



UNIVERSITÀ DI PISA

# Regularizing Transformers By Symbolic Knowledge and Deep Graph Networks

Master's Degree in Computer Science

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# OUTLINE

- High Level Overview
- Language Models
- Knowledge Graphs
- KB Graph Attention Network
- Map Words to Node Embeddings
- Masked Language Modeling Regularization Term
- Experiments
- Results

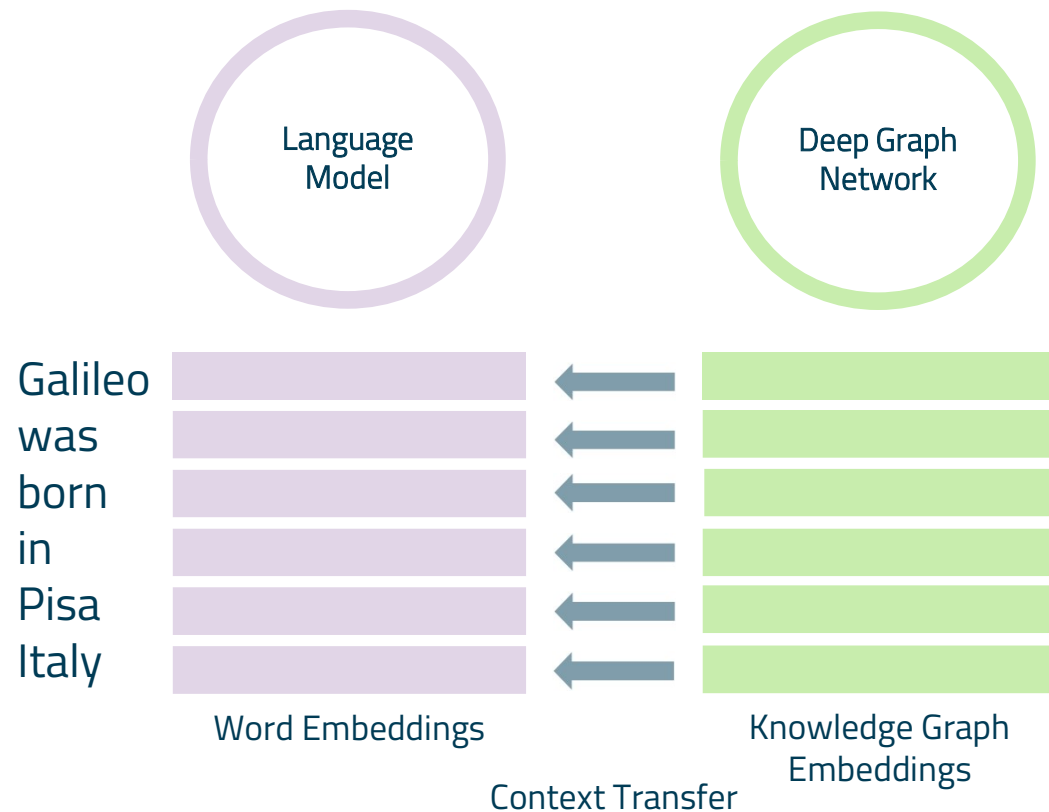


# HIGH LEVEL OVERVIEW

## CORPUS

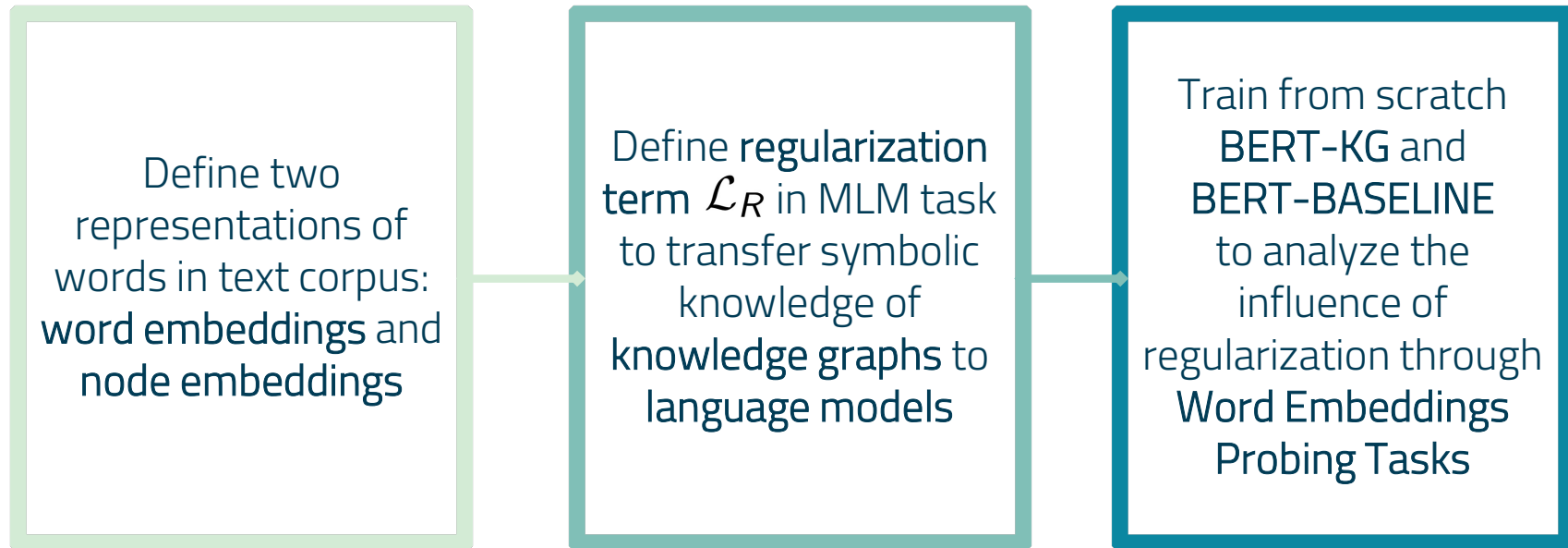
Galileo was born in Pisa, Italy, on 15 February 1564, the first of six children of Vincenzo Galilei, a lutenist, composer, and music theorist, and Giulia Ammannati, who had married in 1562. Galileo studied speed and velocity, gravity and free fall, the principle of relativity, inertia, projectile motion and also worked in applied science and technology, describing the properties of pendulums and "hydrostatic balances". He invented the thermoscope and various military compasses, and used the telescope for scientific observations of celestial objects. His contributions to observational astronomy include telescopic confirmation of the phases of Venus, observation of the four largest satellites of Jupiter, observation of Saturn's rings, and analysis of lunar craters and sunspots.

## "Galileo was born in Pisa, Italy"



# HIGH LEVEL OVERVIEW

## CHALLENGES



# HIGH LEVEL OVERVIEW

## THESIS CONTRIBUTION

### **DGN in Natural Language Processing**

- VGAE (*Kipf and Welling, 2016*)
- Text-GCN (*Yao et al, 2018*)
- VGCN-BERT (*Lu et al, 2020*)

### **Fine Tuning Approaches**



### **Proposed Framework**

Masked Language Modeling from Scratch

### **Adapts Different Embedding Spaces**

- ALC Embedding (*Khodak et al, 2018*)
- DMN Embedding (*Ni et al, 2018*)

### **Context Transfer on Same Embedding Types**



### **Proposed Framework**

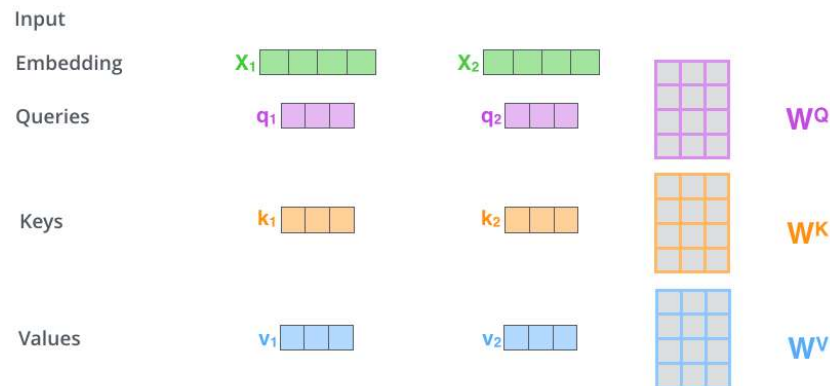
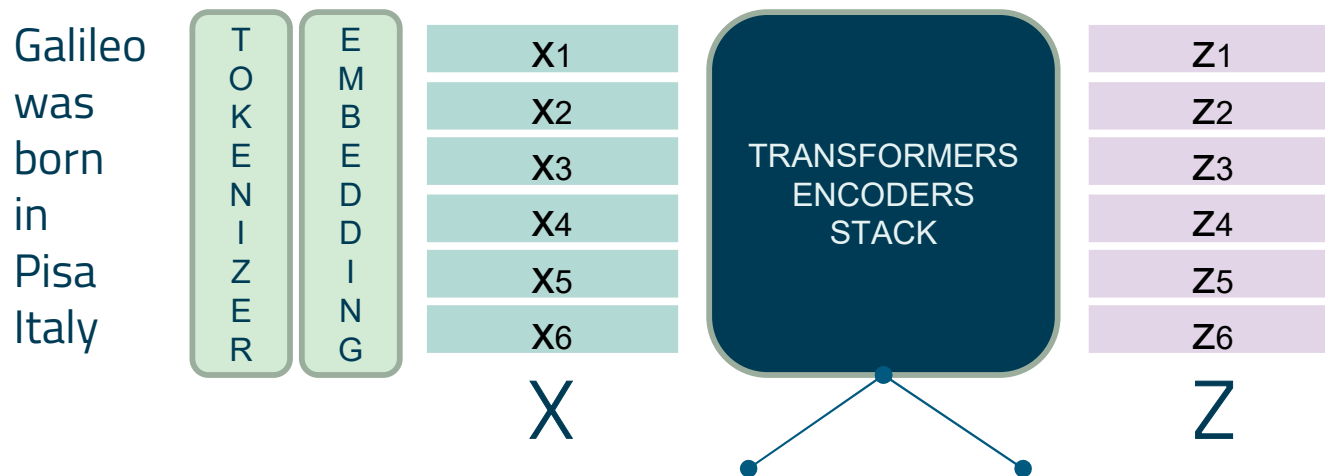
Context Transfer from  
Node Embeddings to Word Embeddings

