

Ajtai commitment expansion

Matthew Klein

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Ajtai Commitments

- ▶ Ajtai commitments allow us to commit to a vector of polynomials
- ▶ We commit to an a vector $\vec{x} \in \mathcal{R}^m$ by multiplying it with a random matrix $\mathbf{A} \in \mathcal{R}_{\mathbf{q}}^{\kappa \times m}$
- ▶ $\|\vec{x}\|_{\infty} < B$ where B is the norm bound
- ▶ Output of commitment is $cm := \mathbf{A} \cdot \vec{x} \bmod \mathbf{q} \in \mathcal{R}_{\mathbf{q}}^{\kappa}$
- ▶ This commitment is considered binding because of the assumed hardness of MSIS

Ajtai commitments as a relation

- ▶ We define relation $\mathcal{R}_{MSIS\infty}^B$ between an ajtati commitment and the \vec{x}
- ▶ $\mathcal{R}_{MSIS\infty}^B := (pp, cm \in \mathcal{R}_q^\kappa; \vec{x} \in \mathcal{R}^m : (cm = \mathbf{A} \cdot \vec{x} \bmod \mathbf{q}) \wedge \|\vec{x}\|_\infty < \mathbf{B})$
- ▶ $pp := (\kappa, m, B, \mathbf{A})$ are the public parameters of the relation
- ▶ Public parameters define the 'meta' information of the relation:
 1. The size of the vectors and matrices
 2. The norm limit of \vec{x}
 3. The random matrix \mathbf{A}