6372: Project 1

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# Introduction

Using the World Health Organization (WHO) data compiled by Kumar Rajarshi, Deeksha Russell, and Duan Wang, we developed three models with three different goals:

* The first model was designed to be easily interpreted using linear regression.
* The second model was designed to be used as a predictive tool using linear regression.
* The third model was developed using non-parametric methods for prediction.

# Data Description

The description and context of the Life Expectancy (WHO) data set can be found [here](https://www.kaggle.com/kumarajarshi/life-expectancy-who). Data has been compiled from several different data sets into a final data set that represents health factors for 193 countries between the years of 2000-2015.

Looking at the data, there are 2,938 observations and 22 variables that cover four broad factors: immunization-related, mortality, economic, and social. Each record in the data contains measurements for a single year within the country being measured. The maximum number of years (or data points) for a single country is sixteen.

# Exploratory Data Analysis

We began by plotting life expectancy into a histogram as well as a Q-Q plot (Figures 1 & 2).

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Figure 1: Histogram of Life Expectancy data Figure 2: Q-Q Plot of Life Expectancy Data

As we would hope, life expectancy tends to skew towards the older side. The Q-Q plot shows some slight deviations from normality towards the edges, but after trying various transformations, the deviations from normality that are evident in the distribution did not seem severe enough to warrant a transformation and we proceeded using the original data.

Next, we began looking at correlation to narrow down our variable list before examining specific relationships (Figure 3). Based on a cut-off of *≥* 0.9 for correlation, we removed the variable in each correlation pair that had the higher number of NA values (Figure 4). We then proceeded to look at what happens when we also remove population, since it has minimal correlation to life\_expectancy (Figure 5). In the end, we made the decision to remove under\_five\_deaths, gdp, thinness\_1\_19\_years, and population due to lack of correlation to the response variable or multicollinearity.

Our next task was to address the missing values in the data set (Figure 6). We limited the scope of our analysis to not include the countries where life expectancy was missing (Figure 7). In doing that, we excluded the following countries from our scope: Cook Islands, Dominica, Marshall Islands, Monaco, Nauru, Niue, Palau, Saint Kitts and Nevis, San Marino, and Tuvalu.

Hepatitis B was now our variable with the most missing values. In looking at the relationship between Hepatitis B and Life Expectancy (Figure 8), our options with regards to the missing values were to drop them, impute them, or fill them in with 0’s. We chose different approaches based on each model.

### Interpretable Model

For our interpretable model, we made the decision to drop the hepatitis\_b variable along with the remainder of the NA’s (Figure 9). As a result of our feature engineering, we were left with only 2 records for 2015. After several looks at the data, we decided to only use the observations from the most recent four years (2011-2014).

### Linear Prediction Model

Knowing that we cannot have missing values for Ridge Regression or LASSO models, we examined the relationship of each variable that had more than 100 missing values to see which appeared to be significant.

* Hepatitis B (Figure 10)
* Total Expenditure (Figure 11)
* Alcohol (Figure 12)
* Income Composition of Resources (Figure 13)
* Schooling (Figure 14)

After reviewing the plots, we made the decision to remove Hepatitis B, total expenditure, and alcohol since the trend for those three variables was relatively flat. We then removed the remainder of the missing values from the data set before proceeding to modeling.

# Objective 1:

## Restatement of Problem

For our first objective, we developed two linear models for life expectancy: the first to be easily interpretable, and the second to be purely for purposes of prediction. For both models, we need to perform variable selection to minimize dimensionality and validate our assumptions with respect to linear regression.

Building the Model

After completion of the initial data clean up, we applied various variable selection techniques and chose final models based on metric comparisons, primarily MSE.

### Interpretable Model Variable Selection

For the interpretable model, we applied forward and backward stepwise selection algorithms and they both returned the same significant variables via the regsubsets model selection process: adult\_mortality, percentage\_expenditure, total\_expenditure, hiv\_aids, and income\_composition\_of\_resources.

### Best Subsets

We also used the best subsets technique when we ran the stepwise regression to find and visualize our model. We visually inspected how the model was performing using metrics R-squared, adjusted R-squared, BIC and CP (Figure 15, Figure 16).

Looking at the top row of the BIC plot in Figure 16, the best subsets technique visually shows that our variables (adult\_mortality, percentage\_expenditure, total\_expenditure, hiv\_aids, and income\_composition\_of\_resources) are the best choices for proceeding with the model.

Table : Test MSE values from regfit\_best

|  |
| --- |
| MSE |
| 15.170997 |
| 11.270808 |
| 10.081603 |
| 9.479321 |
| 9.470498 |
| 9.471813 |
| 9.558630 |
| 9.520908 |

Table : Coefficients of regfit\_best using lowest MSE

|  |  |
| --- | --- |
| Coefficient | Value |
| Intercept | 47.5535 |
| adult\_mortality | -0.0114 |
| percentage\_expenditure | 0.0002 |
| total\_expenditure | 0.2109 |
| hiv\_aids | -0.9767 |
| income\_composition\_of\_resources | 36.1682 |

### Predictive Model Variable Selection

After producing an easily interpretable linear regression model, we re-evaluated our predictors by including all of the years in the data set and performing additional dimensionality reduction techniques. Additionally, we imputed values for the NA rows by using either 0, the mean, or the median of the distribution depending on what the distribution looked like (see Figure 18 through Figure 20). We used the following methods with the goal of reducing variance and ensuring that our least squares estimates are reliable when determining our best subset of predictors.

**Ridge Regression**

We used the Ridge regression to have our sum of squared coefficients penalized to reduce our ASE. This highlighted the variables with the largest coefficients to possibly narrow down our list of predictors.

**LASSO**

After obtaining our optimal lambda, we checked for the non-zero coefficients in the model and made decisions about the variables to remove and keep based on ASE.

Our final decision for the variables to use in the predictive model were based on variables with the largest coefficient from the LASSO selection, which included country, income\_composition\_of\_resources, schooling, hiv\_aids, and status). (see Figures 25 & 26).

### Cross-Validation

We applied cross-validation for all our models to ensure that the results from our train model are valid when the same model is applied to the test data.

To avoid overfitting our models, we used a cross validation technique to reserve a particular sample of dataset and made sure that we did not train the model. To measure the accuracy of our model, we used the MSE metric which is the average difference between the actual value and the predicted value of the life\_expectancy variable. This metric gave us the model’s average prediction error and our goal was to decrease this metric as much as possible to increase the accuracy of the model. We ended comparing the MSEs for our models to determine the best model.

## First Model and Interpretation

### Model Interpretation

* **Adult Mortality:**It is estimated that for a 1 unit increase in adult mortality, there is a 0.013 unit decrease associated with years of life expectancy holding the other predictors fixed.
* **Total Expenditure**: It is estimated that for a 1 unit increase in total expenditure, there is a 0.289 unit increase associated with years of life expectancy holding the other predictors fixed.
* **HIV/AIDS:** It is estimated that for a 1 unit increase in HIV/AIDS, there is a 0.911 unit decrease associated with years of life expectancy holding the other predictors fixed.
* **Income Composition of Resources:** It is estimated that for a 1 unit increase in income composition of resources, there is a 36.649 unit increase associated with years of life expectancy holding the other predictors fixed.

We are 95% confident that the model’s intercept is between (45.41, 48.689) and the true regression coefficient’s for the predicted variables are: adult mortality (-0.016, -0.01), total expenditure (0.183, 0.359), HIV/AIDS (-1.062, -0.772), and income composition of resources (34.999, 38.894).

## Influential Data Points

Table

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Table 3: Outliers within our interpretable model

Our outliers include Bangladesh in 2012, Niger in 2013, Swaziland in 2011, Zimbabwe in 2011, and Sierra Leone in 2014. Sierra Leone in 2014 has a lower than average life expectancy of 48.1 years, and Bangladesh has a higher than average life expectancy at 77 years (which is seemingly rare for a developing country in this data set). The HIV/AIDs rate for Swaziland and Zimbabwe are notably high for these years, but it does not appear to be due to any anomaly in the data.

## Checking Assumptions

Our models assume the following:

* **Independent Variables**: The value of the response variable is the result of linear combination of predictors.
* **Equal Variance**: Error variance is the same for all predictors.
* **Normal Distribution**: Distribution of errors have a normal distribution.

Looking at diagnostic plots (Figure 22 - Figure 23) we can see that:

* **Linearity**: There is a roughly linear relationship between each of our chosen explanatory variables and the response variable
* **Equal Variance**: For each fitted value on the plot, we can see that the spread of the residuals is approximately equivalent.
* **Normal Distribution**: Looking at the Q-Q plot, we see that the points are very close to the line. This indicates that errors are normally distributed. Also note that a few points are a bit far from the line but because we have such a large sample size we will not worry about these few points and will conclude that the data was sampled from a normal distribution.

## Predictive Model

Based on the variable selection outlined above using LASSO, we developed a final predictive model that included country, income\_composition\_of\_resources, schooling, hiv\_aids, and status. The coefficients of the model and associated metrics can be found in the appendix in Table 5. The ASE and adjusted R-squared associated with this model were 4.115 and 0.9513, respectively.

## Checking Assumptions

For our predictive model, we also reviewed residual and diagnostic plots to validate our assumptions.

Looking at diagnostic plots for this model (Figure 27) we can see that:

* **Linearity**: There is a roughly linear relationship between each of our chosen explanatory variables and the response variable
* **Equal Variance**: There does not appear to be a large difference in variance in the errors, with the exception of a few outlier data points. These data points related to Haiti in 2010 (which was the year of the devastating earthquake) and Eritrea in 2000 (which at the time was at war with Ethiopia). The model was re-run after excluding these data points but the ASE did not change significantly so they were kept in the final model.
* **Normal Distribution**: Looking at the Q-Q plot, we see that the points are very close to a normal distribution except for the larger life expectancies (approximately greater than 75). We should use caution when our predictions return with values in the range above 75 years, as our model seems to over-estimate the life expectancy in this range.

# Objective 2:

## Strategy

Once we had developed a linear regression model, we then looked at developing a non-parametric model for predicting the life expectancy. Although our ASE and adjusted R-squared metrics were very good for the linear regression models, there could be some question about the normality of our residuals, independence of the errors, and equal variance. By using a non-parametric model, it is no longer required that we meet those assumptions and we can proceed with as many variables as we think would be useful in our model.

As discussed in our EDA section, we used the imputed data set to run our non-parametric models, which already removed highly correlated variables and ones we suspected were not related to our response variable. For the KNN model, we used the caret package to iterate through several different K values to find the optimal K value using all the variables we had left. We also ran a KNN model using the four variables we determined were significant from our interpretable model for comparison. We proceeded to do the same with a random forest model and our results will be discussed in the Metrics section below.

## Data Sets

There are limits to the levels of a factor that can be used in a KNN or tree model. For this reason, country was removed from the data sets used in our non-parametric models. Additionally, the model performance was tested on both an imputed data set and a data set with the NA values were removed instead of imputed.

## Metrics

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| Model Type | Data Set | # of Predictors | | Train ASE | Train R2 | Test ASE | Test R2 |
| KNN | Imputed | 16 | 7.437 | | 0.919 | 5.438 | 0.943 |
| KNN | Removed <NA> | 16 | 7.241 | | 0.920 | 6.175 | 0.930 |
| KNN | Imputed | 4 | 6.559 | | 0.927 | 5.302 | 0.943 |
| Tree | Imputed | 4\* | 13.7 | | - | 12.823 | - |
| Random Forest | Imputed | 16 | 3.606 | | 0.96 | 2.727 | 0.971 |
| Random Forest | Imputed | 4 | 5.855 | | 0.935 | 4.169 | 0.957 |

Table 4. Metrics for multiple non-parametric models. \*See appendix for variables used.

Based on the metrics, as seen above, the ASE and R-squared values from each model were surprisingly good. Since our R-squared was over 90% on our training data set, there was concern about over-fit, but we did not see a decrease in performance once applying to our test data set. The models were run again with the same parameters but with a different train and test split to perform an additional check against over-fit and performed similarly. This indicates that our model is not overfitting *specific to our current data set*. We could further verify whether the data overfits by running this model against a larger data set (for example, with years up to 2019 populated). The plots of our predicted output versus our actual values can be seen in Figure 29 to Figure 31 in the appendix.

