# SW 1: Introduction

Model's three properties

- **Mapping**: models act as a representation of natural or artificial originals and can be models in turn;
- **Reduction**: models function as abstraction. They do not capture every attribute of the original; instead, they isolate and retain only those attributes relevant to the specific objective, intentionally omitting detail to manage complexity and focus on the problem at hand;
- **Pragmatic**: models function as utilitarian substitutes. They do not replace the original universally but serve as a representative for a specific user (subject), within a defined time frame, and for a particular purpose or operation.

Example
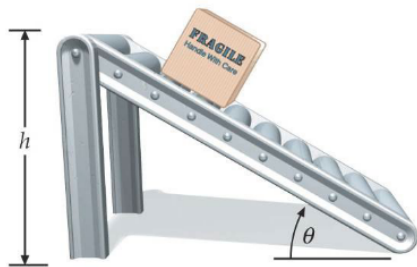
- **Generaliz.**: point mass sliding down an inclined plane;
- **Mapping**: box as mass, conveyor slope as an angle θ, vertical drop as height h, gravity;
- **Reduction**: no structure flexibility, no air movement, no friction, no rollers $\rightarrow$ flat plane;
- **Pragmatic**: it allows a, v_f, t of the box to be calculated, it enables the prediction of how to build a belt mockup.
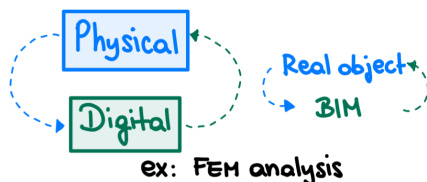
Digital representation

- - - - - - - - ▶ Manual Data Flow (Offline)
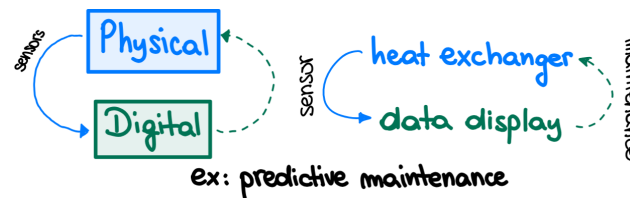——————▶ Automatic Data Flow (Real-time)

Digital model (simulation)
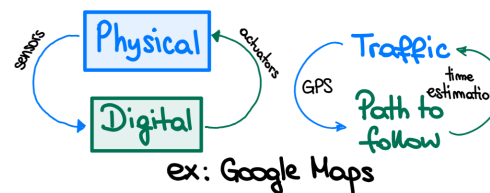
No direct connection between digital and physical object:

ex: FEM analysis

Digital shadow

Unidirectional, automated data flow from physical object to digital model:

ex: predictive maintenance

Digital twin

Automated data exchange between physical object and model:

ex: Google Maps

Role of time

Stationary behavior

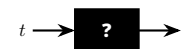Steady-state operation: $\dot{m}_\alpha = \dot{m}_\omega$

Dynamic behavior

Non stationary/transient/unsteady: $\dfrac{dm}{dt} = \dot{m}_\alpha - \dot{m}_\omega$
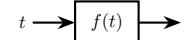
Governing dynamics

Empirical (black box)

Data based, without direct physics link. (ex: machine learning, fitting of functions)

Physics-based (white box)

Based on physical laws. (ex: conservation of mass)

Grey-box (hybrid)

Combining physics and data parameters.

Role of space

Point model (0D)

Assumes the whole system is perfectly mixed. (ex: ideal mixer with isotropic distribution). Software: Excel, MATLAB

Linked point

Connects several simple models together to create a basic network or layout. (ex: space shown via linking of 0D-models). Software: Simulink, Modelica

Spatial model (1-3D)

Considers real position of state variables or entities; spatial relationships affect the dynamics. (ex: real mixer with anisotropic, heterogeneous distribution). Software: COMSOL, ANSYS, AutoCAD, REVIT

Example with a heat pump

- **Purpose**: digital shadow $\rightarrow$ automated data;
- **Governing dynamics**: physics-based $\rightarrow$ based on thermodyn. laws;
- **Time**: time dependent, dynamic behavior $\rightarrow$ heating load, power of the hp, on/off cycles;
- **Space**: linked point $\rightarrow$ el. inputs, thermal energy exchange, 4 components to monitor.

