$$\begin{cases} \dot{\boldsymbol{u}} = \frac{\boldsymbol{X} + \left(\boldsymbol{m} + \boldsymbol{m}_{\boldsymbol{y}}\right) \boldsymbol{v}_{\boldsymbol{m}} \boldsymbol{r} + \boldsymbol{x}_{\boldsymbol{G}} \boldsymbol{m} \boldsymbol{r}^2}{(\boldsymbol{m} + \boldsymbol{m}_{\boldsymbol{x}})} \\ \dot{\boldsymbol{v}}_{\boldsymbol{m}} = \frac{\boldsymbol{Y} - (\boldsymbol{m} + \boldsymbol{m}_{\boldsymbol{x}}) \boldsymbol{u} \boldsymbol{r} - \boldsymbol{x}_{\boldsymbol{G}} \boldsymbol{m} \dot{\boldsymbol{r}}}{(\boldsymbol{m} + \boldsymbol{m}_{\boldsymbol{y}})} \\ \dot{\boldsymbol{r}} = \frac{N_{\boldsymbol{m}} - \boldsymbol{x}_{\boldsymbol{G}} \boldsymbol{m} (\dot{\boldsymbol{v}}_{\boldsymbol{m}} + \boldsymbol{u} \boldsymbol{r})}{(I_{\boldsymbol{Z}\boldsymbol{G}} + \boldsymbol{x}_{\boldsymbol{G}}^2 \boldsymbol{m} + J_{\boldsymbol{Z}})} \\ \dot{\boldsymbol{\psi}} = \boldsymbol{r} \\ \dot{\boldsymbol{x}} = \boldsymbol{u} \cos \boldsymbol{\psi} - \boldsymbol{v}_{\boldsymbol{m}} \sin \boldsymbol{\psi} \\ \dot{\boldsymbol{y}} = \boldsymbol{v}_{\boldsymbol{m}} \cos \boldsymbol{\psi} + \boldsymbol{u} \sin \boldsymbol{\psi} \end{cases}$$

$$\begin{cases} X = X_H + X_R + X_P \\ X_H = 0.5\rho L_{pp}d(u^2 + v_m^2)(-R_0' + X_{vv}'v_m'^2 + X_{vr}'v_m'r' + X_{rr}'r'^2 + X_{vvvv}'v_m'^4) \\ X_R = -(1 - t_R)0.5\rho A_R(u_R^2 + v_R^2)f_\alpha\sin\left(\delta - \frac{v_R}{u_R}\right)\sin\delta \\ X_P = (1 - t_P)\rho n_P^2 D_P^4 \left(k_2 J_P^2 + k_1 J_P + k_0\right) \\ \begin{cases} Y = Y_H + Y_R \\ Y_H = 0.5\rho L_{pp}d(u^2 + v_m^2)(Y_v'v_m' + Y_R'r' + Y_{vvv}'v_m'^3 + Y_{vvr}'v_m'^2r' + Y_{vrr}'v_m'r'^2 + Y_{rrr}'r'^3) \\ Y_R = -(1 + a_H)0.5\rho A_R(u_R^2 + v_R^2)f_\alpha\sin(\delta - \frac{v_R}{u_R})\cos\delta \end{cases} \\ \begin{cases} N_M = N_H + N_R \\ N_H = 0.5\rho L_{pp}^2 d(u^2 + v_m^2)(N_v'v_m' + N_R'r' + N_{vvv}'v_m'^3 + N_{vvr}'v_m'^2r' + N_{vrr}'v_m'r'^2 + N_{rrr}'r'^3) \\ N_R = -(x_R + a_H x_H)0.5\rho A_R(u_R^2 + v_R^2)f_\alpha\sin(\delta - \frac{v_R}{u_R})\cos\delta \end{cases}$$

$$\begin{cases} v'_{m} = \frac{v_{m}}{\sqrt{u^{2} + v_{m}^{2}}} \\ r' = \frac{rL_{pp}}{\sqrt{u^{2} + v_{m}^{2}}} \\ J_{P} = \frac{u(1 - w_{P})}{n_{P}D_{P}} \\ v_{R} = \sqrt{u^{2} + v_{m}^{2}} \gamma_{R} \beta_{R} \\ u_{R} = \varepsilon u(1 - w_{P}) \sqrt{\eta \left\{ 1 + \kappa \left( \sqrt{1 + \frac{8[k_{2}J_{P}^{2} + k_{1}J_{P} + k_{0}]}{\pi J_{P}^{2}}} - 1 \right) \right\} + (1 - \eta)} \\ \beta_{R} = (\beta - l'_{R}r') \\ \beta = tan^{-1} \frac{-v_{m}}{u} \\ \eta = \frac{D_{P}}{H_{R}} \\ \beta_{P} = (\beta - x'_{P}r') \\ w_{P} = -(1 - \exp(-C_{1}|\beta_{P}|))(C_{2} - 1)(1 - w_{P0}) \\ I_{Z} = m(0.25L_{pp})^{2} \end{cases}$$

## Elenco parametri noti:

- $J_z = Jz'*0.5$ rhoLpp^4d
- $m_y = my'*0.5rhoLpp^2d$
- $m_{\chi}$
- $L_{pp}$
- d
- $R_0'$
- $\bullet \quad X'_{vv}$
- $X'_{vr}$
- $X'_{rr}$
- $X'_{vvvv}$
- $Y_{v}'$
- $Y_R'$
- $Y'_{vvv}$
- $Y'_{vvr}$
- $Y'_{vrr}$
- $Y'_{rrr}$
- $N_v'$
- $N_R'$
- $N'_{vvv}$
- $N'_{vvr}$
- $N'_{vrr}$
- $N'_{rrr}$
- $t_R$
- $t_P$
- $(k_2, k_1, k_0)$
- $f_{\alpha}$
- $D_P$
- $A_R$
- κ
- $a_H$
- $l_R'$
- $x_H$  moltiplicare per Lpp
- пр
- $\bullet$   $H_R$
- $m = \nabla rho$
- $\mathcal{C}_1$
- $\mathcal{C}_2$

## Elenco parametri non utilizzati:

- B
- *C<sub>b</sub>*