## Comparison to Objective 1

Even with a non-parametric model, both KNN and random forest performed optimally when using the same four predictors as our interpretable model from the first objective. Additionally, the KNN model that used all predictors performed about the same with an imputed data set and a data set with the NA values removed. Overall, with small changes to the data set and predictors, all the nonparametric models performed similarly with ASE generally below 10 and R-squared above 90%. This is interesting to note in comparison to our purely predictive linear regression model which deemed country as an important predictor, and we were not able to use it in our non-parametric models. As noted in our analysis, we did get very high R-squared values and low ASE values which indicates there is likely some overfit (and high variance) in our models.

# Conclusion & Final Recommendations

As with any data set, weeks upon weeks could be sent exploring all variable options, transformations, selections, and other methods to develop a good predictive model for life expectancy. The ASE and adjusted R-squared values for our interpretable model give us high confidence in our variable selection on our reduced data set, as they do not indicate overfit. On the contrary, the metrics for our predictive model and our non-parametric models all were high enough to suspect high variance and possible overfit. Additional analysis could be done by removing only specific countries in our models and also checking for interactions for each variable to further refine the variable selection and reduce risk of overfit.

# Appendix

## Tables & Figures

Chart, timeline, treemap chart

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Figure 3: Correlation Matrix, original data

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Figure 4: Correlation Matrix: excluding under 5 deaths, gdp, and thinness 1-19 years

Chart, treemap chart

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Figure 5: Correlation Matrix: exluding all from Figure 2 along with population

Table

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Figure 6: Missing Values, original data Figure 7: Missing values, removed life expectancy

Chart

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Figure 8: Relationship between Hepatitis B and Life Expectancy

Table

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Figure 9: Missing Data, remove Hep B & remaining NA's

Chart

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Figure 10: Life Expectancy & Hepatitis B  Figure 11: Life Expectancy & Total Expenditure

Chart, scatter chart

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Figure 12: Life Expectancy & Alcohol Figure 13: Life Expectancy & Inc. Comp. of Resources

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Figure 14: Life Expectancy & Schooling

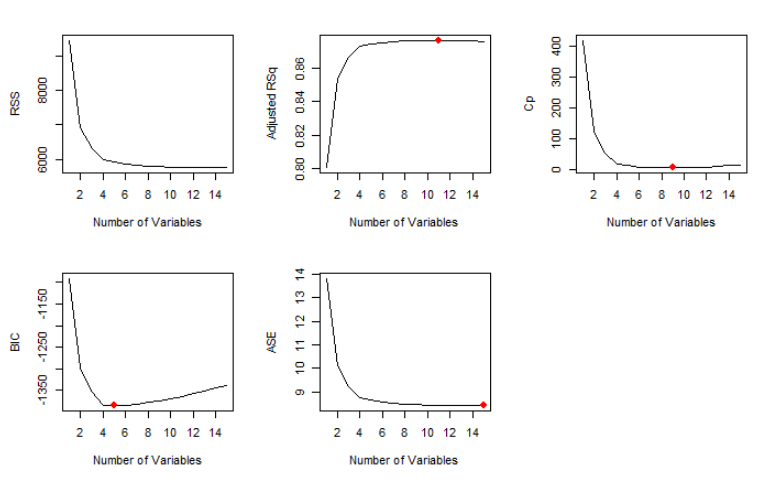


Figure 15: Plot of RSS, Adjusted RSq, Cp, BIC and ASE for Best Subset Selection

A picture containing calendar

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Figure 16: Variable Selection of Best Subset Selection

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Figure 17: Coefficients of Full Model, Forward Selection, and Backwards Selection

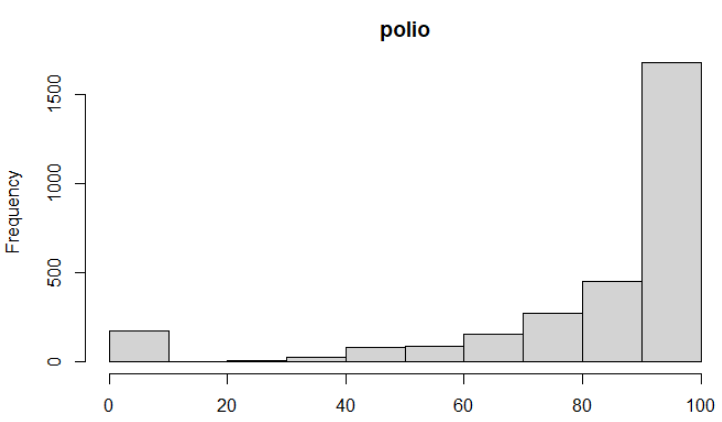
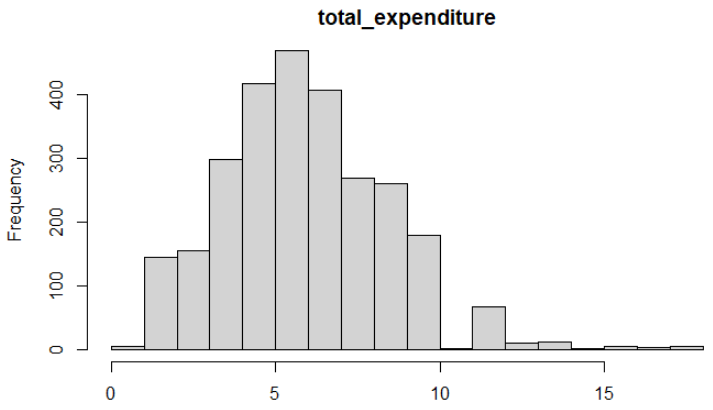
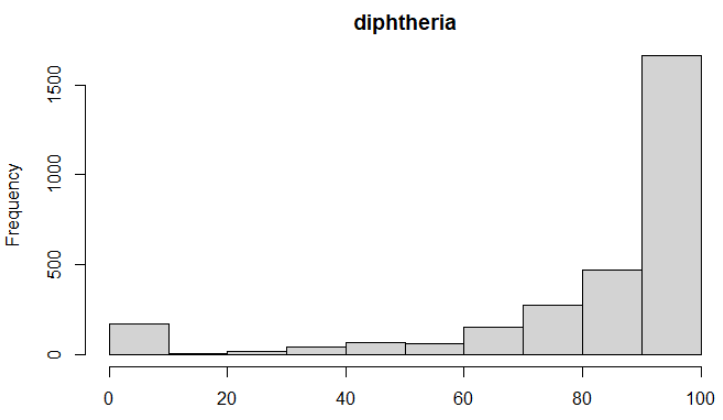
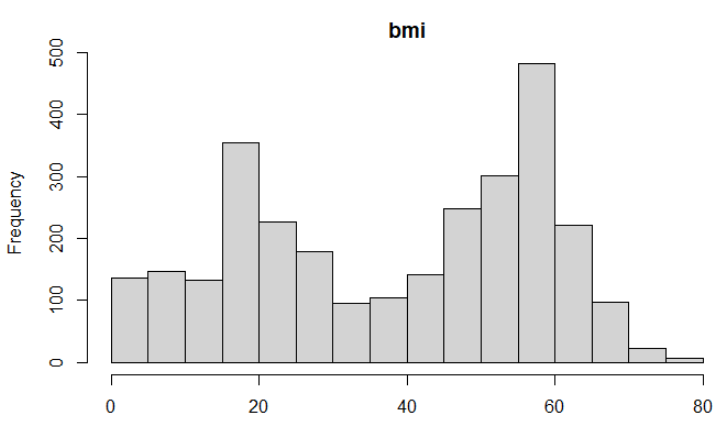
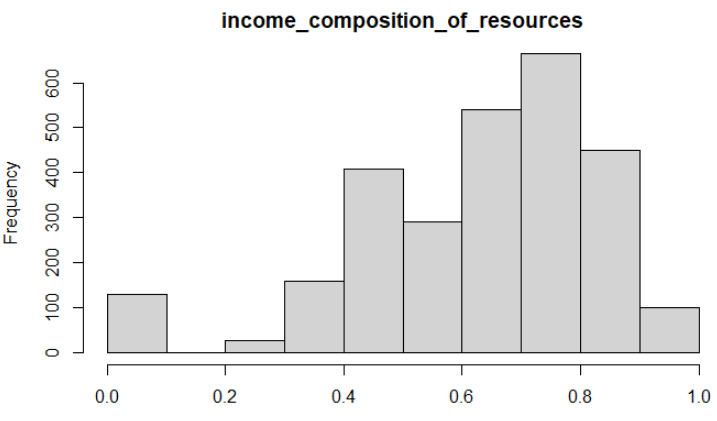
  

Figure 18: Histograms of variables where missing values were imputed as the median

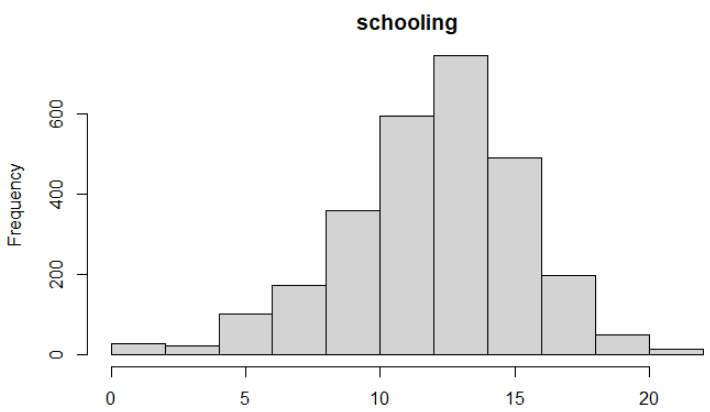


Figure 19: Histograms for variables where missing values were imputed as the mean

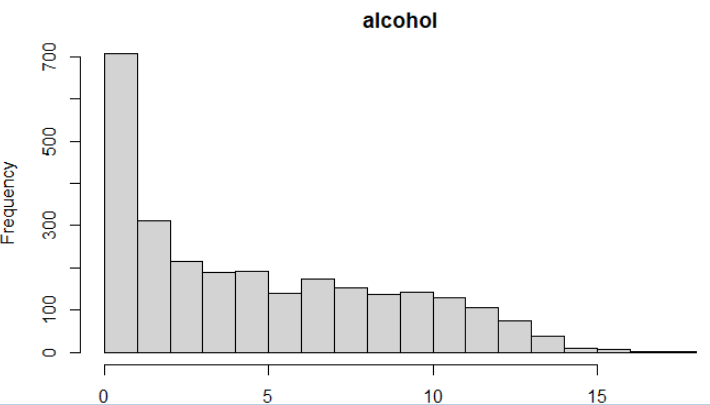
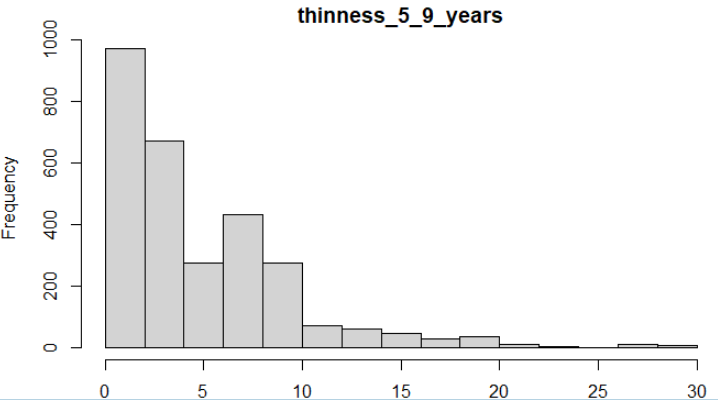
 

Figure 20: Histograms for variables where the missing values were imputed as 0

Chart, scatter chart

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Figure 21: Comparison of Predicted Values and Life Expectancy for interpretable model

