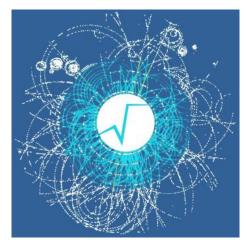
Analysis of Higgs boson decay into four leptons at 8 TeV

Matteo Malucchi

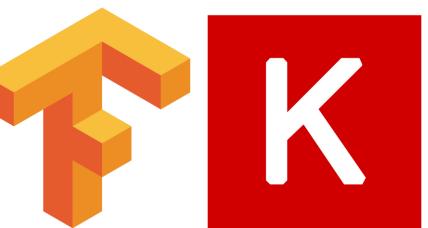
October 2022







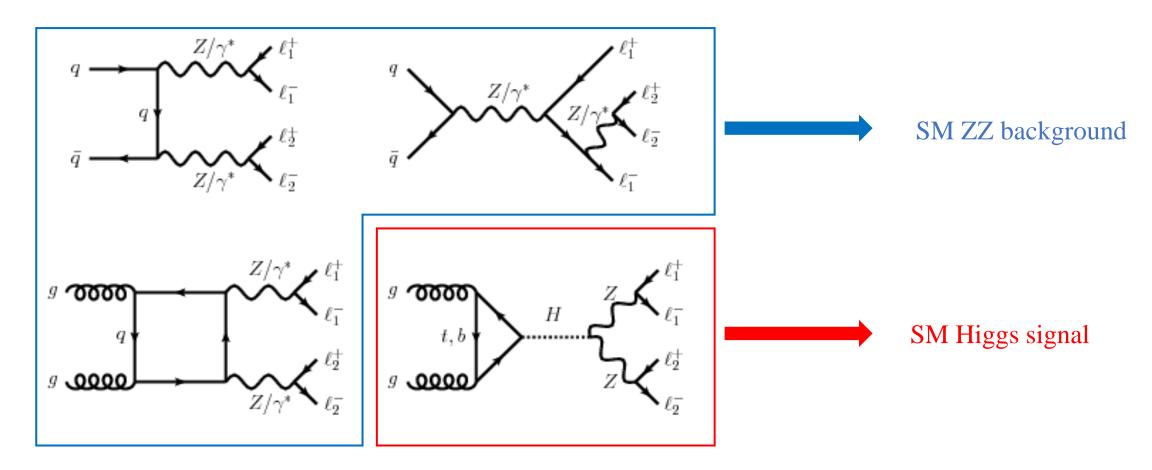






$$H \to ZZ^* \to l_1^+ l_1^- l_2^+ l_2^-$$

The datasets used throughout the analysis were reduced NanoAOD files created from CMS Open Data using data from Run 1 for a total of 11.6 fb^{-1} at 8 TeV.





Set up and run the analysis

if args global.download != "":

set_up.py

```
args.typeDistribution = check val(logger, args.typeDistribution,
      ["all", "data", "background", "signal", "sig bkg normalized", "total"], "typeDistribution")
except AttributeError:
# Create the directory to save the outputs if doesn't already exist
     create dir(logger, args.output, False)
except AttributeError:
 ef check val(log, input, correct list, name):
      if not any(correct in in input.split(",") for correct in in correct list):
         list str=', '.join(correct list)
         raise argparse.ArgumentTypeError(f"{name} {input} is invalid: it must be either {list_str}")
   except argparse.ArgumentTypeError as arg err:
      log.exception("%s \n>>>%s is set to %s \n", arg_err, name, correct_list[0], stack_info=True)
      return correct list[0]
     return input
def create dir(log, dir, ignore):
    try:
        os.makedirs(dir)
         log.debug("Directory %s/ Created", dir)
    except FileExistsError:
         log.debug("The directory %s/ already exists", dir)
    finally:
        if ignore == True:
             file path=os.path.join(dir, ".gitignore")
             if os.path.exists(file path):
             else:
                  with open(file path, 'w') as fp:
                      fp.write("# Ignore everything in this directory \n*")
                      fp.write("\n# Except this file \n!.gitignore")
```