Solvability of models

Analytical

Closed formula as solution. Only for simple problems.

$$A = \left.\frac{x^3}{3}\right|_0^2 = \frac{8}{3}$$

Numerical

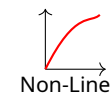Numerical approximation. For complex problems.

$$A \approx \sum_{i=1}^{n} f(x_i)dx \approx 2.6667$$

Further modelling properties

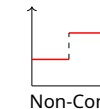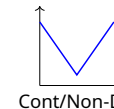### Linear vs Non-linear

Linear   Non-Linear

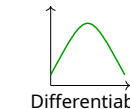### Continuity vs Differentiability
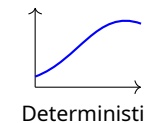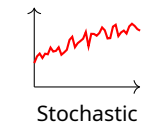

Non-Cont   Cont/Non-Diff   Differentiable

Deterministic vs Stochastic

Deterministic   Stochastic

Modelling approaches

Top-down

Largest components broken down into smaller. ex: marble block sculpture, railway network.
$\oplus$ Efficient model, $\ominus$ Misses details

Bottom-up

Individual components combined into larger. ex: LEGO model, human body.
$\oplus$ Detailed model, $\ominus$ Complex

SW2: How to model a system

1. Problem formulation
2. Mathematical representation
3. Mathematical analysis
4. Interpretation and evaluation of results

Problem formulation

Task 1 - Defining goals

What do we want to achieve?
How well/closely does our model need to represent reality?
What could be the goals for this specific system?

Task 2 - Characterize the system

What are the relevant parameters and variables of the system?
What are the system boundaries?
What are the inputs and outputs of the system?

Task 3 - Simplify and idealize the system

Still reproduce the significant behaviors of the system, while reducing complexity.
Reduce model to the main parameters and variables (ex. for hp: COP? Max. power? Avg power? Yearly values? Temperature levels?).

Mathematical formulation

Task 1 - Identify fundamental theories and laws

If no laws are available, use ad-hoc or empirical data to derive relationships:
Thermodynamic laws, material properties, ad-hoc
$P_{out} = COP(T_{amb}) \cdot P_{in}$

Task 2 - Derivation of relationships

Transfer system into a mathematical formulation.
Top-down (black/grey box): Use generic relationship, data from measurement to determine parameters. For more complex systems, add more parameters. Use techniques such as machine learning.

Bottom-up: Detailed physical modelling of the device. Physical laws to describe each component. Exact geometry, material properties, boundary conditions.

Task 3 - Reduce to standard mathematical problem

Simple algebra, linear programming, differential equation, diffusion problem, wave propagation, FEM problem, using suitable methods and software/programming tools.

Interpretation and evaluation of the results

Task 1 - Calibration of results

Use existing data to calibrate the model.

Task 2 - Validation

Check underlying physics law, such as energy or mass conservation, compare to known solutions, look at extreme cases, compare to measured data.
$\rightarrow$ What is it and why do we have to do it?

Before the modelling:
What do we model how?:

a) Aims: does the model describe the process under test?
b) Output: does the model provide the required output to describe the process?
c) Type: is the type of the model suitable to describe the process?

During modelling:
Can we reproduce the measurements?
Does the model behave like to system under study?

d) Fitting data: does the model reproduce the fitting data? How to measure accuracy?
e) Reproducing novel data: does the model also predict novel measurement data correctly?
f) Sensitivity analysis: does the model predict the behavior of the system correctly when system parameters are changed?