Diagram, schematic

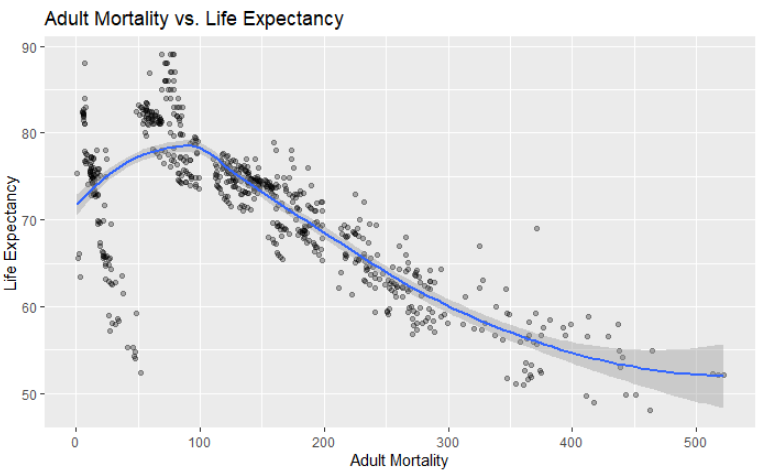
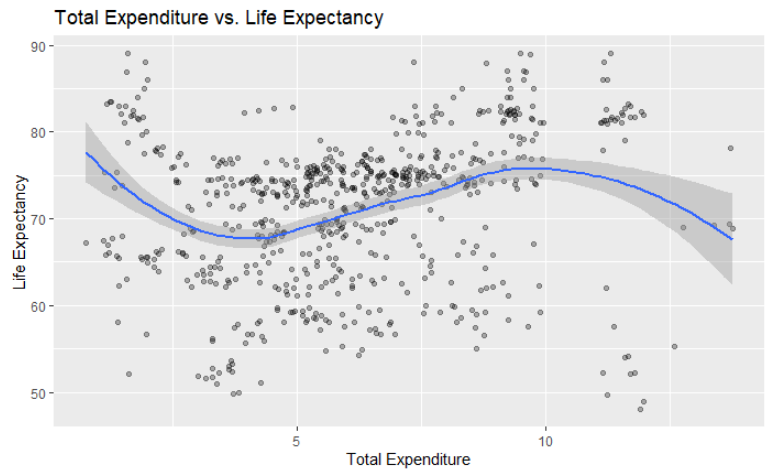
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Figure 22: Analysis of Residuals for Interpretable Model

Chart, scatter chart

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Figure 23: Residuals from fitting interpretable model to the data

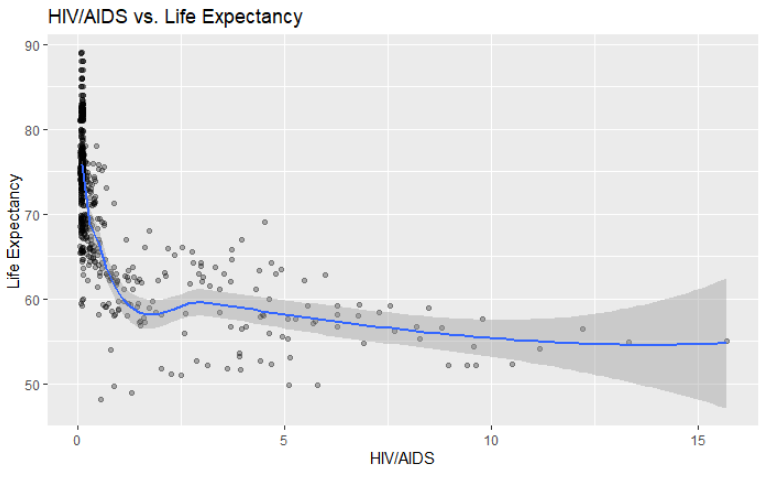
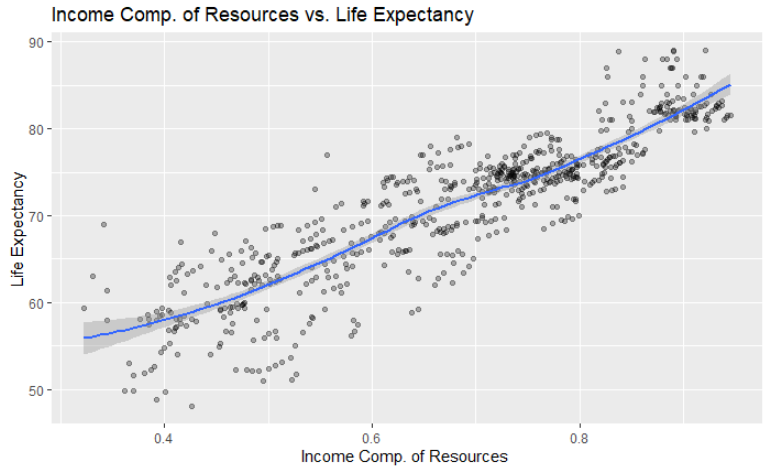
 

Figure 24: Plots of response variables versus each of the predictors on our reduced data set for the interpretable model