run_analysis.py

download dataset.download(args global, logger global)

```
if args global.skim:
    skim.skim(args global, logger global)
                                                                             args global.graphPlots:
if args global.ml:
                                                                              make histo.make histo(args global, logger global)
    ml training.ml training(args global, logger global)
                                                                               make plot.make plot(args global, logger global)
    ml evaluation.ml evaluation(args global, logger global)
    ml selection.ml selection(args global, logger global)
    ml histo.ml histo(args global, logger global)
                                                                         if args global.invariantMassFit:
    ml_plot.ml_plot(args_global, logger_global)
                                                                               fit mass.fit mass(args global, logger global)
Analysis Tool
options:
                      show this help message and exit
  -h, --help
  -1 LOGLEVEL, --logLevel LOGLEVEL
                      integer representing the level of the logger: DEBUG=10, INFO = 20, WARNING = 30, ERROR = 40
  -d [DOWNLOAD], --download [DOWNLOAD]
                      enables the download of input data. If not specified otherwise the files are saved in the 'Input/' directory
                      base path where to find the input data. If enabled it automatically gets the input data from EOS unless a local directory is specified
  -o OUTPUT, --output OUTPUT
                      name of the output directory
  -c [CLEAROUTPUT], --clearOutput [CLEAROUTPUT]
                      name of output folder to be deleted. If not specified otherwise the 'Output/' directory is deleted
  -q, --skim
                      disables the skimming step
  -m, --ml
                      disables machine learning algorithm
                      disables the graphing of the distribution plots
  i, --invariantMassFit
                      disables fit of the Higgs mass
  s SAMPLE, --sample SAMPLE
                      string with comma separated list of samples to analyse: Run2012B DoubleElectron, Run2012B DoubleMuParked, Run2012C DoubleElectron,
                      Run2012C DoubleMuParked, SMHiggsToZZTo4L, ZZTo2e2mu, ZZTo4e, ZZTo4mu
                      comma separated list of the final states to analyse: FourMuons, FourElectrons, TwoMuons TwoElectrons
  e, --typeOfParallel parallel type for the downloads: default is multi-thread, if activated is multi-process-
  -p, --parallel
                      disables running in parallel
  -n NWORKERS, --nWorkers NWORKERS
                      number of workers for multi-threading
  -r [RANGE], --range [RANGE]
                      number of events on which the analysis is ran over (does not work in parallel)
                              the set of variables to be used in the ML algorithm defined 'Analysis/Definitions/variables ml def.py': tot, angles, higgs
                       string with comma separated list of the variables to plot. The complete list is defined in 'Analysis/Definitions/variables def.py'
                      comma separated list of the type of distributions to plot: data, background, signal, sig_bkg_normalized, total
```

