



UNIVERSITÀ DEGLI STUDI DI PADOVA

The SIFT feature

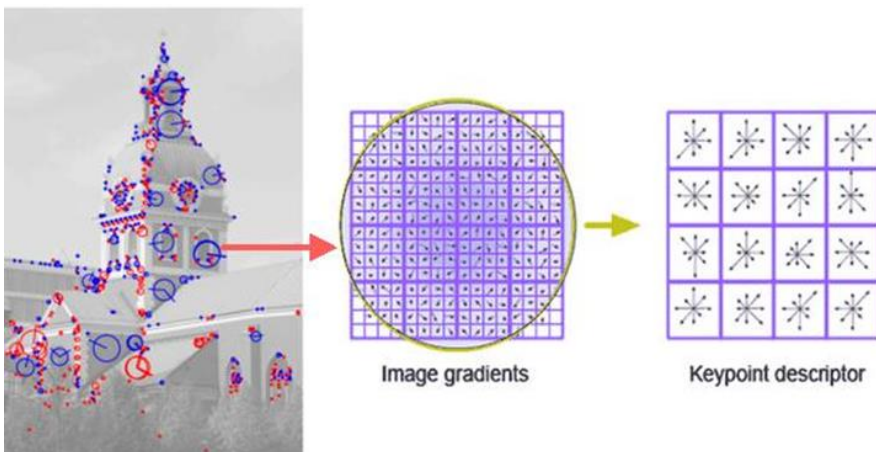
Stefano Ghidoni





- SIFT feature in detail
 - Keypoint detection
 - Descriptor calculation
- SIFT performance measurement

- Very reliable keypoint detector and descriptor
- Widely used



Although it's not always the case that a paper cited more contributes more to the field, a highly cited paper usually indicates that something interesting have been discovered. The following are the papers to my knowledge being cited the most in Computer Vision. (updated on 11/24/2013) If you want your "friend's" paper listed here, just comment below.

Cited by 21528 + 6830 (Object recognition from local scale-invariant features)

Distinctive image features from scale-invariant keypoints
DG Lowe - International journal of computer vision, 2004

Cited by 17671

A theory for multiresolution signal decomposition: The wavelet representation
SG Mallat - Pattern Analysis and Machine Intelligence, IEEE ..., 1989

Cited by 17611

A computational approach to edge detection
J Canny - Pattern Analysis and Machine Intelligence, IEEE ..., 1986

Cited by 15422

Snakes: Active contour models
M Kass, A Witkin, Demetri Terzopoulos - International journal of computer ..., 1988

Cited by 15188

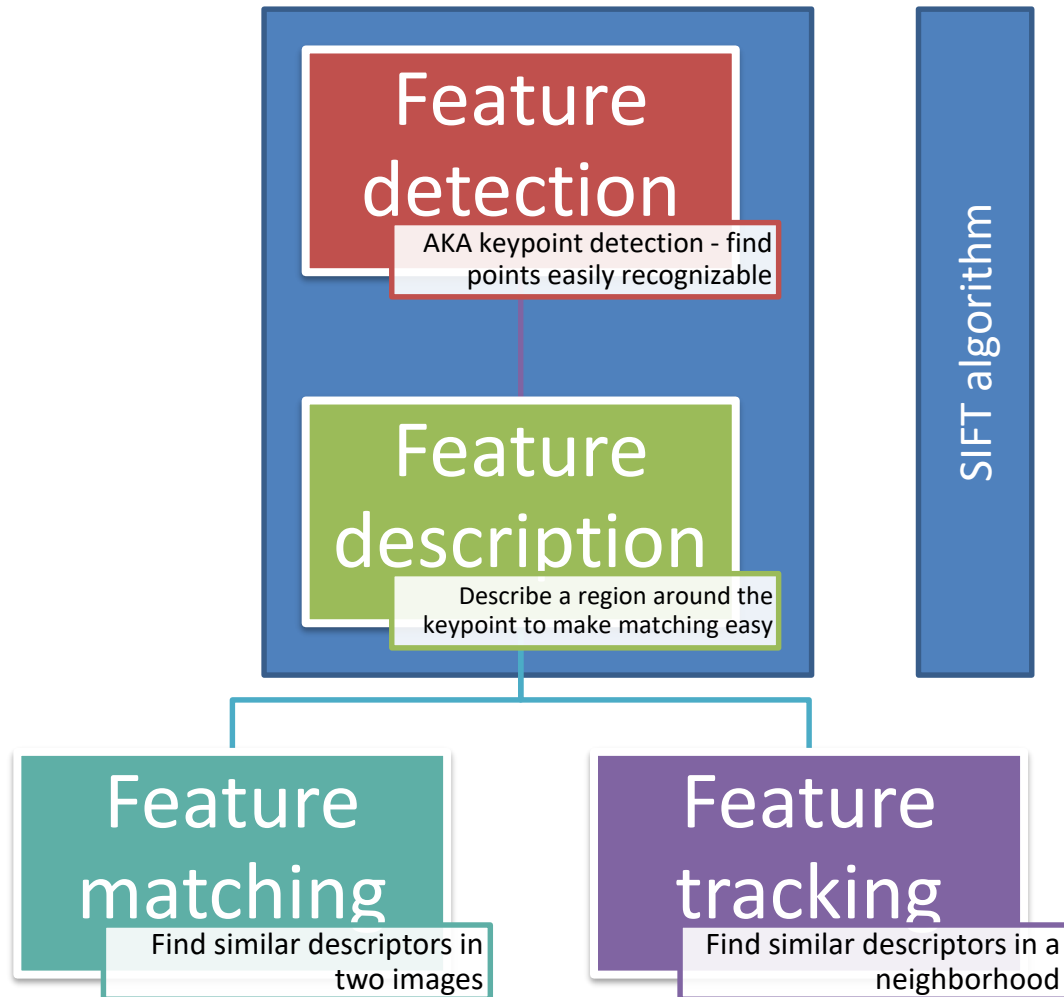
Stochastic relaxation, Gibbs distributions, and the Bayesian restoration of images
Geman and Geman - Pattern Analysis and Machine ..., 1984

Cited by 11630+ 4138 (Face Recognition using Eigenfaces)

Eigenfaces for Recognition
Turk and Pentland, Journal of cognitive neuroscience Vol. 3, No. 1, Pages 71-86, 1991 (9358 citations)

Cited by 8788

Determining optical flow
B.K.P. Horn and B.G. Schunck, Artificial Intelligence, vol 17, pp 185-203, 1981





- Why such a strong focus on scale?



- Different scales
- What are the main differences?