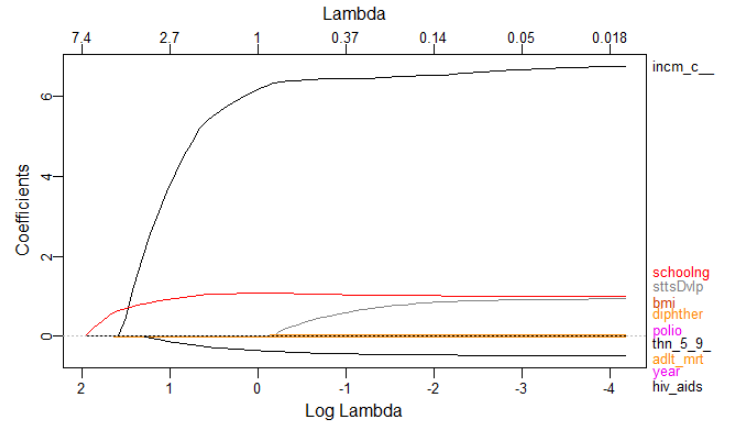


Figure 25: Plot of LASSO results showing the top four predictors

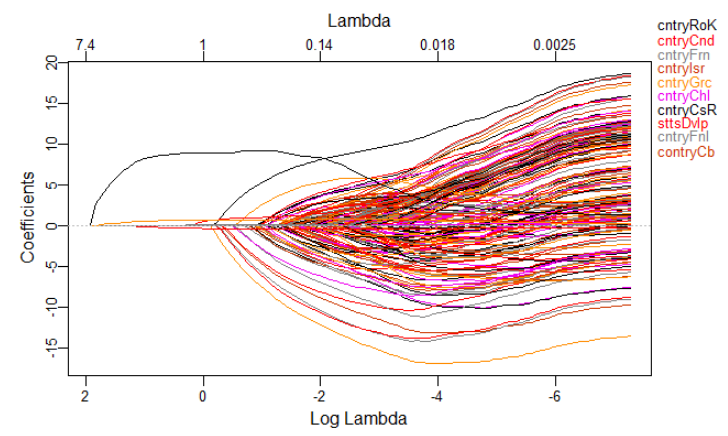


Figure 26: Plot of LASSO results including country

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
|  | Estimate | Std. Error | t value | Pr(>|t|) |  |
| (Intercept) | 52.10404 | 0.59089 | 88.178 | < 2e-16 | \*\*\* |
| countryAlbania | 13.77939 | 0.75408 | 18.273 | < 2e-16 | \*\*\* |
| countryAlgeria | 11.92752 | 0.7566 | 15.765 | < 2e-16 | \*\*\* |
| countryAngola | -8.14776 | 0.7424 | -10.975 | < 2e-16 | \*\*\* |
| countryAntigua and Barbuda | 16.29433 | 0.74172 | 21.968 | < 2e-16 | \*\*\* |
| countryArgentina | 10.87289 | 0.7907 | 13.751 | < 2e-16 | \*\*\* |
| countryArmenia | 12.2684 | 0.75232 | 16.307 | < 2e-16 | \*\*\* |
| countryAustralia | 15.03373 | 0.83926 | 17.913 | < 2e-16 | \*\*\* |
| countryAustria | 17.70743 | 0.77987 | 22.706 | < 2e-16 | \*\*\* |
| countryAzerbaijan | 9.8574 | 0.75105 | 13.125 | < 2e-16 | \*\*\* |
| countryBahamas | 12.66908 | 0.75624 | 16.753 | < 2e-16 | \*\*\* |
| countryBahrain | 12.87744 | 0.76821 | 16.763 | < 2e-16 | \*\*\* |
| countryBangladesh | 10.54245 | 0.74223 | 14.204 | < 2e-16 | \*\*\* |
| countryBarbados | 11.19765 | 0.77386 | 14.47 | < 2e-16 | \*\*\* |
| countryBelarus | 6.83575 | 0.77229 | 8.851 | < 2e-16 | \*\*\* |
| countryBelgium | 16.0064 | 0.79425 | 20.153 | < 2e-16 | \*\*\* |
| countryBelize | 7.88878 | 0.75533 | 10.444 | < 2e-16 | \*\*\* |
| countryBenin | -0.34291 | 0.74198 | -0.462 | 0.644005 |  |
| countryBhutan | 7.45329 | 0.75942 | 9.814 | < 2e-16 | \*\*\* |
| countryBolivia (Plurinational State of) | 5.43184 | 0.76584 | 7.093 | 1.67E-12 | \*\*\* |
| countryBosnia and Herzegovina | 15.21627 | 0.75656 | 20.112 | < 2e-16 | \*\*\* |
| countryBotswana | 2.38017 | 0.80064 | 2.973 | 0.002976 | \*\* |
| countryBrazil | 10.75841 | 0.76703 | 14.026 | < 2e-16 | \*\*\* |
| countryBrunei Darussalam | 13.56162 | 0.76924 | 17.63 | < 2e-16 | \*\*\* |
| countryBulgaria | 10.38004 | 0.76416 | 13.584 | < 2e-16 | \*\*\* |
| countryBurkina Faso | 0.45413 | 0.74742 | 0.608 | 0.543506 |  |
| countryBurundi | -0.61391 | 0.74321 | -0.826 | 0.408858 |  |
| countryCôte d'Ivoire | -8.59456 | 0.75676 | -11.357 | < 2e-16 | \*\*\* |
| countryCabo Verde | 11.66591 | 0.75325 | 15.487 | < 2e-16 | \*\*\* |
| countryCambodia | 5.34998 | 0.74348 | 7.196 | 7.98E-13 | \*\*\* |
| countryCameroon | -1.95352 | 0.74814 | -2.611 | 0.009073 | \*\* |
| countryCanada | 17.53601 | 0.78514 | 22.335 | < 2e-16 | \*\*\* |
| countryCentral African Republic | -4.20312 | 0.75563 | -5.562 | 2.92E-08 | \*\*\* |
| countryChad | -4.30678 | 0.74673 | -5.768 | 8.95E-09 | \*\*\* |
| countryChile | 16.13553 | 0.77424 | 20.841 | < 2e-16 | \*\*\* |
| countryChina | 13.44575 | 0.74998 | 17.928 | < 2e-16 | \*\*\* |
| countryColombia | 11.92617 | 0.75381 | 15.821 | < 2e-16 | \*\*\* |
| countryComoros | 2.6352 | 0.74778 | 3.524 | 0.000432 | \*\*\* |
| countryCongo | 1.63344 | 0.74857 | 2.182 | 0.029188 | \* |
| countryCosta Rica | 16.71573 | 0.75825 | 22.045 | < 2e-16 | \*\*\* |
| countryCroatia | 13.45887 | 0.7661 | 17.568 | < 2e-16 | \*\*\* |
| countryCuba | 14.94203 | 0.77178 | 19.361 | < 2e-16 | \*\*\* |
| countryCyprus | 17.12687 | 0.76543 | 22.375 | < 2e-16 | \*\*\* |
| countryCzechia | 15.69215 | 0.75186 | 20.871 | < 2e-16 | \*\*\* |
| countryDemocratic People's Republic of Korea | 8.11715 | 0.75186 | 10.796 | < 2e-16 | \*\*\* |
| countryDemocratic Republic of the Congo | -4.60436 | 0.75289 | -6.116 | 1.10E-09 | \*\*\* |
| countryDenmark | 14.27378 | 0.79922 | 17.86 | < 2e-16 | \*\*\* |
| countryDjibouti | 6.13605 | 0.75497 | 8.128 | 6.56E-16 | \*\*\* |
| countryDominican Republic | 11.26123 | 0.75742 | 14.868 | < 2e-16 | \*\*\* |
| countryEcuador | 12.88166 | 0.75851 | 16.983 | < 2e-16 | \*\*\* |
| countryEgypt | 10.4357 | 0.75158 | 13.885 | < 2e-16 | \*\*\* |
| countryEl Salvador | 10.28885 | 0.75583 | 13.613 | < 2e-16 | \*\*\* |
| countryEquatorialGuinea | -0.96616 | 0.74744 | -1.293 | 0.196253 |  |
| countryEritrea | 6.35987 | 0.76088 | 8.359 | < 2e-16 | \*\*\* |
| countryEstonia | 10.93383 | 0.78443 | 13.939 | < 2e-16 | \*\*\* |
| countryEthiopia | 3.16678 | 0.74347 | 4.259 | 2.12E-05 | \*\*\* |
| countryFiji | 6.09888 | 0.76718 | 7.95 | 2.71E-15 | \*\*\* |
| countryFinland | 15.73894 | 0.80016 | 19.67 | < 2e-16 | \*\*\* |
| countryFrance | 18.1084 | 0.78482 | 23.073 | < 2e-16 | \*\*\* |
| countryGabon | 4.44979 | 0.76721 | 5.8 | 7.39E-09 | \*\*\* |
| countryGambia | 2.33442 | 0.742 | 3.146 | 0.001672 | \*\* |
| countryGeorgia | 11.88235 | 0.75613 | 15.715 | < 2e-16 | \*\*\* |
| countryGermany | 16.57167 | 0.79247 | 20.911 | < 2e-16 | \*\*\* |
| countryGhana | 2.57936 | 0.74379 | 3.468 | 0.000533 | \*\*\* |
| countryGreece | 17.15917 | 0.78466 | 21.868 | < 2e-16 | \*\*\* |
| countryGrenada | 11.27573 | 0.81268 | 13.875 | < 2e-16 | \*\*\* |
| countryGuatemala | 12.20665 | 0.74437 | 16.399 | < 2e-16 | \*\*\* |
| countryGuinea | -0.45504 | 0.7425 | -0.613 | 0.540032 |  |
| countryGuinea-Bissau | -0.29539 | 0.74856 | -0.395 | 0.693158 |  |
| countryGuyana | 5.76557 | 0.74736 | 7.715 | 1.69E-14 | \*\*\* |
| countryHaiti | 4.21544 | 0.75488 | 5.584 | 2.58E-08 | \*\*\* |
| countryHonduras | 13.02663 | 0.747 | 17.438 | < 2e-16 | \*\*\* |
| countryHungary | 10.36818 | 0.77623 | 13.357 | < 2e-16 | \*\*\* |
| countryIceland | 16.9075 | 0.81135 | 20.839 | < 2e-16 | \*\*\* |
| countryIndia | 5.85822 | 0.74385 | 7.876 | 4.85E-15 | \*\*\* |
| countryIndonesia | 6.72672 | 0.75027 | 8.966 | < 2e-16 | \*\*\* |
| countryIran (Islamic Republic of) | 12.14702 | 0.75671 | 16.052 | < 2e-16 | \*\*\* |
| countryIraq | 10.55097 | 0.74594 | 14.145 | < 2e-16 | \*\*\* |
| countryIreland | 14.90503 | 0.80478 | 18.521 | < 2e-16 | \*\*\* |
| countryIsrael | 17.29809 | 0.7831 | 22.089 | < 2e-16 | \*\*\* |
| countryItaly | 18.09061 | 0.78486 | 23.049 | < 2e-16 | \*\*\* |
| countryJamaica | 13.35235 | 0.7553 | 17.678 | < 2e-16 | \*\*\* |
| countryJapan | 18.98025 | 0.7769 | 24.431 | < 2e-16 | \*\*\* |
| countryJordan | 10.88427 | 0.7604 | 14.314 | < 2e-16 | \*\*\* |
| countryKazakhstan | 4.13306 | 0.76619 | 5.394 | 7.47E-08 | \*\*\* |
| countryKenya | 1.94904 | 0.75702 | 2.575 | 0.010087 | \* |
| countryKiribati | 4.95057 | 0.75689 | 6.541 | 7.28E-11 | \*\*\* |
| countryKuwait | 11.28265 | 0.76504 | 14.748 | < 2e-16 | \*\*\* |
| countryKyrgyzstan | 7.81661 | 0.75371 | 10.371 | < 2e-16 | \*\*\* |
| countryLao People's Democratic Republic | 3.34474 | 0.74231 | 4.506 | 6.89E-06 | \*\*\* |
| countryLatvia | 10.0286 | 0.78041 | 12.85 | < 2e-16 | \*\*\* |
| countryLebanon | 12.46318 | 0.7698 | 16.19 | < 2e-16 | \*\*\* |
| countryLesotho | -0.58211 | 0.83206 | -0.7 | 0.484239 |  |
| countryLiberia | -0.62347 | 0.74582 | -0.836 | 0.403253 |  |
| countryLibya | 9.39647 | 0.77269 | 12.161 | < 2e-16 | \*\*\* |
| countryLithuania | 8.73986 | 0.78606 | 11.119 | < 2e-16 | \*\*\* |
| countryLuxembourg | 18.04233 | 0.76832 | 23.483 | < 2e-16 | \*\*\* |
| countryMadagascar | 3.94817 | 0.74218 | 5.32 | 1.12E-07 | \*\*\* |
| countryMalawi | -1.95829 | 0.79204 | -2.472 | 0.013479 | \* |
| countryMalaysia | 12.01548 | 0.75724 | 15.867 | < 2e-16 | \*\*\* |
| countryMaldives | 14.43139 | 0.75198 | 19.191 | < 2e-16 | \*\*\* |
| countryMali | -1.24222 | 0.74394 | -1.67 | 0.095079 | . |
| countryMalta | 17.38731 | 0.76969 | 22.59 | < 2e-16 | \*\*\* |
| countryMauritania | 5.50157 | 0.74334 | 7.401 | 1.79E-13 | \*\*\* |
| countryMauritius | 10.44816 | 0.76225 | 13.707 | < 2e-16 | \*\*\* |
| countryMexico | 14.17694 | 0.75549 | 18.765 | < 2e-16 | \*\*\* |
| countryMicronesia (Federated States of) | 8.21313 | 0.74532 | 11.02 | < 2e-16 | \*\*\* |
| countryMongolia | 4.30893 | 0.75591 | 5.7 | 1.32E-08 | \*\*\* |
| countryMontenegro | 14.32514 | 0.74613 | 19.199 | < 2e-16 | \*\*\* |
| countryMorocco | 12.24198 | 0.74505 | 16.431 | < 2e-16 | \*\*\* |
| countryMozambique | 0.63455 | 0.76203 | 0.833 | 0.405078 |  |
| countryMyanmar | 5.91784 | 0.74185 | 7.977 | 2.18E-15 | \*\*\* |
| countryNamibia | 5.88584 | 0.7826 | 7.521 | 7.33E-14 | \*\*\* |
| countryNepal | 6.74243 | 0.74493 | 9.051 | < 2e-16 | \*\*\* |
| countryNetherlands | 16.23365 | 0.79762 | 20.353 | < 2e-16 | \*\*\* |
| countryNew Zealand | 15.34779 | 0.82143 | 18.684 | < 2e-16 | \*\*\* |
| countryNicaragua | 13.03848 | 0.74774 | 17.437 | < 2e-16 | \*\*\* |
| countryNiger | 2.15775 | 0.75497 | 2.858 | 0.004295 | \*\* |
| countryNigeria | -5.03611 | 0.74659 | -6.745 | 1.85E-11 | \*\*\* |
| countryNorway | 16.5597 | 0.80296 | 20.623 | < 2e-16 | \*\*\* |
| countryOman | 13.39838 | 0.75463 | 17.755 | < 2e-16 | \*\*\* |
| countryPakistan | 7.0013 | 0.74635 | 9.381 | < 2e-16 | \*\*\* |
| countryPanama | 14.62977 | 0.75826 | 19.294 | < 2e-16 | \*\*\* |
| countryPapua New Guinea | 3.63899 | 0.74164 | 4.907 | 9.80E-07 | \*\*\* |
| countryParaguay | 11.87385 | 0.75306 | 15.767 | < 2e-16 | \*\*\* |
| countryPeru | 11.67276 | 0.76053 | 15.348 | < 2e-16 | \*\*\* |
| countryPhilippines | 6.71857 | 0.75014 | 8.956 | < 2e-16 | \*\*\* |
| countryPoland | 12.08928 | 0.77756 | 15.548 | < 2e-16 | \*\*\* |
| countryPortugal | 16.03169 | 0.7843 | 20.441 | < 2e-16 | \*\*\* |
| countryQatar | 14.90658 | 0.76198 | 19.563 | < 2e-16 | \*\*\* |
| countryRepublic of Korea | 19.4109 | 0.75186 | 25.817 | < 2e-16 | \*\*\* |
| countryRepublic of Moldova | 8.90465 | 0.75186 | 11.843 | < 2e-16 | \*\*\* |
| countryRomania | 11.43616 | 0.76574 | 14.935 | < 2e-16 | \*\*\* |
| countryRussian Federation | 5.33544 | 0.76453 | 6.979 | 3.72E-12 | \*\*\* |
| countryRwanda | 2.42639 | 0.7458 | 3.253 | 0.001154 | \*\* |
| countrySaint Lucia | 12.01418 | 0.75619 | 15.888 | < 2e-16 | \*\*\* |
| countrySaint Vincent and the Grenadines | 11.67663 | 0.75936 | 15.377 | < 2e-16 | \*\*\* |
| countrySamoa | 12.01276 | 0.75595 | 15.891 | < 2e-16 | \*\*\* |
| countrySao Tome and Principe | 5.81372 | 0.74456 | 7.808 | 8.19E-15 | \*\*\* |
| countrySaudi Arabia | 11.19463 | 0.76215 | 14.688 | < 2e-16 | \*\*\* |
| countrySenegal | 5.19568 | 0.74273 | 6.995 | 3.31E-12 | \*\*\* |
| countrySerbia | 11.63924 | 0.76257 | 15.263 | < 2e-16 | \*\*\* |
| countrySeychelles | 10.57526 | 0.75769 | 13.957 | < 2e-16 | \*\*\* |
| countrySierra Leone | 11.30503 | 0.7419 | -15.238 | < 2e-16 | \*\*\* |
| countrySingapore | 18.55412 | 0.76964 | 24.108 | < 2e-16 | \*\*\* |
| countrySlovakia | 11.76849 | 0.76981 | 15.288 | < 2e-16 | \*\*\* |
| countrySlovenia | 15.2938 | 0.79057 | 19.345 | < 2e-16 | \*\*\* |
| countrySolomon Islands | 9.08787 | 0.74157 | 12.255 | < 2e-16 | \*\*\* |
| countrySomalia | -7.42112 | 0.75219 | -9.866 | < 2e-16 | \*\*\* |
| countrySouth Africa | 4.26747 | 0.81697 | 5.224 | 1.89E-07 | \*\*\* |
| countrySouth Sudan | 2.17173 | 0.774 | 2.806 | 0.005054 | \*\* |
| countrySpain | 17.73013 | 0.78916 | 22.467 | < 2e-16 | \*\*\* |
| countrySri Lanka | 11.31826 | 0.76021 | 14.888 | < 2e-16 | \*\*\* |
| countrySudan | 4.76263 | 0.7455 | 6.388 | 1.96E-10 | \*\*\* |
| countrySuriname | 9.79701 | 0.75271 | 13.016 | < 2e-16 | \*\*\* |
| countrySwaziland | 6.55044 | 0.91041 | 7.195 | 8.02E-13 | \*\*\* |
| countrySweden | 18.36865 | 0.78511 | 23.396 | < 2e-16 | \*\*\* |
| countrySwitzerland | 18.42635 | 0.78158 | 23.576 | < 2e-16 | \*\*\* |
| countrySyrian Arab Republic | 10.42405 | 0.74751 | 13.945 | < 2e-16 | \*\*\* |
| countryTajikistan | 6.57562 | 0.74606 | 8.814 | < 2e-16 | \*\*\* |
| countryThailand | 11.6217 | 0.75582 | 15.376 | < 2e-16 | \*\*\* |
| countryThe former Yugoslav republic of Macedonia | 13.2499 | 0.75759 | 17.49 | < 2e-16 | \*\*\* |
| countryTimor-Leste | 4.76573 | 0.74579 | 6.39 | 1.94E-10 | \*\*\* |
| countryTogo | -1.39206 | 0.74965 | -1.857 | 0.063426 | . |
| countryTonga | 9.90355 | 0.76751 | 12.904 | < 2e-16 | \*\*\* |
| countryTrinidad and Tobago | 9.69877 | 0.75663 | 12.818 | < 2e-16 | \*\*\* |
| countryTunisia | 11.84464 | 0.76612 | 15.461 | < 2e-16 | \*\*\* |
| countryTurkey | 12.22228 | 0.75655 | 16.155 | < 2e-16 | \*\*\* |
| countryTurkmenistan | 5.96213 | 0.75435 | 7.904 | 3.89E-15 | \*\*\* |
| countryUganda | -0.5828 | 0.75706 | -0.77 | 0.441471 |  |
| countryUkraine | 7.22489 | 0.77121 | 9.368 | < 2e-16 | \*\*\* |
| countryUnited Arab Emirates | 13.62142 | 0.76136 | 17.891 | < 2e-16 | \*\*\* |
| countryUnited Kingdom of Great Britain and Northern Ireland | 19.71715 | 0.75186 | 26.224 | < 2e-16 | \*\*\* |
| countryUnited Republic of Tanzania | -1.79441 | 0.76251 | -2.353 | 0.018677 | \* |
| countryUnited States of America | 16.9859 | 0.75186 | 22.592 | < 2e-16 | \*\*\* |
| countryUruguay | 12.65011 | 0.77693 | 16.282 | < 2e-16 | \*\*\* |
| countryUzbekistan | 7.28581 | 0.74996 | 9.715 | < 2e-16 | \*\*\* |
| countryVanuatu | 11.87003 | 0.74897 | 15.848 | < 2e-16 | \*\*\* |
| countryVenezuela (Bolivarian Republic of) | 11.56669 | 0.75771 | 15.265 | < 2e-16 | \*\*\* |
| countryViet Nam | 14.01884 | 0.74961 | 18.702 | < 2e-16 | \*\*\* |
| countryYemen | 5.33099 | 0.74152 | 7.189 | 8.36E-13 | \*\*\* |
| countryZambia | -0.94739 | 0.77374 | -1.224 | 0.220894 |  |
| countryZimbabwe | 1.81562 | 0.83018 | 2.187 | 0.028826 | \* |
| income\_composition\_of\_resources | 2.61344 | 0.46052 | 5.675 | 1.53E-08 | \*\*\* |
| statusDeveloped | NA | NA | NA | NA |  |
| schooling | 0.61489 | 0.03994 | 15.395 | < 2e-16 | \*\*\* |
| hiv\_aids | -0.45658 | 0.0157 | -29.083 | < 2e-16 | \*\*\* |

