

A Formal Axiomatization of Advaita Vedanta: Non-Dual Metaphysics in Higher-Order Logic

Executive Summary

The Research Question

Can the non-dual metaphysics of Advaita Vedanta—one of India’s most influential philosophical traditions—be formalized with the same logical rigor as contemporary analytic metaphysics? And if so, can machine verification establish its logical consistency?

This project answers both questions affirmatively.

What Is Advaita Vedanta?

Advaita Vedanta (“non-dual conclusion”) is the philosophical system articulated in the Upaniṣads (c. 800-400 BCE) and systematized by Ādi Śaṅkara (8th century CE). Its core claims:

1. **Brahman** is the sole, unconditioned reality (the Absolute)
2. **Ātman** (the innermost self) is identical with Brahman
3. **Maya** (phenomenal world) is dependent on Brahman but not ultimately real
4. **Liberation** comes through recognition of this identity: *tat tvam asi* (“That Thou Art”)

Despite its historical influence and sophisticated philosophical arguments, Advaita has remained largely outside formal analytic philosophy, often dismissed as mysticism rather than systematic metaphysics.

The Formal System

Eight Axioms in Higher-Order Logic

Using predicates $A(x)$ = “ x is Absolute”, $C(x)$ = “ x is Conditioned”, $Y(x)$ = “ x is You”, and $\Phi(x)$ = “ x is phenomenal” (exists in time, space, or has qualities):

1. **A1:** $\exists y E(y)$ — *Something exists*
2. **A2b:** $\forall y [E(y) \rightarrow \exists! a (A(a) \wedge \text{Cond}(a,y))]$ — *Every existent has exactly one absolute ground*
3. **A3:** $\forall a [A(a) \rightarrow \neg C(a)]$ — *The Absolute is unconditioned*
4. **A4:** $\forall x [\Phi(x) \rightarrow C(x)]$ — *All phenomena are conditioned*
5. **A5c:** Identity of indiscernibles for conditioned entities
6. **A6:** $\forall P \forall x [\text{AdmissibleProp}(P) \rightarrow \text{Holds}(P,x) \rightarrow \Phi(x)]$ — *Phenomenal properties apply only to phenomena*
7. **A7:** $\exists! u Y(u)$ — *There is exactly one “You”*
8. **A7a:** $\forall x [Y(x) \rightarrow A(x)]$ — *You are the Absolute*
9. **A8:** $\forall x [A(x) \vee C(x)]$ — *Everything is either absolute or conditioned*

Key Theorems Derived

- **T1:** $\exists! a A(a)$ — *Exactly one Absolute exists*
- **T4:** $\exists a [A(a) \wedge \forall x (x \neq a \rightarrow C(x))]$ — *Everything else is conditioned*
- **T5:** $\exists u [Y(u) \wedge A(u)]$ — *You are that unique Absolute*

Main Result: Tat Tvam Asi

$$\exists! u [Y(u) \wedge A(u) \wedge \forall P (\text{AdmissibleProp}(P) \rightarrow \neg \text{Holds}(P,u))]$$

There exists exactly one “You” which is the Absolute and to which no phenomenal property applies.

This is the formal rendering of the Upaniṣadic mahāvākya “tat tvam asi” (“That Thou Art”).

Methodology: Machine Verification

The complete system is being verified in **Isabelle/HOL**, a proof assistant used for mathematical and logical verification. This means:

- Every inference is checked by automated theorem provers
- No hidden assumptions or logical gaps
- Reproducible verification (anyone can run the code)

- Standard used in computer science and formal mathematics

This represents the first time, to our knowledge, that a complete non-dual metaphysical system has been machine-verified.

Philosophical Significance

1. Cross-Cultural Philosophy

Demonstrates that non-Western metaphysics can engage with contemporary analytic methods without losing its distinctive insights. Provides a formal framework for precise comparison between:

- Advaita Vedanta and Buddhist Mādhyamaka
- Advaita and Spinoza's substance monism
- Advaita and contemporary consciousness studies

2. Formal Metaphysics

Shows that:

- Apophatic theology (negative characterization of ultimate reality) has logical structure
- First-person ontology can be formally stated (the "You" predicate)
- The two-truth doctrine (absolute vs. conventional) can be modeled systematically
- Non-dual awareness is not incoherent but has precise metaphysical commitments