Download the datasets

download_dataset.py

```
def download(args, logger):
   logger.info(">>> Executing %s \n", os.path.basename(__file__))
   t= perf counter()
   if args.parallel:
       logger.info(">>> Executing in parallel \n")
       parallel list = []
       #Loop over the various samples
       for sample name, number in SAMPLES DOWNLOAD.items():
           # Check if the sample is one of those requested by the user
           if sample name not in args.sample and args.sample != "all":
           logger.info(">>> Process sample: %s \n", sample_name)
           file_name=os.path.join(args.download, f"{sample_name}.root")
           if args.typeOfParallel == "thread":
               logger.info(">>> Executing multi-threading \n")
               parallel_list.append(thr.Thread(target=get_file_parallel, args=(logger, number, sample_name, file_name)))
           elif args.typeOfParallel == "process":
               logger.info(">>> Executing multi-processing \n")
               parallel_list.append(mp.Process(target=get_file_parallel, args=(logger, number, sample_name, file_name)))
       for parallel elem in parallel list:
           parallel elem.start()
       #join parallel
       for parallel elem in parallel list:
           parallel elem.join()
       logger.info(">>> Executing not in parallel \n")
       #Loop over the various samples
       for sample name, number in SAMPLES DOWNLOAD.items():
           # Check if the sample is one of those requested by the user
           if sample name not in args.sample and args.sample != "all":
               continue
           logger.info(">>> Process sample: %s \n", sample name)
           file_name=os.path.join(args.download, f"{sample_name}.root")
           get file(logger, number, sample name, file name)
```

```
:lass MyProgressBar():
  def init (self):
       self.pbar = None
  def __call__(self, block_num, block_size, total_size):
       if not self.pbar:
           self.pbar=progressbar.ProgressBar(maxval=total size)
           self.pbar.start()
       downloaded = block num * block size
       if downloaded < total size:
           self.pbar.update(downloaded)
           self.pbar.finish()
  count(func):
  @wraps(func)
  def counted(*args):
       counted.call count += 1
       return func(*args)
  counted.call count = 0
  return counted
ef get_file(log, num, sample, file):
     urllib.request.urlretrieve(f"http://opendata.cern.ch/record/{num}/files/{sample}.root", file, MyProgressBar())
  except urllib.error.HTTPError as http_err:
     log.exception("File %s.root can't be found %s",
                    sample, http_err, stack_info=True)
  except urllib.error.ContentTooShortError:
     log.exception("Network conditions is not good. Reloading for %d time file %s.root",
                    get_file.call_count, sample)
         log.exception("Download of %s.root has failed due to bad network conditions! \n", sample)
         get_file.call_count=0
     get file(log, num, sample, file)
     get file.call count=0
 get_file_parallel(log, num, sample, file):
  count = 1
  while count <= 4:
          urllib.request.urlretrieve(f"http://opendata.cern.ch/record/{num}/files/{sample}.root", file)
      except urllib.error.HTTPError as http err:
          log.exception("File %s.root can't be found %s",
                          sample, http err, stack info=True)
     except urllib.error.ContentTooShortError:
          log.exception("Network conditions is not good. Reloading for %d time file %s.root", count, sample)
  log.exception("Download of %s.root has failed due to bad network conditions!", sample)
```



Skim the dataset

```
#Enamble multi-threading if range is not active
if args.parallel and args.range == 0:
    ROOT.ROOT.EnableImplicitMT(args.nWorkers)
    thread_size = ROOT.ROOT.GetThreadPoolSize()
    logger.info(">>>> Thread pool size for parallel processing: %s", thread_size)

try:
    rdf2 = skim_tools.event_selection(rdf, final_state)
    rdf3 = skim_tools.four_vec(rdf2, final_state)
    rdf4 = skim_tools.order_four_vec(rdf3, final_state)
except RuntimeError as run_time_err:
    logger.exception("Sample %s ERROR: %s ", sample_name, run_time_err, stack_info=True)
    continue

rdf5 = skim_tools.def_mass_pt_eta_phi(rdf4)
rdf6 = skim_tools.def_angles(rdf6)
rdf_final = skim_tools.add_event_weight(rdf7, WEIGHTS[sample_name])
```

skim_functions.h

```
RVec<float> sipDef(VecF dxy, VecF dz, VecF sigma_dxy, VecF sigma_dz){
    auto ip=sqrt(dxy*dxy + dz*dz);
    auto sigma_ip=sqrt((sigma_dxy)*(sigma_dxy) + (sigma_dz)*(sigma_dz));
    auto sip=(ip/sigma_ip);
    return sip;
};

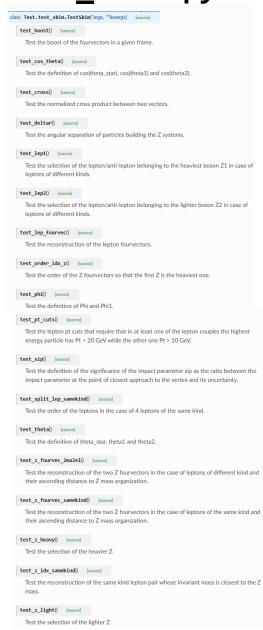
bool ptCuts(VecF mu_pt, VecF el_pt){
    if (Max(mu_pt)>20 && Min(mu_pt)>10) return true;
    if (Max(el_pt)>20 && Min(el_pt)>10) return true;
    return false;
};
```