Table 5. Coefficients, standard error, t-value, and p-value of Predictive Model

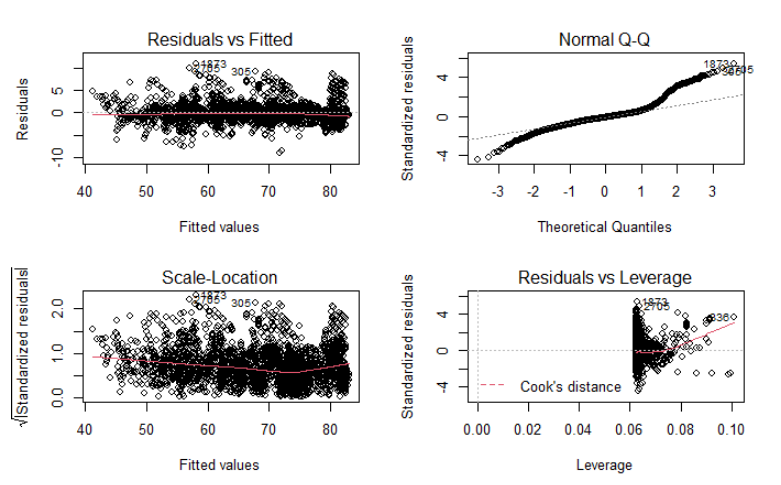


Figure 27: Analysis of residuals for our predictive model

# Remove country because this tree function has a maximum of 32 levels  
tree1 <- tree(life\_expectancy ~ ., data = tree\_train[, -1])  
summary(tree1)

##   
## Regression tree:  
## tree(formula = life\_expectancy ~ ., data = tree\_train[, -1])  
## Variables actually used in tree construction:  
## [1] "hiv\_aids" "income\_composition\_of\_resources"  
## [3] "adult\_mortality" "infant\_deaths"   
## Number of terminal nodes: 9   
## Residual mean deviance: 13.7 = 29990 / 2189   
## Distribution of residuals:  
## Min. 1st Qu. Median Mean 3rd Qu. Max.   
## -16.51000 -2.11000 -0.05483 0.00000 2.19300 16.19000

Figure 28: Output chunk for tree model showing the four variables used in the tree construction

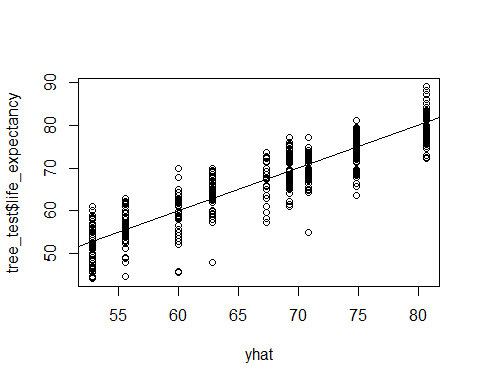


Figure 29: Model fit for our test data set using a tree regression

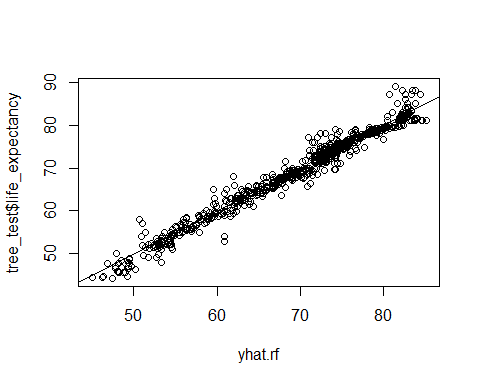


Figure 30: Model fit for our test data set using a random forest regression which used all predictors and 5 splits per node

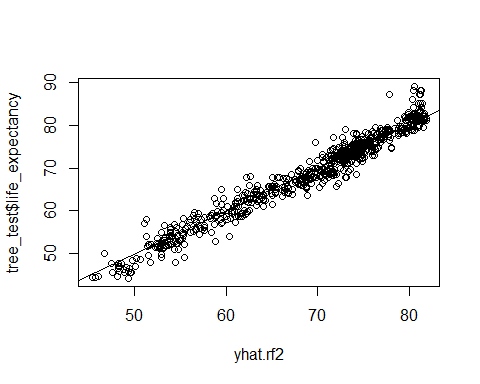


Figure 31: Model fit for our test data set using a random forest regression which used only the top four predictors and 1 split per node

## R Code

knitr::opts\_chunk$set(echo = TRUE)

**library**(tidyverse)

**library**(corrplot)

**library**(GGally)

**library**(gt)

**library**(hrbrthemes)

**library**(car)

**library**(leaps)

**library**(caret)

**library**(tree)

**library**(randomForest)

**library**(plotmo)

**library**(webshot)

*# Load data*

df <- read\_csv(here::here("data - raw", "Life Expectancy Data.csv"))

*# Clean up column names*

df\_clean <- janitor::clean\_names(df)

*# Look at the data*

glimpse(df\_clean)

df\_clean %>%

ggplot(aes(life\_expectancy)) +

geom\_histogram(fill = "steelblue", color = "black") +

labs(title = "Histogram of Life Expectancy",

x = "Age",

y = "Count") +

theme\_ipsum()

df\_clean %>%

ggplot(aes(sample = life\_expectancy)) +

geom\_qq(pch = 21, size = 3, na.rm = TRUE) +

geom\_qq\_line(color = "indianred", na.rm = TRUE) +

labs(title = "Q-Q Plot of Life Expectancy",

x = "Theoretical",

y = "Sample") +

theme\_ipsum()

*# Convert country and status to factors*

df\_clean$country <- as\_factor(df\_clean$country)

df\_clean$status <- as\_factor(df\_clean$status)

*# Run correlations and save output as images to be used in the appendix.*

ggcorr(

df\_clean,

label = TRUE,

label\_alpha = TRUE,

label\_size = 3,

layout.exp = 2,

cex = 3.5,

hjust = 1

)

*# ggsave(here::here("images", "correlation 1.png"))*

df\_clean %>%

select(-c(under\_five\_deaths, gdp, thinness\_1\_19\_years)) %>%

ggcorr(

label = TRUE,

label\_alpha = TRUE,

label\_size = 3,

layout.exp = 2,

cex = 3.5,

hjust = 1

)

*# ggsave(here::here("images", "correlation 2.png"))*

df\_clean %>%

select(-c(under\_five\_deaths, gdp, thinness\_1\_19\_years, population)) %>%

ggcorr(

label = TRUE,

label\_alpha = TRUE,

label\_size = 3,

layout.exp = 2,

cex = 3.5,

hjust = 1

)

*# ggsave(here::here("images", "correlation 3.png"))*

df\_clean <- df\_clean %>%

select(-c(under\_five\_deaths, gdp, thinness\_1\_19\_years, population))

*# Check for missing values*

tibble(variable = names(colSums(is.na(df\_clean))),

missing = colSums(is.na(df\_clean))) %>%

gt() %>%

tab\_header(title = "Missing Values in Data") %>%

*# gtsave(here::here("images", "missing-1.png")) %>%*

{.}

*# Check which countries have NA rows for life expectancy*

as\_tibble(df\_clean$country[which(is.na(df\_clean$life\_expectancy))])

*# Drop all rows where life expectancy is NA*

df\_clean <- df\_clean %>%

filter(!is.na(life\_expectancy))

*# Recheck missing value counts*

tibble(variable = names(colSums(is.na(df\_clean))),

missing = colSums(is.na(df\_clean))) %>%

gt() %>%

tab\_header(title = "Missing Values in Data") %>%

*# gtsave(here::here("images", "missing-2.png")) %>%*

{.}

*# Look at how many missing hepatitis measurements there are by country*

df\_clean %>%

group\_by(country) %>%

count(missing = is.na(hepatitis\_b)) %>%

filter(missing == TRUE) %>%

select(-missing) %>%

rename(missing = n) %>%

arrange(desc(missing))

*# Visualize the relationship to see if it looks significant*

df\_clean %>%

ggplot(aes(x = hepatitis\_b, y = life\_expectancy)) +

geom\_jitter(alpha = 0.3) +

geom\_smooth() +

labs(title = "Hepatitis B vs. Life Expectancy",

x = "Hepatitis B",

y = "Life Expectancy")

*# ggsave(here::here("images", "hepatitis-lifeexp.png"))*

*# Drop hepatitis B variable*

df\_interp <- df\_clean %>%

select(-hepatitis\_b)

*# Drop remaining rows with NA's for the interpretable model*

df\_interp <- na.omit(df\_interp)

*# Final check of missing values*

tibble(variable = names(colSums(is.na(df\_interp))),

missing = colSums(is.na(df\_interp))) %>%

gt() %>%

*# gtsave(here::here("images", "missing-3.png")) %>%*

{.}

df\_interp %>% count(year)

df\_interp <- df\_interp %>% filter(year %**in**% 2011:2014)

*# Set the maximum number of variables to consider in the model. Although the*

*# model can handle up to 20, the more we add, the less interpretable the final*

*# model will be.*

consider <- 17

*# Fit the model. We'll remove country, but keep it in the data set for*

*# interpretation.*

regfit\_full <-

regsubsets(life\_expectancy ~ .,

df\_interp[, -1],

nvmax = consider)

*# Store the regression summary*

reg\_summary <- summary(regfit\_full)

*# Look at the names of reg\_summary*

names(reg\_summary)

*# What are the R-squared values?*

reg\_summary$rsq

par(mfrow = c(2, 2))

plot(reg\_summary$rss,

xlab = "Number of Variables",

ylab = "RSS",

type = "l")

plot(reg\_summary$adjr2,

xlab = "Number of Variables",

ylab = "Adjusted RSq",

type = "l")

*# which.max(reg\_summary$adjr2)*

points(

11,

reg\_summary$adjr2[which.max(reg\_summary$adjr2)],

col = "red",

cex = 2,

pch = 20

)

plot(reg\_summary$cp,

xlab = "Number of Variables",

ylab = "Cp",

type = "l")

