



UNIVERSITÀ DEGLI STUDI DI PADOVA

The bilateral filter

Stefano Ghidoni



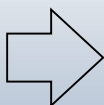


- Very commonly used
- A spatial filtering!
- Recent method
 - Carlo Tomasi, Roberto Manduchi, “Bilateral Filtering for Gray and Color Images”, Proceedings of the ICCV 1998
- Many applications with high quality results
- Based on the gaussian filter
 - But: edge-preserving filter

- What is left behind when we use a gaussian filter?



input



smoothed



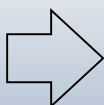
residual

Gaussian Convolution

- What is left behind when we use a bilateral filter?



input



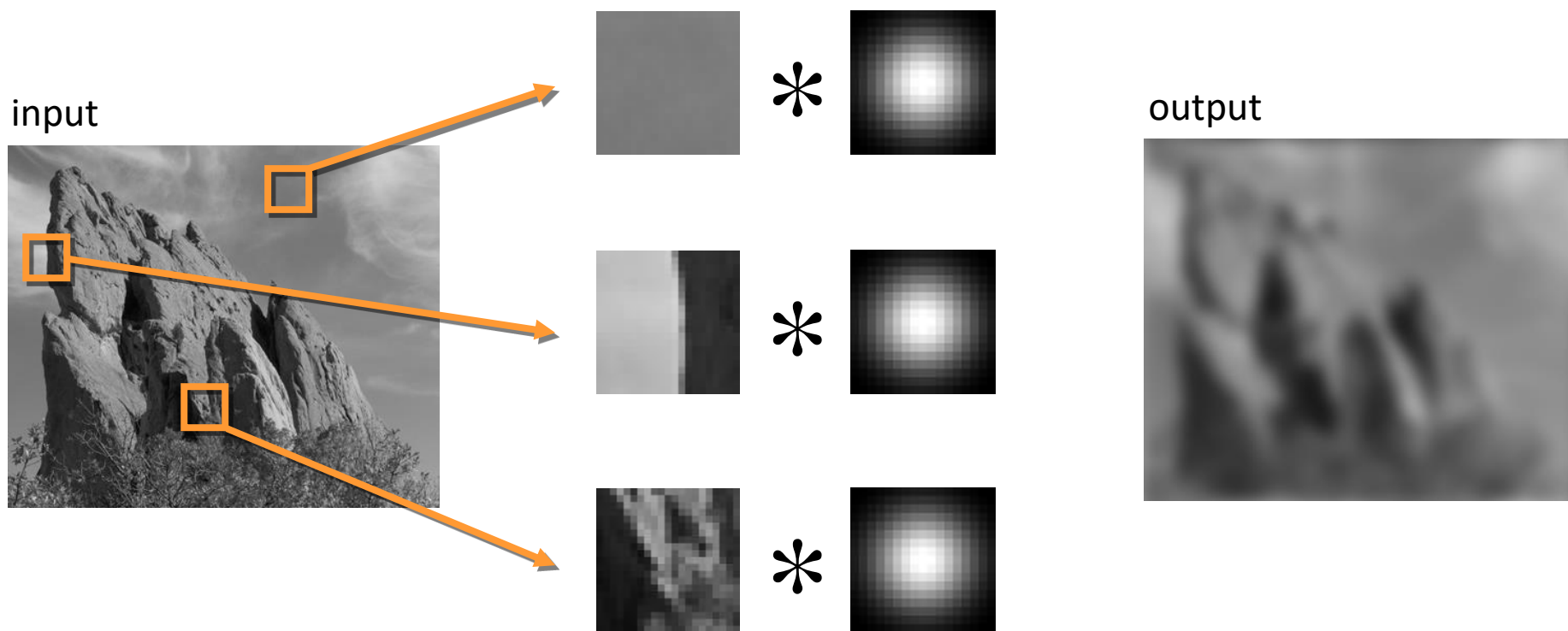
smoothed



residual

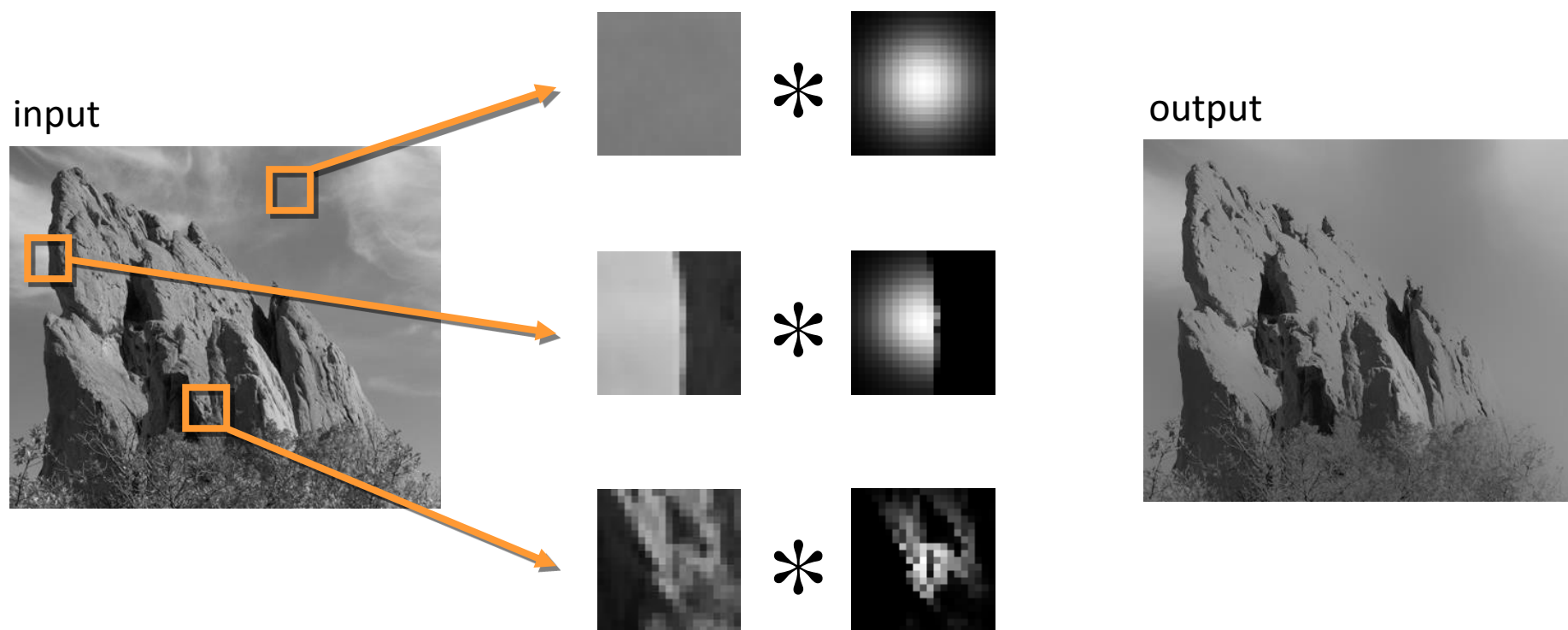
Edge-preserving: Bilateral Filter

- Kernel with the gaussian filter



Same Gaussian kernel everywhere

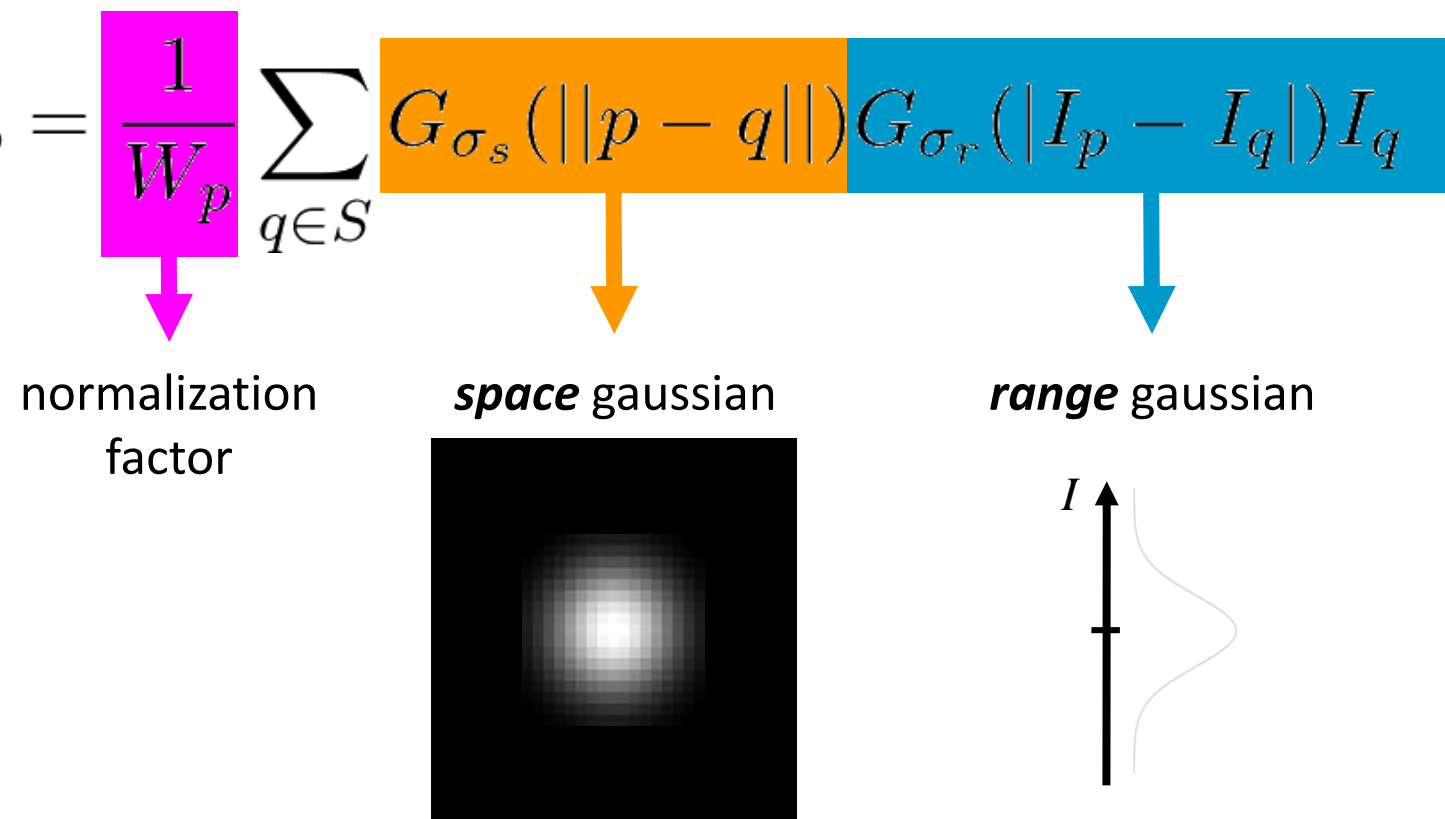
- Kernel with the bilateral filter



The kernel shape depends on the image content

Bilateral filter: **weighted average of pixels with a new weight**

$$BF[I]_p = \frac{1}{W_p} \sum_{q \in S} G_{\sigma_s}(\|p - q\|) G_{\sigma_r}(|I_p - I_q|) I_q$$



normalization factor

space gaussian

range gaussian

- The factor G_{σ_s} depends on geometrical distance
 - Decreases the influence of distant pixels
- The factor G_{σ_r} depends on the gray level distance
 - Decreases the influence of pixels with different intensity values