skim_tools.py

```
event selection(rdf, final state):
if final state == "FourMuons":
    return rdf.Filter("nMuon==4",
              .Filter("Sum(Muon charge==1)==2 && Sum(Muon charge==-1)==2",
                       'Two positive and two negative muons")
              .Filter("All(abs(Muon_pfRelIso04_all)<0.40)",
                      "Good isolation of the muons")\
              .Filter("All(Muon pt>5) && All(abs(Muon eta)<2.4)",
                      "Good muon kinematics")\
              .Define("Muon_3d_sip",
                       "sipDef(Muon dxy, Muon dz, Muon dxyErr, Muon dzErr)")\
              .Filter("All(Muon 3d sip<4) && All(abs(Muon dxy)<0.5) && All(abs(Muon dz)<1.0)"
                      "Muons originate from the same primary vertex")
if final state == "FourElectrons":
    return rdf.Filter("nElectron==4",
                       "Four electrons")\
              .Filter("Sum(Electron_charge==1)==2 && Sum(Electron_charge==-1)==2",
                       "Two positive and two negative electrons")
              .Filter("All(abs(Electron pfRelIso03 all)<0.40)",
                       "Good isolation of the electrons")\
              .Filter("All(Electron pt>7) && All(abs(Electron eta)<2.5)",
                       "Good electron kinematics")\
              .Define("Electron 3d sip",
                       "sipDef(Electron dxy, Electron dz, Electron dxyErr, Electron dzErr)")\
              .Filter("All(Electron 3d sip<4) && All(abs(Electron dxy)<0.5)
                      && All(abs(Electron dz)<1.0)",
                      "Electrons originate from the same primary vertex")
```

```
if final state == "TwoMuonsTwoElectrons":
   return rdf.Filter("nMuon==2 && nElectron==2",
                      "Two muons and two electrons")\
             .Filter("Sum(Electron_charge) == 0 && Sum(Muon_charge) == 0",
             .Filter("All(abs(Electron eta)<2.5) && All(abs(Muon eta)<2.4)",
                      "Eta cuts")\
             .Filter("All(abs(Muon pfRelIso04 all)<0.40) && \
                     All(abs(Electron pfRelIso03 all)<0.40)",
                      "Require good isolation")
             .Filter("ptCuts(Muon_pt, Electron_pt)", "Pt cuts")\
             .Define("Muon dr",
                      "ROOT::VecOps::DeltaR(Muon eta[0], Muon eta[1], \
                      Muon_phi[0], Muon_phi[1])")\
             .Filter("Muon_dr>0.02 && Electron dr>0.02",
                      "Delta R cuts")\
             .Define("Muon 3d sip",
                      "sipDef(Muon_dxy, Muon_dz, Muon_dxyErr, Muon_dzErr)")\
             .Filter("All(Muon 3d sip<4) && All(abs(Muon dxy)<0.5) && All(abs(Muon dz)<1.0)",
                      "Muons originate from the same primary vertex")
              .Define("Electron_3d_sip",
                      "sipDef(Electron_dxy, Electron_dz, Electron_dxyErr, Electron_dzErr)")\
                     "Electrons originate from the same primary vertex")\
```

test_skim.py





Define the decay angles

Let us consider, of all the possible combinations of same-flavor opposite-sign lepton pairs, the one that has mass closest to $m_Z = 91.2$ GeV. The on-shell Z boson associated with it is referred to as Z_{close} . The other off-shell Z boson is reconstructed using the remaining lepton pair and is called Z_{far} . Subsequently, the reconstructed Z boson with highest mass is called Z_1 and the another one Z_2 . The three-momentum of the Z_i boson is called \mathbf{q}_i , while \mathbf{q}_{i1} and \mathbf{q}_{i2} indicate respectively the three-momenta of the lepton and antilepton associated with Z_i . Indicating as superscript the rest frame in which the three-momenta are taken, the definitions of the angles are:

• $\theta^* \in [0, \pi]$ is the production angle of the leading Z in the four-lepton rest frame

$$\cos \theta^* = \frac{q_{1z}^{4l}}{|\mathbf{q}_1^{4l}|}$$

where q_{1z}^{4l} is the z component of the three-momentum of Z_1 in the four-leptons rest frame

• $\Phi_1 \in [-\pi, \pi]$ is the angle between the decay plane of the leading lepton pair and a plane defined by Z_1 in the four-lepton rest frame and the positive direction of the collision axis $\hat{n}_z = (0,0,1)$

$$\Phi_1 = \frac{\mathbf{q}_1^{4l} \cdot (\hat{n}_1 \times \hat{n}_{coll})}{|\mathbf{q}_1^{4l} \cdot (\hat{n}_1 \times \hat{n}_{coll})|} \times \arccos(\hat{n}_1 \cdot \hat{n}_{coll})$$

where the normal vectors to the two planes are defined as

$$\hat{n}_1 = \frac{\mathbf{q}_{11}^{4l} \times \mathbf{q}_{12}^{4l}}{|\mathbf{q}_{11}^{4l} \times \mathbf{q}_{12}^{4l}|}, \qquad \hat{n}_{coll} = \frac{\hat{n}_z \times \mathbf{q}_1^{4l}}{|\hat{n}_z \times \mathbf{q}_1^{4l}|}$$

• $\Phi \in [-\pi, \pi]$ is the angle between the decay planes of the two lepton pairs in the four-leptons rest frame

$$\Phi = \frac{\mathbf{q}_1^{4l} \cdot (\hat{n}_1 \times \hat{n}_2)}{|\mathbf{q}_1^{4l} \cdot (\hat{n}_1 \times \hat{n}_2)|} \times \arccos(-\hat{n}_1 \cdot \hat{n}_2)$$

where

$$\hat{n}_2 = \frac{\mathbf{q}_{21}^{4l} \times \mathbf{q}_{22}^{4l}}{|\mathbf{q}_{21}^{4l} \times \mathbf{q}_{22}^{4l}|}$$

• $\theta_1 \in [0,\pi]$ and $\theta_2 \in [0,\pi]$ are the angles between final-state negatively charged leptons and the direction of flight of their respective Z bosons

$$\cos \theta_1 = -\frac{\mathbf{q}_2^{Z_1} \cdot \mathbf{q}_{11}^{Z_1}}{|\mathbf{q}_2^{Z_1}||\mathbf{q}_{11}^{Z_1}|}, \qquad \cos \theta_2 = -\frac{\mathbf{q}_1^{Z_2} \cdot \mathbf{q}_{21}^{Z_2}}{|\mathbf{q}_1^{Z_2}||\mathbf{q}_{21}^{Z_2}|}$$

skim_tools.py

Analysis. Skimming. skim tools. four vec(rdf, final state)

Reconstruct fourvector for leptons, Z and Higgs candidates.

rdf (ROOT.RDataFrame) - Input RDataFrame

final_state (str) - Final state to be analysed

RuntimeError - Raised when an unknown final state is passed

ROOT.RDataFrame

Analysis.Skimming.skim tools.order four vec(rdf, final_state)

Put the four vectors in order according to the following criteria

- Z1 = heavier boson candidate
- Lep11 = lepton belonging to the heavier boson Z1
- · Lep12 = anti-lepton belonging to the heavier boson Z1
- Lep21 = lepton belonging to the lighter boson Z2 Lep22 = anti-lepton belonging to the lighter boson Z2
- rdf (ROOT RDataFrame) Input RDataFrame

 final_state (str) - Final state to be analysed. RuntimeError - Raised when an unknown final state is passed

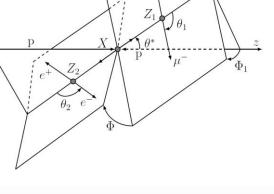
ROOT.RDataFrame Return type:

Analysis.Skimming.skim tools.def mass pt eta phi(rdf)

Define Mass, Pt, Eta and Phi of Higgs boson and Z candidates

rdf (ROOT.RDataFrame) - Input RDataFrame

ROOT.RDataFrame



Analysis.Skimming.skim tools.four vec boost(rdf)