*# which.min(reg\_summary$cp)*

points(

9,

reg\_summary$cp[which.min(reg\_summary$cp)],

col = "red",

cex = 2,

pch = 20

)

plot(reg\_summary$bic,

xlab = "Number of Variables",

ylab = "BIC",

type = "l")

*# which.min(reg\_summary$bic)*

points(

5,

reg\_summary$bic[which.min(reg\_summary$bic)],

col = "red",

cex = 2,

pch = 20

)

plot(regfit\_full, scale = "r2")

plot(regfit\_full, scale = "adjr2")

plot(regfit\_full, scale = "Cp")

plot(regfit\_full, scale = "bic")

coef(regfit\_full, 5)

*# Forward*

regfit\_fwd <-

regsubsets(

life\_expectancy ~ .,

data = df\_interp[,-1],

nvmax = 17,

method = "forward"

)

*# summary(regfit\_fwd)*

*# Backward*

regfit\_bwd <-

regsubsets(

life\_expectancy ~ .,

data = df\_interp[,-1],

nvmax = 17,

method = "backward"

)

*# summary(regfit\_bwd)*

*# How many variables do we want to use?*

x <- 4

*# Compare coefficients*

tibble(

variables = names(coef(regfit\_full, x)),

full = round(coef(regfit\_full, x), 4),

fwd = round(coef(regfit\_fwd, x), 4),

bwd = round(coef(regfit\_bwd, x), 4)

) %>%

gt()

*# Set seed*

set.seed(123)

*# Build test and training data sets, dropping country from regfit\_best &*

*# test\_mat because I was getting a warning that 1 linear dependencies found*

train <- sample(c(TRUE, FALSE), nrow(df\_interp), rep = TRUE)

test <- (!train)

regfit\_best <- regsubsets(life\_expectancy ~ ., data = df\_interp[train, -1])

test\_mat <- model.matrix(life\_expectancy ~ ., data = df\_interp[test, -1])

*# Run a loop, and for each size `i`, extract the coefficients from `regfit\_best`*

*# for the best model of that size, multiply them into the appropriate columns of*

*# the test model matric to form the predictions, and compute the test MSE.*

val\_errors <- rep(NA, 8)

**for** (i **in** 1:8) {

coefi <- coef(regfit\_best, id = i)

pred <- test\_mat[, names(coefi)] %\*% coefi

val\_errors[i] <- mean((df\_interp$life\_expectancy[test] - pred)^2)

}

*# Find the best model*

val\_errors

coef(regfit\_best, which.min(val\_errors))

*# Write a prediction function*

predict\_regsubsets <- **function**(object, newdata, id, **...**) {

form <- as.formula(object$call[[2]])

mat <- model.matrix(form, newdata)

coefi <- coef(object, id = id)

xvars <- names(coefi)

mat[, xvars] %\*% coefi

}

*# Perform best subset selection on the full data set, and select the best model.*

regfit\_best <- regsubsets(life\_expectancy ~ ., data = df\_interp[,-1])

coef(regfit\_best, which.min(val\_errors))

k <- 10

set.seed(123)

folds <- sample(1:k, nrow(df\_interp), replace = TRUE)

cv\_errors <- matrix(NA, k, consider, dimnames = list(NULL, paste(1:consider)))

predict.regsubsets <- **function**(object, newdata, id, **...**) {

form <- as.formula(object$call[[2]])

mat <- model.matrix(form, newdata)

coefi <- coef(object, id = id)

mat[, names(coefi)] %\*% coefi

}

*# Perform cross-validation*

**for** (j **in** 1:k) {

best\_fit <-

regsubsets(life\_expectancy ~ ., data = df\_interp[folds != j, -1], nvmax = consider)

**for** (i **in** 1:15) {

pred <- predict(best\_fit, df\_interp[folds == j, -1], id = i)

cv\_errors[j, i] <-

mean((df\_interp$life\_expectancy[folds == j] - pred) ^ 2)

}

}

*# Use the apply function to average over the columns of the matrix in order to*

*# obtain a vector for which the jth element is the cross-validation error for*

*# the j-variable model.*

mean\_cv\_errors <- apply(cv\_errors, 2, mean)

mean\_cv\_errors

par(mfrow = c(1, 1))

plot(mean\_cv\_errors, type = "b")

*# Perform best subset selection on the full data set in order to obtain the*

*# variables for the final model*

reg\_best <- regsubsets(life\_expectancy ~ ., data = df\_interp[, -1])

coef(reg\_best, 4) *# the number sets the number of variables we want*

*# Build the final model using the best subset selection results*

final\_model <-

lm(

life\_expectancy ~ adult\_mortality +

total\_expenditure +

hiv\_aids +

income\_composition\_of\_resources,

data = df\_interp

)

*# Final model summary*

final\_model\_summary <- summary(final\_model)

final\_model\_summary

*# Confidence intervals*

confint(final\_model)

par(mfrow = c(1, 1))

plot(

final\_model$fitted.values,

df\_interp$life\_expectancy,

xlab = "Predicted",

ylab = "Life Expectancy"

)

lines(c(0, 90), c(0, 90), col = "red")

par(mfrow=c(2,2))

plot(final\_model)

par(mfrow = c(1, 2))

test.model <- lm(life\_expectancy ~ ., df\_interp[, -1])

plot(test.model$fitted.values,

test.model$residuals,

xlab = "Fitted Values",

ylab = "Residuals")

plot(df\_interp$life\_expectancy,

test.model$residuals,

xlab = "Life Expectancy",

ylab = "Residuals")

*# Remove all rows with an NA*

*# df\_clean <- na.omit(df\_clean)*

*# sum(is.na(df\_clean))*

*# Maximum number of variables to consider*

consider <- 4

*# Fit model*

regfit\_full <- regsubsets(life\_expectancy ~ ., df\_clean[,-1], nvmax = consider)

*# Examine regression summary*

reg\_summary <- summary(regfit\_full)

names(reg\_summary)

reg\_summary$rsq

*# Plot RSS, adjusted $R^2$ $C\_p$ and BIC for all models*

par(mfrow = c(2, 2))

plot(reg\_summary$rss, xlab = "Number of Variables", ylab = "RSS", type = "l")

plot(reg\_summary$adjr2, xlab = "Number of Variables", ylab = "Adjusted RSq", type = "l")

which.max(reg\_summary$adjr2)

points(consider, reg\_summary$adjr2[consider], col = "red", cex = 2, pch = 20)

plot(reg\_summary$cp, xlab = "Number of Variables", ylab = "Cp", type = "l")

which.min(reg\_summary$cp)

points(consider, reg\_summary$cp[consider], col = "red", cex = 2, pch = 20)

which.min(reg\_summary$bic)

plot(reg\_summary$bic, xlab = "Number of Variables", ylab = "BIC", type = "l")

points(consider, reg\_summary$bic[consider], col = "red", cex = 2, pch = 20)

*# Display selected variables for the best model with a given number of predictors*

plot(regfit\_full, scale = "r2")

plot(regfit\_full, scale = "adjr2")

plot(regfit\_full, scale = "Cp")

plot(regfit\_full, scale = "bic")

coef(regfit\_full, consider)

*# Forward*

regfit\_fwd <- regsubsets(life\_expectancy ~ ., data = df\_clean, method = "forward")

summary(regfit\_fwd)

*# Backward*

regfit\_bwd <- regsubsets(life\_expectancy ~ ., data = df\_clean, method = "backward")

summary(regfit\_bwd)

*# Compare coefficients*

coef(regfit\_full, consider)

coef(regfit\_fwd, consider)

coef(regfit\_bwd, consider)

*# Build test and training data sets*

set.seed(100)

index = sample(1:nrow(df\_clean), 0.7\*nrow(df\_clean))

train = df\_clean[index,] *# Create the training data*

test = df\_clean[-index,] *# Create the test data*

dim(train)

dim(test)

regfit\_best <- regsubsets(life\_expectancy ~ ., data = df\_clean[, -1])

test\_mat <- model.matrix(life\_expectancy ~ ., data = df\_clean)

*#standardize the data by scaling the numeric variables*

*# MF: commenting out gdp, but it had been previously removed*

cols = c(

'alcohol',

'hepatitis\_b',

'measles',

'bmi',

'polio',

'diphtheria',

'hiv\_aids',

*# 'gdp',*

'thinness\_5\_9\_years',

'schooling'

)

pre\_proc\_val <- preProcess(train[,cols], method = c("center", "scale"))

train[,cols] = predict(pre\_proc\_val, train[,cols])

test[,cols] = predict(pre\_proc\_val, test[,cols])

summary(train)

*#check for multicolinearity*

*#note the highly correlated variables*

*# MF: the Performance Analytics package is required for chart.Correlation. Also,*

*# the original my\_data object contains status which, as a non-numeric value*

*# appears to be giving an error. I'm going to remove both it and country and see*

*# if that fixes things.*

*# my\_data <- train[, c(1-2)]*

my\_data <- train[, -c(1:3)]

PerformanceAnalytics::chart.Correlation(my\_data, histogram=TRUE, pch=19)

*#Checking the VIF*

Auto<-train[,-1]

*# MF: the full.model call below was giving me an error that "there are aliased*

*# coeffifients in the model. I again removed country, year and status and it*

*# seems to now run.*

*# full.model<-lm(life\_expectancy~.,data=train)*

full.model<-lm(life\_expectancy~.,data=train[, -c(1:3)])

vif(full.model)

*# Build the final model using the best subset selection results*

*# MF: I commented out gdp since we'd originally excluded it from df\_clean*

final\_model <-

lm(

life\_expectancy ~ status +

alcohol +

bmi +

diphtheria +

hiv\_aids +

*# gdp +*

schooling,

data = train

)

*# Final model summary*

summary(final\_model)

**library**(glmnet)

*#Step 1 - create the evaluation metrics function*

eval\_metrics = **function**(model, df, predictions, target){

resids = df[,target] - predictions

resids2 = resids\*\*2

N = length(predictions)

r2 = as.character(round(summary(model)$r.squared, 2))

adj\_r2 = as.character(round(summary(model)$adj.r.squared, 2))

print(adj\_r2) *#Adjusted R-squared*

print(as.character(round(sqrt(sum(resids2)/N), 2))) *#RMSE*

}

*#this is out best training model that we will use for prediction*

*#Step 3 - predicting and evaluating the model on train data*

predictions = predict(final\_model, newdata = train)

eval\_metrics(final\_model, train, predictions, target = 'life\_expectancy')

*# Step 4 - predicting and evaluating the model on test data*

predictions = predict(final\_model, newdata = test)

eval\_metrics(final\_model, test, predictions, target = 'life\_expectancy')

*#lasso*

*#will use lib glmet*

*#glmnet does not work with numeric data frames*

*#Step 1 -> we will create a numeric matrix for the training*

*# MF: commenting out gdp again*

cols\_reg = c(

'life\_expectancy',

'alcohol',

'hepatitis\_b',

'measles',

'bmi',

'polio',

'diphtheria',

'hiv\_aids',

*# 'gdp',*

'thinness\_5\_9\_years',

'schooling'

)

dummies <- dummyVars(life\_expectancy ~ ., data = df\_clean[,cols\_reg])

train\_dummies = predict(dummies, newdata = train[,cols\_reg])

test\_dummies = predict(dummies, newdata = test[,cols\_reg])

print(dim(train\_dummies)); print(dim(test\_dummies))

lambdas <- 10^seq(2, -3, by = -.1)

*#create the training data matrices for x and y*

x = as.matrix(train\_dummies)

y\_train = train$life\_expectancy

x\_test = as.matrix(test\_dummies)

y\_test = test$life\_expectancy

*# Setting alpha = 1 implements lasso regression*

lasso\_reg <- cv.glmnet(x, y\_train, alpha = 1, lambda = lambdas, standardize = TRUE, nfolds = 5)

*# Best optimal lambda*

lambda\_optimal <- lasso\_reg$lambda.min

lambda\_optimal *#will give the best optimal value*

*#let's train the lasso model*

lasso\_model <- glmnet(x, y\_train, alpha = 1, lambda = lambda\_optimal, standardize = TRUE)

*#let's make predictions for both test and training*

*#also view the evaluation metrics*

*# Compute R^2 from true and predicted values*

eval\_results <- **function**(true, predicted, df) {

SSE <- sum((predicted - true)^2)

SST <- sum((true - mean(true))^2)

R\_square <- 1 - SSE / SST

RMSE = sqrt(SSE/nrow(df))