# LANGUAGE MODELS

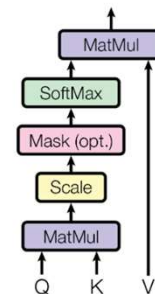


# BERT

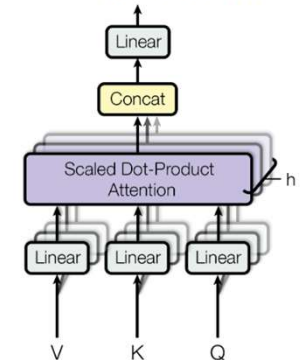
Bidirectional Encoder Representations from Transformers (*Devlin et al, 2018*)



Scaled Dot-Product Attention

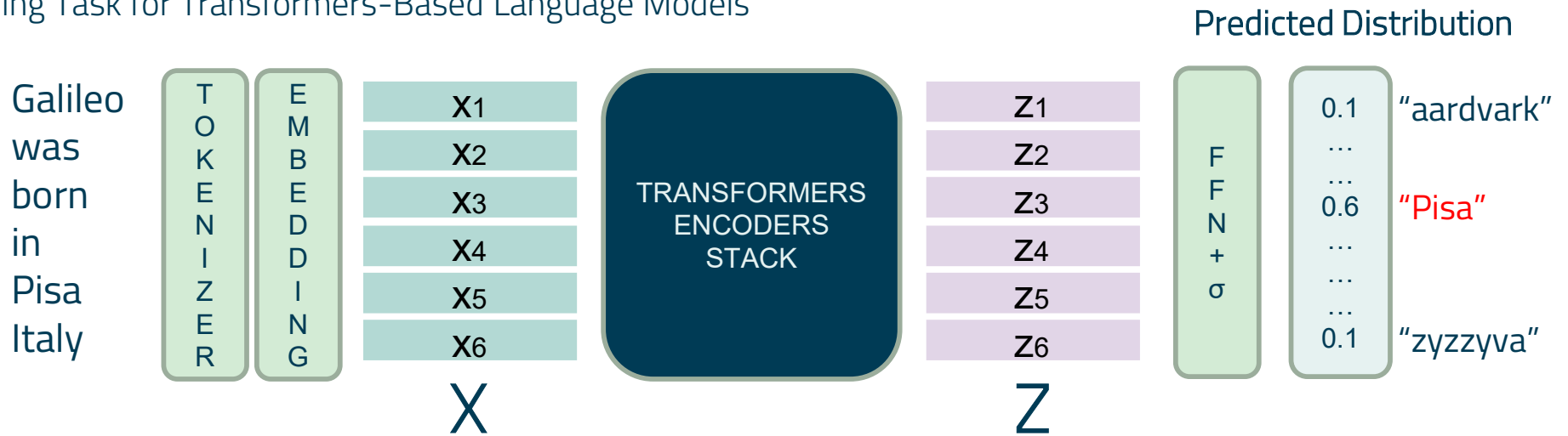


Multi-Head Attention



# MASKED LANGUAGE MODELING

Training Task for Transformers-Based Language Models



## Training Objective

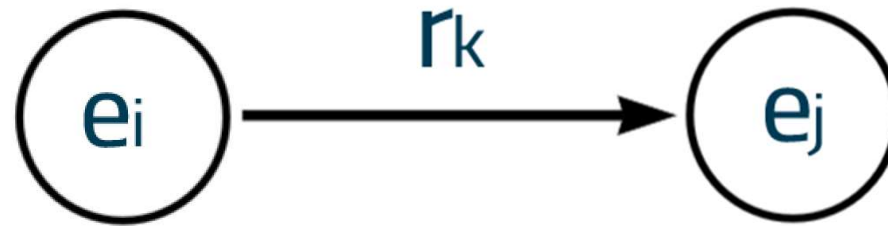
$$\mathcal{L}_{\text{MLM}}(\mathbf{X}_{\Pi} \mid \mathbf{X}_{-\Pi}, \theta) = \frac{1}{K} \sum_{k=1}^K \log p(\mathbf{x}_{\pi_k} \mid \mathbf{X}_{-\Pi}; \theta)$$



# KNOWLEDGE GRAPHS



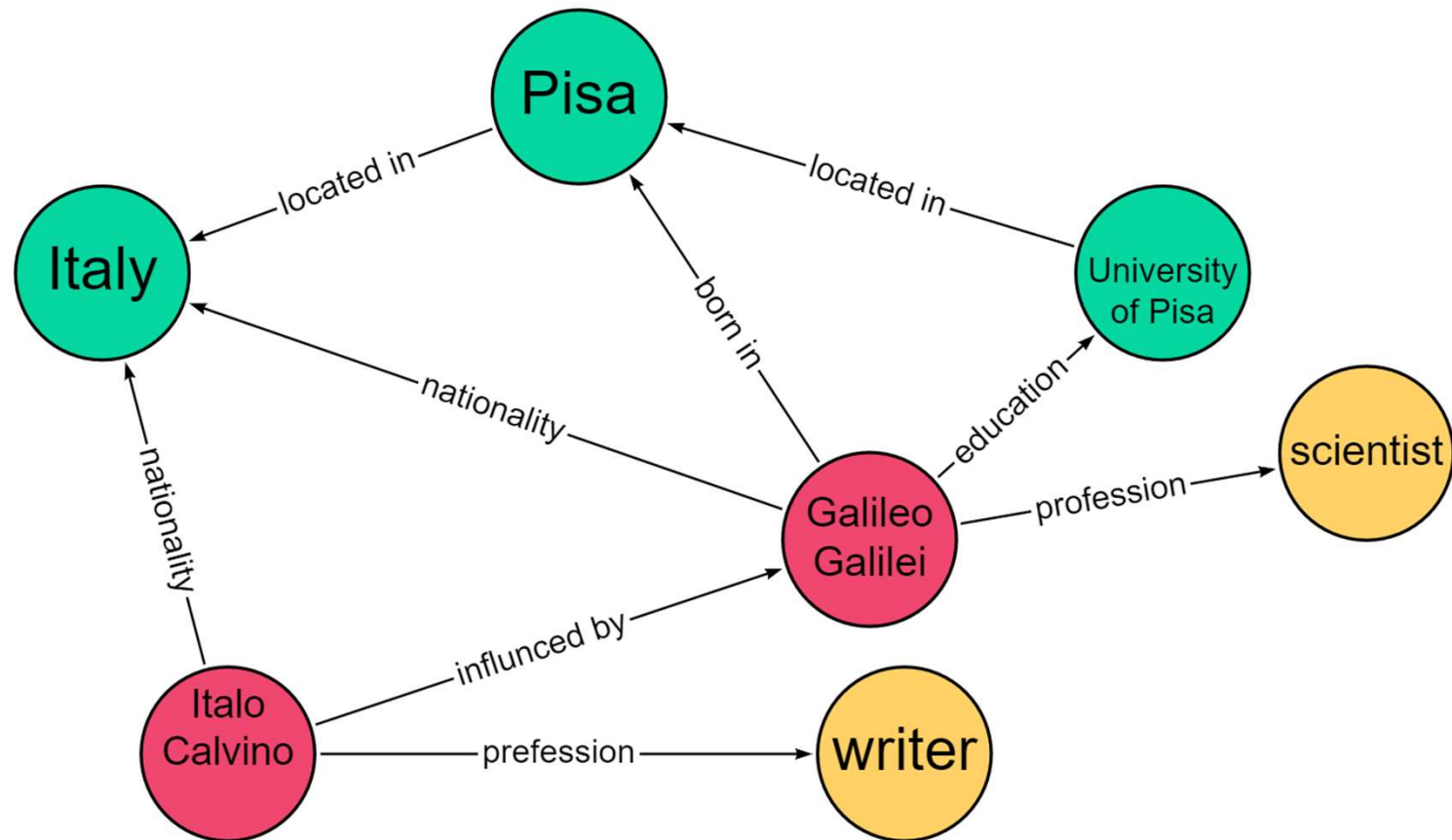
# RDF GRAPHS



## RDF TRIPLE

- Subject  $e_i$
- Predicate  $r_k$
- Object  $e_j$
- Entities:  $e_i, e_j$
- Relationships:  $r_k$
- Facts and Concepts:  $(e_i, r_k, e_j)$
- Ontology with Domain  $D$

