k)$ and
compute $\pi(i, j, X_k)$

	12	23	34	
11 $\{X_k \rightarrow w_1\}_k$	22 $\{X_k \rightarrow w_2\}_k$	33 $\{X_k \rightarrow w_3\}_k$	44 $\{X_k \rightarrow w_4\}_k$	
1	2	3	4	

CKY Algorithm

\forall_k shot $\{X_k \rightarrow Y_s Z_t\}$ to get $\varphi(i, j, X_k)$ and compute $\pi(i, j, X_k)$

\forall_k shot $\{X_k \rightarrow Y_s Z_t\}$ to get $\varphi(i, j, X_k)$ and compute $\pi(i, j, X_k)$

		13	24
	12	23	34
11 $\{X_k \rightarrow w_1\}_k$	22 $\{X_k \rightarrow w_2\}_k$	33 $\{X_k \rightarrow w_3\}_k$	44 $\{X_k \rightarrow w_4\}_k$
1	2	3	4

CKY Algorithm

Suppose $s = w_1 w_2 w_3 w_4$ and $G = \langle N, \Sigma, S, R, q \rangle$ a PCFG

$$R = \{X_k \rightarrow Y_s Z_t\} \cup \{X_k \rightarrow \alpha\}$$

Recursive case:

\forall_k shot $\{X_k \rightarrow Y_s Z_t\}$ to get $\varphi(i, j, X_k)$ and
compute $\pi(i, j, X_k)$

			14
		13	24
	12	23	34
11 $\{X_k \rightarrow w_1\}_k$	22 $\{X_k \rightarrow w_2\}_k$	33 $\{X_k \rightarrow w_3\}_k$	44 $\{X_k \rightarrow w_4\}_k$
1	2	3	4

CKY Algorithm

Suppose $s = w_1 w_2 w_3 w_4$ and $G = \langle N, \Sigma, S, R, q \rangle$ a PCFG

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Recursive case:

\forall_k shot $\{X_k \rightarrow Y_s Z_t\}$ to get $\varphi(i, j, X_k)$ and
compute $\pi(i, j, X_k)$

Example for (1,3)

		13 $\{X_k \rightarrow Y_{s,11} Z_{t,23}\}_k$	24
	12	23	34
11 $\{X_k \rightarrow w_1\}_k$	22 $\{X_k \rightarrow w_2\}_k$	33 $\{X_k \rightarrow w_3\}_k$	44 $\{X_k \rightarrow w_4\}_k$
1	2	3	4

CKY Algorithm

Suppose $s = w_1 w_2 w_3 w_4$ and $G = \langle N, \Sigma, S, R, q \rangle$ a PCFG

$$R = \{X_k \rightarrow Y_s Z_t\} \cup \{X_k \rightarrow \alpha\}$$

Recursive case:

\forall_k shot $\{X_k \rightarrow Y_s Z_t\}$ to get $\varphi(i, j, X_k)$ and
compute $\pi(i, j, X_k)$

Example for (1,3)

		13 $\{X_k \rightarrow Y_{s,12} Z_{t,33}\}_k$	24
	12	23	34
11 $\{X_k \rightarrow w_1\}_k$	22 $\{X_k \rightarrow w_2\}_k$	33 $\{X_k \rightarrow w_3\}_k$	44 $\{X_k \rightarrow w_4\}_k$
1	2	3	4

Exercise

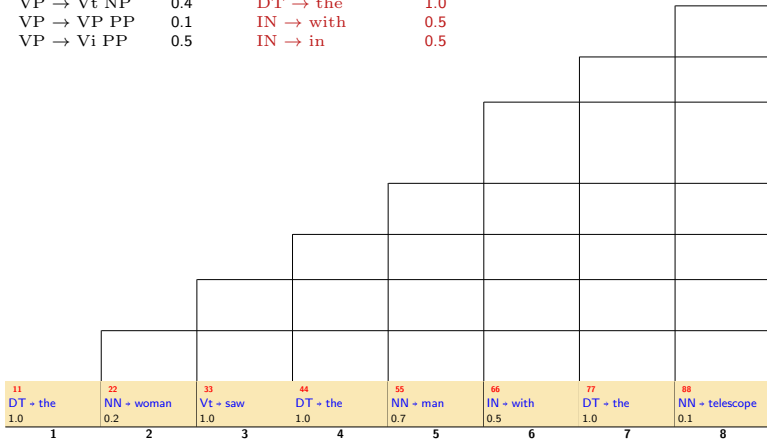
Compute the best parse tree and its probability for the following input sentence using the PCFG:

“the woman saw the man with the telescope”

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
$NP \rightarrow NP PP$	0.6	$NN \rightarrow \text{woman}$	0.2
$PP \rightarrow IN NP$	1.0	$NN \rightarrow \text{telescope}$	0.1
$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

CKY Algorithm - Example

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
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$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5



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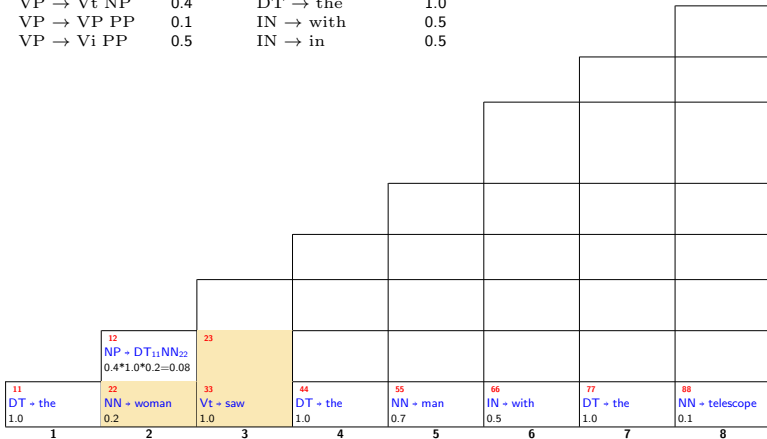
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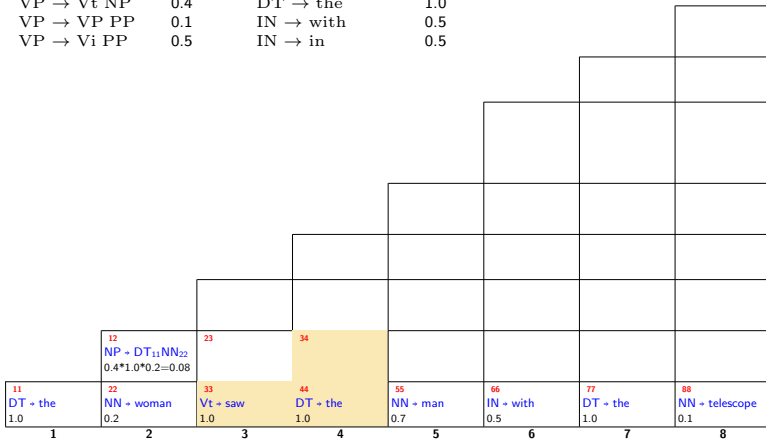
CKY Algorithm - Example

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
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$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5



CKY Algorithm - Example

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$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5



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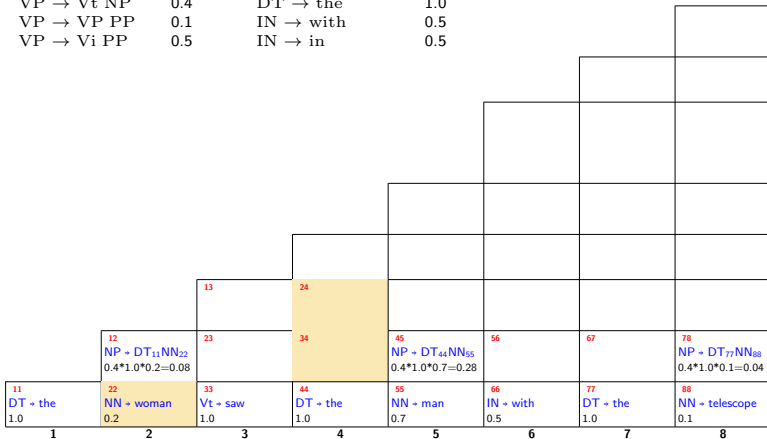
[illegible]

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[illegible]

CKY Algorithm - Example

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
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[illegible]

CKY Algorithm - Example

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
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$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

		13	24	35				
	12	23	34	45	56	67	78	
	$NP \rightarrow DT_{11} NN_{22}$ $0.4 * 1.0 * 0.2 = 0.08$			$NP \rightarrow DT_{44} NN_{55}$ $0.4 * 1.0 * 0.7 = 0.28$			$NP \rightarrow DT_{77} NN_{88}$ $0.4 * 1.0 * 0.1 = 0.04$	
11	22	33	44	55	66	77	88	
$DT \rightarrow \text{the}$ 1.0	$NN \rightarrow \text{woman}$ 0.2	$Vt \rightarrow \text{saw}$ 1.0	$DT \rightarrow \text{the}$ 1.0	$NN \rightarrow \text{man}$ 0.7	$IN \rightarrow \text{with}$ 0.5	$DT \rightarrow \text{the}$ 1.0	$NN \rightarrow \text{telescope}$ 0.1	
1	2	3	4	5	6	7	8	

