Polynomials: Solving+Factoring

1) Solve
$$x^3 + x^2 - 2x - 2 = 0$$

2) Solve
$$x^4 - 4x^3 + 6x^2 - 4x - 2005 = 0$$
.

3) Solve
$$x^4 - 2x^3 + 4x^2 - 2x + 1 = 0$$

4) Solve
$$x^4 - x^3 - 5x^2 + 2x + 6 = 0$$

5) Factor $a^3 + b^3 + c^3 - 3abc$ as the product of two symmetric polynomials.

6) Find all reals such that
$$2000x^6 + 100x^5 + 10x^3 + x - 2 = 0$$

7) Find all real
$$x$$
 such that $5x^4 - 10x^3 + 10x^2 - 11 = 0$

8) Factor
$$x^4 + 4y^4$$
.

9) Factor x^8+34x^4+1 as the product of two polynomials with integer coefficients