Physics Notes

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Part I

Physics C: Mechanics

1 Kinematics

1.1 Describing Motion 1

1.1.1 Average Speed

- Average speed is the distance traveled over change in time
- It is a scaler
- Measured in meters/second.
- Magnitude of Velocity Vector

1.1.2 Average Velocity

- Average velocity is a vector.
- Measured in meters/second.

$$v_{avg} = \frac{\delta x}{\delta t} = \frac{x_f - x_i}{t_f - t_i}$$

1.1.3 Average Velocity

- Rate that velocity changes
- Is a vector
- Units are meters/second/second

$$a = \frac{\delta v}{\delta t} = \frac{dv}{dt}$$

1.1.4 Displacement

The displacement from t_0 to t_1 of a position function x(t) with velocity function v(t) is

$$\int_{t_0}^{t_1} v(t)dt$$

1.2 Describing Motion 2

1.2.1 Kinematic Equations

Variables			
v_0	Initial velocity		
v	Final velocity		
δx	Displacement		
a	Acceleration		
t	Time		

- $\bullet \ v = v_0 + at$
- $x = x_0 + v_0 t + \frac{1}{2} a t^2$
- $\bullet v^2 = v_0^2 + 2a\delta x$

1.2.2 Acceleration Due to Gravity

- Near the surface of Earth, objects accelerate at a rate of $9.8\frac{m}{s^2}$
- This is acceleration due to gravity (g)
- This can be approximated to $10\frac{m}{s^2}$
- As you move from Earth, acceleration decreases.

1.2.3 Objects Falling From Rest

- Objects starting from rest have $v_0 = 0$
- \bullet Typically down is the positive direction
- Acceleration is +g.

1.2.4 Objects Launched Upward

- \bullet Must examine the motion of object going up and down.
- Since object is going up, that is the positive direction.
- Acceleration is -g.
- At the highest point, v = 0.

1.3 Projectile Motion

A **projectile** is an object that is acted upon only gravity.

1.3.1 Independence of Motion

- Projectiles launched at an angle have motion in 2 dimensions.
 - Vertical acceleration is gravity
 - Horizontal 0 acceleration
- Vertical and Horizontal motion are treated separately

Note: An object will travel the maximum horizontal distance with a launch angle of 45°

1.3.2 Steps for any Projectile Motion Problem

1. First, know that

$$a = \begin{bmatrix} 0 \\ -g \end{bmatrix}$$

- 2. Then find your v_0 as a vector
- 3. Find your x_0 as a vector
- 4. Substitute your vectors into the following formula

$$x(t) = -\frac{1}{2}at^2 + v_0t + x_0$$

1.3.3 Graphing Projectile Motion

In order to graph a path, solve for y = f(x). Do this by solving for t in relation to x and then substitute into the y component. For example:

$$x = f(t)$$

$$y = g(t)$$
Find $y = h(x)$

$$t = f^{-1}(x)$$

$$y = g(f^{-1}(x)) = h(x)$$
so $h(x) = g(f^{-1}(x))$

1.4 Circular And Relative Motion

1.4.1 Converting Linear to Angular Velocity

If we have an object moving counter clockwise around a point, let $\omega = \frac{d\theta}{dt}$. If we know that the object has velocity v and position s, we know that $s = r\theta$ where r is the radius of the circular path. By taking the derivative of both sides, $\dot{s} = r\dot{\theta}$. Now we can substitute to find the angular velocity.

$$\dot{s} = r\omega$$

2 Dynamics

2.1 Newton's First Law and Free Body diagrams

Newton's First Law

An object at rest will remain at rest, and an object in motion will remain in motion, at constant velocity and in a straight line, unless acted upon by a net force.

2.1.1 Force

- A force is a push or pull on an object.
- Units of force are in Newtons (N).
- A newton is roughly the weight of an apple

$$1N = 1\frac{kg * m}{s^2}$$

Contract Force

A force that arises that from direct contact between objects.

- Tension
- Applied Force
- Friction

Field Force

Forces that act at a distance.

- Gravity
- Electrical
- Magnetic

2.1.2 Net Force

A net force is the vector sum of all the forces acting on an object.

$$F_{net} = \sum F$$

2.1.3 Equilibrium

- Static Equilibrium
 - Net force is 0
 - Net torque is 0
 - Object is at rest
- Mechanical Equilibrium
 - Net force is 0
 - Net torque is 0
- Translational Equilibrium
 - Net force is 0

2.1.4 Free Body Diagram

A Free Body Diagram (FBD) is a diagram that maps all of the forces that are applied to a single object.