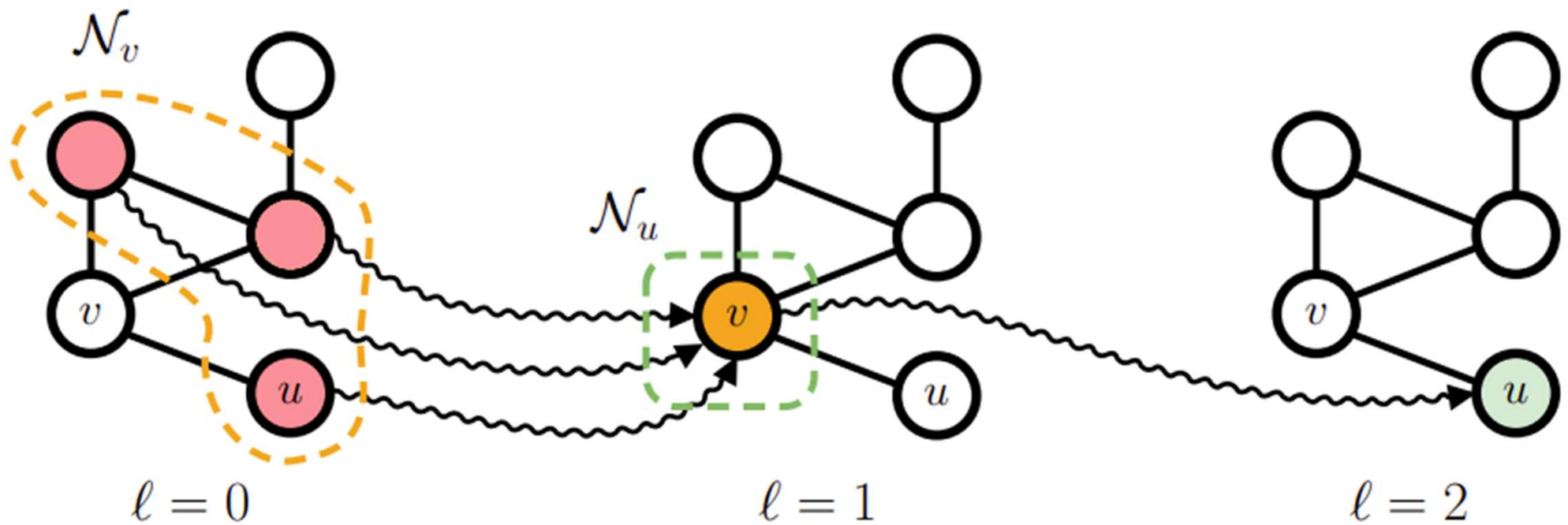
# KNOWLEDGE GRAPH



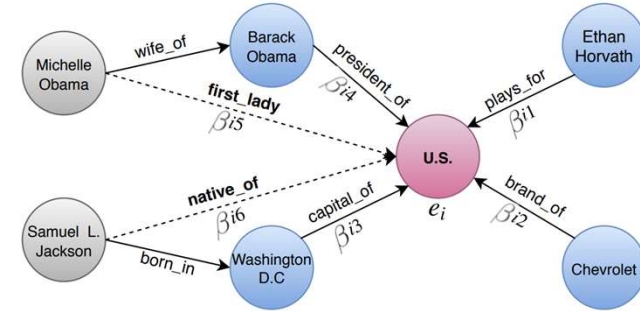
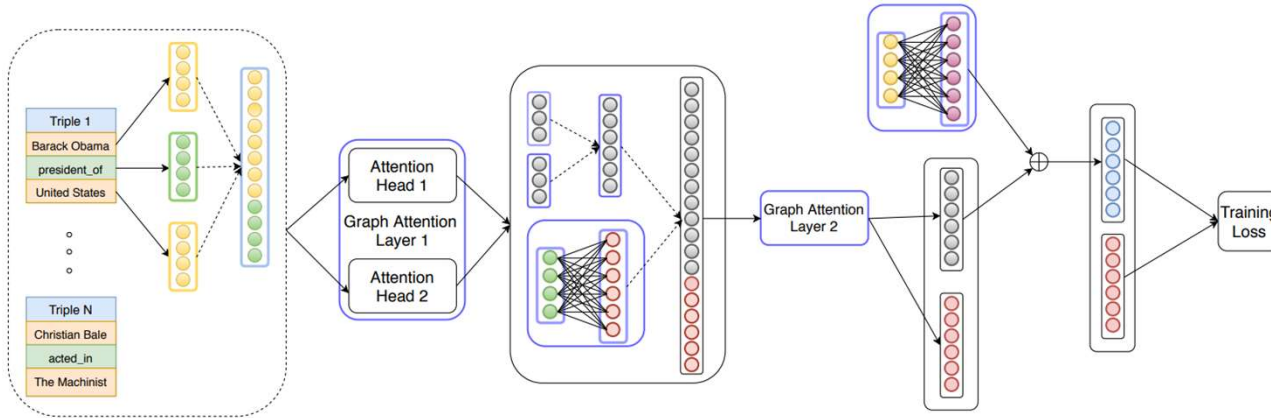
# DEEP GRAPH NETWORKS



