# Physics Notes

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# Part I

# Physics C: Mechanics

# 1 Kinematics

# 1.1 Describing Motion 1

## 1.1.1 Average Speed

- Average speed is the distance traveled over change in time
- It is a scaler
- Measured in meters/second.
- Magnitude of Velocity Vector

## 1.1.2 Average Velocity

- Average velocity is a vector.
- Measured in meters/second.

$$v_{avg} = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i}$$

# 1.1.3 Average Velocity

- Rate that velocity changes
- Is a vector
- Units are meters/second/second

$$a = \frac{\Delta v}{\Delta t} = \frac{dv}{dt}$$

# 1.1.4 Displacement

The displacement from  $t_0$  to  $t_1$  of a position function x(t) with velocity function v(t) is

$$\int_{t_0}^{t_1} v(t)dt$$

# 1.2 Describing Motion 2

### 1.2.1 Kinematic Equations

$\_$ Variables			
$v_0$	Initial velocity		
v	Final velocity		
$\Delta x$	Displacement		
a	Acceleration		
t	Time		

- $\bullet \ v = v_0 + at$
- $x = x_0 + v_0 t + \frac{1}{2}at^2$
- $v^2 = v_0^2 + 2a\Delta x$

## 1.2.2 Acceleration Due to Gravity

- Near the surface of Earth, objects accelerate at a rate of  $9.8\frac{m}{s^2}$
- This is acceleration due to gravity (g)
- This can be approximated to  $10\frac{m}{s^2}$
- As you move from Earth, acceleration decreases.

# 1.2.3 Objects Falling From Rest

- Objects starting from rest have  $v_0 = 0$
- $\bullet$  Typically down is the positive direction
- Acceleration is +g.

# 1.2.4 Objects Launched Upward

- $\bullet$  Must examine the motion of object going up and down.
- Since object is going up, that is the positive direction.
- Acceleration is -g.
- At the highest point, v = 0.

# 1.3 Projectile Motion

A **projectile** is an object that is acted upon only gravity.

## 1.3.1 Independence of Motion

- Projectiles launched at an angle have motion in 2 dimensions.
  - Vertical acceleration is gravity
  - Horizontal 0 acceleration
- Vertical and Horizontal motion are treated separately

**Note:** An object will travel the maximum horizontal distance with a launch angle of  $45^{\circ}$ 

## 1.3.2 Steps for any Projectile Motion Problem

1. First, know that

$$a = \begin{bmatrix} 0 \\ -g \end{bmatrix}$$

- 2. Then find your  $v_0$  as a vector
- 3. Find your  $x_0$  as a vector
- 4. Substitute your vectors into the following formula

$$x(t) = -\frac{1}{2}at^2 + v_0t + x_0$$

## 1.3.3 Graphing Projectile Motion

In order to graph a path, solve for y = f(x). Do this by solving for t in relation to x and then substitute into the y component. For example:

$$x = f(t)$$

$$y = g(t)$$
Find  $y = h(x)$ 

$$t = f^{-1}(x)$$

$$y = g(f^{-1}(x)) = h(x)$$
so  $h(x) = g(f^{-1}(x))$ 

## 1.4 Circular And Relative Motion

### 1.4.1 Converting Linear to Angular Velocity

If we have an object moving counter clockwise around a point, let  $\omega = \frac{d\theta}{dt}$ . If we know that the object has velocity v and position s, we know that  $s = r\theta$  where r is the radius of the circular path. By taking the derivative of both sides,  $\dot{s} = r\dot{\theta}$ . Now we can substitute to find the angular velocity.

$$\dot{s} = r\omega$$

# 2 Dynamics

# 2.1 Newton's First Law and Free Body diagrams

#### Newton's First Law

An object at rest will remain at rest, and an object in motion will remain in motion, at constant velocity and in a straight line, unless acted upon by a net force.

#### 2.1.1 Force

- A force is a push or pull on an object.
- Units of force are in Newtons (N).
- A newton is roughly the weight of an apple

$$1N = 1\frac{kg * m}{s^2}$$

#### **Contract Force**

A force that arises that from direct contact between objects.

- Tension
- Applied Force
- Friction

#### Field Force

Forces that act at a distance.

- Gravity
- Electrical
- Magnetic

#### 2.1.2 Net Force

A net force is the vector sum of all the forces acting on an object.

$$F_{net} = \sum F$$

## 2.1.3 Equilibrium

- Static Equilibrium
  - Net force is 0
  - Net torque is 0
  - Object is at rest
- Mechanical Equilibrium
  - Net force is 0
  - Net torque is 0
- Translational Equilibrium
  - Net force is 0

### 2.1.4 Free Body Diagram

A Free Body Diagram (FBD) is a diagram that maps all of the forces that are applied to a single object.