Boost the various fourvectors in different frames.

rdf (ROOT,RDataFrame) - Input RDataFrame

Returns: Output RDataFrame

ROOT.RDataFrame Return type:

Analysis.Skimming.skim tools.def angles(rdf)

Define the five angles that allow discrimination between signal and background.

rdf (ROOT.RDataFrame) - Input RDataFrame

Output RDataFrame Returns:

Return type: ROOT.RDataFrame

Analysis.Skimming.skim tools.add event weight(rdf, weight) [source]

Add weights for the normalisation of the simulated samples in the histograms.

rdf (ROOT.RDataFrame) - Input RDataFrame

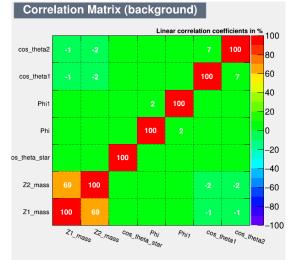
Output RDataFrame Returns: Return type: ROOT.RDataFrame

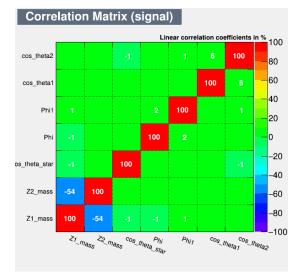


DNN variables and model

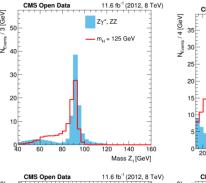
ml_training.py

```
ROOT.TMVA.Tools.Instance()
ROOT.TMVA.PyMethodBase.PyInitialize()
factory = ROOT.TMVA.Factory("TMVAClassification", output,
                    "!V:!Silent:Color:DrawProgressBar:Transformations=D,G:AnalysisType=Classification"
dataloader = ROOT.TMVA.DataLoader("dataset")
or variable in variables:
   dataloader.AddVariable(variable)
  logger.debug(variable)
dataloader.AddSignalTree(signal chain, 1.0)
dataloader.AddBackgroundTree(bkg chain, 1.0)
dataloader.PrepareTrainingAndTestTree(ROOT.TCut(""), "SplitMode=Random:NormMode=NumEvents:!V")
# Define model
model = Sequential()
model.add(Dense(12, activation="relu", input dim=len(variables)))
model.add(Dense(12, activation="relu"))
model.add(Dense(12, activation="relu"))
model.add(Dense(2, activation="sigmoid"))
 Set loss and optimizer
model.compile(loss="binary crossentropy",
           optimizer="adam", metrics=["accuracy", ], weighted_metrics=[])
 Store model to file
model path = os.path.join(dir name, "DNNmodel.h5")
model.save(model path)
model.summary()
                                                                                              cos theta2 (Deco Gauss)
```



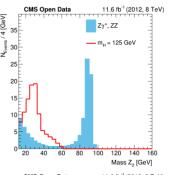


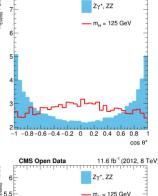
11.6 fb⁻¹ (2012, 8 TeV)