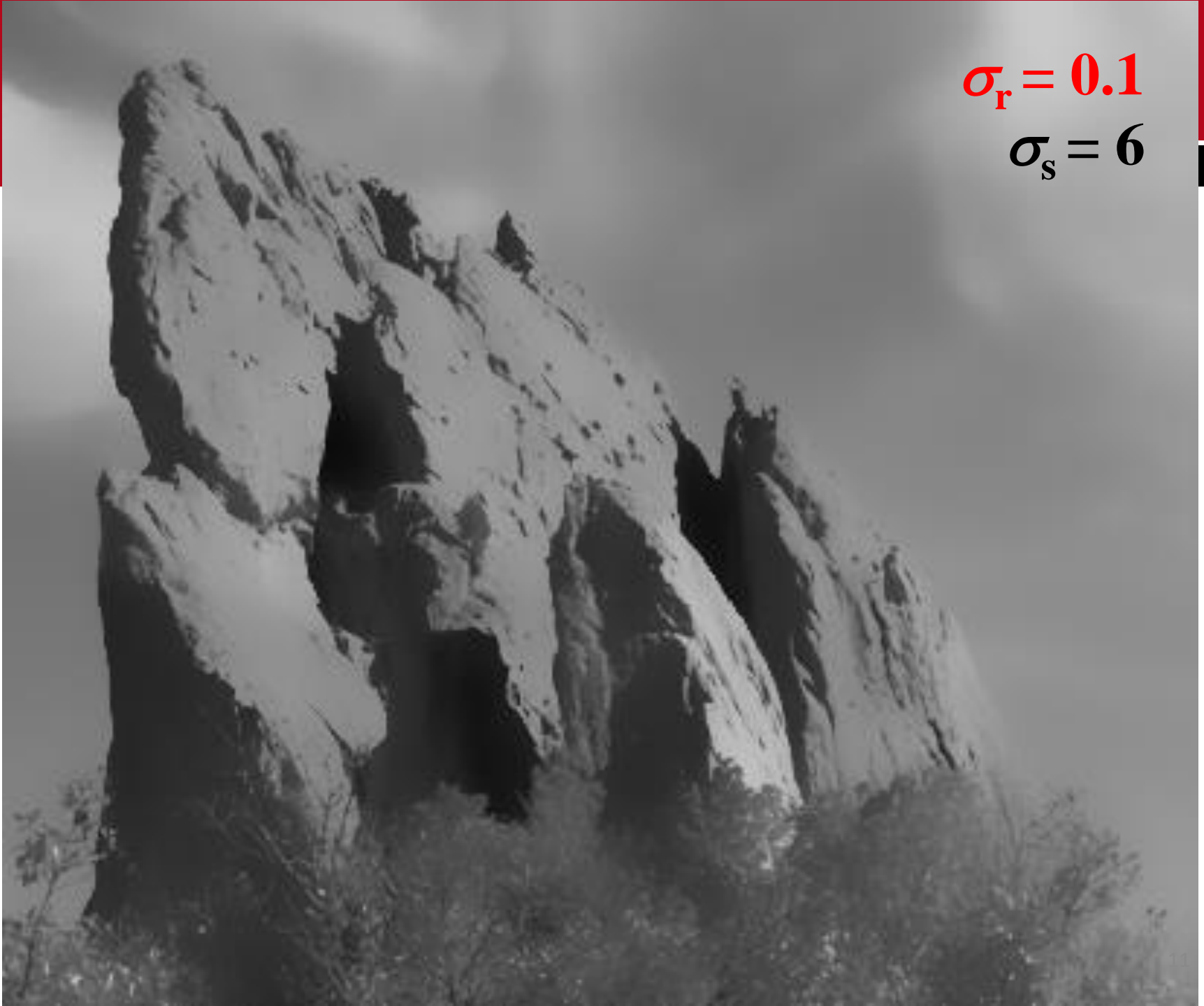
$$BF[I]_p = \frac{1}{W_p} \sum_{q \in S} G_{\sigma_s}(\|p - q\|) G_{\sigma_r}(|I_p - I_q|) I_q$$