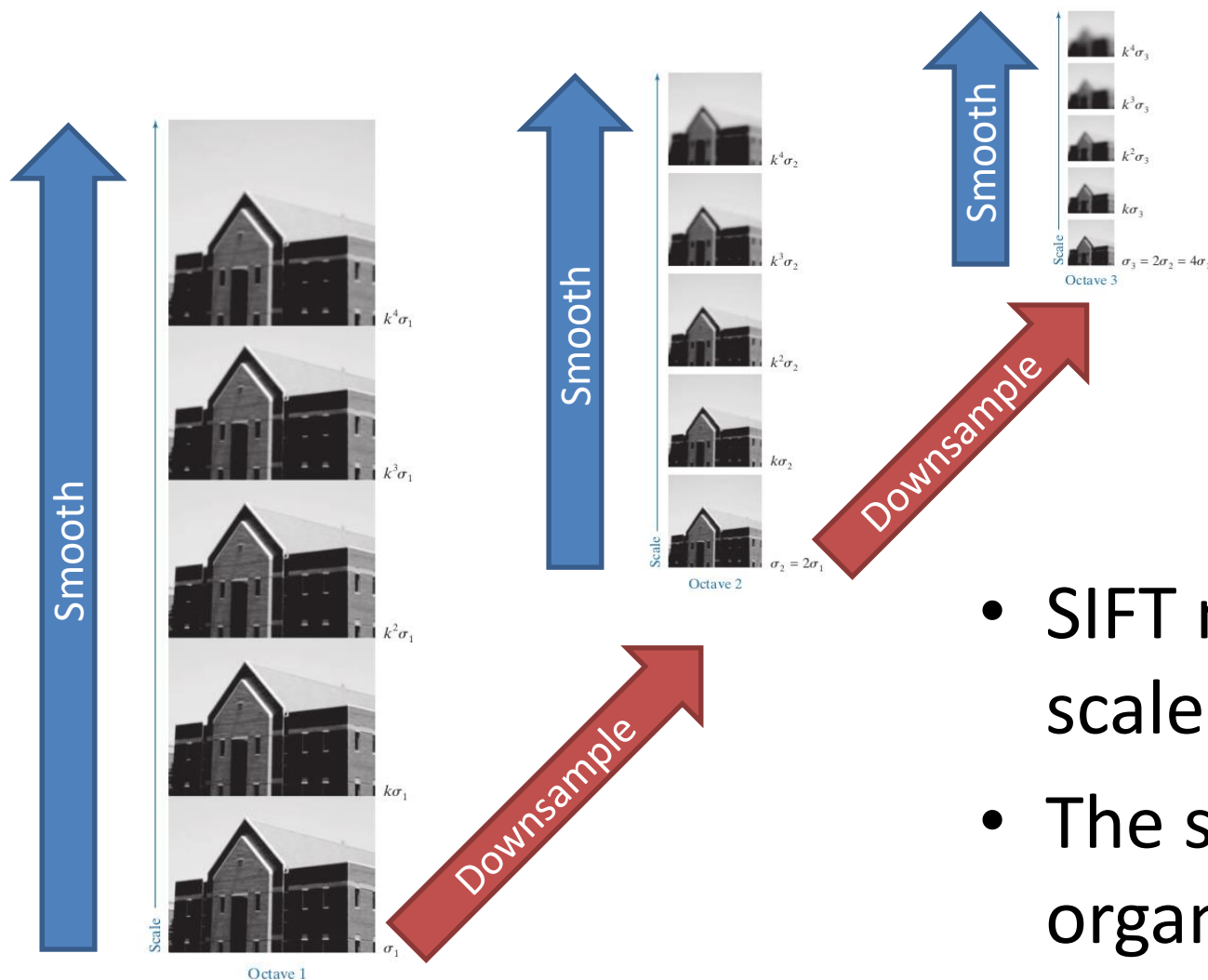




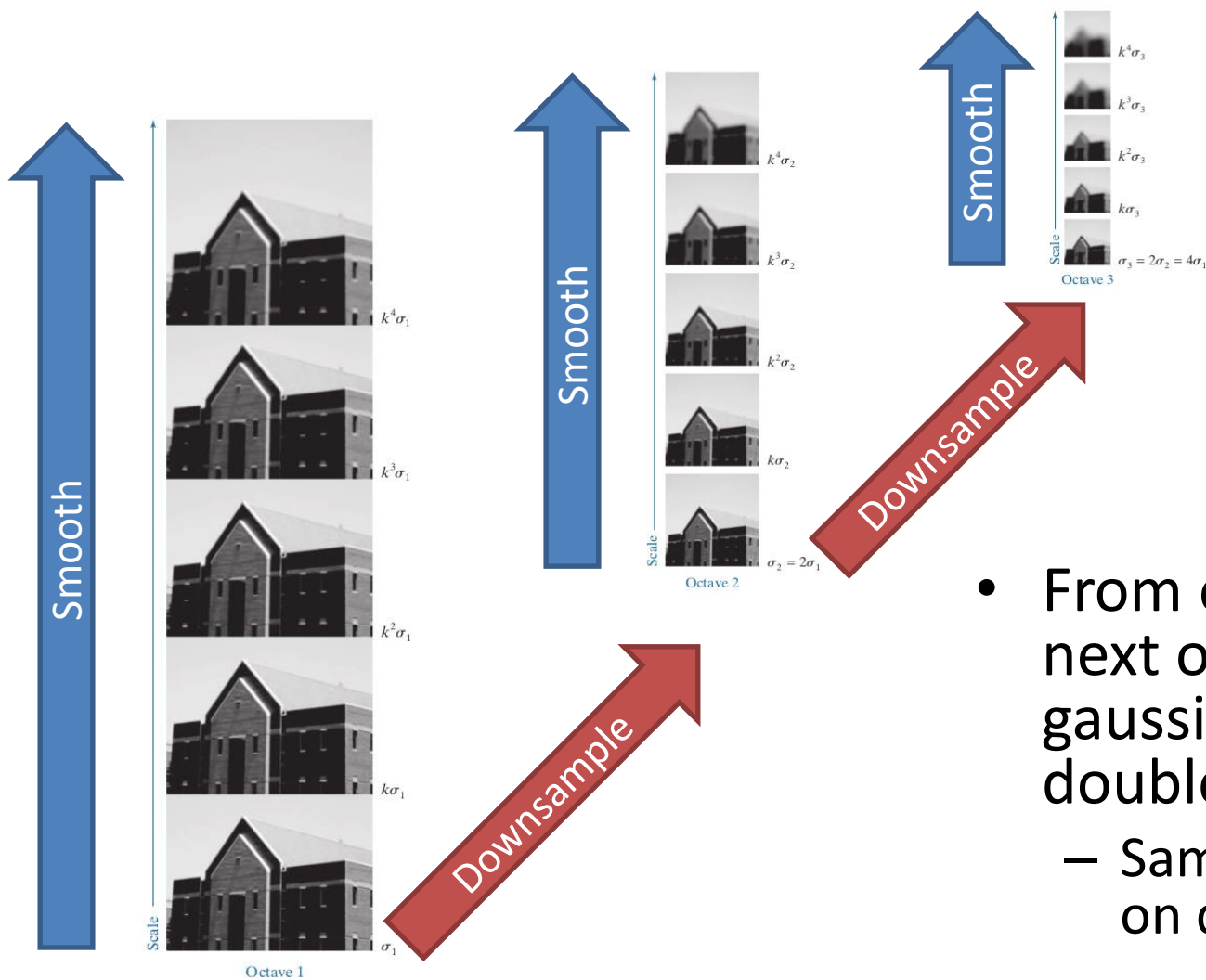
- SIFT features:
 - Local – robust to occlusions
 - Distinctive – distinguish objects in large databases
 - Dense – many features can be found even on small objects
 - Efficiency – (rather) fast computation (**what's the meaning of fast?**)



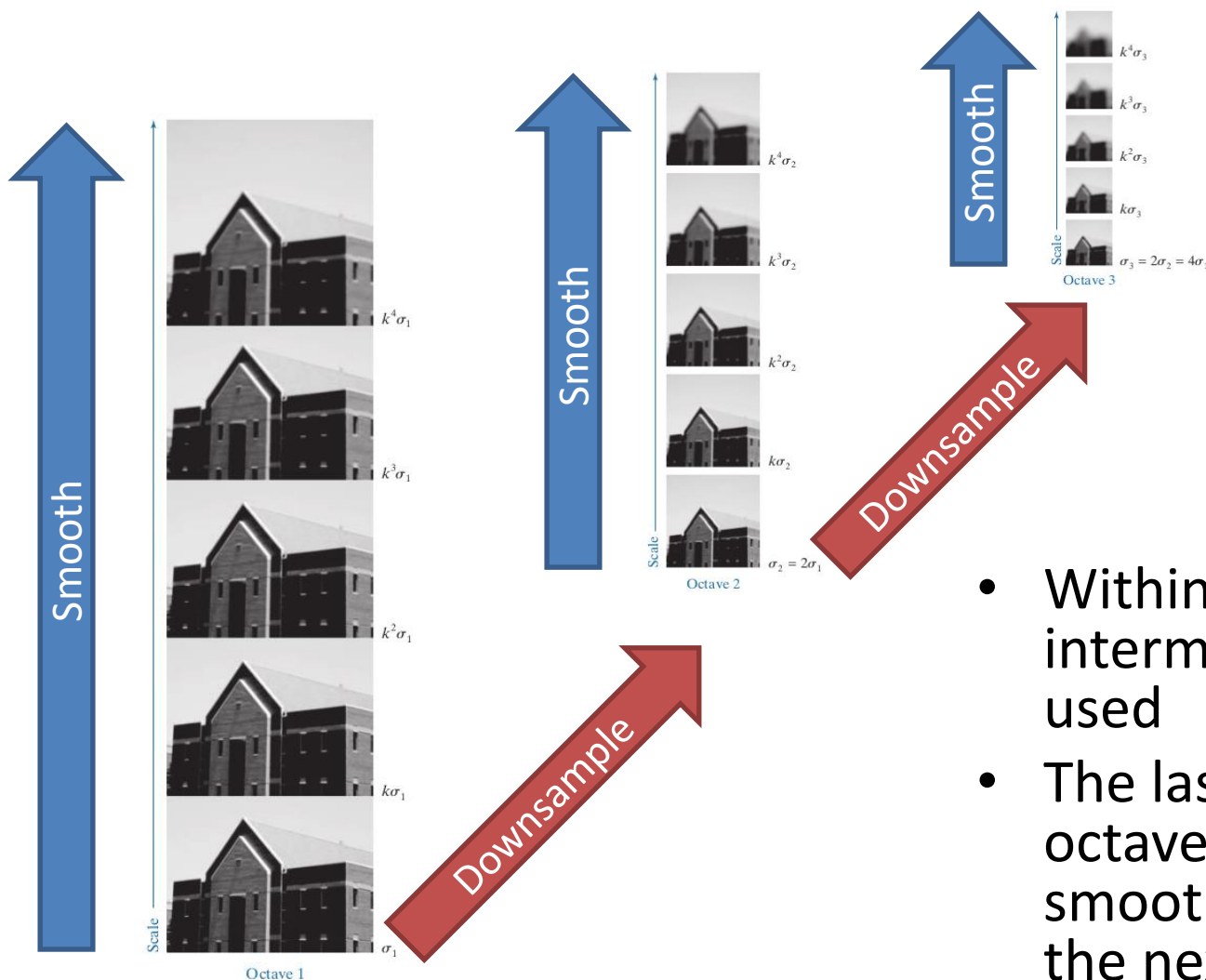
- Scale-space extrema detection
- Keypoint localization
- Orientation measurement
- Descriptor calculation