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$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
$NP \rightarrow NP PP$	0.6	$NN \rightarrow \text{woman}$	0.2
$PP \rightarrow IN NP$	1.0	$NN \rightarrow \text{telescope}$	0.1
$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

		13	24	35	46		
	12	23	34	45	56	67	78
	$NP \rightarrow DT_{11} NN_{22}$ $0.4 * 1.0 * 0.2 = 0.08$			$VP \rightarrow Vt_{33} NP_{45}$ $0.4 * 1.0 * 0.28 = 0.11$			$NP \rightarrow DT_{77} NN_{88}$ $0.4 * 1.0 * 0.1 = 0.04$
11	22	33	44	55	66	77	88
$DT \rightarrow \text{the}$ 1.0	$NN \rightarrow \text{woman}$ 0.2	$Vt \rightarrow \text{saw}$ 1.0	$DT \rightarrow \text{the}$ 1.0	$NN \rightarrow \text{man}$ 0.7	$IN \rightarrow \text{with}$ 0.5	$DT \rightarrow \text{the}$ 1.0	$NN \rightarrow \text{telescope}$ 0.1
1	2	3	4	5	6	7	8

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$S \rightarrow NP VP$	0.5	$Vi \rightarrow sleeps$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow saw$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow man$	0.7
$NP \rightarrow NP PP$	0.6	$NN \rightarrow woman$	0.2
$PP \rightarrow IN NP$	1.0	$NN \rightarrow telescope$	0.1
$VP \rightarrow Vt NP$	0.4	$DT \rightarrow the$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow with$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow in$	0.5

		13	24	35 $VP \rightarrow Vt_{33}NP_{45}$ $0.4 * 1.0 * 0.28 = 0.112$	46	57	
	12 $NP \rightarrow DT_{11}NN_{22}$ $0.4 * 1.0 * 0.2 = 0.08$	23	34	45 $NP \rightarrow DT_{44}NN_{55}$ $0.4 * 1.0 * 0.7 = 0.28$	56	67	78 $NP \rightarrow DT_{77}NN_{88}$ $0.4 * 1.0 * 0.1 = 0.04$
11 $DT \rightarrow the$ 1.0	22 $NN \rightarrow woman$ 0.2	33 $Vt \rightarrow saw$ 1.0	44 $DT \rightarrow the$ 1.0	55 $NN \rightarrow man$ 0.7	66 $IN \rightarrow with$ 0.5	77 $DT \rightarrow the$ 1.0	88 $NN \rightarrow telescope$ 0.1
1	2	3	4	5	6	7	8

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$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
$NP \rightarrow NP PP$	0.6	$NN \rightarrow \text{woman}$	0.2
$PP \rightarrow IN NP$	1.0	$NN \rightarrow \text{telescope}$	0.1
$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

		13	24	35 $VP \rightarrow Vt_{33}NP_{45}$ $0.4 * 1.0 * 0.28 = 0.112$	46	57		
	12 $NP \rightarrow DT_{11}NN_{22}$ $0.4 * 1.0 * 0.2 = 0.08$	23	34	45 $NP \rightarrow DT_{44}NN_{55}$ $0.4 * 1.0 * 0.7 = 0.28$	56	67	78 $NP \rightarrow DT_{77}NN_{88}$ $0.4 * 1.0 * 0.1 = 0.04$	
11 $DT \rightarrow \text{the}$ 1.0	22 $NN \rightarrow \text{woman}$ 0.2	33 $Vt \rightarrow \text{saw}$ 1.0	44 $DT \rightarrow \text{the}$ 1.0	55 $NN \rightarrow \text{man}$ 0.7	66 $IN \rightarrow \text{with}$ 0.5	77 $DT \rightarrow \text{the}$ 1.0	88 $NN \rightarrow \text{telescope}$ 0.1	
1	2	3	4	5	6	7	8	

