

Networks and Computational Neuroscience  
Neurosci 613 Fall 2014  
Computer Lab 2

**Due: Friday, November 21, 2014 by 5pm**

1. Use the matlab code ILIF2cells.m to simulate 2 ILIF neurons, Cell 1 and Cell 2, with an excitatory synapse from Cell 1 to Cell 2, but no synaptic connection from Cell 2 back to Cell 1 (connection matrix  $W = \begin{bmatrix} 0 & 0 \\ 1 & 0 \end{bmatrix}$ ). Let both cells have parameter values  $a = 0.02$ ,  $b = 0.2$ ,  $c = -65$  and  $d = 8$ . Set the synaptic weight  $g_{syn} = 3$  and synaptic decay time constant  $\tau_{syn} = 15$ . In this small network, we can consider that the synaptic input from Cell 1 to Cell 2 provides Cell 2 with periodic forcing. When the applied current in Cell 1,  $I_1$ , is set to higher values than the applied current in Cell 2,  $I_2$ , so that the frequency of firing in Cell 1 is higher than in Cell 2, the synaptic input to Cell 2 can entrain its firing so that the network displays stable  $m:n$  periodic firing with Cell 1 firing  $m$  spikes for every  $n$  spikes that Cell 2 fires. To set different applied currents to each cell, set `pulsei = [ I1; I2 ]` in the program call command.
  - a. Keep  $I_2$  fixed at 4 and increase  $I_1$  starting from 4 by integer values. Find values of  $I_1$  that result in 1:1, 2:1 and 3:1 firing patterns. Also find one  $I_1$  value with  $m:n$  firing where  $m/n$  is between 1 and 2, and another  $I_1$  value where  $m/n$  is between 2 and 3. Provide plots of firing patterns for each case. Note: there exist  $I_1$  values that result in  $m:n$  firing for all rational numbers  $m/n$ .
  - b. Find the interval of  $I_1$  values where 1:1 firing is stable (to integer values of  $I_1$ ).
  - c. The stability of  $m:n$  phase-locked solutions is dependent on the strength of the synaptic input  $g_{syn}$ . Find intervals of  $I_1$  values where 1:1 firing is stable (to integer values of  $I_1$ ) when  $g_{syn} = 2, 5$  and  $8$ .
  - d. Using the values found in b) and c), construct a plot with  $g_{syn}$  values on the y-axis and  $I_1$  values on the x-axis that shows the  $I_1$  intervals where 1:1 firing is stable. If you assume that when  $g_{syn} = 0$ , 1:1 firing is stable only when  $I_1 = 4$ , then this plot should define the triangular region known as an Arnold Tongue.
2. Use the matlab code ILIF2cells.m to simulate 2 ILIF neurons with reciprocal inhibitory synapses between them (connection matrix  $W = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$ ). Let both cells have parameter values  $a = 0.02$ ,  $b = 0.2$ ,  $c = -65$  and  $d = 8$ . Set the synaptic weight  $g_{syn} = -8$  and applied current to both cells `pulsei = 8`. As we discussed in class, if the synaptic input is short lasting ( $\tau_{syn}$  small) then this small network will display anti-phase firing and if the synaptic input is very long lasting ( $\tau_{syn}$  very large) then 1 cell will be able to completely suppress firing in the other cell. For values of  $\tau_{syn}$  between these two regimes, the cells will synchronize. In this mechanism for synchronization, the frequency of synchronized firing depends on synaptic weight and the synaptic time constant  $\tau_{syn}$ .
  - a. For  $\tau_{syn}$  values greater than 1, find the intervals of  $\tau_{syn}$  values where the cells fire in anti-phase, are synchronized and where one cell is suppressed (to integer values of  $\tau_{syn}$ ).

Provide plots of firing patterns for  $\tau_{\text{syn}}$  values resulting in each of these behaviors.

- b. Compute the frequencies of the synchronized firing (in Hz, assuming time units of the model are ms) for the  $\tau_{\text{syn}}$  values where synchronous firing occurs. What is the relationship between synaptic decay time constant  $\tau_{\text{syn}}$  and frequency? How do the frequencies of synchronous firing compare to the frequency of each cell when they are uncoupled (synaptic weight  $g_{\text{syn}}=0$ )?
- c. Set  $\tau_{\text{syn}}$  to a value in the middle of the above interval and keep it fixed. Increase and decrease  $g_{\text{syn}}$  to find the interval of  $g_{\text{syn}}$  values where the cells are synchronized (this interval will be small, so consider  $g_{\text{syn}}$  values to the first decimal place). Compute the frequencies of synchronized firing (in Hz) for  $g_{\text{syn}}$  values in this interval. What is the relationship between synaptic strength and frequency?
- d. Now consider the same 2 cell network with reciprocal excitatory synapses by setting  $g_{\text{syn}} = 3$ . Compute the frequency of synchronized firing for  $\tau_{\text{syn}}$  values between 5 and 20. Then set  $\tau_{\text{syn}} = 15$  and compute the frequency of synchronized firing for  $g_{\text{syn}}$  values between 1 and 8. What are the relationships between frequency and synaptic decay time constant  $\tau_{\text{syn}}$  and synaptic strength  $g_{\text{syn}}$ ? How do the frequencies of synchronized firing compare to the frequency of each cell when they are uncoupled ( $g_{\text{syn}}=0$ )? How do these relationships compare to the relationships computed in b and c?