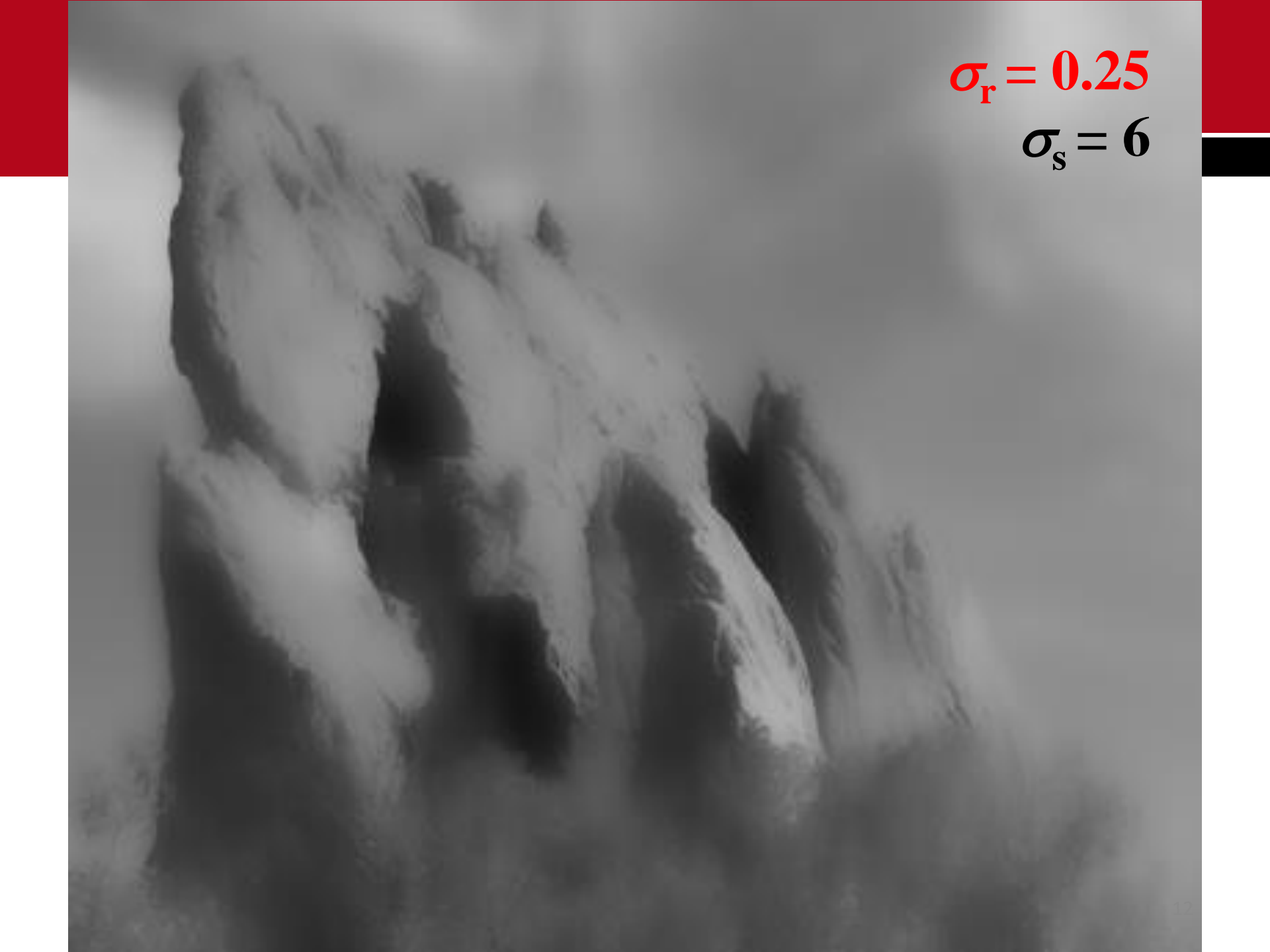
Effect of σ_r

input



$$\sigma_r = 0.1$$
$$\sigma_s = 6$$




$$\sigma_r = 0.25$$

$$\sigma_s = 6$$



$\sigma_r = \infty$
(Gaussian blur)