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VP → Vt NP	0.4	DT → the	1.0					
VP → VP PP	0.1	IN → with	0.5					
VP → Vi PP	0.5	IN → in	0.5					
		13	24	35 VP → Vt ₃₃ NP ₄₅ 0.4*1.0*0.28=0.112	46	57	68 PP → IN ₆₆ NP ₇₈ 1.0*0.5*0.04=0.02	
	12 NP → DT ₁₁ NN ₂₂ 0.4*1.0*0.2=0.08	23	34	45 NP → DT ₄₄ NN ₅₅ 0.4*1.0*0.7=0.28	56	67	78 NP → DT ₇₇ NN ₈₈ 0.4*1.0*0.1=0.04	
11 DT → the 1.0	22 NN → woman 0.2	33 Vt → saw 1.0	44 DT → the 1.0	55 NN → man 0.7	66 IN → with 0.5	77 DT → the 1.0	88 NN → telescope 0.1	
1	2	3	4	5	6	7	8	

CKY Algorithm - Example

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
$NP \rightarrow NP PP$	0.6	$NN \rightarrow \text{woman}$	0.2
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			14				
		13	24	35 $VP \rightarrow Vt_{33}NP_{45}$ $0.4 * 1.0 * 0.28 = 0.112$	46	57	68 $PP \rightarrow IN_{66}NP_{78}$ $1.0 * 0.5 * 0.04 = 0.02$
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1	2	3	4	5	6	7	8

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$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
$NP \rightarrow NP PP$	0.6	$NN \rightarrow \text{woman}$	0.2
$PP \rightarrow IN NP$	1.0	$NN \rightarrow \text{telescope}$	0.1
$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
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$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

			14				
		13	24	35 $VP \rightarrow Vt_{33}NP_{45}$ $0.4 * 1.0 * 0.28 = 0.112$	46	57	68 $PP \rightarrow IN_{66}NP_{78}$ $1.0 * 0.5 * 0.04 = 0.02$
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1	2	3	4	5	6	7	8

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$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
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			14				
		13	24	35 $VP \rightarrow Vt_{33}NP_{45}$ $0.4 * 1.0 * 0.28 = 0.112$	46	57	68 $PP \rightarrow IN_{66}NP_{78}$ $1.0 * 0.5 * 0.04 = 0.02$
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11 $DT \rightarrow \text{the}$ 1.0	22 $NN \rightarrow \text{woman}$ 0.2	33 $Vt \rightarrow \text{saw}$ 1.0	44 $DT \rightarrow \text{the}$ 1.0	55 $NN \rightarrow \text{man}$ 0.7	66 $IN \rightarrow \text{with}$ 0.5	77 $DT \rightarrow \text{the}$ 1.0	88 $NN \rightarrow \text{telescope}$ 0.1
1	2	3	4	5	6	7	8

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CKY Algorithm - Example

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
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$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

			14	25	36	47	58
		13	24	35 $VP \rightarrow Vt_{33}NP_{45}$ $0.4 * 1.0 * 0.28 = 0.112$	46	57	68 $PP \rightarrow IN_{66}NP_{78}$ $1.0 * 0.5 * 0.04 = 0.02$
	12 $NP \rightarrow DT_{11}NN_{22}$ $0.4 * 1.0 * 0.2 = 0.08$	23	34	45 $NP \rightarrow DT_{44}NN_{55}$ $0.4 * 1.0 * 0.7 = 0.28$	56	67	78 $NP \rightarrow DT_{77}NN_{88}$ $0.4 * 1.0 * 0.1 = 0.04$
11 $DT \rightarrow \text{the}$ 1.0	22 $NN \rightarrow \text{woman}$ 0.2	33 $Vt \rightarrow \text{saw}$ 1.0	44 $DT \rightarrow \text{the}$ 1.0	55 $NN \rightarrow \text{man}$ 0.7	66 $IN \rightarrow \text{with}$ 0.5	77 $DT \rightarrow \text{the}$ 1.0	88 $NN \rightarrow \text{telescope}$ 0.1
1	2	3	4	5	6	7	8

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					15 S → NP ₁₂ VP ₃₅ 0.5*0.08*0.112= 4.48e-3			
			14		25	36	47	58
		13	24		35 VP → Vt ₃₃ NP ₄₅ 0.4*1.0*0.28=0.112	46	57	68 PP → IN ₆₆ NP ₇₈ 1.0*0.5*0.04=0.02
	12 NP → DT ₁₁ NN ₂₂ 0.4*1.0*0.2=0.08	23	34		45 NP → DT ₄₄ NN ₅₅ 0.4*1.0*0.7=0.28	56	67	78 NP → DT ₇₇ NN ₈₈ 0.4*1.0*0.1=0.04
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1	2	3	4	5	6	7	8	