After modelling:
Does the model also work with new data?

g) System potentially changed.
h) Differences in system behavior is only manifest in new experiments.

SW 3: Data-based modelling

Linear regression

Used to find a linear function $y = f(x) = a + bx$ that best fits a dataset (x_i, y_i).

Least squares method

Minimize the sum of squared errors (SSE):

$$S = \sum_{i=1} (y_i - (a + bx_i))^2$$

If measurement uncertainties Δy_i exist, weight the error:

$$S_i = \frac{y_i - y(x)}{\Delta y_i}$$

Optimal parameter formulas

Finding a and b when S is minimal:

$$\frac{\partial S}{\partial a} = 0 \quad ; \quad \frac{\partial S}{\partial b} = 0$$

Slope b:

$$b = \frac{\sum_i x_i y_i - \frac{1}{n} \left(\sum_i x_i\right)\left(\sum_i y_i\right)}{\sum_i x_i^2 - \frac{1}{n}\left(\sum_i x_i\right)^2}$$

Intercept a:

$$a = \bar{y} - b\bar{x}$$

where:

$$\bar{x} = \frac{\sum_i x_i}{n} \quad ; \quad \bar{y} = \frac{\sum_i y_i}{n}$$

Quality of fit (R^2)

The coefficient of determination R^2 indicates the percentage of variation explained by the model:

$$R^2 = \frac{\sum_i (y(x) - \bar{y})^2}{\sum_i (y_i - \bar{y})^2}$$

- $R^2 = 1$ (100%): the model explains all data;
- $R^2 = 0$ (0%): the model doesn't (random).

Multilinear regression

Used when the target depends on multiple variables:

$$y(x_1, \ldots, x_n) = a + b_1 x_1 + \cdots + b_n x_n = a + \sum_{j=1}^{n} b_j x_j$$

Non-linear regression

The goal is to fit data using non-linear functions when the underlying process is not linear.

Linearization techniques

Function	Equation	Trasformation	Variables
Exp	$y = ae^{bx}$	$\ln y = \ln a + bx$	x vs $\ln y$
Power	$y = ab^x$	$\ln y = \ln a + x \ln b$	x vs $\ln y$
Inverse	$y = \dfrac{a}{x}$	$\dfrac{1}{y} = \dfrac{x}{a}$	x vs $\dfrac{1}{y}$
Square offset	$y = ax^2 + b$	$y = a(x^2) + b$	x^2 vs y
Root / Cubic	$y = \sqrt{ax^3 + b}$	$y^2 = ax^3 + b$	x^3 vs y^2

Maximum likelihood method (MLE)

Determines the parameters of a probability distribution that best describes a dataset, independent of histogram binning.

Likelihood function

Defines as the product of probability densities for all data points:

$$L(\sigma, \mu) = \prod_i f(x_i, \sigma, \mu)$$

Log-likelihood

To simplify calculation and avoid small numbers, minimize the negative logarithm:

$$-\log L = -\sum_i \log(f(x_i, \sigma, \mu))$$

Common distribution

Normal distribution:

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2\right)$$

Weibull distribution (Reliability):

$$f(x) = \begin{cases} \lambda k (\lambda x)^{k-1} e^{-(\lambda x)^k}, & x > 0 \\ 0 & \text{else} \end{cases}$$

Weibull cumulative distribution function

$$F(x) = \int_{-\infty}^{x} f(u)\,du = \begin{cases} 1 - e^{-(\lambda x)^k} & \text{for } x > 0 \\ 0 & \text{else} \end{cases}$$

SW4: Modelling with ODEs

Fundamentals of ODEs

An ODE contains functions of one independent variable and their derivatives.

Ordinary (ODE)

Involves one independent variable:

$$\frac{d^2 x}{dt^2} = -g$$

Partial (PDE)

Involves multiple independent variables:

$$\frac{d^2 u}{dt^2} = c^2 \frac{d^2 u}{dx^2}$$

Analytical solution method

Separation of variables

Used when terms involving y and x can be moved to opposite sides.