$\sigma_s = 6$

Effect of σ_s

input

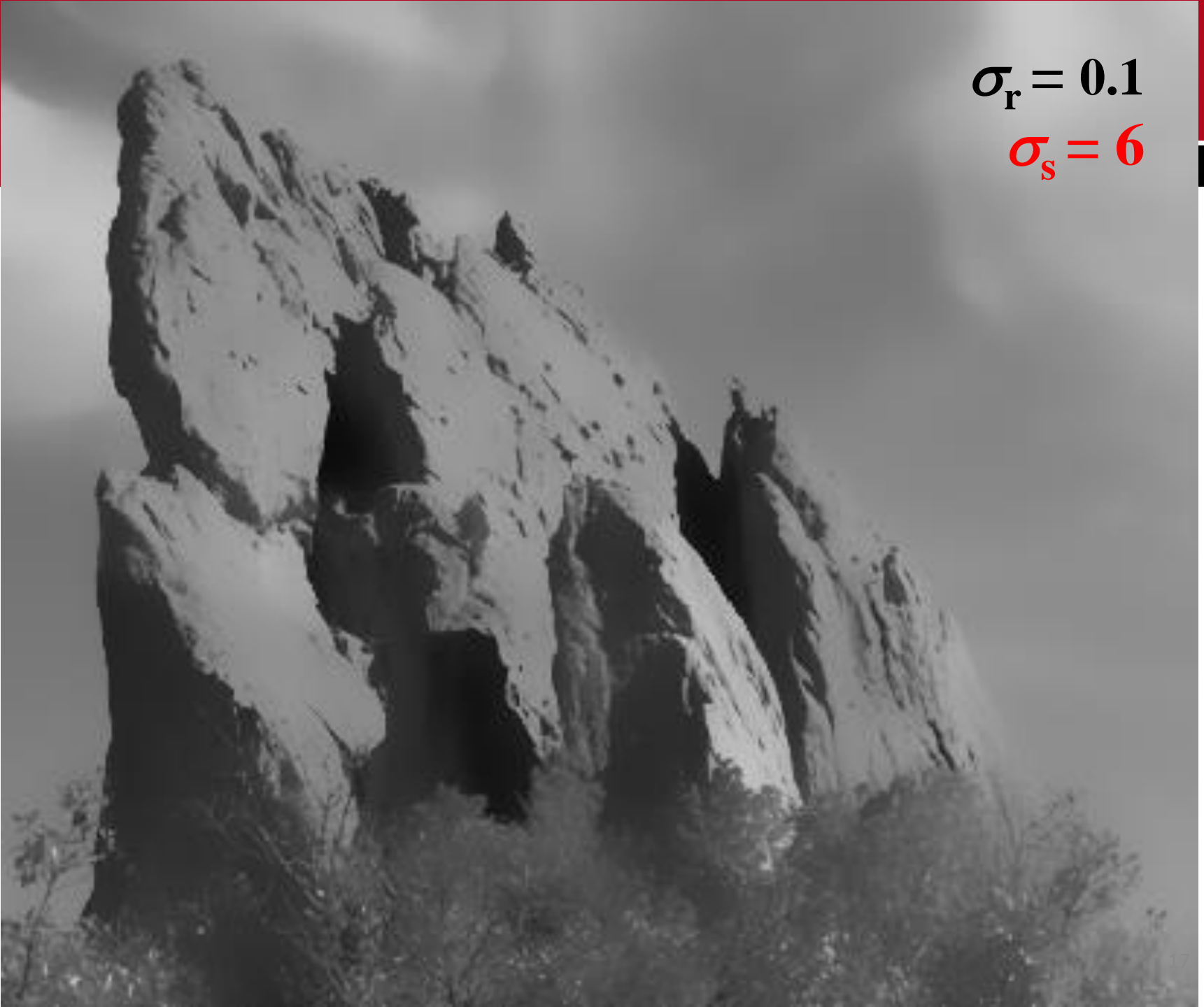


$$\sigma_r = 0.1$$
$$\sigma_s = 2$$



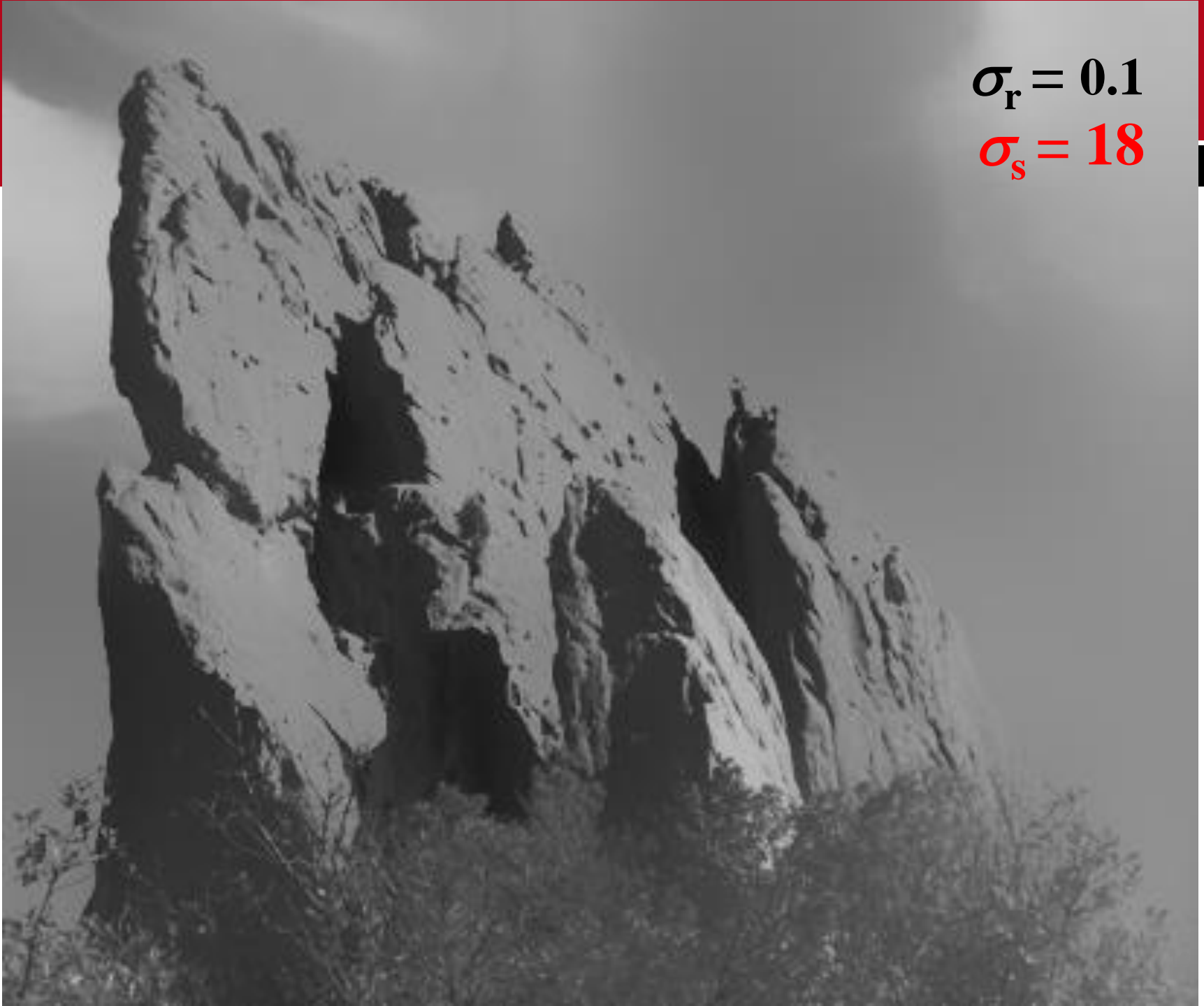
$$\sigma_r = 0.1$$

$$\sigma_s = 6$$



$$\sigma_r = 0.1$$

$$\sigma_s = 18$$



Denoising: an example



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Basic denoising