## 2.2 Newton's 2nd and 3rd Laws of Motion

#### 2.2.1 Newton's 2nd Law of Motion

- The acceleration of an object is in the direction of and directly proportional to the net force applied, and inversely proportional to the object's mass.
- Valid only in *inertial reference frames*.

$$F_{net} = \sum F = ma$$

### 2.2.2 Mass vs. Weight

- Mass is the amount of stuff that something is made up of (independent of gravity)
- Weight is the force of gravity on an object. (dependent on gravity)

#### 2.2.3 Newton's 3rd Law of Motion

• All forces come in pairs

- If Object 1 exerts a force on Object 2, then Object 2 must exert a force back on Object 2.
- This counter force is equal in magnitude and opposite in direction.

$$F_{1on2} = -F_{2on1}$$

## 2.3 Friction

#### 2.3.1 Coefficient of Friction

- Ratio of the frictional force and the normal force
- 2 kinds:
  - 1. Kinetic (when 2 objects are rubbing)
  - 2. Static (when 2 objects are not sliding)

$$\mu = \frac{F_f}{F_N}$$

which results in

$$F_f = \mu F_N$$

where  $F_f$  is the force of friction,  $F_N$  is the normal force, and  $\mu$  is the coefficient of friction.

# 2.4 Retarding or Drag Forces

## 2.4.1 Retarding Forces

- Frictional forces can be functions of the object's velocity
- These forces are called drag or retarding forces

#### 2.4.2 The Skydiver

Typically drag forces on a free-falling object take the form of

$$F_{drag} = bv$$

or

$$F_{drag} = cv^2$$

By using Newton's 2nd Law, create a differential equation. Then use separation of variables to solve for velocity, then acceleration, then position.

# 2.5 Ramps and Inclines

### 2.5.1 Drawing FBD for Ramps

1. Choose the object and draw it as a dot or box

- 2. Draw and Label all the External Forces
- 3. Sketch a Coordinate System

#### 2.6 Atwood Machine

#### 2.6.1 What is an Atwood Machine

Two objects connected by a light string over a massless pulley

### 2.6.2 Properties of Atwood Machines

- Ideal pulleys are frictionless and massless
- Tension is constant in a light string passing over an ideal pulley

## 2.6.3 Setup for Atwood Machines

- 1. Adopt a sign convention for positive and negative motion
- 2. Analyze each mass separately using Newton's 2nd Law.

#### 2.6.4 Solution

$$F_y = m_1 g - m_2 g = (m_1 + m_2)a$$
$$(m_1 - m_2)g = (m_1 + m_2)a$$
$$a = g \frac{(m_1 - m_2)}{(m_1 + m_2)}$$

# 3 Work, Energy, and Power

## 3.1 Work

#### 3.1.1 What is Work

- Work is the process of moving an object by applying a force
- The object must move
- The force must cause the movement
- Work is measured in Joules

$$W = F \cdot \Delta x$$

#### 3.1.2 Non-Constant Forces

• Work done is the area under the force vs. displacement graph.

$$W = \int_{x_i}^{x_f} F(x) dx$$

#### 3.1.3 Hook's Law

- The more you stretch or compress a spring, the greater the force of the spring.
- The spring's force is opposite the direction of its displacement from equilibrium.
- This is modeled as a linear relationship.

$$F_s = -kx$$

#### 3.1.4 Determining the Spring Constant

- Graph Force vs Displacement for the Spring
- The slope of this graph is the Spring Constant

$$k = \frac{\Delta F}{\Delta x}$$

### 3.1.5 Work in Multiple Dimensions

$$W = \int dW$$
$$W = \int_{r_1}^{r_2} F \cdot dr$$

#### 3.1.6 Work-Energy Theorem

$$W = \int_{x_i}^{x_f} F(x) dx$$

$$F = ma = m \frac{dv}{dt} \qquad v = \frac{dx}{dt} = v dt$$

$$W = \int m \frac{dv}{dt} v dt$$

$$W = \int_{v_i}^{v_f} mv dv$$

$$\mathbf{W} = \mathbf{m} \int_{\mathbf{v_i}}^{\mathbf{v_f}} \mathbf{v} d\mathbf{v}$$

$$= m \left. \frac{v^2}{2} \right|_{v_i}^{v_f}$$

$$= m(\frac{v_f^2 - v_i^2}{2})$$
 
$$K = \frac{1}{2} m v^2 \quad K \text{ is kinetic energy}$$
 
$$W = K_f - K_i = \Delta K$$

Energy Formula:

$$\mathbf{K} = \frac{1}{2} m \mathbf{v^2}$$

# 3.2 Energy and Conservative Forces

## 3.2.1 What is Energy?

- Energy is the ability to do work
- in other words, Energy is the ability to move an object

## 3.2.2 Kinetic Energy

- Kinetic Energy is energy of motion.
  - The ability or capacity of moving object move another object.

$$K = \frac{1}{2}mv^2$$

#### 3.2.3 Potential Energy

- Potential Energy (U) is energy an object possesses due to its position or state of being.
- A single object can only have kinetic energy, because potential energy requires an interaction between objects.

#### 3.2.4 Internal Energy

- The internal energy of a system includes the kinetic energy and potential energy.
- By changing a system's internal structure, you can change its internal energy.

# 3.2.5 Gravitational Potential Energy $(U_g)$

$$U_g = mg\Delta h$$

#### 3.2.6 Conservative Forces

- A force in which the work done on an object is independent of the path taken
- A force in which the work done moving along a closed path is zero

• A force in which the work done is directly related to the change in potential energy

$$W = -\Delta U$$

## Conservative Forces

- Gravity
- Elastic Forces
- Coulumbic

# Non-Conservative Forces

- Friction
- Drag
- Air Resistance