*# Model performance metrics*

data.frame(

RMSE = RMSE,

Rsquare = R\_square

)

}

*#predictions*

predictions\_train <- predict(lasso\_model, s = lambda\_best, newx = x)

eval\_results(y\_train, predictions\_train, train)

predictions\_test <- predict(lasso\_model, s = lambda\_best, newx = x\_test)

eval\_results(y\_test, predictions\_test, test)

*# Check for missing values*

tibble(variable = names(colSums(is.na(df\_clean))),

missing = colSums(is.na(df\_clean))) %>%

gt()

*#Visualize the relationship to see if it looks significant (plot again)*

*# hepatitis b*

df\_clean %>%

ggplot(aes(x = hepatitis\_b, y = life\_expectancy)) +

geom\_jitter(alpha = 0.3) +

geom\_smooth() +

labs(title = "Relationship of Hepatitis B and Life Expectancy",

x = "Hepatitis B",

y = "Life Expectancy") +

theme\_ipsum()

*# ggsave(here::here("images", "pred-mod-hepb.png"))*

*# total expenditure*

df\_clean %>%

ggplot(aes(x = total\_expenditure, y = life\_expectancy)) +

geom\_jitter(alpha = 0.3) +

geom\_smooth() +

labs(title = "Relationship of Total Expenditure and Life Expectancy",

x = "Total Expenditure",

y = "Life Expectancy") +

theme\_ipsum()

*# ggsave(here::here("images", "pred-mod-expen.png"))*

*# alcohol*

df\_clean %>%

ggplot(aes(x = alcohol, y = life\_expectancy)) +

geom\_jitter(alpha = 0.3) +

geom\_smooth() +

labs(title = "Relationship of Alcohol and Life Expectancy",

x = "Alcohol",

y = "Life Expectancy") +

theme\_ipsum()

*# ggsave(here::here("images", "pred-mod-alcohol.png"))*

*# income composition of resources*

df\_clean %>%

ggplot(aes(x = income\_composition\_of\_resources, y = life\_expectancy)) +

geom\_jitter(alpha = 0.3) +

geom\_smooth() +

labs(title = "Relationship of Income Composition of Resources\nand Life Expectancy",

x = "Income Composition of Resources",

y = "Life Expectancy") +

theme\_ipsum()

*# ggsave(here::here("images", "pred-mod-inc-comp.png"))*

*# schooling*

df\_clean %>%

ggplot(aes(x = schooling, y = life\_expectancy)) +

geom\_jitter(alpha = 0.3) +

geom\_smooth() +

labs(title = "Relationship of Schooling and Life Expectancy",

x = "Schooling",

y = "Life Expectancy") +

theme\_ipsum()

*# ggsave(here::here("images", "pred-mod-school.png"))*

*#remove hepatitis b and total\_expenditure*

df\_predict <- df\_clean %>%

select(-c(hepatitis\_b, total\_expenditure, alcohol))

*#remove the remaining NA's*

df\_predict <- na.omit(df\_predict)

*#check for NA's*

tibble(variable = names(colSums(is.na(df\_predict))),

missing = colSums(is.na(df\_predict))) %>%

gt()

*#replot after removing Na's*

*# income composition of resources*

df\_predict %>%

ggplot(aes(x = income\_composition\_of\_resources, y = life\_expectancy)) +

*# geom\_point() +*

geom\_jitter(alpha = 0.3) +

geom\_smooth() +

labs(title = "Relationship of Income Composition of Resources\nand Life Expectancy",

x = "Income Composition of Resources",

y = "Life Expectancy") +

theme\_ipsum()

*# schooling*

df\_predict %>% ggplot(aes(x = schooling, y = life\_expectancy)) +

*# geom\_point() +*

geom\_jitter(alpha = 0.3) +

geom\_smooth() +

labs(title = "Relationship of Schooling and Life Expectancy",

x = "Schooling",

y = "Life Expectancy") +

theme\_ipsum()

**library**(glmnet)

*# Ridge regression and lasso require the format 'x matrix' and 'y'. The*

*# model.matrix() function produces a matrix and automatically transforms*

*# qualitative variables into dummy variables.*

x <- model.matrix(life\_expectancy ~ ., df\_predict[,-1])[, -1]

y <- df\_predict$life\_expectancy

*# Run ridge regression*

ridge\_mod <- glmnet(x, y, alpha = 0)

dim(coef(ridge\_mod))

*# Split data into training and testing sets*

set.seed(1)

train <- sample(1:nrow(x), nrow(x)/2)

test <- (-train)

y\_test <- y[test]

*# Fit a ridge regression model on the training set, and evaluate its MSE on the*

*# test set*

ridge\_mod <- glmnet(x[train, ], y[train], alpha = 0)

ridge\_pred <- predict(ridge\_mod, s = 4, newx = x[test, ])

mean((ridge\_pred - y\_test) ^ 2)

*#[1] 17.4224*

*# The test MSE is 17.4224. If we had simply fit a model with just an intercept,*

*# we would have observed each test observation using the mean of the training*

*# observations. In that case, we could compute the test set MSE like this:*

mean((mean(y[train]) - y\_test) ^ 2)

*#[1] 89.45262*

*# We could also get the same result by fitting a ridge regression model with a*

*# very large value of ƛ.*

ridge\_pred <- predict(ridge\_mod, s = 1e10, newx = x[test, ])

mean((ridge\_pred - y\_test) ^ 2)

*#[1] 89.45262*

*# Use cross-validation to choose the tuning parameter ƛ.*

set.seed(1)

cv\_out <- cv.glmnet(x[train, ], y[train], alpha = 0)

plot(cv\_out)

bestlambda <- cv\_out$lambda.min

bestlambda

*# What is the test MSE associated with bestlambda?*

ridge\_pred <- predict(ridge\_mod, s = bestlambda, newx = x[test, ])

mean((ridge\_pred - y\_test) ^ 2)

*#[1] 16.2937*

*# Refit the ridge regression model on the full data set using the value of ƛ*

*# chosen by cross-validation*

out <- glmnet(x, y, alpha = 0)

predict(out, type = "coefficients", s = bestlambda)[1:14,]

*# Fit the lasso model*

lasso\_mod <- glmnet(x[train, ], y[train], alpha = 1)

*# Plot the lasso model*

plot\_glmnet(lasso\_mod)

*# Run cross-validation and compute the associated test error*

set.seed(1)

cv\_out <- cv.glmnet(x[train, ], y[train], alpha = 1)

plot(cv\_out)

bestlambda <- cv\_out$lambda.min

lasso\_pred <- predict(lasso\_mod, s = bestlambda, newx = x[test, ])

mean((lasso\_pred - y\_test) ^ 2)

*#[1] 16.41776*

*# Compute lasso coefficients*

out <- glmnet(x, y, alpha = 1)

lasso\_coef <- predict(out, type = "coefficients", s = bestlambda)[1:14,]

lasso\_coef[lasso\_coef != 0]

*#plot distributions*

df\_plot <- as.data.frame(df\_clean)

**for** (col **in** 5:ncol(df\_plot)) {

hist(df\_plot[,col], main=names(df\_plot[col]))

}

*# Copy the data*

df\_predict2 <- df\_clean %>%

select(-c(hepatitis\_b))

*# Impute the data set*

df\_predict2 <- df\_predict2 %>%

mutate(across(

c(polio, total\_expenditure, diphtheria),

~ replace\_na(., median(.x, na.rm = TRUE))

)) %>%

mutate(across(

c(bmi, income\_composition\_of\_resources, schooling),

~ replace\_na(., mean(.x, na.rm = TRUE))

)) %>%

mutate(across(

c(alcohol, thinness\_5\_9\_years),

~ replace\_na(., 0)

))

*#check for NA's*

tibble(variable = names(colSums(is.na(df\_predict2))),

missing = colSums(is.na(df\_predict2))) %>%

gt()

*# Ridge regression and lasso require the format 'x matrix' and 'y'. The*

*# model.matrix() function produces a matrix and automatically transforms*

*# qualitative variables into dummy variables.*

sum(is.na(df\_predict2))

x2 <- model.matrix(life\_expectancy ~ ., df\_predict2[,-1])[, -1]

y2 <- df\_predict2$life\_expectancy

*# Run ridge regression*

ridge\_mod2 <- glmnet(x2, y2, alpha = 0)

dim(coef(ridge\_mod2))

*# Split data into training and testing sets*

set.seed(1)

train2 <- sample(1:nrow(x2), nrow(x2)/2)

test2 <- (-train2)

y\_test2 <- y2[test2]

*# Fit a ridge regression model on the training set, and evaluate its MSE on the*

*# test set*

ridge\_mod2 <- glmnet(x2[train2,], y2[train2], alpha = 0)

ridge\_pred2 <- predict(ridge\_mod2, s = 4, newx = x2[test2, ])

mean((ridge\_pred2 - y\_test2) ^ 2)

*#[1] 19.39197*

*# The test MSE is 19.39197. If we had simply fit a model with just an intercept,*

*# we would have observed each test observation using the mean of the training*

*# observations. In that case, we could compute the test set MSE like this:*

mean((mean(y2[train2]) - y\_test2) ^ 2)

*#[1] 88.25497*

*# Use cross-validation to choose the tuning parameter ƛ.*

set.seed(1)

cv\_out2 <- cv.glmnet(x2[train2, ], y2[train2], alpha = 0)

plot(cv\_out2)

bestlambda2 <- cv\_out2$lambda.min

bestlambda2

*#[1] 0.6900917*

*# What is the test MSE associated with bestlambda?*

ridge\_pred2 <- predict(ridge\_mod2, s = bestlambda2, newx = x2[test2, ])

mean((ridge\_pred2 - y\_test2) ^ 2)

*#[1] 18.68608*

*# Refit the ridge regression model on the full data set using the value of ƛ*

*# chosen by cross-validation*

out2 <- glmnet(x2, y2, alpha = 0)

predict(out2, type = "coefficients", s = bestlambda2)[1:14,]

*# Fit the lasso model*

lasso\_mod2 <- glmnet(x2[train2, ], y2[train2], alpha = 1)

*# Plot the lasso model*

plot\_glmnet(lasso\_mod2)

*# Run cross-validation and compute the associated test error*

set.seed(1)

cv\_out2 <- cv.glmnet(x2[train2, ], y2[train2], alpha = 1)

plot(cv\_out2)

bestlambda2 <- cv\_out2$lambda.min

lasso\_pred2 <- predict(lasso\_mod2, s = bestlambda2, newx = x2[test2, ])

mean((lasso\_pred2 - y\_test2) ^ 2)

*#[1] 18.74681*

*# Compute lasso coefficients*

out2 <- glmnet(x2, y2, alpha = 1)

lasso\_coef2 <- predict(out2, type = "coefficients", s = bestlambda2)[1:14,]

lasso\_coef2[lasso\_coef2 != 0]

*# Fit the lasso model with data set including country*

x3 <- model.matrix(life\_expectancy ~ ., df\_predict2)[, -1]

y3 <- df\_predict2$life\_expectancy

*# Split data into training and testing sets*

set.seed(1)

train3 <- sample(1:nrow(x3), nrow(x3)/2)

test3 <- (-train3)

y\_test3 <- y3[test3]

lasso\_mod3 <- glmnet(x3[train3, ], y3[train3], alpha = 1)

*# Plot the lasso model*

plot\_glmnet(lasso\_mod3)

*# Run cross-validation and compute the associated test error*

set.seed(1)

cv\_out3 <- cv.glmnet(x3[train3, ], y3[train3], alpha = 1)

plot(cv\_out3)

bestlambda3 <- cv\_out3$lambda.min

lasso\_pred3 <- predict(lasso\_mod3, s = bestlambda3, newx = x3[test3, ])

mean((lasso\_pred3 - y\_test3) ^ 2)

*#[1] 18.74681*

*# Compute lasso coefficients*

out3 <- glmnet(x3, y3, alpha = 1)

lasso\_coef3 <- predict(out3, type = "coefficients", s = bestlambda3)[1:14,]

lasso\_coef3[lasso\_coef3 != 0]

*#build a linear model using the top 3 variables from LASSO along with country for both imputed data set and removed NA data set*

*# Build the final model using the best subset selection results on the imputed data set*

predict\_model1 <-

lm(

life\_expectancy ~

country +

income\_composition\_of\_resources +

status +

schooling +

hiv\_aids,

data = df\_predict2

)