CKY Algorithm - Example

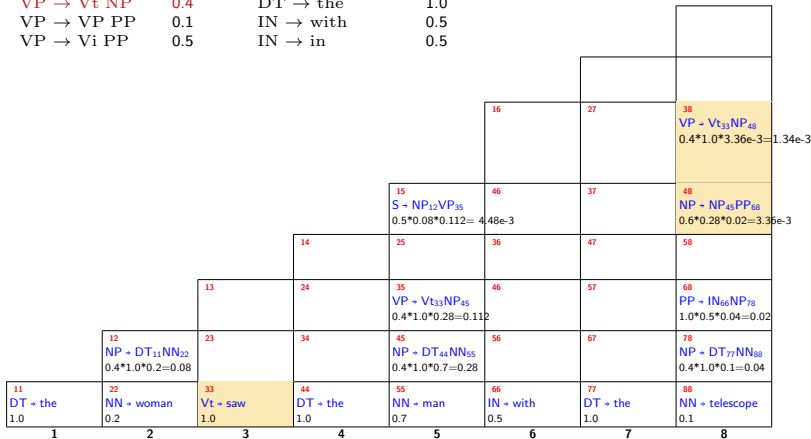
$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
$NP \rightarrow NP PP$	0.6	$NN \rightarrow \text{woman}$	0.2
$PP \rightarrow IN NP$	1.0	$NN \rightarrow \text{telescope}$	0.1
$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

Syntactic
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Trees and
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Constituent
Parsing

CKY Algorithm



CKY Algorithm

[illegible]

CKY Algorithm

VP → Vt NP	0.4	DT → the	1.0					
VP → VP PP	0.1	IN → with	0.5					
VP → Vi PP	0.5	IN → in	0.5					
					16	27	38	VP → Vt ₃₃ NP ₄₈ 0.4*1.0*3.36e-3=1.34e-3
				15	46	37	48	NP → NP ₄₅ PP ₆₈ 0.6*0.28*0.02=3.36e-3
				S → NP ₁₂ VP ₃₅ 0.5*0.08*0.112=4.48e-3				
			14	25	36	47	58	
		13	24	35	46	57	68	NP → IN ₆₆ NP ₇₈ 1.0*0.5*0.04=0.02
				VP → Vt ₃₃ NP ₄₅ 0.4*1.0*0.28=0.112				
	12	23	34	45	56	67	78	NP → DT ₇₇ NN ₈₈ 0.4*1.0*0.1=0.04
	NP → DT ₁₁ NN ₂₂ 0.4*1.0*0.2=0.08			NP → DT ₄₄ NN ₅₅ 0.4*1.0*0.7=0.28				
11	22	33	44	55	66	77	88	
DT → the 1.0	NN → woman 0.2	Vt → saw 1.0	DT → the 1.0	NN → man 0.7	IN → with 0.5	DT → the 1.0	NN → telescope 0.1	
1	2	3	4	5	6	7	8	

CKY Algorithm - Example

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
$NP \rightarrow DT NN$	0.4	$NN \rightarrow \text{man}$	0.7
$NP \rightarrow NP PP$	0.6	$NN \rightarrow \text{woman}$	0.2
$PP \rightarrow IN NP$	1.0	$NN \rightarrow \text{telescope}$	0.1
$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

							18 $S \rightarrow NP_{12} VP_{38}$ $0.5 * 0.08 * 1.34e-3 = 5.38e-5$
						17	28
				16		27	38 $VP \rightarrow Vt_{33} NP_{48}$ $0.4 * 1.0 * 3.36e-3 = 1.34e-3$
			15 $S \rightarrow NP_{12} VP_{35}$ $0.5 * 0.08 * 0.112 = 4.48e-3$	46		37	48 $NP \rightarrow NP_{45} PP_{68}$ $0.6 * 0.28 * 0.02 = 3.36e-3$
		14	25	36		47	58
		13	24	35 $VP \rightarrow Vt_{33} NP_{45}$ $0.4 * 1.0 * 0.28 = 0.112$	46	57	68 $PP \rightarrow IN_{66} NP_{78}$ $1.0 * 0.5 * 0.04 = 0.02$
	12 $NP \rightarrow DT_{11} NN_{22}$ $0.4 * 1.0 * 0.2 = 0.08$	23	34	45 $NP \rightarrow DT_{44} NN_{55}$ $0.4 * 1.0 * 0.7 = 0.28$	56	67	78 $NP \rightarrow DT_{77} NN_{88}$ $0.4 * 1.0 * 0.1 = 0.04$
11 $DT \rightarrow \text{the}$ 1.0	22 $NN \rightarrow \text{woman}$ 0.2	33 $Vt \rightarrow \text{saw}$ 1.0	44 $DT \rightarrow \text{the}$ 1.0	55 $NN \rightarrow \text{man}$ 0.7	66 $IN \rightarrow \text{with}$ 0.5	77 $DT \rightarrow \text{the}$ 1.0	88 $NN \rightarrow \text{telescope}$ 0.1
1	2	3	4	5	6	7	8