- SIFT makes use of a scale space
- The scale space is organized in octaves



- From one octave to the next one the σ of the gaussian smoothing is doubled
 - Same smoothing filter on downsampled image

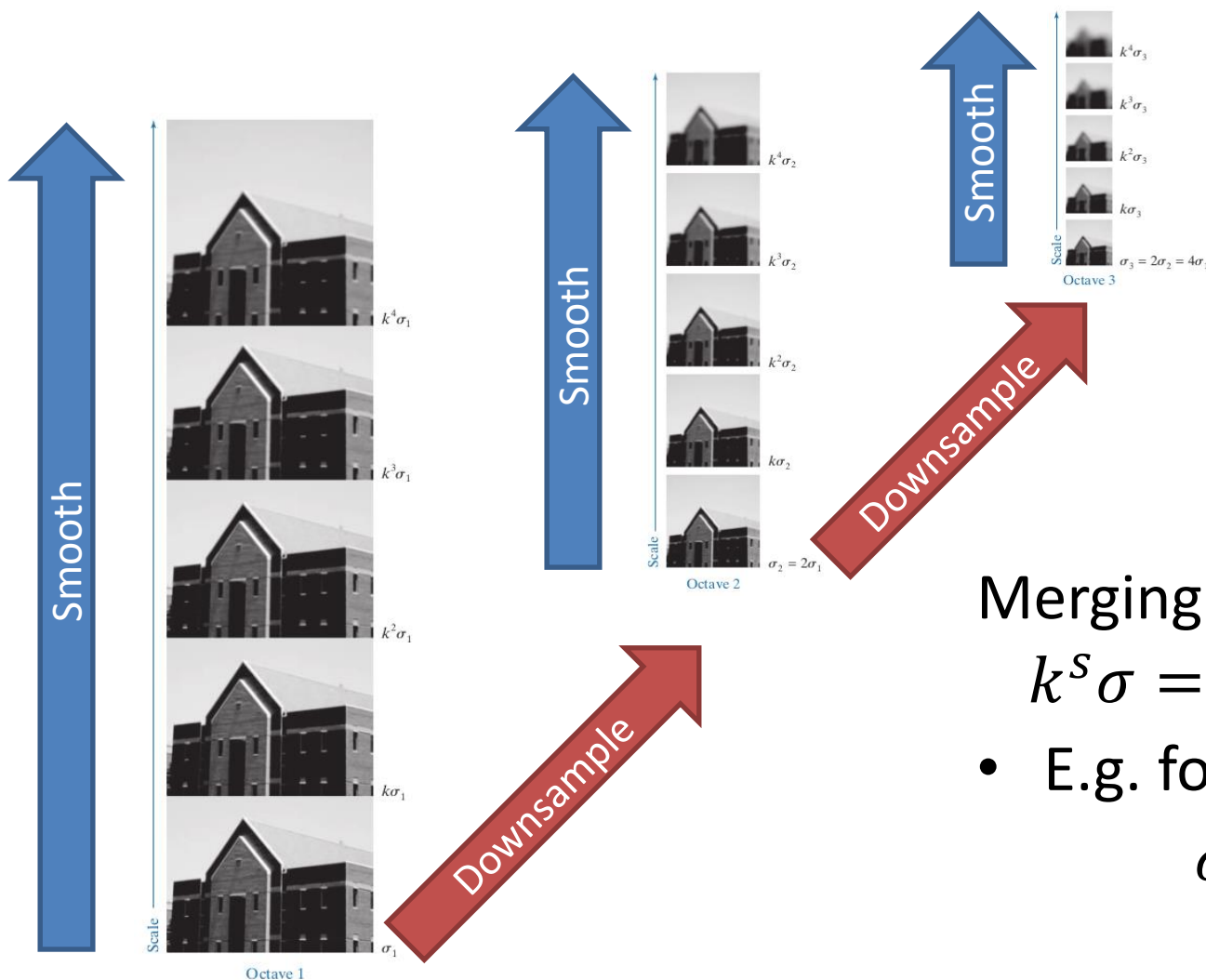


- Within one octave intermediate scales are used
- The last image of one octave has the same smoothing as the first in the next octave



Within one octave:

- s intervals
 - $s+1$ images
- Standard deviations
 - $\sigma, k\sigma, k^2\sigma, \dots, k^s\sigma$



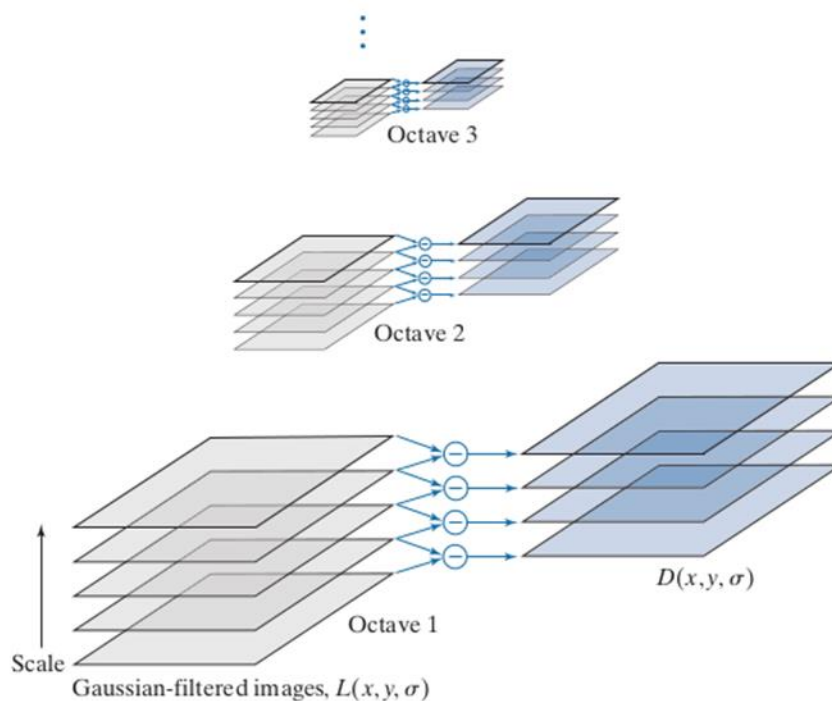
Merging of two octaves:

$$k^s \sigma = 2\sigma \rightarrow k = 2^{1/s}$$

- E.g. for $s=2$ (3 images)