*# Final model summary*

predict\_model1\_sum <- summary(predict\_model1)

predict\_model1\_sum

*# Get MSE*

mean(predict\_model1\_sum$residuals ^ 2)

*#[1] 4.39226*

*# Build the final model using the best subset selection results on removed NA data set*

predict\_model2 <-

lm(

life\_expectancy ~

country +

income\_composition\_of\_resources +

status +

schooling +

hiv\_aids,

data = df\_predict

)

*# Final model summary*

predict\_model2\_sum <- summary(predict\_model2)

predict\_model2\_sum

*# Get MSE*

mean(predict\_model2\_sum$residuals ^ 2)

*#[1] 4.189329*

par(mfrow = c(1, 1))

plot(

predict\_model2$fitted.values,

df\_predict$life\_expectancy,

xlab = "Predicted Life Expectancy",

ylab = "Actual Life Expectancy"

)

lines(c(0, 90), c(0, 90), col = "red")

par(mfrow=c(2,2))

plot(predict\_model2)

*#copy and rename imputed data set for KNN models*

df\_knn <- df\_predict2

*#Make new data set that does not impute values for comparison*

df\_knn2 <- df\_clean %>% select(-c(hepatitis\_b))

df\_knn2 <- drop\_na(df\_knn2)

*# Set seed*

set.seed(123)

*# Standardize the data to prep for KNN first - everything except life expectancy*

preProcValues <- preProcess(df\_knn[, -4], method = c("scale"))

df\_knn\_standard <- predict(preProcValues, df\_knn)

*# Split training/test data sets*

inTraining <-

createDataPartition(df\_knn\_standard$life\_expectancy,

p = 0.75,

list = FALSE)

knn\_train <- df\_knn\_standard[inTraining, ]

knn\_test <- df\_knn\_standard[-inTraining, ]

*# Perform same splits for data with NA's removed*

*# Standardize the data to prep for KNN first - everything except life expectancy*

preProcValues\_2 <- preProcess(df\_knn2[, -4], method = c("scale"))

df\_knn\_standard2 <- predict(preProcValues\_2, df\_knn2)

*# Split training/test data sets*

inTraining2 <-

createDataPartition(df\_knn\_standard2$life\_expectancy,

p = 0.75,

list = FALSE)

knn\_train\_na <- df\_knn\_standard2[inTraining2, ]

knn\_test\_na <- df\_knn\_standard2[-inTraining2, ]

*# Set seed*

set.seed(567)

*# Set train control: 5 repeat, 10-fold CV*

ctrl <-

trainControl(

method = "repeatedcv",

number = 10, *# 10-fold CV*

repeats = 5, *#repeat 5 times*

returnResamp = "all" *#return all metrics*

)

*# Run everything with the train control above*

knnFit <-

train(

life\_expectancy ~ .,

data = knn\_train,

method = "knn",

trControl = ctrl,

tuneLength = 10 *#run for 10 different k's*

)

knnFit

*# Check the metrics on the test set*

Predictions\_knn5 <- predict(knnFit, newdata = knn\_test)

ASE\_knn5 <- mean((Predictions\_knn5 - knn\_test$life\_expectancy)^2)

ASE\_knn5

*# Performance measurement*

postResample(knn\_test$life\_expectancy, Predictions\_knn5)

*# Plotting*

plot(knnFit, main = "knnFit Results")

plot(knnFit, metric = "Rsquared", main = "knnFit Results (R-Squared)")

plot(knnFit, metric = "MAE", main = "knnFit Results (MAE)")

*# Try another knn with a k value of less than 5*

knnFit2 <-

train(

life\_expectancy ~ .,

data = knn\_train,

method = "knn",

trControl = ctrl,

tuneGrid = expand.grid(k = c(1, 3, 5)) *#run only with k = 1, 3, 5*

)

knnFit2

*# Check the metrics on the test set*

Predictions\_knn3 <- predict(knnFit2, newdata = knn\_test)

ASE\_knn3 <- mean((Predictions\_knn3 - knn\_test$life\_expectancy)^2)

ASE\_knn3

*# Performance measurement*

postResample(knn\_test$life\_expectancy, Predictions\_knn3)

*# Plotting*

plot(knnFit2, main = "knnFit2 Results")

plot(knnFit2, metric = "Rsquared", main = "knnFit2 Results (R-Squared)")

plot(knnFit2, metric = "MAE", main = "knnFit2 Results (MAE)")

*# Run knn on data set with NA's removed*

knnFit\_na <-

train(

life\_expectancy ~ .,

data = knn\_train\_na,

method = "knn",

trControl = ctrl,

tuneLength = 10 *#run through 10 different k's*

)

knnFit\_na

*# Check the metrics on the test set*

Predictions\_knn\_na <- predict(knnFit\_na, newdata = knn\_test\_na)

ASE\_knn\_na <- mean((Predictions\_knn\_na - knn\_test\_na$life\_expectancy)^2)

ASE\_knn\_na

*# Performance measurement*

postResample(knn\_test\_na$life\_expectancy, Predictions\_knn\_na)

knnFit3 <-

train(

life\_expectancy ~ adult\_mortality +

total\_expenditure +

hiv\_aids +

income\_composition\_of\_resources,

data = knn\_train,

method = "knn",

trControl = ctrl,

tuneLength = 10

)

knnFit3

*#check metrics on test set*

Predictions\_knnfit3 <- predict(knnFit3,newdata=knn\_test)

*#performance measurement*

postResample(knn\_test$life\_expectancy,Predictions\_knnfit3)

ASE\_knn3 <- mean((Predictions\_knnfit3 - knn\_test$life\_expectancy)^2)

ASE\_knn3

plot(knnFit3)

plot(knnFit3, metric = "Rsquared")

plot(knnFit3, metric = "MAE")

*# Split training/test data sets - round 2*

set.seed(1)

inTraining\_x <-

createDataPartition(df\_knn\_standard$life\_expectancy,

p = 0.75,

list = FALSE)

knn\_train\_x <- df\_knn\_standard[inTraining\_x, ]

knn\_test\_x <- df\_knn\_standard[-inTraining\_x, ]

*# Run everything with the train control above*

knnFit\_x <-

train(

life\_expectancy ~ .,

data = knn\_train\_x,

method = "knn",

trControl = ctrl,

tuneLength = 10

)

knnFit\_x

*# Check the metrics on the test set*

Predictions\_knnFit\_x <- predict(knnFit\_x, newdata = knn\_test\_x)

ASE\_x <- mean((Predictions\_knnFit\_x - knn\_test\_x$life\_expectancy)^2)

ASE\_x

*# Performance measurement*

postResample(knn\_test\_x$life\_expectancy, Predictions\_knnFit\_x)

*# Plotting*

plot(knnFit\_x, main = "knnFit Results")

plot(knnFit\_x, metric = "Rsquared", main = "knnFit Results (R-Squared)")

plot(knnFit\_x, metric = "MAE", main = "knnFit Results (MAE)")

*# Try another knn with a k value of less than 5*

knnFit2\_x <-

train(

life\_expectancy ~ .,

data = knn\_train\_x,

method = "knn",

trControl = ctrl,

tuneGrid = expand.grid(k = c(1, 3, 5))

)

knnFit2\_x

*# Check the metrics on the test set*

Predictions\_knnFit2\_x <- predict(knnFit2\_x, newdata = knn\_test\_x)

ASE\_x <- mean((Predictions\_knnFit2\_x - knn\_test\_x$life\_expectancy)^2)

ASE\_x

*# Performance measurement*

postResample(knn\_test\_x$life\_expectancy, Predictions\_knnFit2\_x)

*# Plotting*

plot(knnFit2\_x, main = "knnFit2 Results")

plot(knnFit2\_x, metric = "Rsquared", main = "knnFit2 Results (R-Squared)")

plot(knnFit2\_x, metric = "MAE", main = "knnFit2 Results (MAE)")

knnFit3\_x <-

train(

life\_expectancy ~ adult\_mortality +

total\_expenditure +

hiv\_aids +

income\_composition\_of\_resources,

data = knn\_train\_x,

method = "knn",

trControl = ctrl,

tuneLength = 10

)

knnFit3\_x

*# Check the metrics on the test set*

Predictions\_knnFit3\_x <- predict(knnFit3\_x, newdata = knn\_test\_x)

ASE\_3x <- mean((Predictions\_knnFit3\_x - knn\_test\_x$life\_expectancy)^2)

ASE\_3x

*# Performance measurement*

postResample(knn\_test\_x$life\_expectancy, Predictions\_knnFit3\_x)

*# Plotting*

plot(knnFit3\_x, main = "knnFit2 Results")

plot(knnFit3\_x, metric = "Rsquared", main = "knnFit2 Results (R-Squared)")

plot(knnFit3\_x, metric = "MAE", main = "knnFit2 Results (MAE)")

*# Set seed*

set.seed(123)

*# Split training/test data sets*

inTraining <- createDataPartition(df\_knn$life\_expectancy, p = 0.75, list = FALSE)

tree\_train <- df\_knn[inTraining,]

tree\_test <- df\_knn[-inTraining,]

*# Remove country because this tree function has a maximum of 32 levels*

tree1 <- tree(life\_expectancy ~ ., data = tree\_train[, -1])

summary(tree1)

plot(tree1)

mean((tree1$y - tree\_train$life\_expectancy) ^ 2)

*# Check tree performance*

cv.tree1 <- cv.tree(tree1)

plot(cv.tree1$size, cv.tree1$dev, type = 'b')

*# Check the predictions*

yhat = predict(tree1, newdata = tree\_test[, -1])

plot(yhat, tree\_test$life\_expectancy)

abline(0, 1)

mean((yhat - tree\_test$life\_expectancy) ^ 2)

*# Try a random forest compared to a single tree model*

set.seed(1)

*# Remove country again*

rfFit <- randomForest(life\_expectancy ~ ., data = tree\_train[, -1])

rfFit

*# Test using all predictors for each tree*

set.seed(1)

*# Have to remove country again - using top 4 predictors*

rfFit2 <- randomForest(life\_expectancy ~ adult\_mortality +

total\_expenditure +

hiv\_aids +

income\_composition\_of\_resources, data = tree\_train[,-1])

rfFit2

*#compare y-hat for the two random forest models*

yhat.rf <- predict(rfFit, newdata = tree\_test[, -1])

yhat.rf2 <- predict(rfFit2, newdata = tree\_test[, -1])

*# Performance measurement*

postResample(tree\_test$life\_expectancy, yhat.rf)

postResample(tree\_test$life\_expectancy, yhat.rf2)

ASE\_rf <- mean((yhat.rf - tree\_test$life\_expectancy)^2)

ASE\_rf

ASE\_rf2 <- mean((yhat.rf2 - tree\_test$life\_expectancy)^2)

ASE\_rf2

plot(yhat.rf, tree\_test$life\_expectancy)

abline(0,1)

plot(yhat.rf2,tree\_test$life\_expectancy)

abline(0,1)

*# Set seed*

set.seed(1)

*# Split training/test data sets*

inTraining\_t <- createDataPartition(df\_knn$life\_expectancy, p = 0.75, list = FALSE)

tree\_train\_x <- df\_knn[inTraining\_t,]

tree\_test\_x <- df\_knn[-inTraining\_t,]

*# Try a random forest compared to a single tree model*

set.seed(567)

*# Remove country again*

rfFit\_x <- randomForest(life\_expectancy ~ ., data = tree\_train\_x[, -1])

rfFit\_x

*# Test using all predictors for each tree*

set.seed(5)

*# Have to remove country again - using top 4 predictors*

rfFit2\_x <- randomForest(life\_expectancy ~ adult\_mortality +

total\_expenditure +

hiv\_aids +

income\_composition\_of\_resources, data = tree\_train\_x[,-1])

rfFit2\_x

*#compare y-hat for the two random forest models*

yhat.rf\_x <- predict(rfFit\_x, newdata = tree\_test\_x[, -1])

yhat.rf2\_x <- predict(rfFit2\_x, newdata = tree\_test\_x[, -1])

*# Performance measurement*

postResample(tree\_test\_x$life\_expectancy, yhat.rf\_x)

postResample(tree\_test\_x$life\_expectancy, yhat.rf2\_x)

plot(yhat.rf\_x, tree\_test\_x$life\_expectancy)

abline(0,1)

plot(yhat.rf2\_x,tree\_test\_x$life\_expectancy)

abline(0,1)