



# UNIVERSITÀ DEGLI STUDI DI PADOVA

## Image mapping

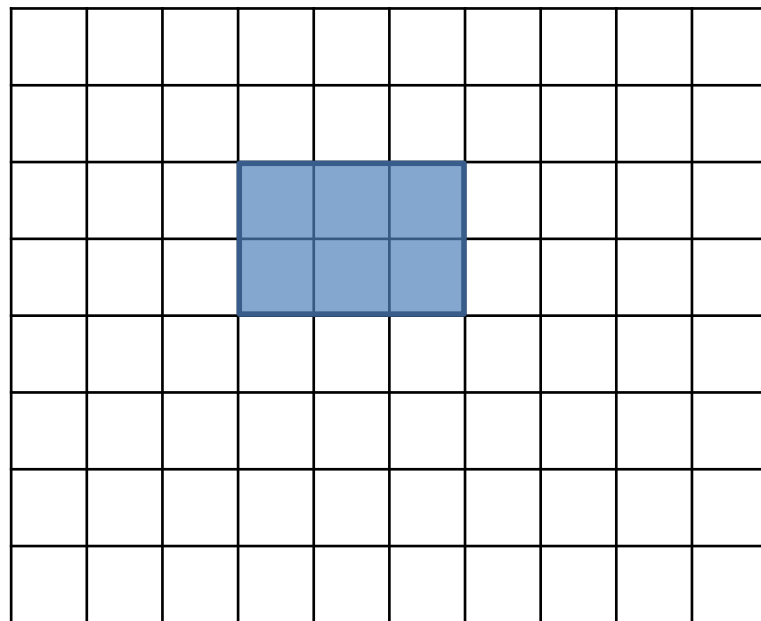
Stefano Ghidoni



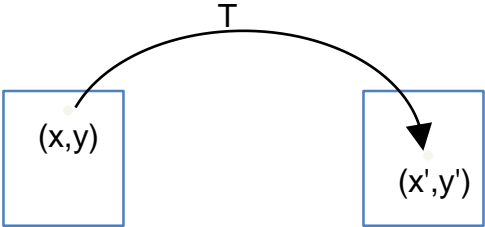
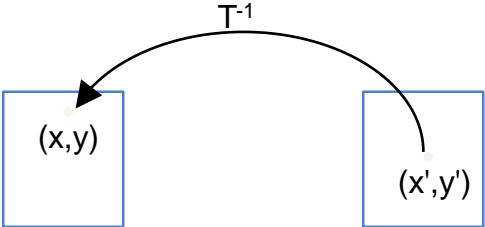


- Moving points vs moving pixels
- Forward & backward mappings
- How to code mapping

- A geometric transform is a modification of the spatial relationship among pixels
- Two steps
  - Coordinate transform
$$(x', y') = T\{(x, y)\}$$
  - Image resampling
- Coord transform works on **geometrical points**
- Mapping/resampling goes back to pixels



# Forward vs backward mapping

	
<i>Forward mapping</i>	<i>Backward mapping</i>
$(x',y') = T\{(x,y)\}$	$(x,y) = T^{-1}\{(x',y')\}$
For each $(x,y)$ compute corresponding $(x',y')$	For each $(x',y')$ compute corresponding $(x,y)$
Ambiguity issue: multiple points on the same $(x',y')$	Find each $(x',y')$ only once
$(x',y')$ decimals $\rightarrow$ resampling is needed (e.g., bilinear)	$(x,y)$ decimals $\rightarrow$ resampling is needed (e.g., bilinear)
Missing pixels	Fills all pixels
Less used	Better!

not integers



- Images are usually remapped using the backward mapping
  - Check `cv::warpAffine()` function
- The low-level details of backward mapping are managed automatically by OpenCV
- We shall only provide the transformation matrix
- Other ways of specifying a transformation are provided!

```
void cv::warpAffine(
cv::InputArray src, // input image
cv::OutputArray dst, // output image
cv::InputArray M, // 2x3 transform matrix
cv::Size dsize, // destination image size
int flags = cv::INTER_LINEAR, // interpolation, inverse
int borderMode = cv::BORDER_CONSTANT, // handling of missing pixels
const cv::Scalar& borderValue = cv::Scalar() // constant borders
);
```