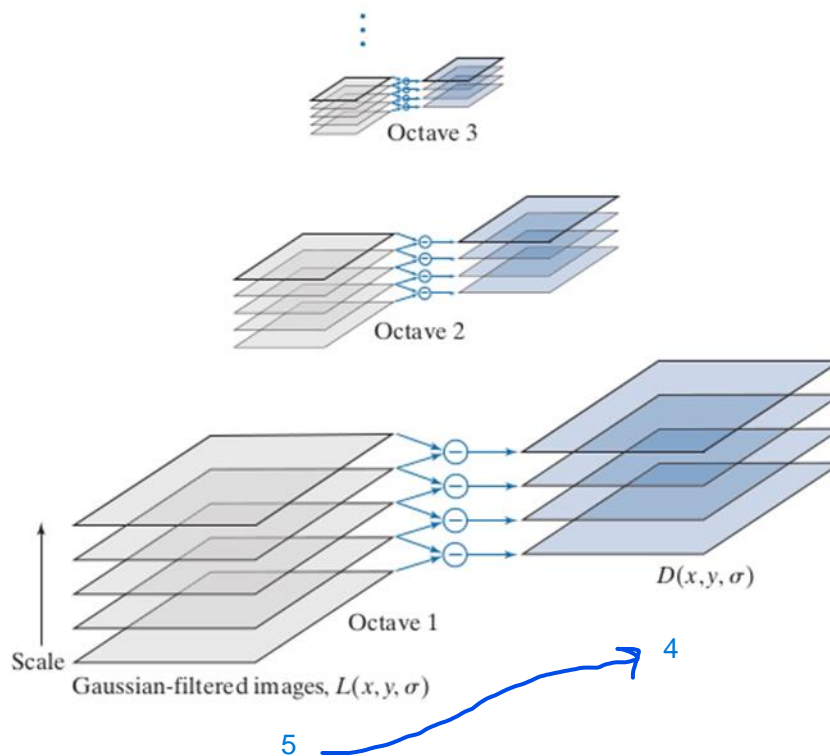
$$\sigma, \sqrt{2}\sigma, 2\sigma$$

- Layers in the scale space are combined by subtracting consecutive layers



L – gaussian filtered image
D – difference of gaussian filtered images

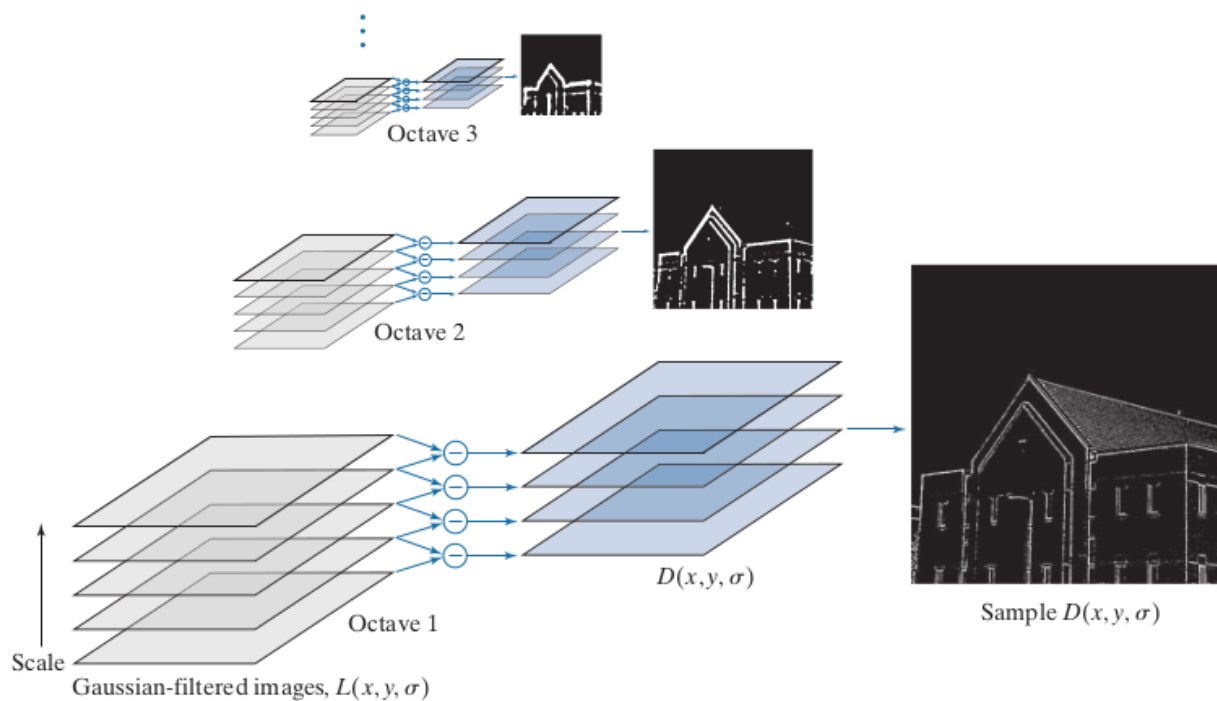
- This requires two additional images in the scale space to process the first and last image



Octaves for $s = 2$

Octave	Scale				
	1	2	3	4	5
1	0.707	1.000	1.414	2.000	2.828
2	1.414	2.000	2.828	4.000	5.657
3	2.828	4.000	5.657	8.000	11.314

- Output images



- Subtracting consecutive layers means:
evaluate the difference between two
smoothed images
 - Same smoothing, different smoothing intensity
- Such filtering is called Difference of Gaussians
(DoG) and is represented by the function

$$D(x, y, \sigma)$$



- Subtracting consecutive layers means:
evaluate the difference between two
smoothed images
 - Same smoothing, different smoothing intensity
- What is the meaning of this filter?
 - Let's go one step back: derivative filters



- Recall – we observed many times the pattern:
 - Smoothing
 - Derivative filter (edge detection filter)
- They can be combined into one filter
 - Derivative of the smoothing filter
- This is the concept exploited in the Laplacian of Gaussian (LoG) filter

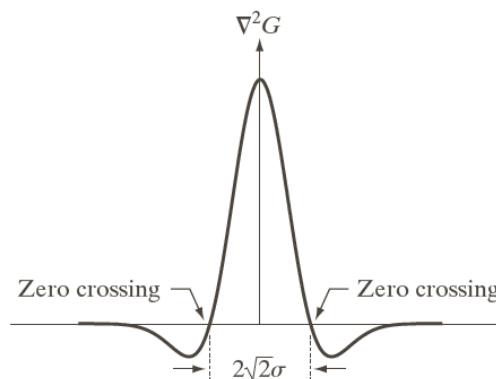
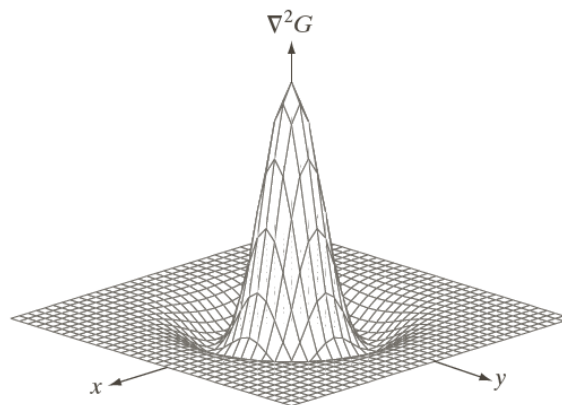
- Laplacian of a Gaussian (LoG) is obtained using the gaussian filter:

$$G(x, y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

And considering its laplacian $\nabla^2 G(x, y)$ to filter the image:

- Filtering with LoG filter corresponds to:
 - Filter the input using $G(x, y)$
 - Compute the Laplacian of the resulting image

- Smoothing
- Noise removal at scales smaller than σ
- Zero-crossing
- Isotropic
- Typ filter size:
 $n \times n$ s.t.
 $n > 6\sigma$



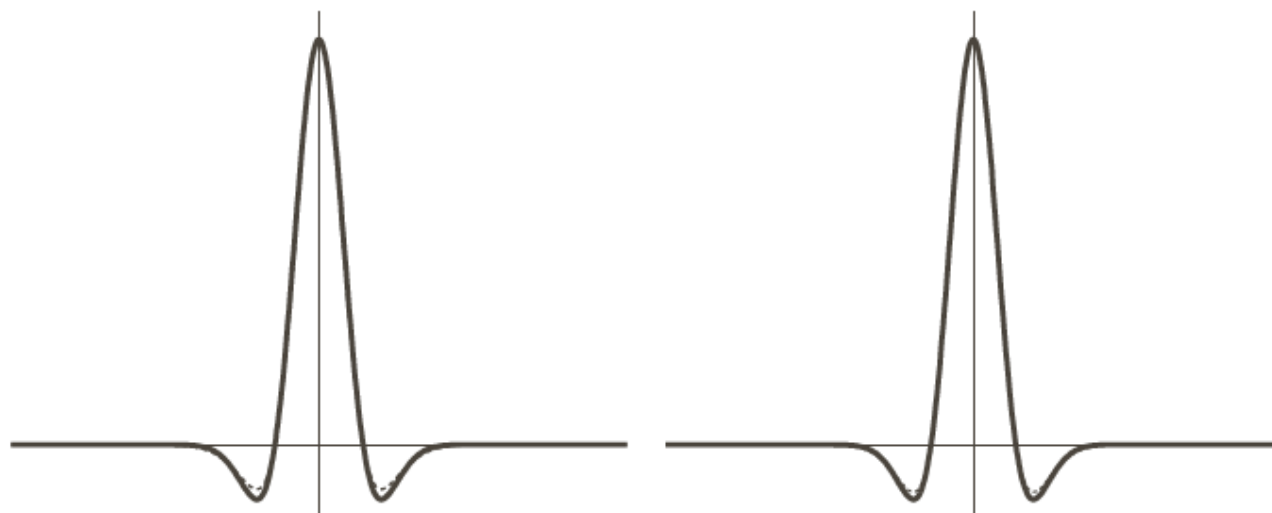
-LoG



0	0	-1	0	0
0	-1	-2	-1	0
-1	-2	16	-2	-1
0	-1	-2	-1	0
0	0	-1	0	0

- An approximation: DoG (Difference of Gaussians) – $\sigma_1 > \sigma_2$

$$D(x, y) = \frac{1}{2\pi\sigma_1^2} e^{-\frac{x^2+y^2}{2\sigma_1^2}} - \frac{1}{2\pi\sigma_2^2} e^{-\frac{x^2+y^2}{2\sigma_2^2}}$$