2.2 Newton's 2nd and 3rd Laws of Motion

2.2.1 Newton's 2nd Law of Motion

- The acceleration of an object is in the direction of and directly proportional to the net force applied, and inversely proportional to the object's mass.
- Valid only in *inertial reference frames*.

$$F_{net} = \sum F = ma$$

2.2.2 Mass vs. Weight

- Mass is the amount of stuff that something is made up of (independent of gravity)
- Weight is the force of gravity on an object. (dependent on gravity)

2.2.3 Newton's 3rd Law of Motion

• All forces come in pairs

- If Object 1 exerts a force on Object 2, then Object 2 must exert a force back on Object 2.
- This counter force is equal in magnitude and opposite in direction.

$$F_{1on2} = -F_{2on1}$$

2.3 Friction

2.3.1 Coefficient of Friction

- Ratio of the frictional force and the normal force
- 2 kinds:
 - 1. Kinetic (when 2 objects are rubbing)
 - 2. Static (when 2 objects are not sliding)

$$\mu = \frac{F_f}{F_N}$$

which results in

$$F_f = \mu F_N$$

where F_f is the force of friction, F_N is the normal force, and μ is the coefficient of friction.

2.4 Retarding or Drag Forces

2.4.1 Retarding Forces

- Frictional forces can be functions of the object's velocity
- These forces are called drag or retarding forces

2.4.2 The Skydiver

Typically drag forces on a free-falling object take the form of

$$F_{drag} = bv$$

or

$$F_{drag} = cv^2$$

By using Newton's 2nd Law, create a differential equation. Then use separation of variables to solve for velocity, then acceleration, then position.

2.5 Ramps and Inclines

2.5.1 Drawing FBD for Ramps

1. Choose the object and draw it as a dot or box

- 2. Draw and Label all the External Forces
- 3. Sketch a Coordinate System

2.6 Atwood Machine

2.6.1 What is an Atwood Machine

Two objects connected by a light string over a massless pulley

2.6.2 Properties of Atwood Machines

- Ideal pulleys are frictionless and massless
- Tension is constant in a light string passing over an ideal pulley

2.6.3 Setup for Atwood Machines

- 1. Adopt a sign convention for positive and negative motion
- 2. Analyze each mass separately using Newton's 2nd Law.

2.6.4 Solution

$$F_y = m_1 g - m_2 g = (m_1 + m_2)a$$
$$(m_1 - m_2)g = (m_1 + m_2)a$$
$$a = g \frac{(m_1 - m_2)}{(m_1 + m_2)}$$

3 Work, Energy, and Power

3.1 Work

3.1.1 What is Work

- Work is the process of moving an object by applying a force
- The object must move
- The force must cause the movement
- Work is measured in Joules

$$W = F \cdot \Delta x$$

3.1.2 Non-Constant Forces

• Work done is the area under the force vs. displacement graph.

$$W = \int_{x_i}^{x_f} F(x) dx$$

3.1.3 Hook's Law

- The more you stretch or compress a spring, the greater the force of the spring.
- The spring's force is opposite the direction of its displacement from equilibrium.
- This is modeled as a linear relationship.

$$F_s = -kx$$

3.1.4 Determining the Spring Constant

- Graph Force vs Displacement for the Spring
- The slope of this graph is the Spring Constant

$$k = \frac{\Delta F}{\Delta x}$$

3.1.5 Work in Multiple Dimensions

$$W = \int dW$$
$$W = \int_{r_1}^{r_2} F \cdot dr$$

3.1.6 Work-Energy Theorem

$$W = \int_{x_i}^{x_f} F(x) dx$$

$$F = ma = m \frac{dv}{dt} \qquad v = \frac{dx}{dt} = v dt$$

$$W = \int m \frac{dv}{dt} v dt$$

$$W = \int_{v_i}^{v_f} mv dv$$

$$\mathbf{W} = \mathbf{m} \int_{\mathbf{v_i}}^{\mathbf{v_f}} \mathbf{v} d\mathbf{v}$$

$$= m \left. \frac{v^2}{2} \right|_{v_i}^{v_f}$$

$$= m(\frac{v_f^2 - v_i^2}{2})$$

$$K = \frac{1}{2} m v^2 \quad K \text{ is kinetic energy}$$

$$W = K_f - K_i = \Delta K$$

3.2 Energy and Conservative Forces