

## Instability result:

$x_e = 0$  is unstable if  $\exists$  a  $C^1$   $V(x)$  s.t.:

- a)  $P = \{x : V(x) > 0\}$  has  $x_e$  as accumulation point
- b)  $\dot{V} > 0$  in  $U = P \cap S(x_e, r)$ , for some  $r > 0$

The theorem is useful because while the necessary and sufficient condition for stability is the existence of a Lyapunov function, we cannot exclude it a priori without an instability criterion.