Original



Rotated

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} t_{11} & t_{12} & t_{13} \\ t_{21} & t_{22} & t_{23} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$



 **OpenCV** 3.3.1  
Open Source Computer Vision

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[OpenCV Tutorials](#) > [Image Processing \(imgproc module\)](#)

## Affine Transformations

### Goal

In this tutorial you will learn how to:

- Use the OpenCV function `cv::warpAffine` to implement simple remapping routines.
- Use the OpenCV function `cv::getRotationMatrix2D` to obtain a  $2 \times 3$  rotation matrix

### Theory

#### What is an Affine Transformation?

1. A transformation that can be expressed in the form of a *matrix multiplication* (linear transformation) followed by a *vector addition* (translation).
2. From the above, we can use an Affine Transformation to express:
  - a. Rotations (linear transformation)
  - b. Translations (vector addition)
  - c. Scale operations (linear transformation)you can see that, in essence, an Affine Transformation represents a **relation** between two images.
3. The usual way to represent an Affine Transformation is by using a  $2 \times 3$  matrix.

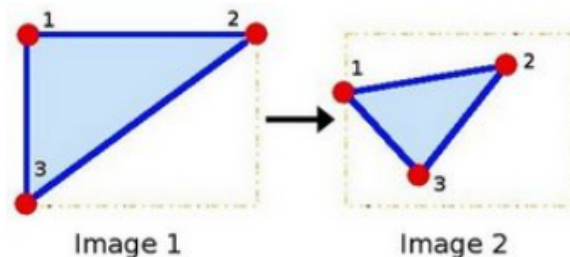
$$A = \begin{bmatrix} a_{00} & a_{01} \\ a_{10} & a_{11} \end{bmatrix}_{2 \times 2} \quad B = \begin{bmatrix} b_{00} \\ b_{10} \end{bmatrix}_{2 \times 1}$$
$$M = [A \quad B] = \begin{bmatrix} a_{00} & a_{01} & b_{00} \\ a_{10} & a_{11} & b_{10} \end{bmatrix}_{2 \times 3}$$

Considering that we want to transform a 2D vector  $X = \begin{bmatrix} x \\ y \end{bmatrix}$  by using  $A$  and  $B$ , we can do the same with:

$$T = A \cdot \begin{bmatrix} x \\ y \end{bmatrix} + B \text{ or } T = M \cdot [x, y, 1]^T$$
$$T = \begin{bmatrix} a_{00}x + a_{01}y + b_{00} \\ a_{10}x + a_{11}y + b_{10} \end{bmatrix}$$

## How do we get an Affine Transformation?

1. We mentioned that an Affine Transformation is basically a **relation** between two images. The information about this relation can come, roughly, in two ways:
  - a. We know both  $X$  and  $T$  and we also know that they are related. Then our task is to find  $M$
  - b. We know  $M$  and  $X$ . To obtain  $T$  we only need to apply  $T = M \cdot X$ . Our information for  $M$  may be explicit (i.e. have the 2-by-3 matrix) or it can come as a geometric relation between points.
2. Let's explain this in a better way (b). Since  $M$  relates 2 images, we can analyze the simplest case in which it relates three points in both images. Look at the figure below:



the points 1, 2 and 3 (forming a triangle in image 1) are mapped into image 2, still forming a triangle, but now they have changed notoriously. If we find the Affine Transformation with these 3 points (you can choose them as you like), then we can apply this found relation to all the pixels in an image.





## Code

### 1. What does this program do?

- Loads an image
- Applies an Affine Transform to the image. This transform is obtained from the relation between three points. We use the function `cv::warpAffine` for that purpose.
- Applies a Rotation to the image after being transformed. This rotation is with respect to the image center
- Waits until the user exits the program