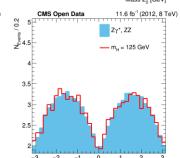
Zγ*, ZZ

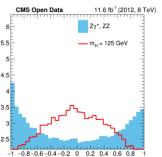
- m_H = 125 GeV

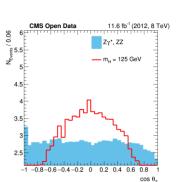




CMS Open Data



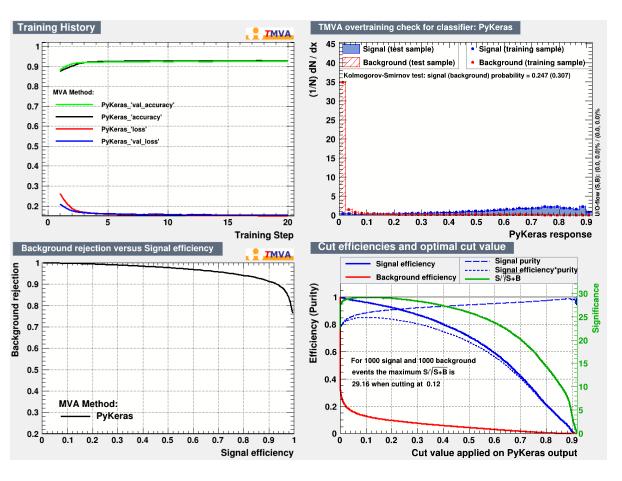






DNN training

ml_training.py



ml_evaluation.py

ml_selection.py



Histograms e plots

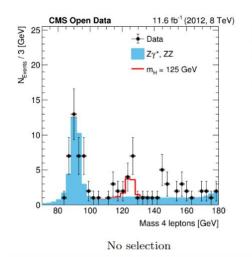
make_histo.py

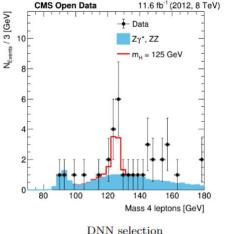
plotting_functions.py

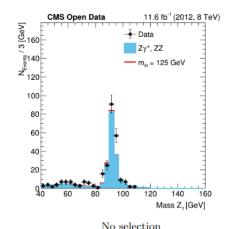
```
def combine_final_states(dict_comb):
    dict_comb["Combined"] = dict_comb["FourMuons"].Clone()
    dict_comb["Combined"].Add(dict_comb["FourElectrons"])
    dict_comb["Combined"].Add(dict_comb["TwoMuonsTwoElectrons"])
```

histogramming_functions.py

```
def write_histogram(histo, name):
    histo.SetName(name)
    histo.Write()
```







CMS Open Data 11.6 fb⁻¹ (2012, 8 TeV)

Data

Zy*, ZZ

m_H = 125 GeV

20

40

20

40

40

Mass Z₂ [GeV]

No selection

```
make_plot.py
```

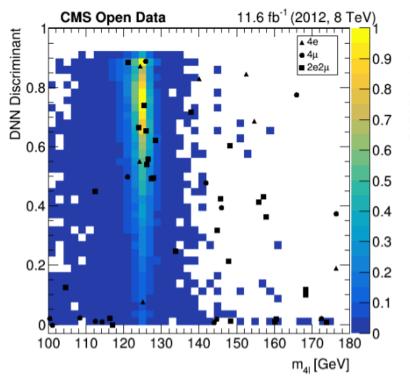


Higgs mass VS DNN Discriminant

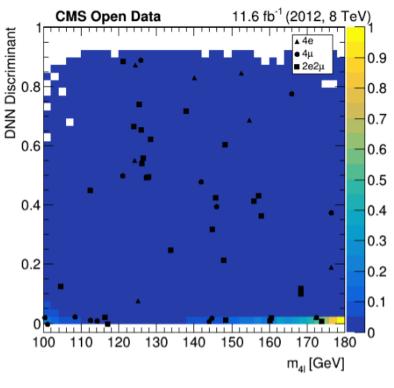
ml_histo.py

ml_plot.py

```
canvas = ROOT.TCanvas("", "", 600, 600)
legend = ROOT.TLegend(0.75, 0.8, 0.85, 0.9)
    plotting_functions.add_title(histos[type_dataset])
    histos[type dataset].Scale(1/histos[type dataset].GetMaximum())
   histos[type_dataset].Draw("COLZ")
    logger.debug("ERROR: Failed to create the %s histogram",
                            type dataset, stack info=True)
   continue
   histos["data_el"].Draw("SAME P")
    logger.debug("ERROR: Failed to create the data histogram of the FourElectrons final state in the %s TH2D",
                            type dataset, stack info=True)
   histos["data mu"].Draw("SAME P")
    logger.debug("ERROR: Failed to create the data histogram of the FourMuons final state in the %s TH2D",
                            type dataset, stack info=True)
   histos["data elmu"].Draw("SAME P")
    logger.debug("ERROR: Failed to create the data histogram of the TwoMuonsTwoElectrons final state in the %s TH2D
```