# MESSAGE PASSING



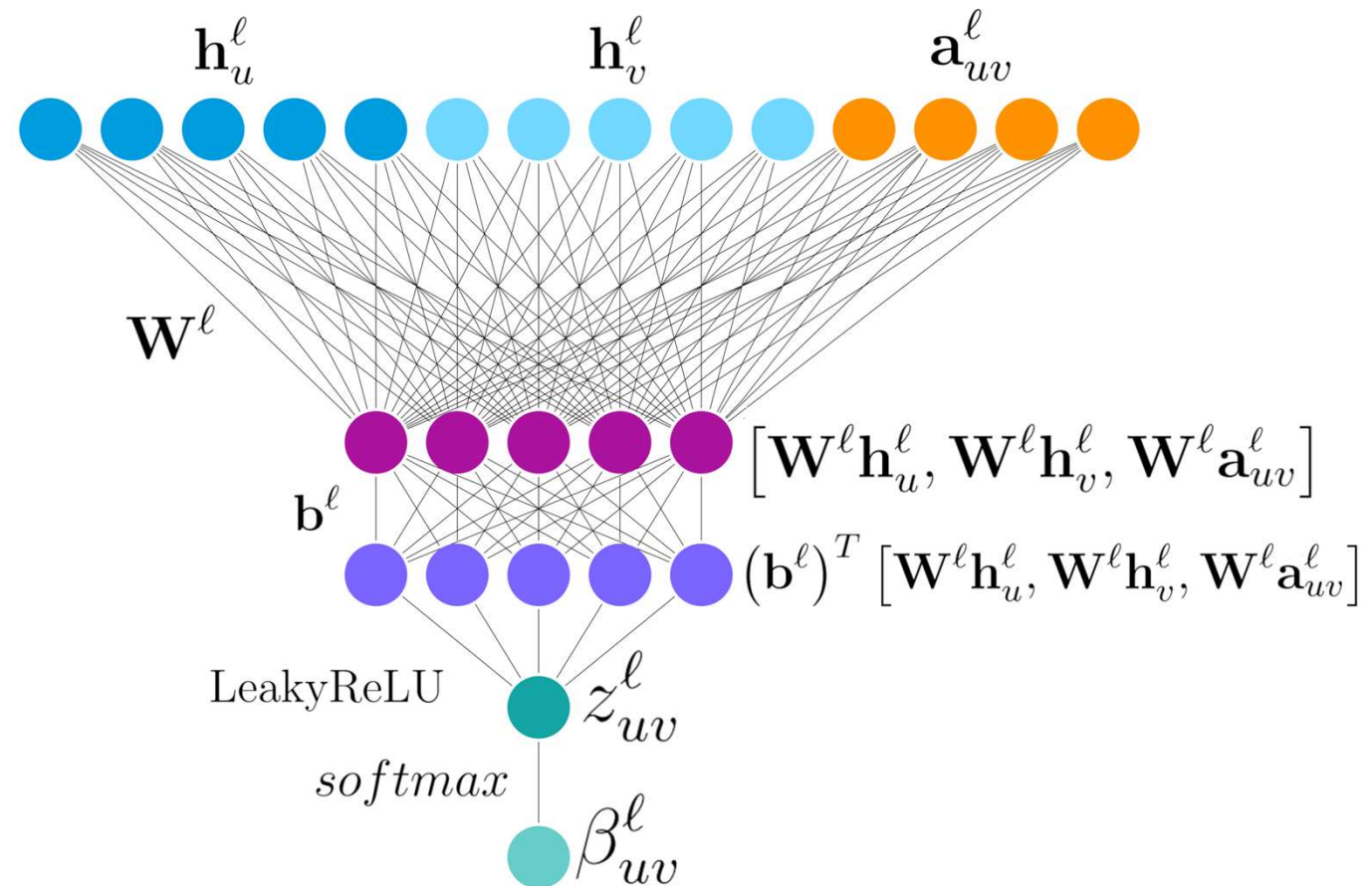
# KB GRAPH ATTENTION NETWORK



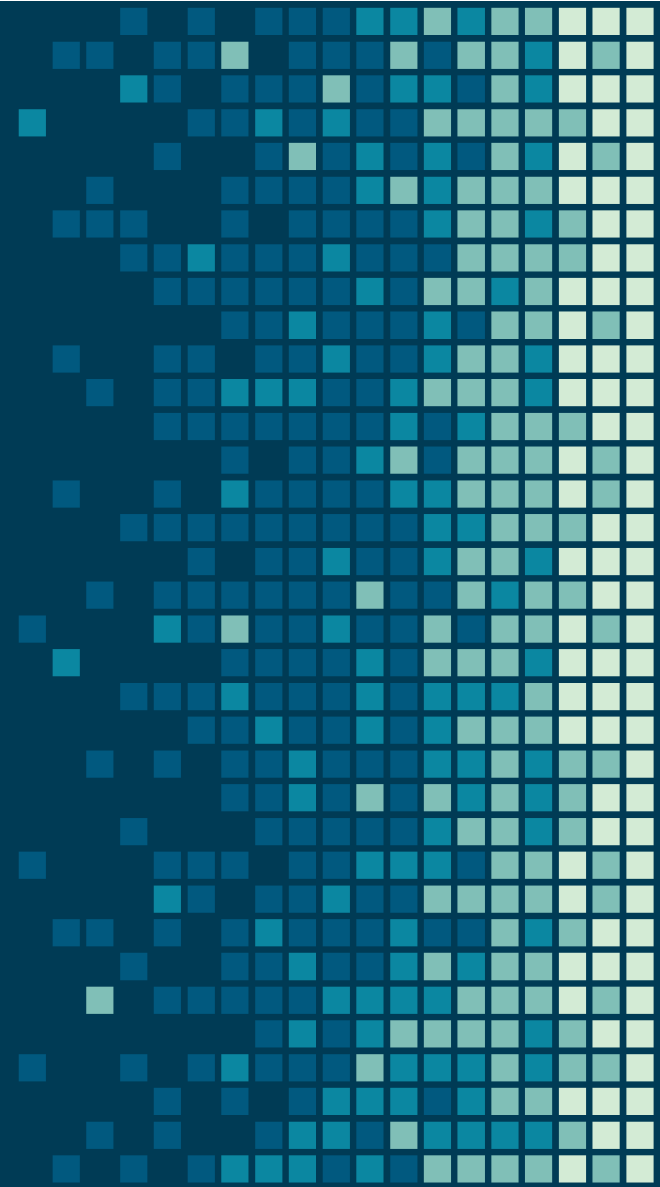
## KBGAT Neighborhood Aggregation Rule

$$\mathbf{h}_v^{\ell+1} = \sigma \left( \sum_{u \in \mathcal{N}_v} \beta_{uv}^{\ell+1} * [\mathbf{W}^{\ell+1} \mathbf{h}_u^{\ell}, \mathbf{W}^{\ell+1} \mathbf{h}_v^{\ell}, \mathbf{W}^{\ell+1} \mathbf{a}_{uv}^{\ell}] \right)$$

# GRAPH ATTENTION LAYER



# MAP WORDS TO NODE EMBEDDINGS

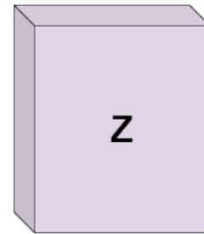
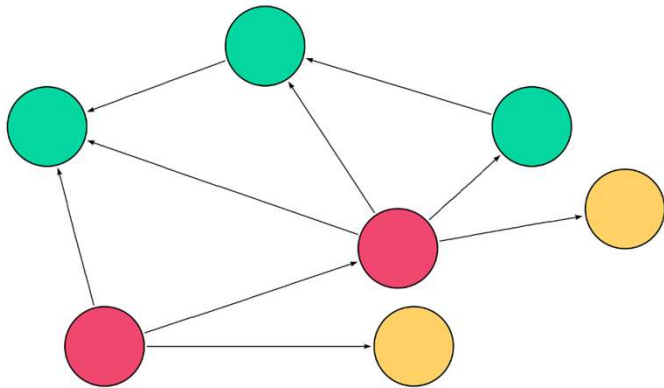




# KGE SENTENCE DICTIONARY

$$\mathcal{D}_{\mathbf{w}}[k \rightarrow v](w_i) = \begin{cases} \mathbf{h}_{\phi(\mathbf{w}, w_i)} & \text{for } w_i = k \\ \mathbf{h}_{\text{none}} & \text{otherwise} \end{cases}$$

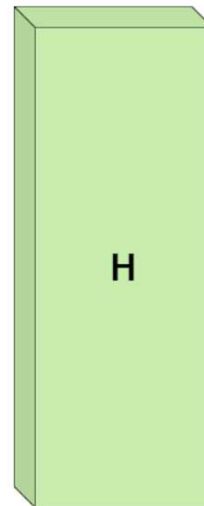
"Galileo was born in Pisa, Italy"



Sentence WE

$$\phi : \mathcal{D}_{LM} \rightarrow \mathcal{V}$$

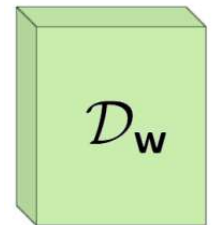
$$\phi(\mathbf{w}, w_i) = i$$



All KGE

$\mathbf{w}$

$\phi$



Sentence KGE

# WORD SENSE DISAMBIGUATION

$\phi : \mathcal{D}_{LM} \rightarrow \mathcal{V}$  as **WSD Problem**

"The **bank** will not be accepting cash on Saturday"

"The river overflowed the **bank**"

Maximize the similarity function  $\psi$  between the candidate nodes  $\mathcal{S}_i$  for the target word  $w_i$  and candidates nodes  $\mathcal{S}_j$  for all the other nodes in the sentence:

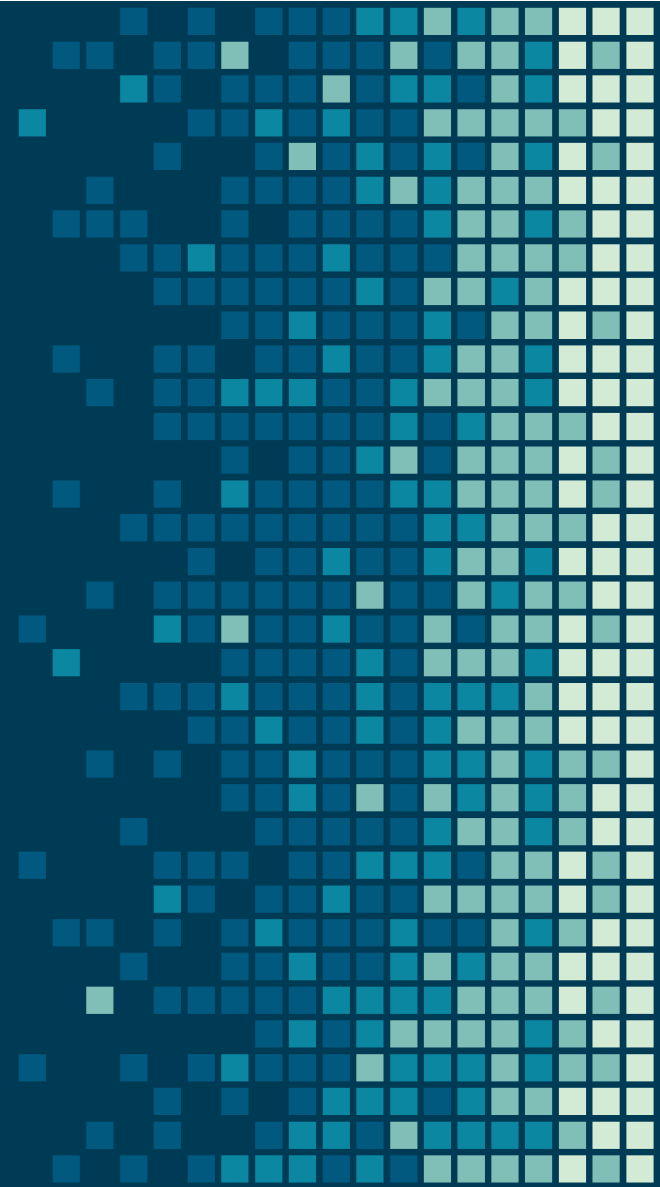
$$\phi(\mathbf{w}, w_i) = \max_{i \in \mathcal{S}_i} \sum_{w_j \in \mathbf{w}} \max_{j \in \mathcal{S}_j} \psi(i, j)$$

**Similarity Function**  $\psi : \mathcal{V} \times \mathcal{V} \rightarrow \mathbb{R}$

**Wu-Palmer similarity**  $\delta_{wup}(i, j) = \frac{2d}{L_i + L_j + 2d}$

**Cosine similarity**

# MLM REGULARIZATION TERM



# REGRESSION FOR CONTEXT TRANSFER

Given the input sentence  $\mathbf{w} = \{w_i\}_{i=0}^N$

- $\mathbf{x}_i = \text{Tokenizer}(w_i)$
- $\mathbf{z}_i = \text{Encoder}(\mathbf{x}_i)$
- $\mathbf{h}_i = \mathcal{D}_{\mathbf{w}}(w_i)$
- $\mathbf{Z}_{\mathbf{w}} = \left[ (\mathbf{z}_1)^T, \dots, (\mathbf{z}_N)^T \right]^T$
- $\mathbf{H}_{\mathbf{w}} = \left[ (\mathcal{D}_{\mathbf{w}}(w_1))^T, \dots, (\mathcal{D}_{\mathbf{w}}(w_N))^T \right]^T = \left[ (\mathbf{h}_1)^T, \dots, (\mathbf{h}_N)^T \right]^T$