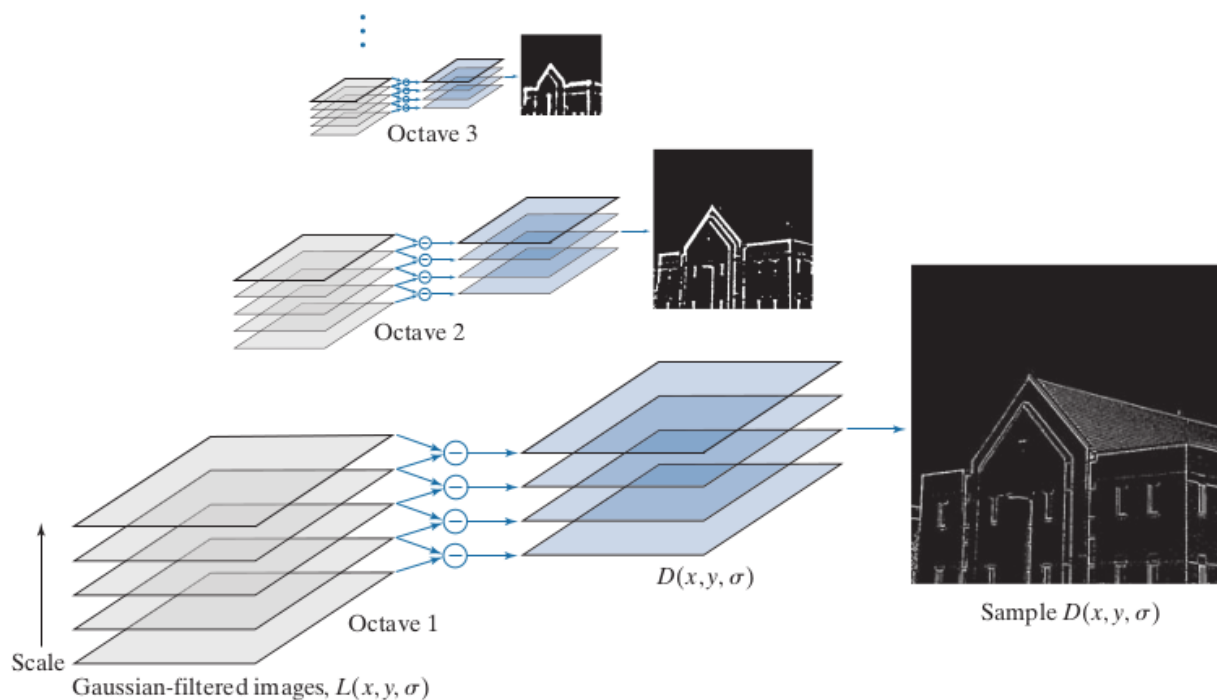
a b

FIGURE 10.23

(a) Negatives of the LoG (solid) and DoG (dotted) profiles using a standard deviation ratio of 1.75:1.

(b) Profiles obtained using a ratio of 1.6:1.

- Back to SIFT: scale space + subtraction of consecutive layers is a DoG filter
 - Output images:



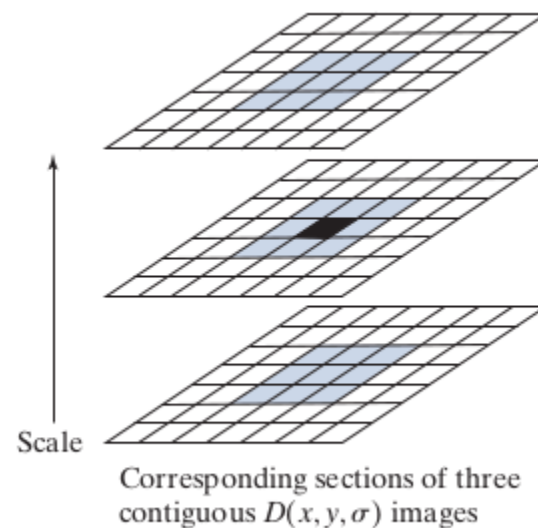


- Scale-space extrema detection
- Keypoint localization
- Orientation measurement
- Descriptor calculation

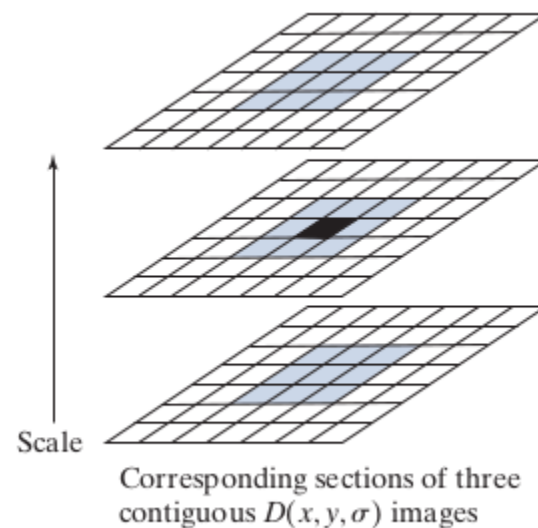


- Scale-space extrema detection
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- Search for maxima and minima of the DoG
- Comparison with the 8-neighbors in the current, previous and next scale level
- This is done at **all scales**
 - This means: **scale independence**



- Sub-pixel accuracy by means of interpolation
 - Taylor series expansion up to the quadratic term
- Interpolation along x, y, σ



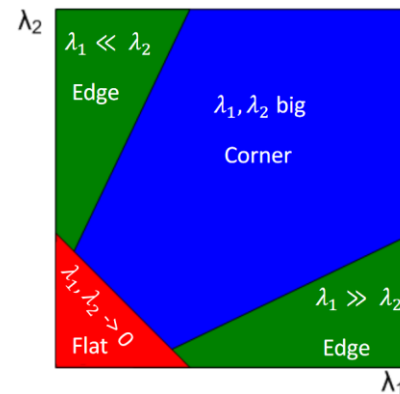
- Recall: SIFT is based on the laplacian – 2nd order derivative
- The Hessian matrix provides all the 2nd order derivatives

$$H = \begin{bmatrix} \partial^2 D / \partial x^2 & \partial^2 D / \partial x \partial y \\ \partial^2 D / \partial y \partial x & \partial^2 D / \partial y^2 \end{bmatrix} = \begin{bmatrix} D_{xx} & D_{xy} \\ D_{yx} & D_{yy} \end{bmatrix}$$

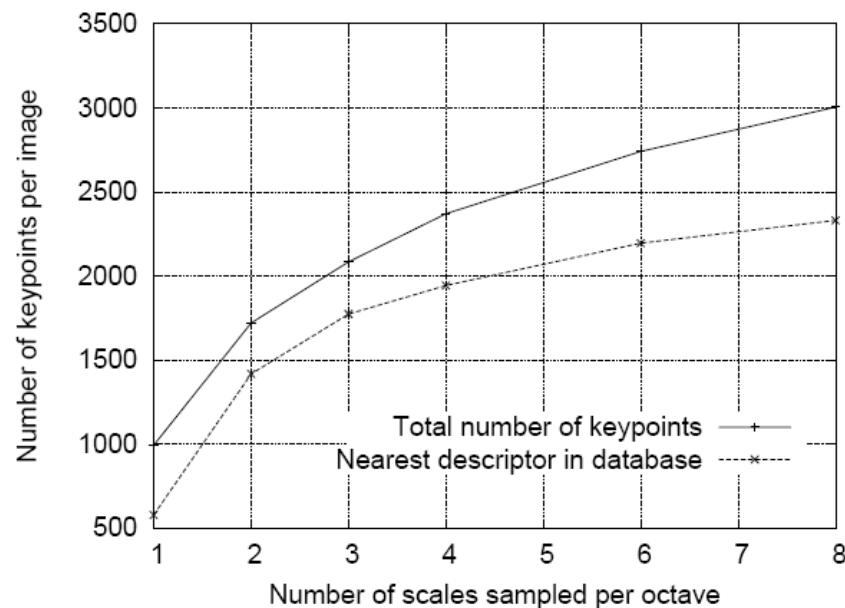
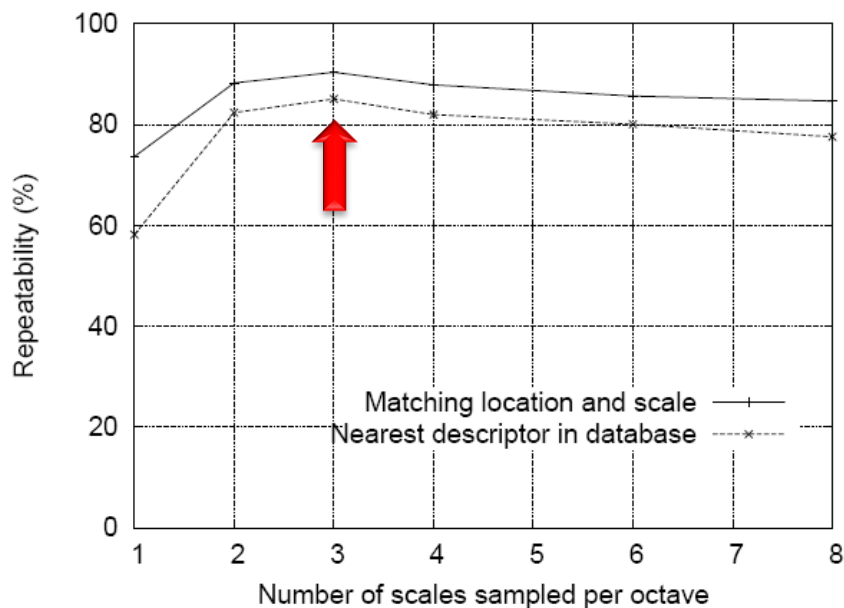
- Further processing is based on H