Distribution for the signal



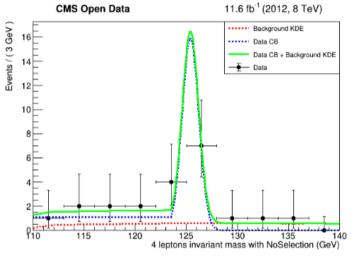
Distribution for the background



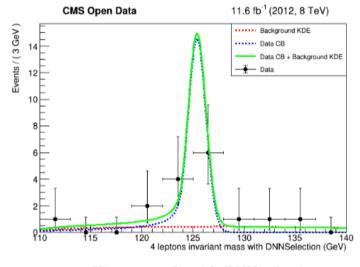
Higgs mass fit

fit_mass.py

```
m41 = ROOT.RooRealVar("Higgs_mass",f"4 leptons invariant mass with {selection}", 110, 140, "GeV")
weight = ROOT.RooRealVar("Weight", "Weight", 0, 1, "GeV")
sig = ROOT.RooDataSet("signal", "", sig_chain, ROOT.RooArgSet(m41, weight) )
bkg = ROOT.RooDataSet("background", "", bkg_chain, ROOT.RooArgSet(m41, weight) )
data = ROOT.RooDataSet("data", "", data_chain, ROOT.RooArgSet(m41, weight) )
sig_frac_count = sig.sumEntries()/(sig.sumEntries()+bkg.sumEntries())
bkg_frac_count = bkg.sumEntries()/(sig.sumEntries()+bkg.sumEntries())
 # KDE for background. In this configuration the input data
bkg_kde = ROOT.RooKeysPdf("bkg_kde", "bkg_kde", m41, bkg, ROOT.RooKeysPdf.MirrorRight)
meanHiggs_sig = ROOT.RooRealVar("meanHiggs_sig", "The mean of the Higgs CB for the signal", 125, 115, 135, "GeV")
sigmaHiggs = ROOT.RooRealVar("sigmaHiggs", "The width of Higgs CB", 5, 0., 20, "GeV")
alphaHiggs = ROOT.RooRealVar("alphaHiggs", "The tail of Higgs CB", 1.5, -5, 5)
nHiggs = ROOT.RooRealVar("nHiggs", "The normalization of Higgs CB", 1.5, 0, 10)
CBHiggs_sig = ROOT.RooCBShape("CBHiggs_sig", "The Higgs Crystall Ball for the signal",
                                m4l, meanHiggs_sig, sigmaHiggs, alphaHiggs, nHiggs)
 # Unbinned ML fit to signal
fitHiggs = CBHiggs sig.fitTo(sig, ROOT.RooFit.Save(True), ROOT.RooFit.AsymptoticError(True))
fitHiggs.Print("v")
meanHiggs_data = ROOT.RooRealVar("m_{H}", "The mean of the Higgs CB for the data", 125, 115, 135, "GeV")
CBHiggs_data = ROOT.RooCBShape("CBHiggs_data", "The Higgs Crystall Ball for the data",
                                m4l, meanHiggs_data, sigmaHiggs, alphaHiggs, nHiggs)
 sig_frac= ROOT.RooRealVar("sigfrac", "signal fraction", sig_frac_count)
bkg_frac= ROOT.RooRealVar("bkg_coeff", "bkg fraction", bkg_frac_count)
totPDF = ROOT.RooAddPdf("totPDF", "Higgs data+bkg", ROOT.RooArgList(CBHiggs data, bkg kde), ROOT.RooArgList(sig frac,bkg frac)
fitdata = totPDF.fitTo(data, ROOT.RooFit.Save(True))
```



Higgs mass fit without DNN selection



Higgs mass fit with DNN selection

| | Without DNN selection | With DNN selection |
|----------------------------|-----------------------|---------------------|
| Higgs mass from MC [GeV] | 124.934 ± 0.016 | 124.938 ± 0.015 |
| Higgs mass from data [GeV] | 125.40 ± 0.26 | 125.39 ± 0.30 |