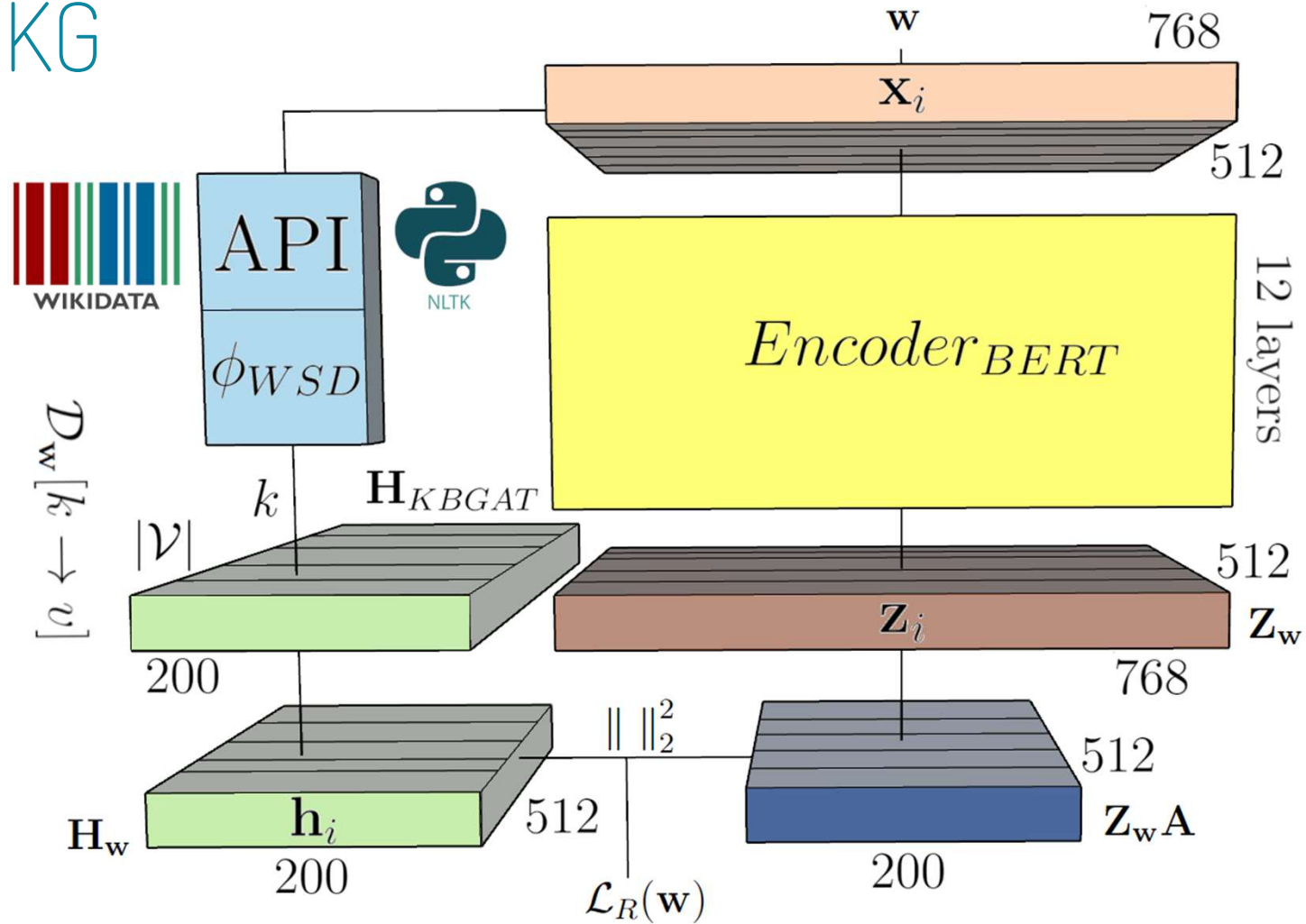
# REGRESSION FOR CONTEXT TRANSFER

- Linear matrix  $\mathbf{A} \in \mathbb{R}^{d_{hidden} \times d_{KGE}}$
- $\mathcal{L}_R(\mathbf{w}) = \sum_{w_i \in \mathbf{w}} \|\mathbf{h}_i - \mathbf{z}_i \mathbf{A}\|_2^2 = \|\mathbf{H}_w - \mathbf{Z}_w \mathbf{A}\|_2^2$

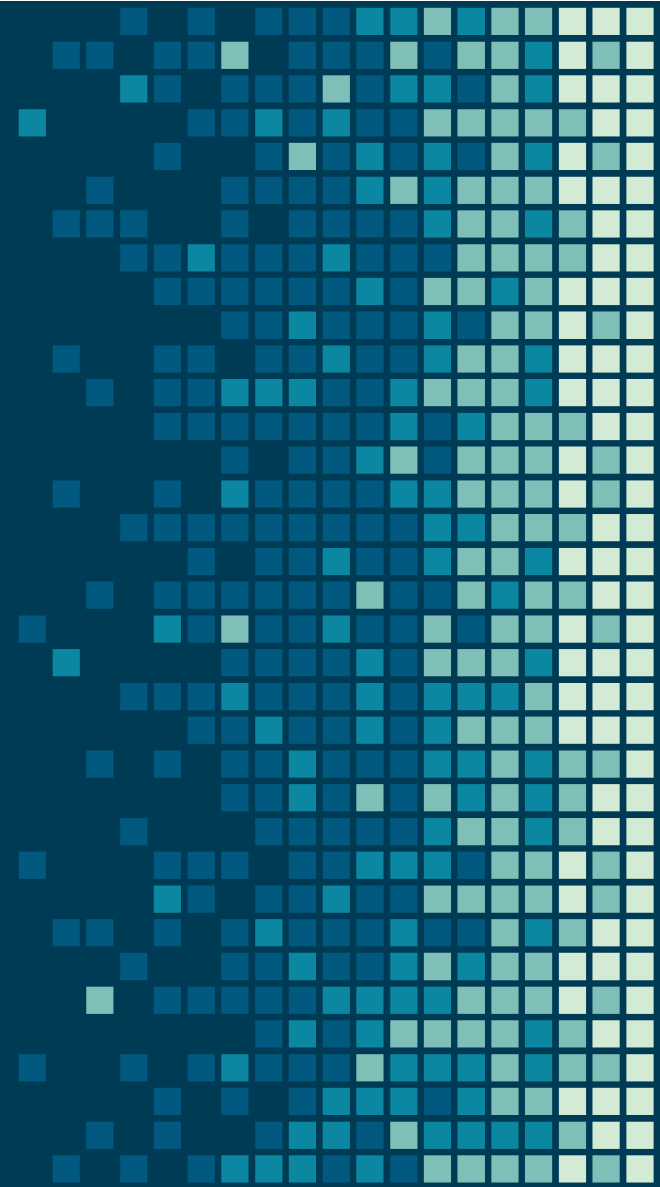
BERT-KG Training Loss:

$$\mathcal{L}_{\text{MLM}}(\mathbf{X}_{\Pi} \mid \mathbf{X}_{-\Pi}, \theta) = \boxed{\frac{1}{K} \sum_{k=1}^K \log p(\mathbf{x}_{\pi_k} \mid \mathbf{X}_{-\Pi}; \theta)} + \boxed{\lambda \mathcal{L}_R(\mathbf{X}_{-\Pi}, \mathbf{H}, \theta)}$$