Variation of parameters

Used for inhomogeneous linear ODEs. General solution is the sum of the homogeneous solution and a particular solution.

Numerical solution methods

Euler method

A simple iterative method to approximate ODEs defined as $\frac{df}{dx} = g(x)$.

The approximation uses the finite difference slope:

$$\frac{df}{dx} \approx \frac{f(x_0 + \Delta x) - f(x_0)}{\Delta x}$$

Iterative steps:

$$f(x_0 + \Delta x) = f(x_0) + g(x_0)\Delta x$$

Modelling principles

Balance equations

Based on the conservation principle:

$$\frac{d}{dt} f(t) = f(t_\alpha) - f(t_\omega)$$

Example in a capacitor

$$U_0 = U_R + U_C \Rightarrow U_0 = RI + \frac{Q}{C} = R\frac{dQ}{dt} + \frac{Q}{C}$$

Mechanics and forces

Equation of motion is derived from Newton's second law $F_{net} = ma$.

Example of a falling drop with drag

$$m\dot{v} = mg - bv \Rightarrow v(t) = \frac{mg}{b}\left(1 - e^{-bt/m}\right)$$

Growth and decay

Describes processes where a quantity increases or decreases over time.

$$\frac{dN}{dt} = kN \Rightarrow N(t) = N_0 e^{kt}$$

with half-time / doubling factor τ:

$$\tau = \left|\frac{\ln 2}{k}\right|$$

Example of logistic growth

$$\frac{dN}{dt} = KN(t) - \frac{K}{K}N^2 \Rightarrow N(t) = \frac{L}{1 + \left(\frac{L}{N_0} - 1\right)e^{-kt}}$$

Recipe to derive the equation of motion

1. Make a sketch of the situation;
2. Define the coordinate system and select variables of interest;
3. Identify all forces and momenta;
4. Formulate the equation of motion;
5. Solve it.

Linear algebra and systems of ODEs

Matrix representation

System of equations:

$$a_{11}x_1 + a_{12}x_2 + a_{13}x_3 = b_1$$
$$a_{21}x_1 + a_{22}x_2 + a_{23}x_3 = b_2$$
$$a_{31}x_1 + a_{32}x_2 + a_{33}x_3 = b_3$$

Matrix form ($Ax = b$):

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$$

If $x = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$, then $\dot{x} = \begin{pmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{pmatrix}$

Inversion and diagonalization

Inverse matrix R^{-1}: $R \cdot R^{-1} = I$ (Identity matrix).

$$I = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Diagonalization: Special matrices can be rewritten as:

$$A = \begin{pmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{pmatrix}$$

This transforms the matrix into a diagonal matrix containing eigenvalues λ.

Why is it called linear algebra

Linearization:
Complex, non-linear functions can be approximated by linear functions in a small neighborhood of a point a:

$$f(x) \approx f(a) + f'(a)(x - a)$$

Benefit of solving ODEs

If A were a number, $\dot{x} = Ax$ would solve to $x(t) = ke^{At}$. Since A is a matrix, if we diagonalize it using eigenvalues λ, the solution becomes a mixture of exponentials:

$$x(t) = R^{-1} \begin{pmatrix} k_1 e^{\lambda_1 t} & 0 & 0 \\ 0 & k_2 e^{\lambda_2 t} & 0 \\ 0 & 0 & k_3 e^{\lambda_3 t} \end{pmatrix} R$$

Solvability of linear systems

Geometric interpretation:
Solving $Ax = b$ is finding the intersenction of lines/planes.

- **Case 1**, consistent: lines intersect at exactly one point;
- **Case 2**, inconsistent: lines are parallel and distinct, there is no solution;
- **Case 3**, infinite solutions: lines are identical and overlap completely.