Similar to the
auto-correlation
matrix A

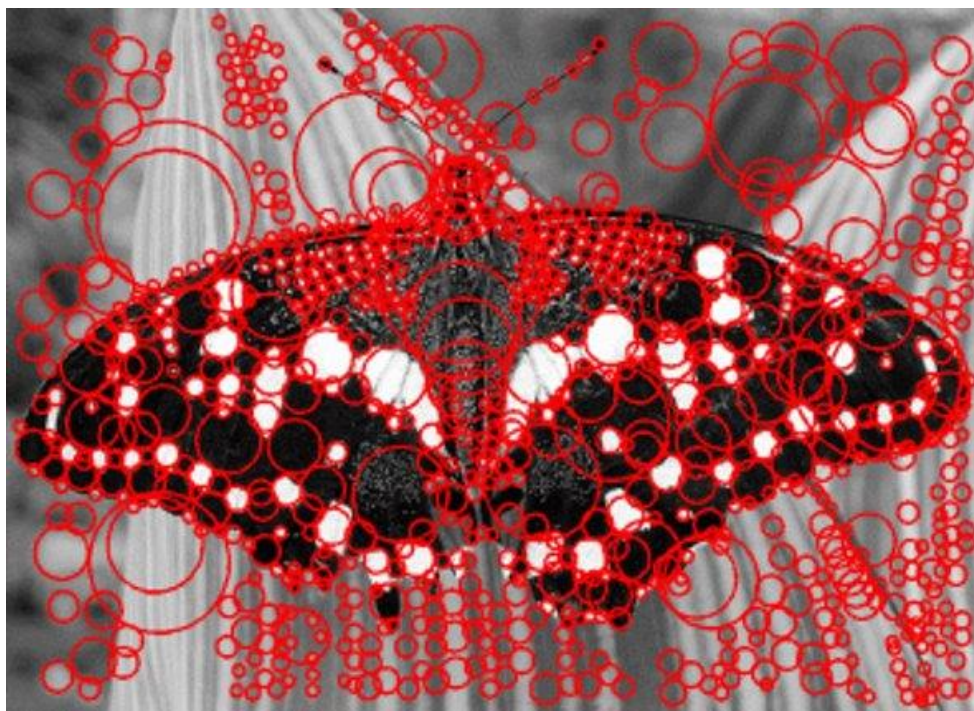
- The Hessian matrix is used to:
 - Discard points with a low gradient
$$|D(\hat{x})| < 0.03$$
 - Discard edge points – require that both eigenvalues of H are large
 - Means: require that both curvatures are high
 - Similar to the discussion about Harris corners
 - Similar considerations about eigenvalues ratios



- More scale levels considered
 - More points
 - More unstable
 - Best value: $s=3$



- The output is a set of keypoints with associated scales





- Scale-space extrema detection
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- Scale-space extrema detection
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- Each keypoint comes with its scale
- The gaussian smoothed image closest to that scale is selected (L)
 - This process is **independent from the scale**
- Compute gradient magnitude and orientation in the keypoint neighborhood using L



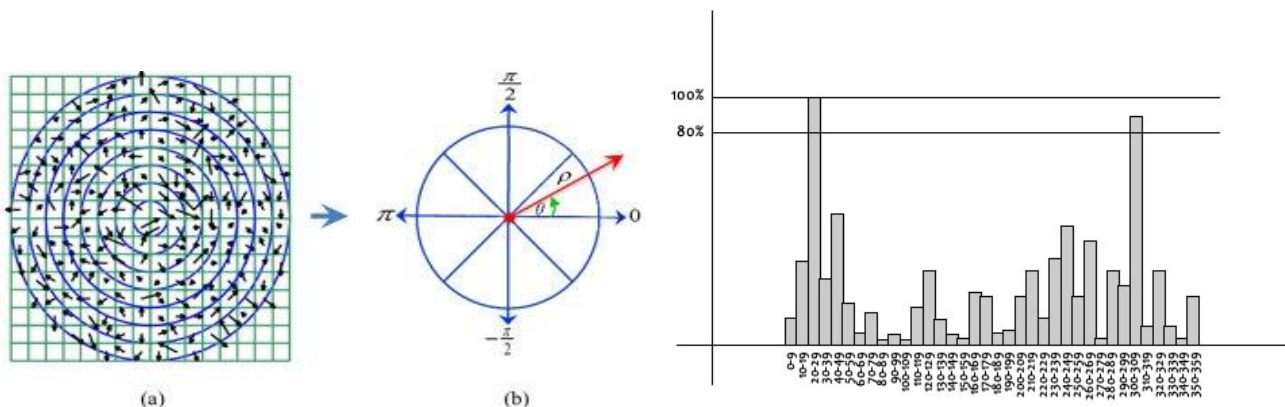
- Gradient magnitude

$$M(x, y) = \sqrt{(L(x + 1, y) - L(x - 1, y))^2 + (L(x, y + 1) - L(x, y - 1))^2}$$

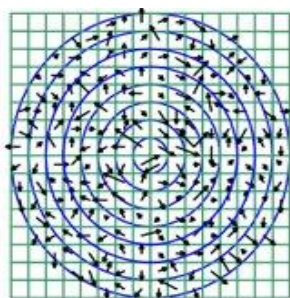
- Gradient orientation angle

$$\theta(x, y) = \tan^{-1} \left[\frac{L(x, y + 1) - L(x, y - 1)}{L(x + 1, y) - L(x - 1, y)} \right]$$

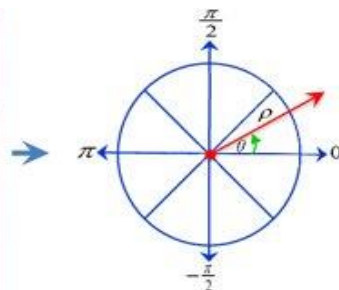
- To achieve **rotation invariance**, the dominant local direction shall be measured
- Build the histogram of gradient orientations
 - 36 bins of 10° each - region around the keypoint



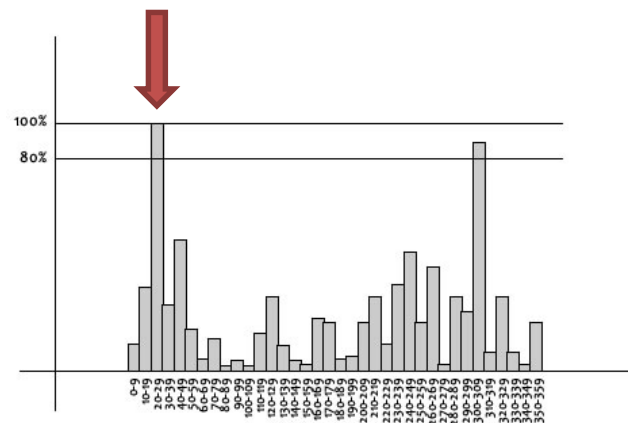
- To achieve **rotation invariance**, the dominant local direction shall be measured
- Build the histogram of gradient orientations
 - 36 bins of 10° each - region around the keypoint
- Look for the peak



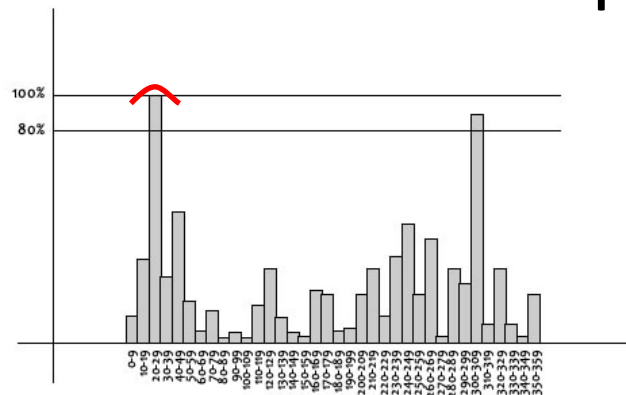
(a)



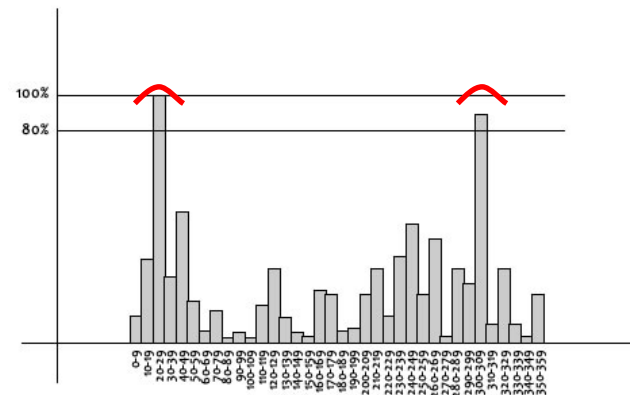
(b)



- To achieve **rotation invariance**, the dominant local direction shall be measured
- Build the histogram of gradient orientations
 - 36 bins of 10° each - region around the keypoint
- Look for the peak
- Fit a parabola to the 3 bins close to the peak
 - Refine the peak location



- Secondary peaks are also considered
 - Peak value $> 80\%$ highest peak
- Secondary peaks duplicate the keypoint
 - A new keypoint is created, with the orientation set to the secondary peak



- Keypoint detection example
 - Arrows represent keypoint orientation



(a)



(b)



(c)



(d)

- (a) 233x189 image*
- (b) 832 DOG extrema*
- (c) 729 left after peak value threshold*
- (d) 536 left after testing ratio of principle curvatures*