3. Philosophy of Mind

Offers a formally rigorous alternative to physicalism and dualism:

- Consciousness is not emergent from matter but the ground of all existence
- The "hard problem" dissolves: no need to explain consciousness from physical processes
- The subject-object distinction is conventional, not absolute
- Provides framework for integrating contemplative phenomenology with formal philosophy

4. Methodological Innovation

Demonstrates that machine verification can be applied to metaphysics, not just mathematics:

- Ancient philosophical systems can be checked for logical consistency
 - Formal methods can serve comparative philosophy
 - Contemplative insight and logical rigor are compatible
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Anticipated Objections and Responses

Objection 1: *"This assumes what it tries to prove—the axioms smuggle in monism."*

Response: All axiomatic systems start with axioms. Our aim is not to prove Advaita is true but to show it's logically consistent. The axioms are defensible on philosophical grounds (parsimony, explanatory power, phenomenological evidence).

Objection 2: *"The ineffable cannot be formalized."*

Response: Correct. The formalization captures the *structure* of non-dual metaphysics, not the experience of non-dual awareness. It's a map, not the territory. But maps are useful.

Objection 3: *"This doesn't engage with quantum mechanics, neuroscience, etc."*

Response: The formalization is pure metaphysics. However, it has clear implications for consciousness studies and can be connected to scientific questions (observer-dependence in quantum mechanics, the binding problem, etc.).

Objection 4: *"Why not use modal/paraconsistent/non-classical logic?"*

Response: Good question. We use classical higher-order logic to show Advaita is consistent even in the most standard framework. Alternative logics could be explored in future work.

Contributions to the Literature

To Comparative Philosophy:

- First complete formalization of Advaita Vedanta
- Enables precise structural comparison with other systems
- Makes Advaita accessible to analytically-trained philosophers

To Formal Philosophy:

- Extends machine verification to ancient metaphysical systems
- Shows first-person ontology can be formalized
- Demonstrates apophatic theology has logical structure

To Philosophy of Mind:




- Provides formal framework for consciousness-first metaphysics
- Alternative to emergence and panpsychism
- Integrates contemplative and analytic approaches

To Indian Philosophy:


- Honors Śaṅkara's systematic rigor with modern tools
- Shows tradition can engage with contemporary methods
- Creates pedagogical resource for teaching Advaita

Current Status and Timeline

Completed:

-  Complete axiomatization (8 axioms, 6 theorems)
-  Isabelle/HOL verification
-  Preliminary paper (~15,000 words)

In Progress:

-  Expert review from scholars of Indian philosophy and formal logic

Why This Matters

For over a millennium, Advaita Vedanta has offered one of humanity's most profound metaphysical visions: that the multiplicity of existence arises from, and resolves into, a single, unconditioned ground—and that this ground is not separate from the knowing subject.

This formalization doesn't prove Advaita is *true*, but it proves it's *coherent*—that its claims form a logically consistent system that can be stated with the same precision as any contemporary metaphysical theory.

In doing so, it:

- **Bridges cultures** (East-West philosophical dialogue)
- **Bridges eras** (ancient wisdom meets modern formal methods)
- **Bridges modes of knowing** (contemplative insight and logical rigor)
- **Bridges disciplines** (philosophy, computer science, consciousness studies)

If ancient wisdom can survive the most rigorous scrutiny available—machine verification—that says something important about its enduring value.

Target Audience

Primary: Analytic metaphysicians, formal philosophers, philosophers of mind, comparative philosophers

Secondary: Scholars of Indian philosophy, consciousness researchers, contemplative studies, philosophy of science

Format: Journal article (~8,000-12,000 words + technical appendix)

Potential Venues: *Synthese*, *Journal of Philosophical Logic*, *Philosophy East and West*, *Philosophy and Phenomenological Research*

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Project Repository: <https://github.com/matthew-scherf/Only-One> **Verification**

Code: Available in Isabelle/HOL format

Key Takeaway: Non-dual metaphysics is not mysticism—it's systematic philosophy that can be formalized, verified, and engaged with using the tools of contemporary analytic philosophy. This project proves it.

"The wise who have realized the truth declare that the Self is one, though the ignorant speak of it in many ways." — R̥g Veda 1.164.46

$\exists!u [Y(u) \wedge A(u)]$ — This Work, 2025