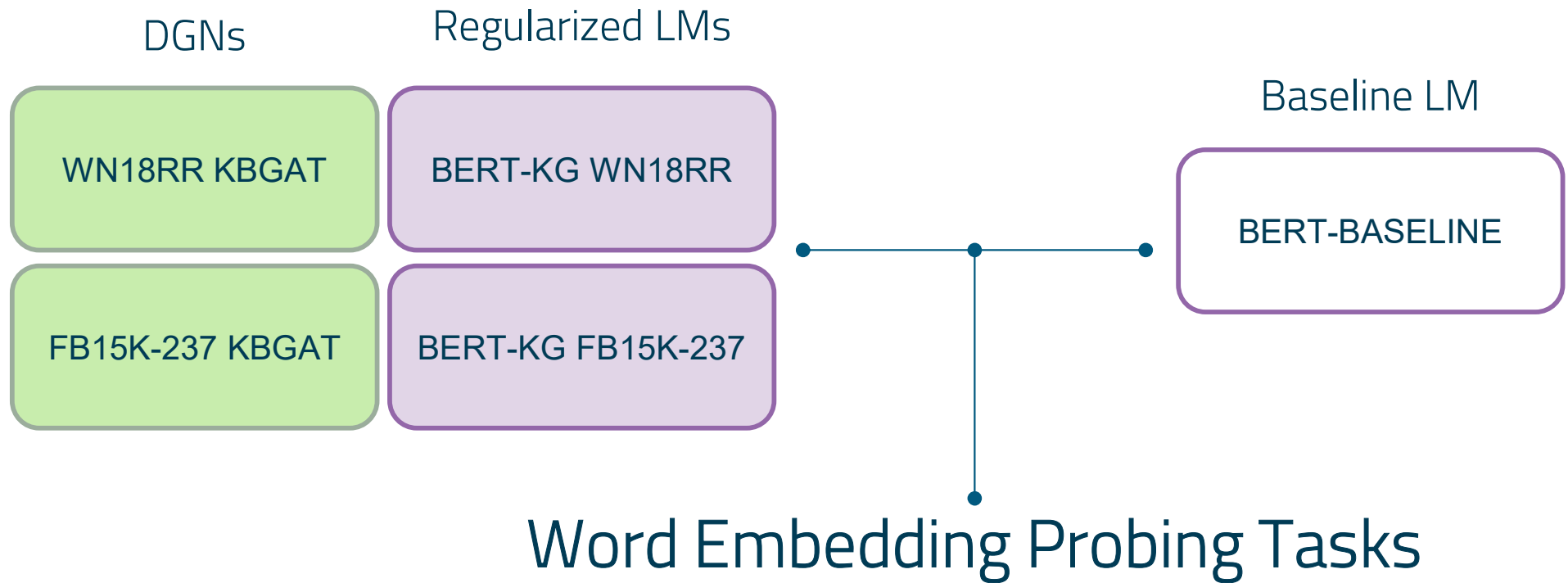
# BERT-KG



# EXPERIMENTS

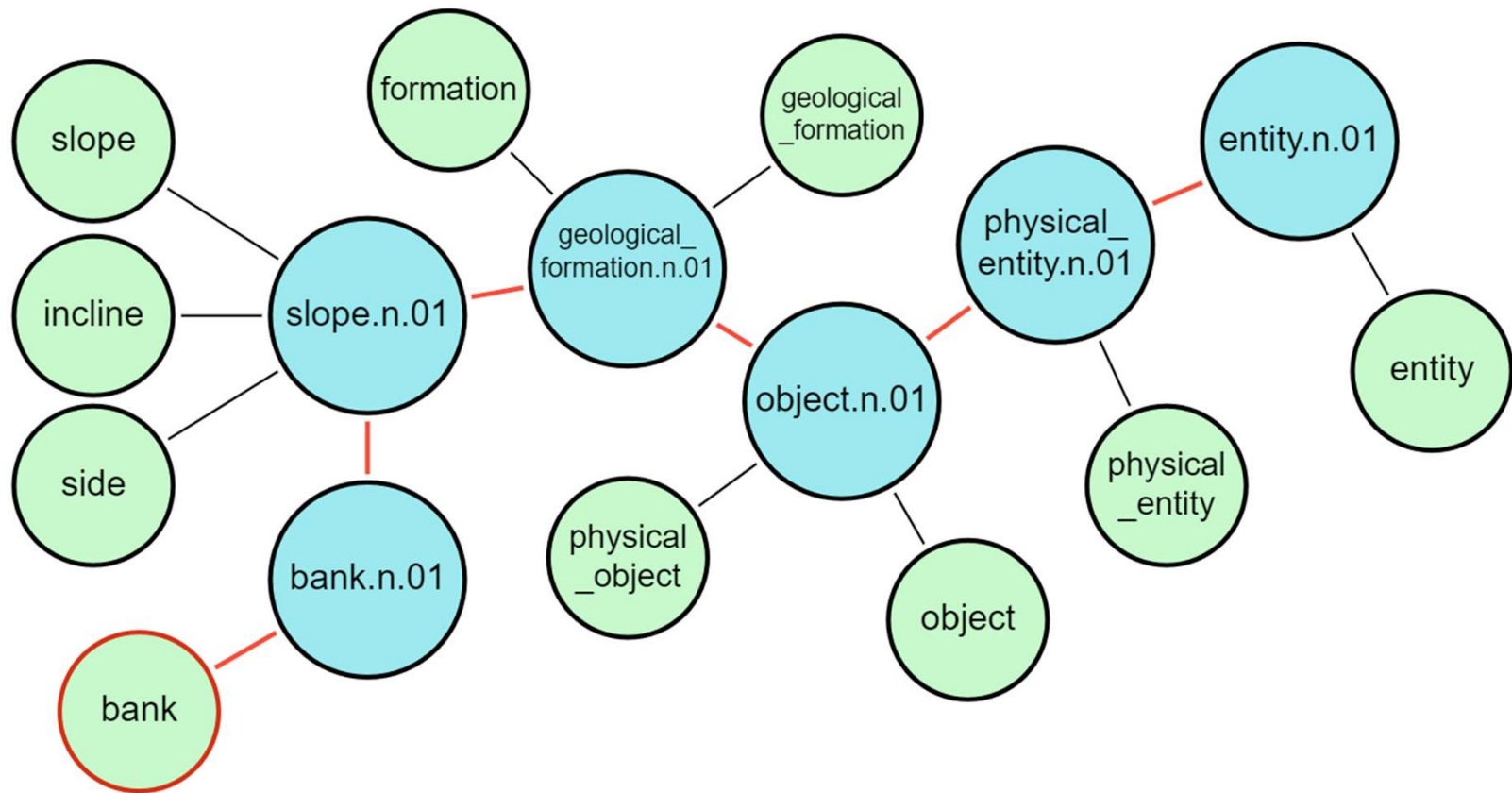


# EXPERIMENTAL SETUP

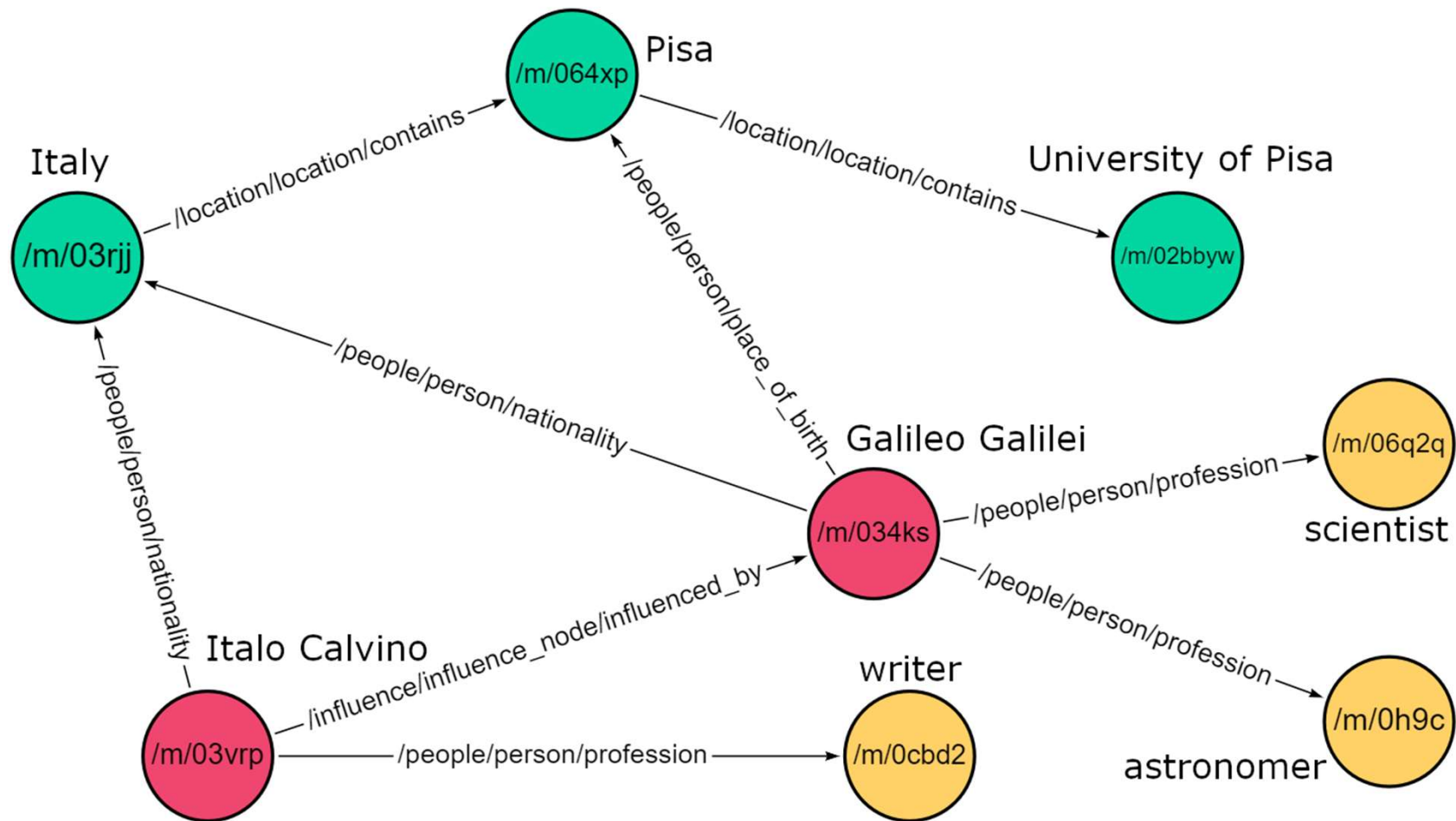




# WN18RR DATASET



# FB15K-237



# WORD SIMILARITY PROBING TASK

MEN Dataset (*Bruni et al, 2014*)  
3000 rows

Word 1	Word 2	Similarity Score
sun	sunlight	50
automobile	car	50
river	water	49
stair	staircase	49
morning	sunrise	49
feather	truck	1
festival	whisker	1
muscle	tulip	1
bikini	pizza	1
bakery	zebra	0

Regression Task to predict Word Embedding Similarity

- k-Fold Cross Validation  $k = \{10, 20, 50, 100\}$

- Metrics:

$$\text{MSE}(\mathbf{y}, \hat{\mathbf{y}}) = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$R^2(\mathbf{y}, \hat{\mathbf{y}}) = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$$

$$\rho(\mathbf{y}, \hat{\mathbf{y}}) = 1 - \frac{6 \sum_{i=1}^n (y_i - \hat{y}_i)^2}{n(n^2 - 1)}$$

# KB COMPLETION PROBING TASK

SQuAD Dataset (*Rajpurkar et al. 2016*)

Q: "Who developed the theory of relativity?"  
A: "The theory of relativity was developed by [MASK]"  
GT: "Albert Einstein"

Q: "Where was Galileo Galilei born?"  
A: "Galileo Galilei was born in [MASK]"  
GT: "Pisa"