### 2. The tutorial's code is shown below. You can also download it here [here](#)

```
#include "opencv2/imgcodecs.hpp"
#include "opencv2/highgui.hpp"
#include "opencv2/imgproc.hpp"
#include <iostream>

using namespace cv;
using namespace std;

{
const char* source_window = "Source image";
const char* warp_window = "Warp";
const char* warp_rotate_window = "Warp + Rotate";
}

int main( int, char** argv )
{
    Point2f srcTri[3];
    Point2f dstTri[3];

    Mat rot_mat( 2, 3, CV_32FC1 );
    Mat warp_mat( 2, 3, CV_32FC1 );
    Mat src, warp_dst, warp_rotate_dst;

    src = imread( argv[1], IMREAD_COLOR );

    warp_dst = Mat::zeros( src.rows, src.cols, src.type() );
```

Old-fashioned



```
srcTri[0] = Point2f( 0,0 );
srcTri[1] = Point2f( src.cols - 1.f, 0 );
srcTri[2] = Point2f( 0, src.rows - 1.f );

dstTri[0] = Point2f( src.cols*0.0f, src.rows*0.33f );
dstTri[1] = Point2f( src.cols*0.85f, src.rows*0.25f );
dstTri[2] = Point2f( src.cols*0.15f, src.rows*0.7f );

{ warp_mat = getAffineTransform( srcTri, dstTri ); } Get affine transform from point correspondence

warpAffine( src, warp_dst, warp_mat, warp_dst.size() );

Point center = Point( warp_dst.cols/2, warp_dst.rows/2 );
double angle = -50.0;
double scale = 0.6;

rot_mat = getRotationMatrix2D( center, angle, scale );

warpAffine( warp_dst, warp_rotate_dst, rot_mat, warp_dst.size() );

namedWindow( source_window, WINDOW_AUTOSIZE );
imshow( source_window, src );

namedWindow( warp_window, WINDOW_AUTOSIZE );
imshow( warp_window, warp_dst );

namedWindow( warp_rotate_window, WINDOW_AUTOSIZE );
imshow( warp_rotate_window, warp_rotate_dst );

waitKey(0);

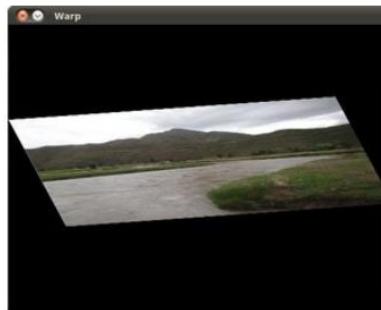
return 0;
}
```

## Result

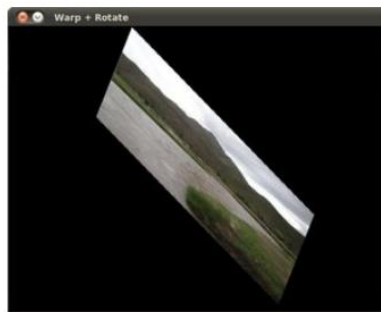
1. After compiling the code above, we can give it the path of an image as argument. For instance, for a picture like:



after applying the first Affine Transform we obtain:



and finally, after applying a negative rotation (remember negative means clockwise) and a scale factor, we get:





- Tutorial:
  - Select matching points
  - Automatic calculation of the transformation matrix
- Pure transformations are also available
  - E.g.: rotation

## \$ getRotationMatrix2D()

```
Mat cv::getRotationMatrix2D ( Point2f center,  
                             double angle,  
                             double scale  
                             )
```

Calculates an affine matrix of 2D rotation.

The function calculates the following matrix:

$$\begin{bmatrix} \alpha & \beta & (1 - \alpha) \cdot \text{center.x} - \beta \cdot \text{center.y} \\ -\beta & \alpha & \beta \cdot \text{center.x} + (1 - \alpha) \cdot \text{center.y} \end{bmatrix}$$

where

$$\begin{aligned} \alpha &= \text{scale} \cdot \cos \text{angle}, \\ \beta &= \text{scale} \cdot \sin \text{angle} \end{aligned}$$

The transformation maps the rotation center to itself. If this is not the target, adjust the shift.

### Parameters

**center** Center of the rotation in the source image.

**angle** Rotation angle in degrees. Positive values mean counter-clockwise rotation (the coordinate origin is assumed to be the top-left corner).

**scale** Isotropic scale factor.

### See also

[getAffineTransform](#), [warpAffine](#), [transform](#)



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