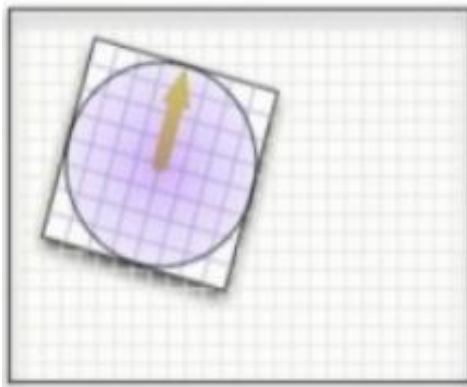


- Scale-space extrema detection
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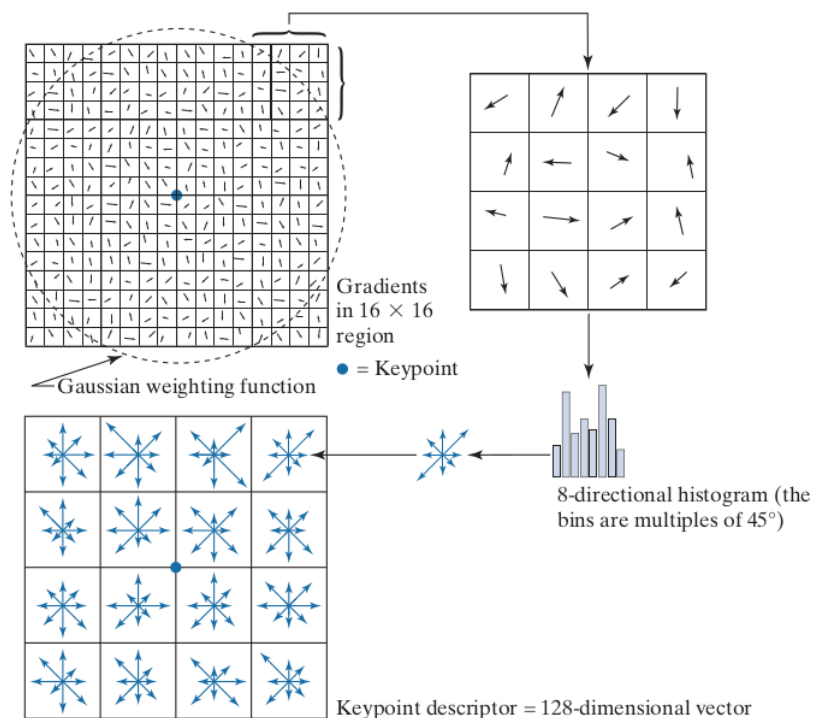


- Scale-space extrema detection
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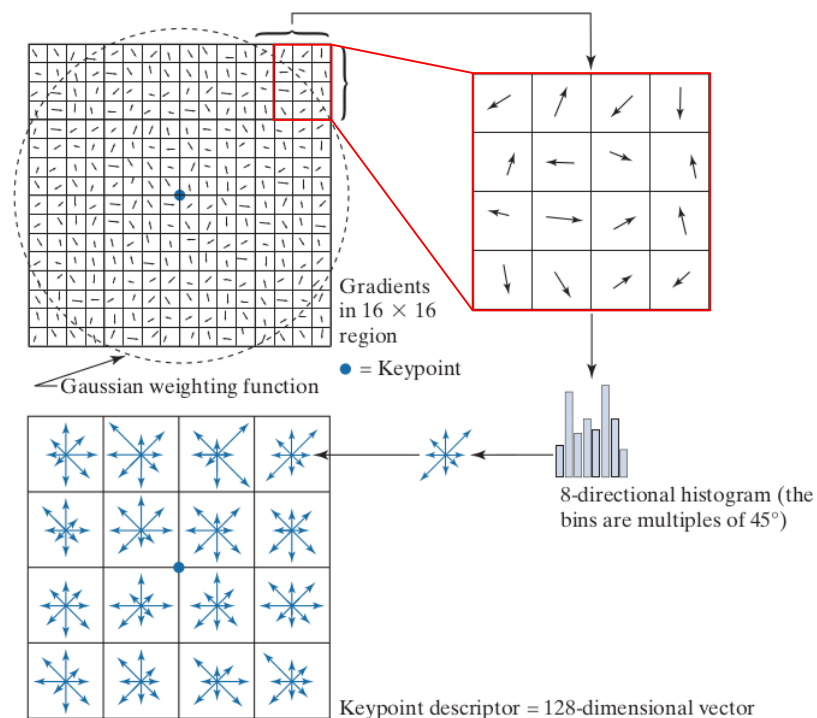
- SIFT evaluates a descriptor for each keypoint
 - In the image L corresponding to the keypoint scale
 - Considering coordinates that are rotated based on the measured keypoint orientation



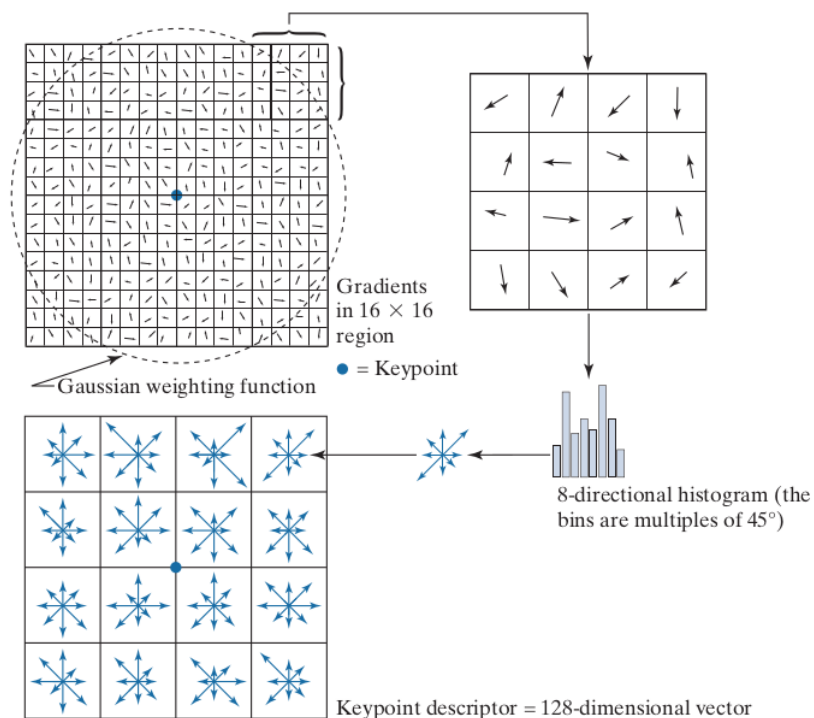
- Compute gradient magnitude and direction
 - neighborhood: 16×16
- Values weighted with a gaussian function centered on the keypoint



- 16x16 neighborhood divided into regions of 4x4 pixels
- Evaluate histogram of each region
 - 8 bins (45° each)
- Save the values



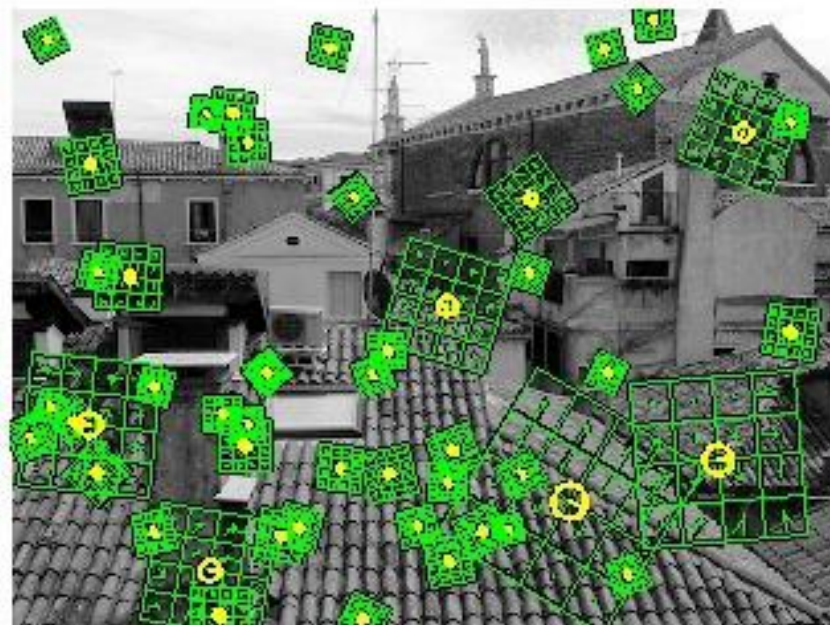
- Descriptor size:
 - 16 regions
 - 8 histogram values per region
- 128 elements
 - 1 byte per element