Determinant

A scalar value derived from a square matrix that tells us if it is invertible. If det $A = 0$, the matrix is not invertible.

2x2 formula: For $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$, det $A = ad - bc$.

3x3 formula: For $A = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix}$,

$$\det A = a_{11} \det \begin{bmatrix} e & f \\ h & i \end{bmatrix} - a_{12} \det \begin{bmatrix} d & f \\ g & i \end{bmatrix} + a_{13} \det \begin{bmatrix} d & e \\ g & h \end{bmatrix}$$

$$\det A = \sum_j^n a_{1j} C1j, \quad \underbrace{C1j = (-1)^{1+j} \det A_{ij}}_{\text{Cofactors}}$$

The Eigenvalue problem

For a square n×n matrix A, we look for a Eigenvector x and a Eigenvalues a such that:

$$Ax = \lambda x$$

Calculation method:

1. Solve the characteristic equation $\det(A - \lambda I) = 0$
2. This result in an n-th order polynomial $(a_1 \lambda^n + \cdots = 0)$
3. The roots of this polynomial are the Eigenvalues.

SW5-10: Modelica

Equation-based modelling

Describes a system by using physical relationships.

Problem definition - Double layer wall

A wall consists of two layers with different thermal conductance values G_1 and G_2.

We consider two steady-state cases:
1. A heat flow $\dot{Q}_1$ passes throughs the wall and the right temperature is T_2. The interface temperature T_i and the left temperature T_1 are unknown.
2. Both boundary temperatures T_1 and T_2 are given and the interface temperature T_i and the heat flow $\dot{Q}$ are unknown.
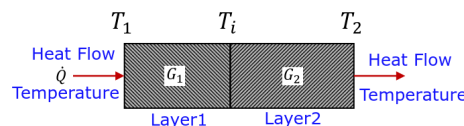
Formulas

Heat conduction equation [W]:

$$\dot{Q} = G\Delta T = G(T_\alpha - T_\omega) = G_1(T_1 - T_i) = G_2(T_i - T_2)$$

Thermal conductance [W/K]:

$$G = \frac{A}{L}\lambda$$

Conservation of energy:

$$\dot{Q}_1 = \dot{Q}_2 = \dot{Q}$$

Component-based modelling

Instead of rewriting equations each time, an instance of the needed physics law component is added.

Thermal components

thermalConductor

Models heat linear heat flow between two ports determined by a constant thermal conductance G

$$\dot{Q} = G(T_a - T_b) \quad ; \quad \dot{Q} = \frac{\lambda \cdot A}{L}$$
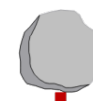
fixedHeatFlow

A source that injects a constant heat flow into the connected component

$$port.\dot{Q} = -\dot{Q}_{\text{component}}$$

fixedTemperature

Defines a constant temperature boundary condition (acting like an infinite heat reservoir).

$$port.T = T_{\text{parameter}}$$

heatCapacitor

Thermal mass that stores energy, where temperature changes based on heat flow and heat capacity C.

$$C \cdot \frac{dT}{dt} = m \cdot c_p \cdot \frac{dT}{dt} = \dot{Q}$$

convection

Models the heat transfer between a solid surface and a moving fluid based on a convection coefficient G_{conv}.

$$\dot{Q} = \alpha \cdot A \cdot \Delta T = G_{\text{conv}} \cdot (T_{\text{solid}} - T_{\text{fluid}})$$

temperatureSensor

Measures the absolute temperature at the thermal port and outputs that value as a real signal.

$$y = T_{port} \quad ; \quad \dot{Q} = 0$$

Electrical components

resistor

Resists the flow of electric current, creating a voltage drop proportional to the current.

$$U = R \cdot I \quad ; \quad \dot{Q} = P = U \cdot I$$

constantVoltage

An ideal voltage source that maintains a constant voltage difference between its prositive and negative pins.