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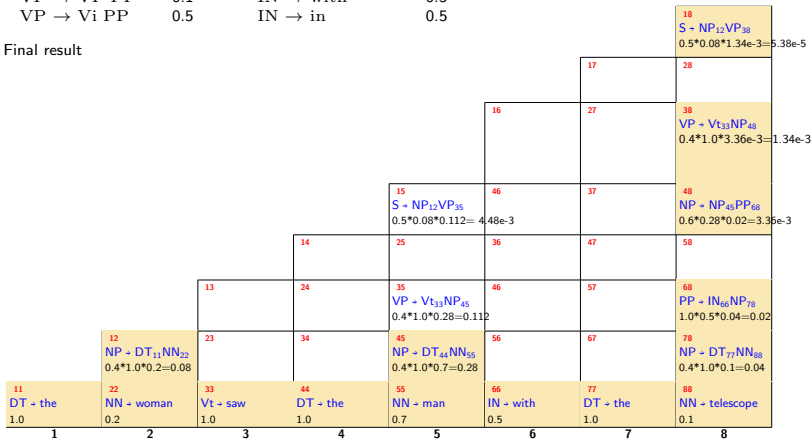
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CKY Algorithm - Example

$S \rightarrow NP VP$	0.5	$Vi \rightarrow \text{sleeps}$	1.0
$S \rightarrow NP Vi$	0.5	$Vt \rightarrow \text{saw}$	1.0
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$VP \rightarrow Vt NP$	0.4	$DT \rightarrow \text{the}$	1.0
$VP \rightarrow VP PP$	0.1	$IN \rightarrow \text{with}$	0.5
$VP \rightarrow Vi PP$	0.5	$IN \rightarrow \text{in}$	0.5

Final result



Syntactic
parsing

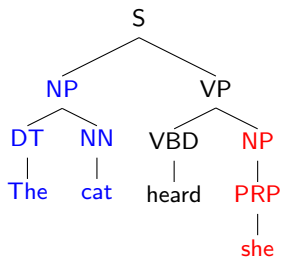
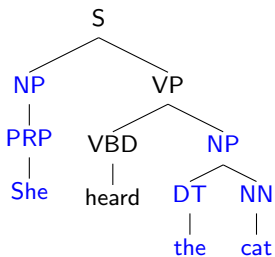
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Why *context-free* ?

- Context-free means *context independent*, i.e, assumes that any expansion of a non-terminal is applicable, regardless of the context in which it occurs.



Natural Language is not Context-Free

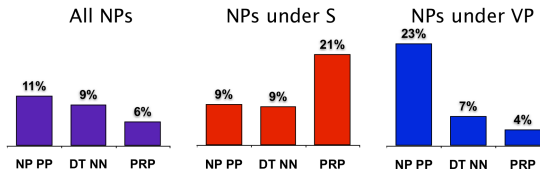
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Trees and
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CKY Algorithm

- NP expansion (for instance) is highly dependent on the parent of the NP



- Complete context independence is a too strong independence assumption for natural language.

Natural Language is not Context-Free

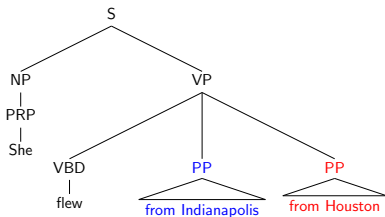
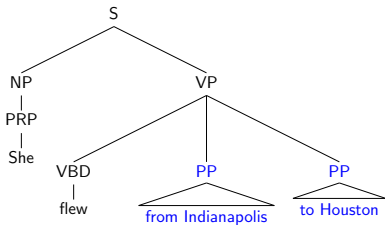
- The application of a rule may affect the applicability of others

Syntactic
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Natural Language is not Context-Free

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- May contain non-projective structures:

John saw the dog yesterday which was a Yorkshire Terrier