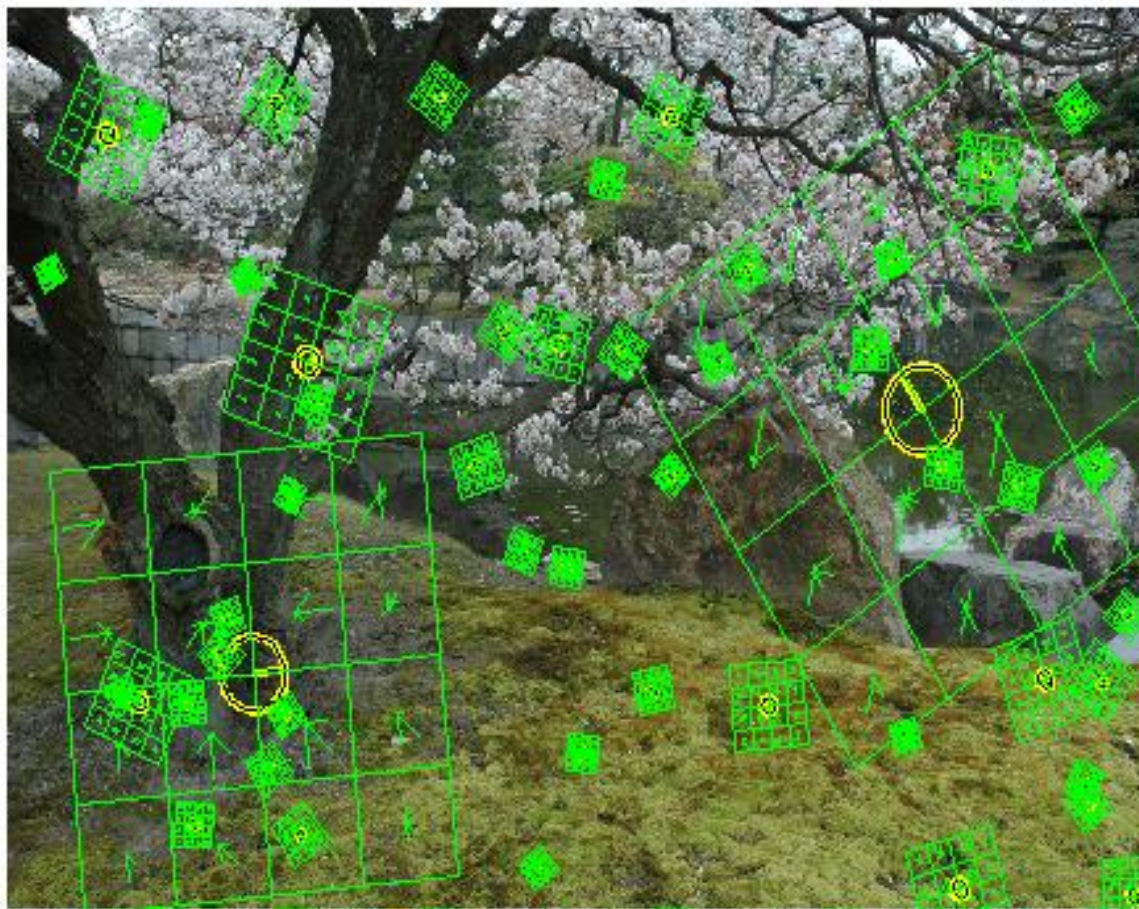


- Additional details are considered by the SIFT algorithm
- Enhanced **invariance to illumination**: feature vector normalized to unit length
- Enhanced **robustness to large gradient magnitudes**: threshold to 0.2 on all the components
 - Nonlinear illumination effect – e.g., camera saturation
 - Further normalization to 1 after thresholding

- SIFT (VLFeat library)



- SIFT (VLFeat library)



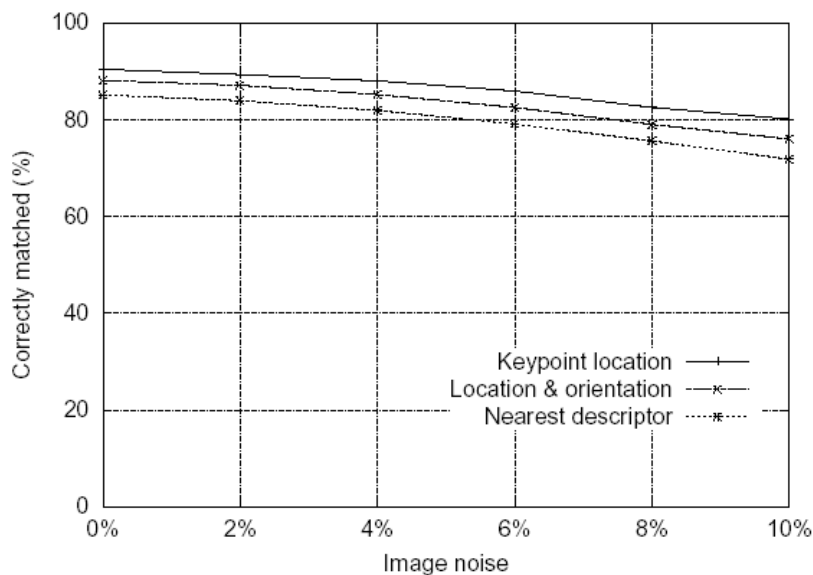
- SIFT (OpenCV)





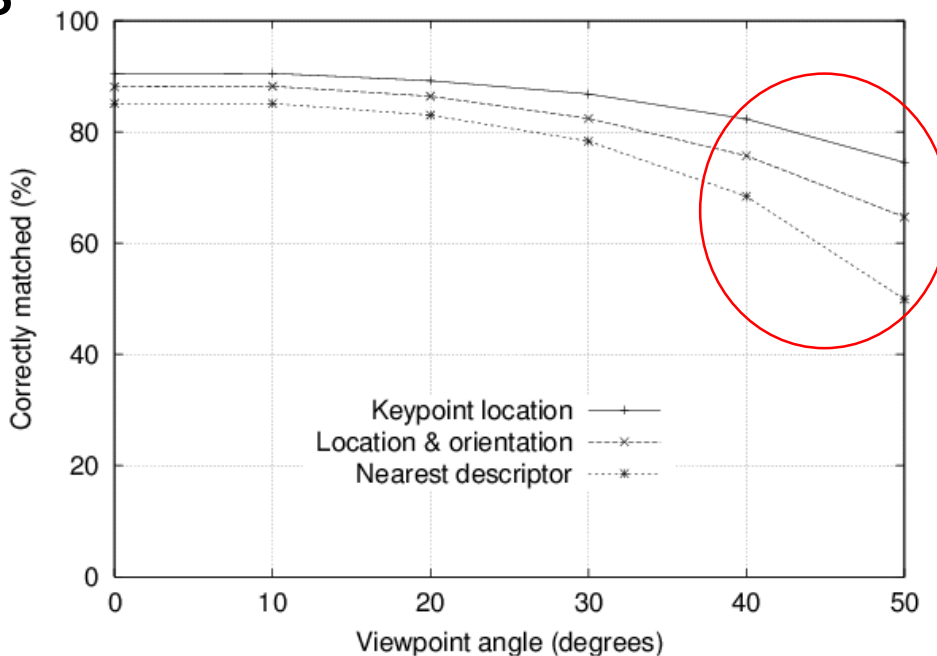
- The robustness of the SIFT features to noise factor was accurately measured

- Random rotation and scale change with different noise levels
 - Nearest neighbor on 30,000 feature database



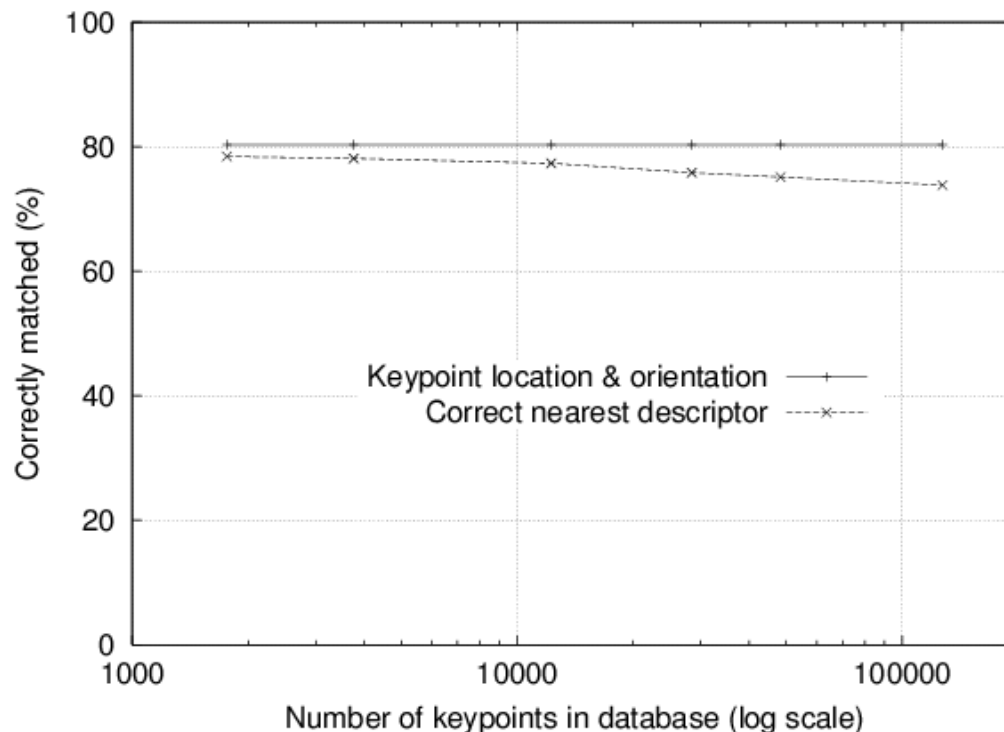


- Random scale change + rotation with 2% noise and affine distortion
 - Nearest neighbor on 30,000 feature database
- Strong for small angles





- 2% Noise and 30° viewpoint change





- Why is SIFT invariant to scale?
- Why is SIFT invariant to illumination changes?
- Why is SIFT invariant to orientation?



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