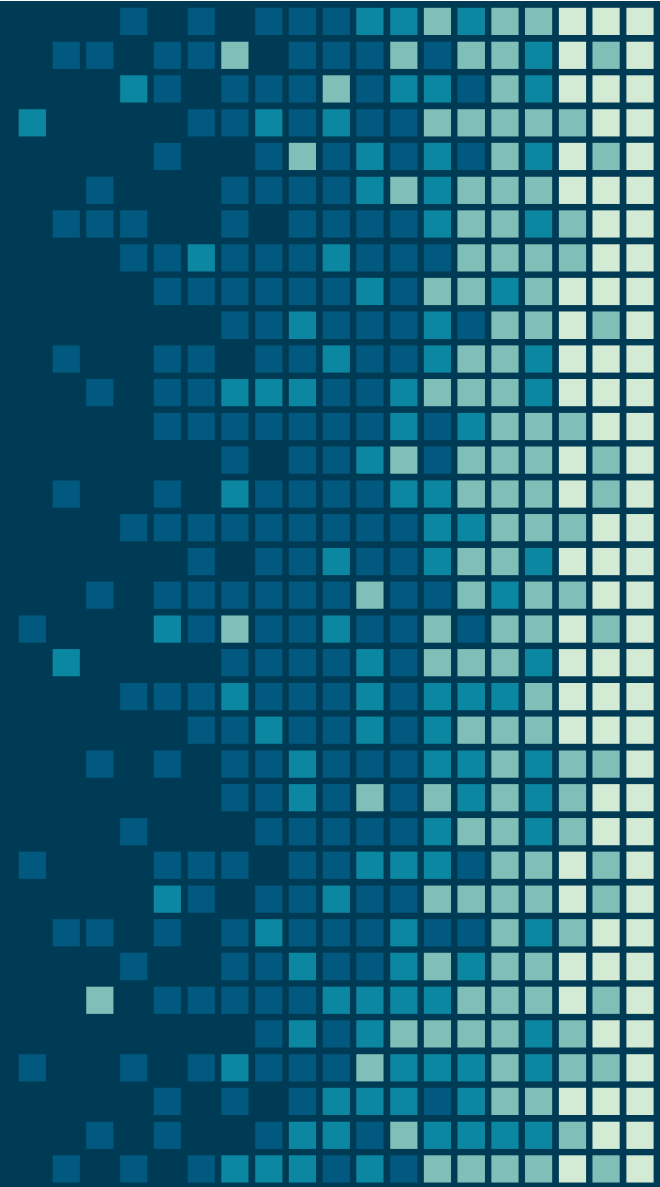
Querying a language model for factual knowledge as cloze test

- LAMA Probe (Petroni et al. 2019):  
305 question-answer rows from SQuAD
- Metrics:

$$MRR = \frac{1}{|Q|} \sum_{i=1}^{|Q|} \frac{1}{\text{rank}(\text{token}_*^i)}$$

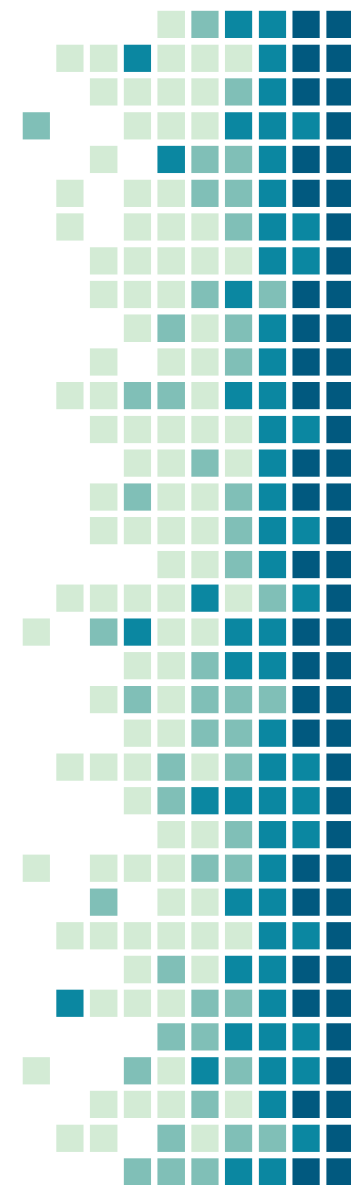
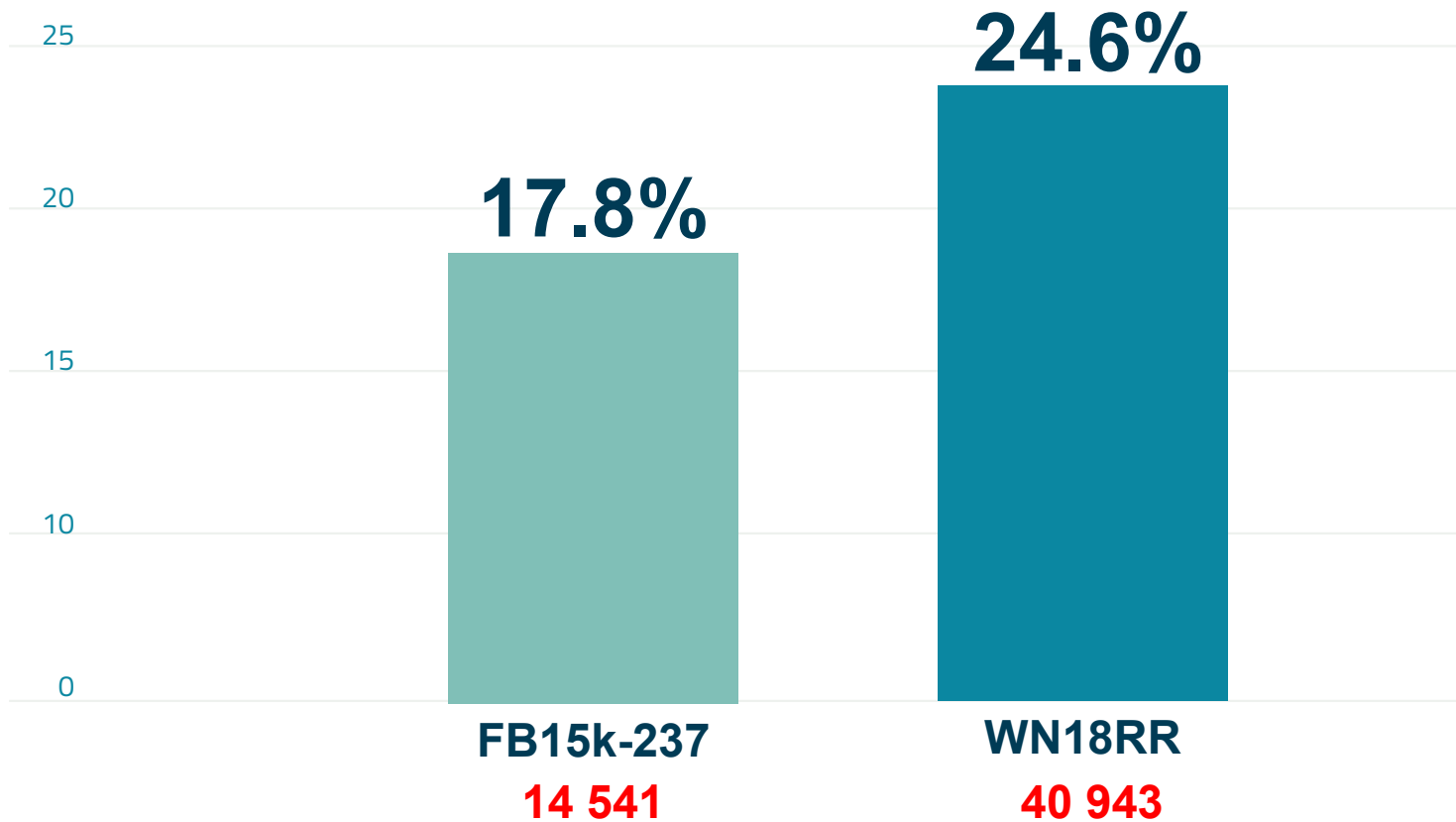
$$P@K = \frac{1}{|Q|} \sum_{i=1}^{|Q|} H(K - \text{rank}(\text{token}_*^i))$$