IAS-LAB

Noisy input



Bilateral filter 7x7 window





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Basic denoising

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Bilateral filter



Median 3x3





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Median 5x5





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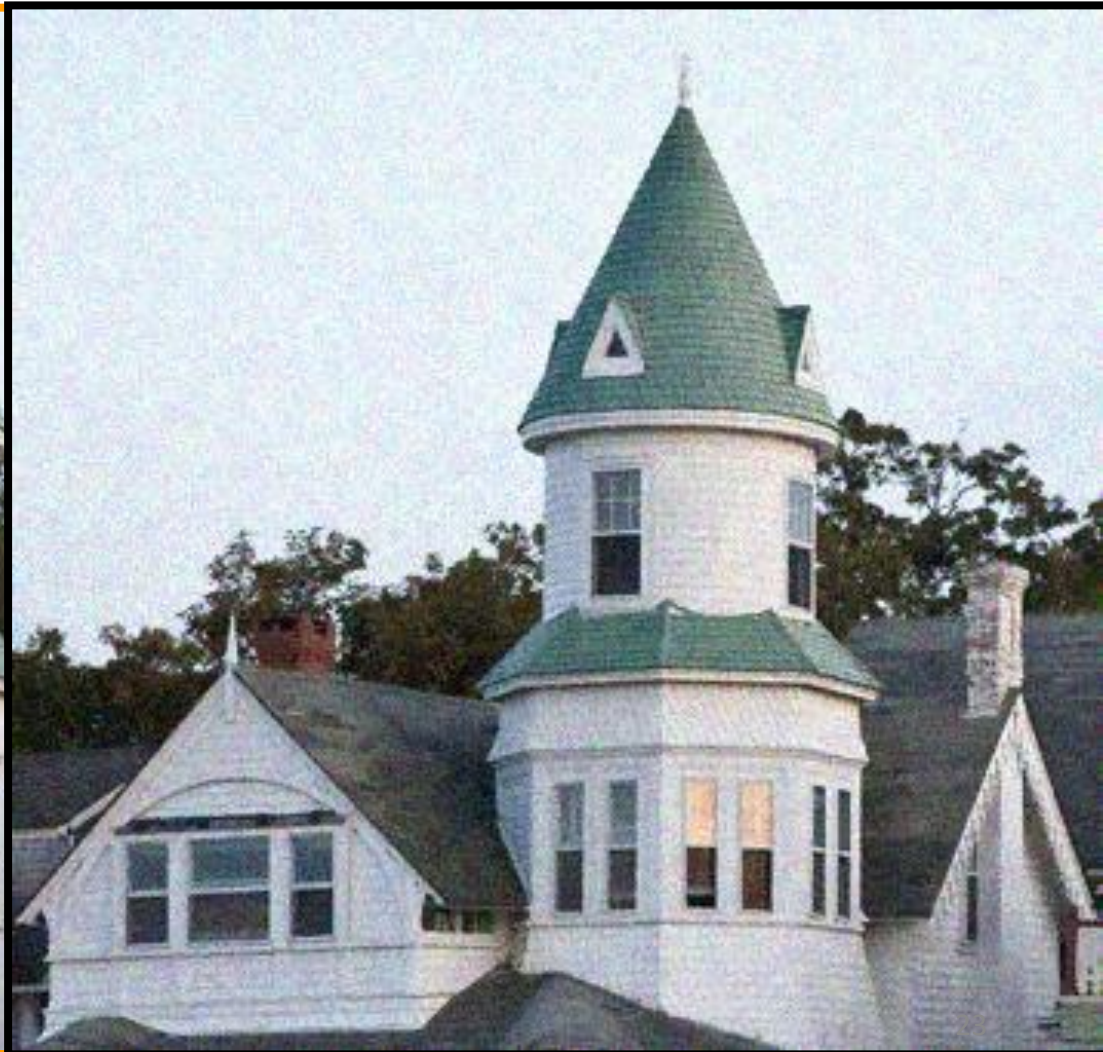
Basic denoising

IAS-LAB

Bilateral filter



Bilateral filter – lower sigma





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Basic denoising

IAS-LAB

Bilateral filter



Bilateral filter – higher sigma





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