$$u_{port} = U_{\text{const}}$$

ground

Defines the reference potential (zero voltage) for an electric circuit.

$$u_{port} = 0$$

Signal components

pulse

Generates a signal that alternates between two values (amplitude and offset) with a defined period and pulse width.

$$y = \begin{cases} \text{offset + ampl.,} & \text{if} \in \text{pulse width} \\ \text{offset,} & \text{otherwise} \end{cases}$$

constant

A signal source that outputs a fixed numerical value.

$$y = k$$

gain

A signal block that multiplies the input signal u by a constant parameter k to produce the output signal y.

$$y = ku$$

onOffController

A logical controller that switches its output between true and false based on comparing a measured signal u to a reference value.

$$y = \begin{cases} \text{true} & \text{if } u < (\text{reference} - \frac{\text{bandswitch}}{2}) \\ \text{false} & \text{if } u > (\text{reference} - \frac{\text{bandswitch}}{2}) \end{cases}$$

booleanToReal

Converts a Boolean signal into a Real float number.

$$y = \begin{cases} \text{realTrue} & \text{if input is True} \\ \text{realFalse} & \text{if input is False} \end{cases}$$
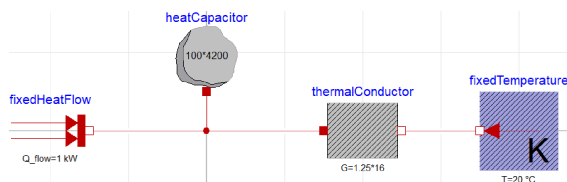
Dynamic systems

Two things can lead to time-varying behavior:

1. Transient boundary conditions
2. A dynamic system starting from a non-eq. state

First-order thermal model

A mass is heated by a constant source while simultaneously losing heat to a cooler environment
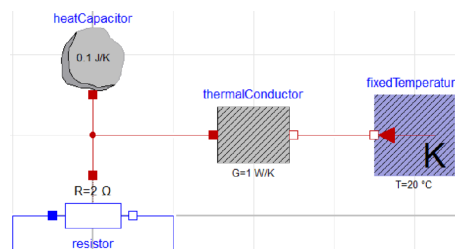
Conservation of energy at the central node:

$$C \cdot \frac{dT}{dt} = Q_{in} - G(T - T_{\text{sink}})$$

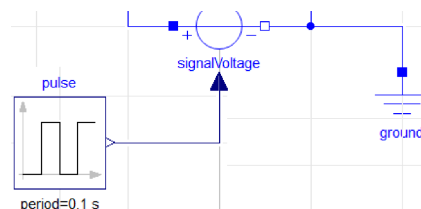## Multi-domain modelling

Multi-domain model

Allows representing different physical domains such as electrical, mechanical, thermodynamic, and fluid dynamics in a single model.

Resistor heat interacts with the thermal system

Cyber-physical model

A model combining physical domains with a software.

One-dimensional model

Simulation technique used to calculate spatial distribution by discretizing a continuous object into multiple discrete, lumped segments.

About Modelica

Definition and structure

Open source, equation-based, non-casual language for modelling dynamic behavior of multidisciplinary systems. Component-based (graphical connection), object oriented (inheritance), and hierarchical.

Equation-based / non-casual modelling

- Component diagram: topological (physical) structure;
- Equation-based: no fixed input/output direction;
- Connections: represent physical wiring/piping;
- Pros: reusable, multi-domain, closer to physics.

Casual modelling

- Block diagram: represents computational data flow;
- Assignment-based: fixed input/output;
- Connections: represent signal flow variables;
- Cons: prone to errors when modifying structure.

Hierarchical structure

Components are built from connected subcomponents and/or equations, allowing complex systems to be broken down into reusable parts.

Object-oriented

Allows creating general base definitions (superclasses) that specific components extend, rather than defining every component from scratch.

