



**POLITECNICO**  
**MILANO 1863**

SCUOLA DI INGEGNERIA INDUSTRIALE  
E DELL'INFORMAZIONE

# Exercise IEEE 802.15.4

INTERNET OF THINGS

Authors: **Kevin Zioldi - 10764177**  
**Matteo Volpari - 10773593**

Professors: Alessandro Redondi, Fabio Palmese, Antonio Boiano  
Academic Year: 2024-2025  
Version: 1.0  
Release date: 25-5-2025

# Contents

Contents	i
<b>1 Exercise IEEE 802.15.4</b>	<b>1</b>
1.1 Data . . . . .	1
1.2 Exercise 2.1 . . . . .	1
1.3 Exercise 2.2 . . . . .	2
1.4 Exercise 2.3 . . . . .	3

# 1 | Exercise IEEE 802.15.4

## 1.1. Data

- $\lambda = 0.15$  persons/frame
- Beacon-enabled mode
- CFP only
- 1 packet fits 1 slot
- 1 PAN coordinator
- 3 camera nodes
- $R = 250$  kbps
- $L = 128$  Byte

## 1.2. Exercise 2.1

We can compute the Probability Mass Function of the output rate using the Poisson distribution.

$$P(N = k) = \frac{e^{-\lambda} \lambda^k}{k!} = \frac{e^{-0.15} 0.15^k}{k!} \quad (1.1)$$

We can compute the PMF of the output rate by setting the right value of  $k$  in the Poisson distribution formula, where  $N$  is the observed number of people in the frame.

$$P(r = r_0) = P(N = 0) = \frac{e^{-0.15} 0.15^0}{0!} = e^{-0.15} = 0.8607 \quad (1.2)$$

$$P(r = r_1) = P(N = 1) = \frac{e^{-0.15} 0.15^1}{1!} = 0.15e^{-0.15} = 0.129 \quad (1.3)$$

$$\begin{aligned}
P(r = r_2) &= P(N > 1) = 1 - P(N = 0) - P(N = 1) = \\
&= 1 - 0.8607 - 0.1291 = 0.0102
\end{aligned} \tag{1.4}$$

### 1.3. Exercise 2.2

We can compute the slot time  $T_s$  from the definition of nominal bit rate.

$$R = \frac{L}{T_s} \tag{1.5}$$

$$T_s = \frac{L}{R} = \frac{128 \cdot 8 \text{ bit}}{250 \text{ kbit/s}} = 4.096 \text{ ms} \tag{1.6}$$

We can compute the number of slots needed by the camera nodes, considering the worst case, in which they need to send 6 KByte.

$$N_{node} = \frac{6 \text{ kByte}}{128 \text{ Byte}} = 46.875 \tag{1.7}$$

In order to compute  $N_{CFP}$ , we need to consider the ceiling of  $N_{node}$ , which is the same for the three camera nodes, since they work in the same way and transmit the same packets.

$$N_{CFP} = 3 \cdot \lceil 46.875 \rceil = 3 \cdot 47 = 141 \tag{1.8}$$

Since the system doesn't use the CAP, but only the CFP, the active part is formed by the beacon, which uses one slot, and  $N_{CFP}$  slots for the camera nodes.

$$T_{ACTIVE} = (N_{CFP} + 1) \cdot T_s = 581.632 \text{ ms} \tag{1.9}$$

From the pseudocode, we observe that camera nodes use a timer of 10 seconds before processing a new frame. For this reason, nodes will use a beacon interval of 10 seconds. We can compute the inactive time and the duty cycle accordingly.

$$BI = 10 \text{ s} \tag{1.10}$$

$$T_{INACTIVE} = BI - T_{ACTIVE} = 10 \text{ s} - 581.632 \text{ ms} = 9.418368 \text{ s} \quad (1.11)$$

$$\eta = \frac{T_{ACTIVE}}{BI} = 0.0581632 = 5.81632 \% \quad (1.12)$$

## 1.4. Exercise 2.3

We need to compute the maximum  $N_{CFP}$  to have  $\eta \leq 10\%$ . We express  $\eta$  as a function of  $N_{CFP}$  and impose the limit on  $\eta$ .

$$\eta = \frac{(N_{CFP} + 1) \cdot T_S}{BI} \leq \frac{1}{10} \quad (1.13)$$

$$N_{CFP} \leq \frac{BI}{10 \cdot T_S} - 1 = 243.140625 \quad (1.14)$$

Finally, we compute the number of additional cameras,  $N_{additional}$ , considering that every camera node uses 47 slots and we have 3 camera nodes.

$$N_{additional} = \lfloor \frac{243.140625}{47} - 3 \rfloor = 2 \quad (1.15)$$