# RESULTS AND ANALYSIS

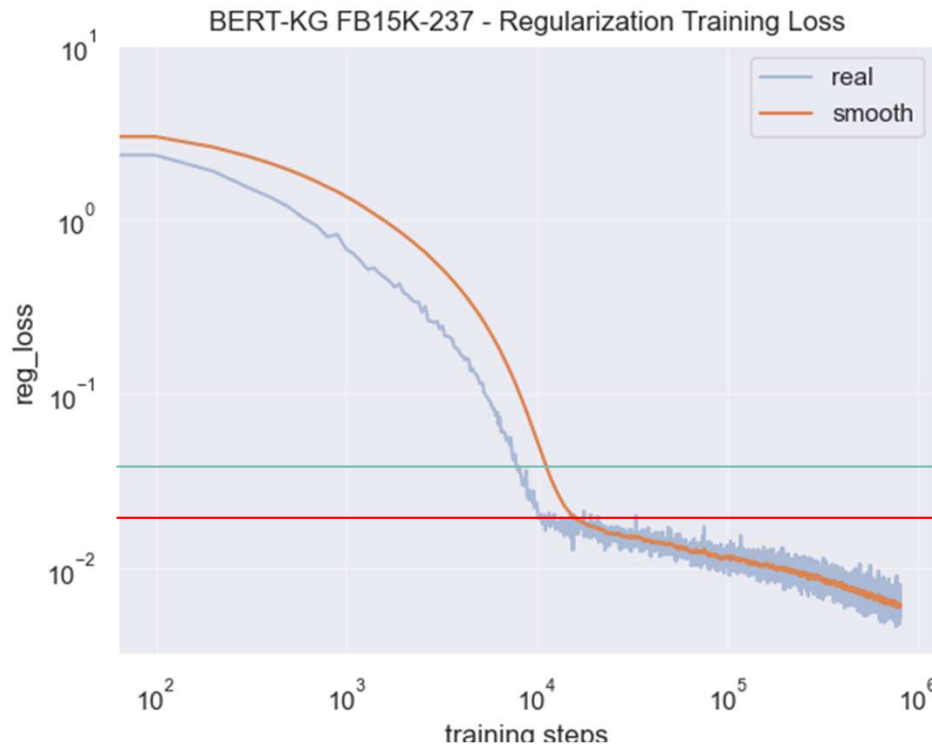


# REGULARIZATION RATIO

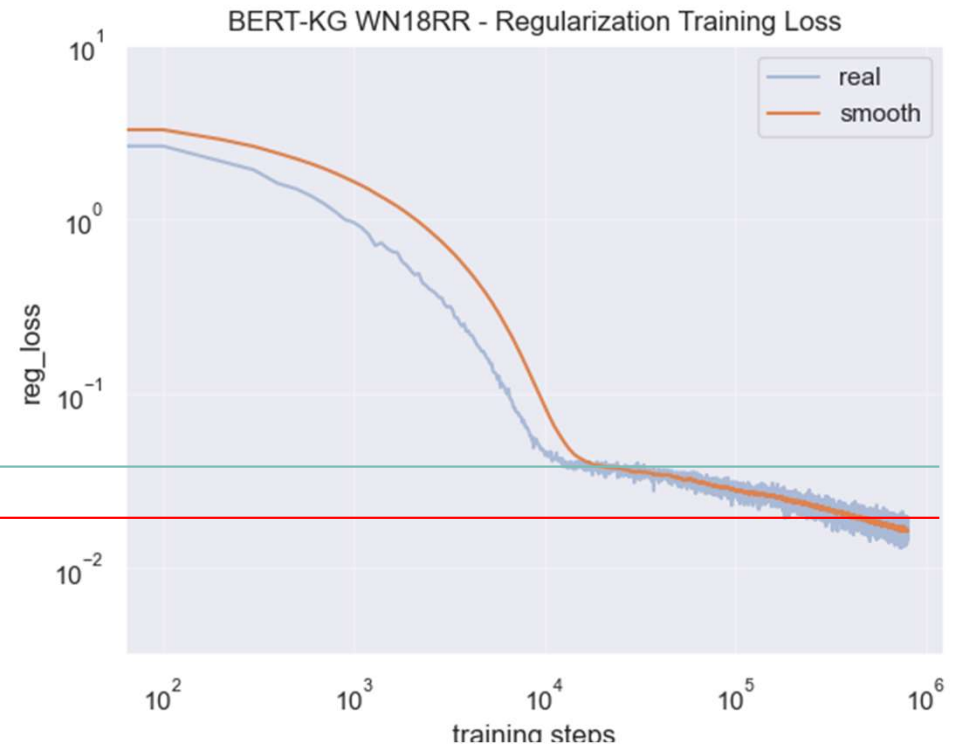
Regularized Tokens / Tot. Input Tokens



# LMs REGULAIZATION LOSS

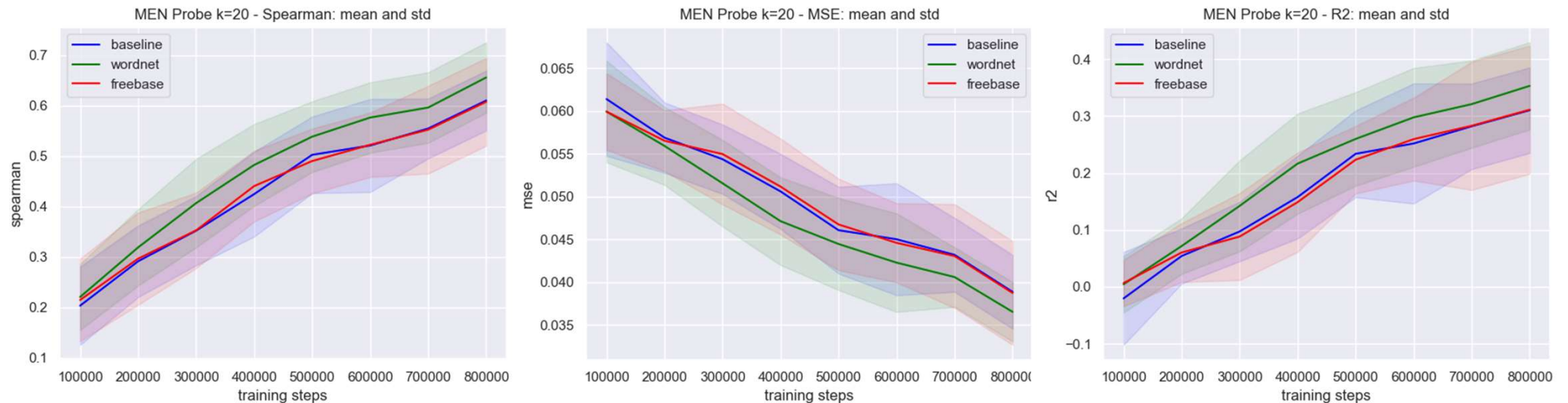


**FB15k-237**



**WN18RR**

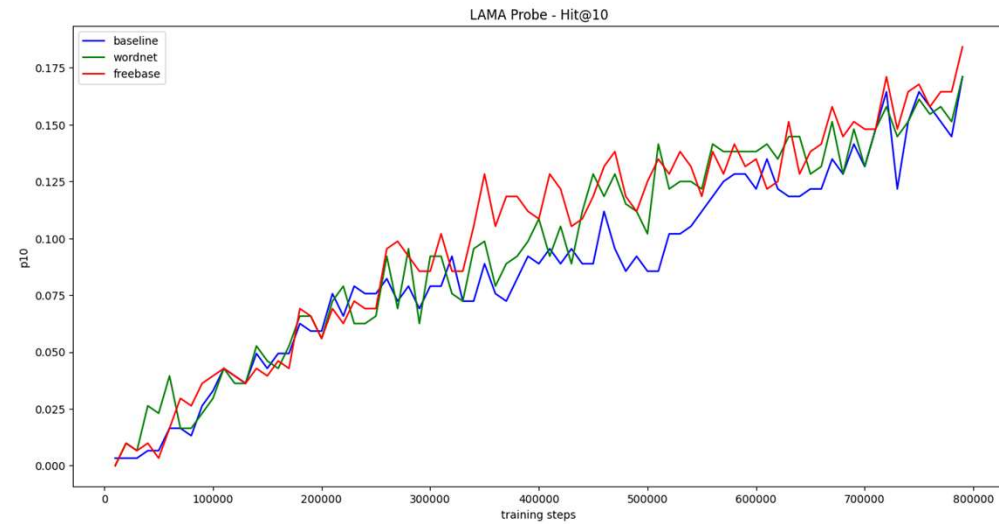
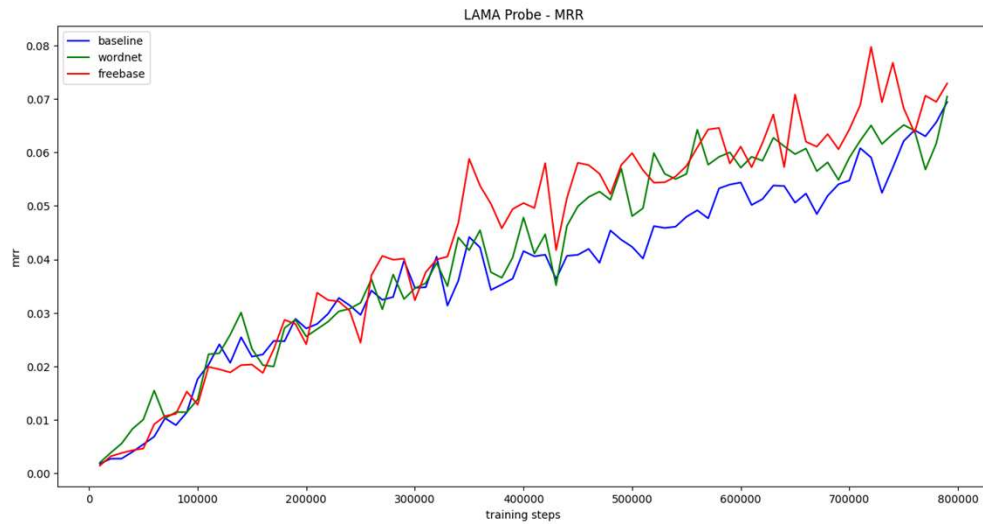
# WORD SIMILARITY



Model	MSE		R2		$\rho$	
	mean	std	mean	std	mean	std
20-fold 800k						
BERT-BASELINE	0.039	0.004	0.305	0.075	0.601	0.059
BERT-KG WN18RR	<b>0.036</b>	0.003	<b>0.362</b>	0.076	<b>0.652</b>	0.069
BERT-KG FB15K-237	0.039	0.006	0.311	0.112	0.614	0.087
bert-base-uncased	0.017	0.003	0.714	0.079	0.854	0.034



# KB COMPLETION



Model	MRR	P@10
BERT-BASELINE	0.070	0.172
BERT-KG WN18RR	0.071	0.174
BERT-KG FB15K-237	<b>0.074</b>	<b>0.184</b>
bert-base-uncased	0.47	0.25

# CONCLUSIONS

1. MLM regularization term was able to transfer part of the symbolic knowledge into the parameters of the BERT language model
2. Graph-driven regularization does not degrade the performance of the language models
3. The regularization approach can be extended to other deep learning models, encoding symbolic knowledge as knowledge graph embeddings and transferring it into multi-domain embeddings
4. The regularization is strongly related to the ontological domain underlying the KG employed in regularization
5. Analyze the influence of KG-regularization on multiple graphs in language modeling
6. Reduce the high number of transformer parameters

THANK YOU FOR YOUR ATTENTION.

Any questions?