Physical mapping

Icons represent physical components, connections represent actual physical couplings.
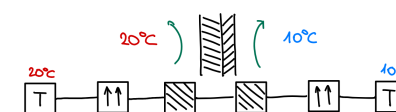
Application examples

- Multiphase flow: refrigeration systems;
- Multi-domain: Pneumatic piston pump;
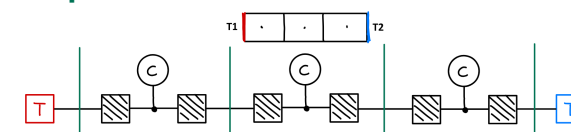- Compressible media: Medical pulse wave analysis.

Examples wrap-up

Thermal circuit

$$\frac{dE}{dT} = \frac{dU}{dT} = m \cdot c \cdot \frac{dT}{dt} = \dot{Q}$$

Heat flow

Heaten up rod

Physical units

Heat flow	$\dot{Q}$	$[W]$	Heat capacity	C	$[J/K]$
Thermal conductivity	λ	$[W/mK]$	Thermal conductance	G	$[W/K]$
Specific heat capacity	c_p	$[J/kgK]$	Convection coefficient	α	$[W/m^2K]$

SW11: Model and control energy systems

Energy system model

Model dynamics of energy systems to study consumption peaks, self-sufficiency and storage sizing, planning.

How to build an energy system model

Single building

Component list + properties; hydraulic connections; usage profiles; pricing information.

Quarter/community/city

Single-building info for ALL buildings + grid/connection properties + control scheme (balance demand/supply).

Main challenges in energy system modelling

Acquiring
Layout, parameters, installed-component details, control-system detailsm shading/clouds, usage profiles.

Modelling
Reliable component behavior and coupling, environment interaction (solar/shading/clouds, wind shielding, contributions from neighboring buildings).
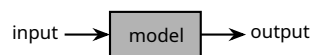
Models availability

Software frameworks
Built-in, pre-made models for specific component types.

Simplified models
Basic blackbox representation:

input → model → output

Literature
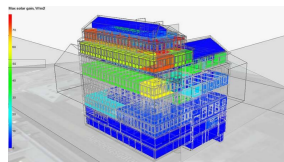Models taken from published research and publications.

Data-science models
Models learned or fitted from data.

White-/Grey-/Black-box models

- **White box**: theory-based, parameters from measurement or ab initio calculations;
- **Grey-box**: simplified theory, parameters estimated from data;
- **Black-box**: fit a model and parameters (data-based).

White-box

Each white-box model is a digital twin, but not all digital twins are white-box models.

Digital twin
Virtual representation that serves as the real-time digital counterpart of a physical object or process:

- **Detailed**: detailed, ab initio / measured parameters;
- **Simplified**: key mechanisms, simple assumptions;
- **Numerical**: fitting data, parameters are fitted.

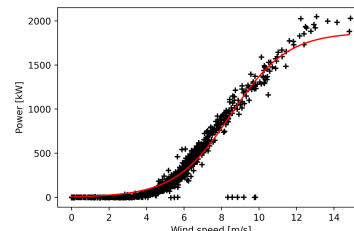## Heat pump modelling example (white to gray box)
Evaporator and condenser cycles, refrigerant dynamics, expansion valve control algorithm. COP dependence, interpolate experimental data with non-linear regression.

Grey-box example (1st order building / RC idea)
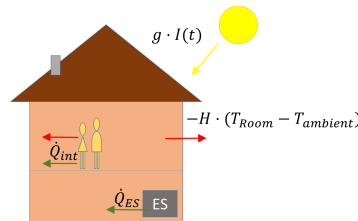
$$C\frac{dT_{\text{room}}}{dt} = \dot{Q}_{ES} + \dot{Q}_{int} + g\,I(t) - H\left(T_{\text{room}} - T_{\text{ambient}}\right)$$

Black-box example (wind turbine power curve)

$$P(w) = \frac{a}{1 + \exp\bigl(-b \cdot (w - s)\bigr)}$$

Control schemes overview

Control events = CE;
Control decisions = CD;
Control signal = CS.

- **Rule-based**: CE are chosen based on a rule-set;
- **Model-based**: predict the future behavior based on a model and decide such that the model performs best;
- **Neuronal network-based**: trains a neuronal network to take CD and act accordingly;
- **A posteriori optimisation-based**: takes historic data and optimise CD.
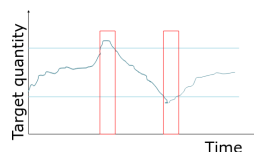
Rule-based

Fixed time plan controllers
CE are chosen based on a fixed time schedule.

Model predictive controllers
CE are chosen based on model prediction of system dynamics.

Set point controllers

CE is triggered if the target quantity is leaving the set point corridor. Ex:

$$\begin{cases} \text{ON} & \text{if } T_{\text{room}} < 19.5°C \\ \text{OFF} & \text{if } T_{\text{room}} > 20.5°C \end{cases}$$

# Feedback based controllers – P & I & D

CE are initiated based on the interaction with the controlled quantity. We have P, PI, PID controllers.

A PID-type controller computes the actuator command $u(t)$ from the error $e(t) = r(t) - y(t)$

$$u(t) = \underbrace{K_P e(t)}_{P} + \underbrace{K_I \int_0^t e(\tau)\,d\tau}_{I} + \underbrace{K_D \frac{d}{dt}e(t)}_{D}$$

- **P**: reacts immediately to error:
  Bigger $K_P \to$ faster response, but can overshoot / oscillate and typically leaves a steady-state error;
- **I**ntegral: accumulates error over time:
  Removes steady-state error (drives output to the setpoint), but makes the response slower and can increase overshoot and "windup" if not handled.
- **D**erivative: reacts to how fast the error is changing:
  reduces overshoot and improves settling, but is sensitive to measurement noise.

Graphical representation
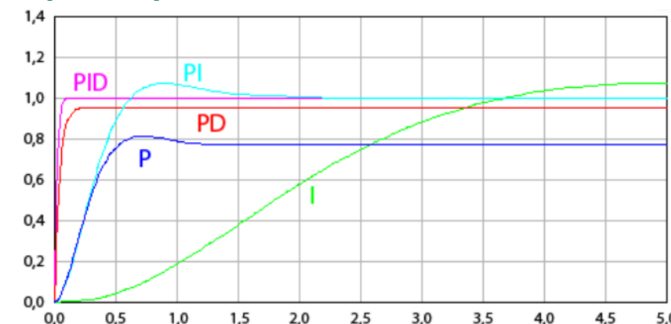
The plot shows the closed-loop step response over time of the same plant controlled with different controllers with setpoint at 1.

- **P**: rises quickly but settles below 1 → steady-state error remains;
- **I**: rises very slowly but eventually reaches (and may slightly exceed) 1 → zero steady-state error, poor speed;
- **PD**: faster than P and with less overshoot / better damping, but still can have steady-state error;
- **PI**: reaches 1 but shows overshoot and slower settling;
- **PID**: fast rise, small overshoot, good settling, and zero steady-state error.

SW12: Design and analysis of experiments

Design of experiments (DoE): systematics sweep of parameter space when no fully-analytical optimum is available. Build an empirical model $y = F(x)$ from sampled runs and use it for optimisation.

Setup of simulation study

Aim: what do you want to archieve?
- control optimisation for given energy
- retrofitting of existing energy system by adding or replacing technologies
- design of novel energy system

Quantification: choose KPI / cost function.
- total energy consumption
- cost for energy provision
- share/amount of renewable energy

Decision variables: which variable can be influenced.
- Ex: size, orientation, capacity, ...

Measure of success: optimal configuration with respect to the KPI.
- Ex: among all system configuration we find the solution with highest share of renewable energy