Artificial Intelligence

Uninformed search Chapter 3, AIMA

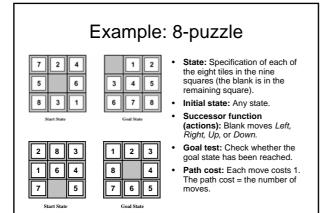
A goal based agent

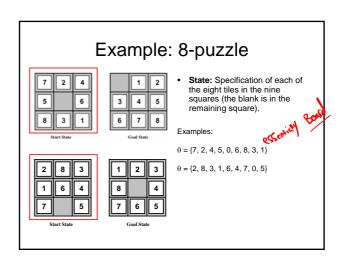
A "problem" consists of

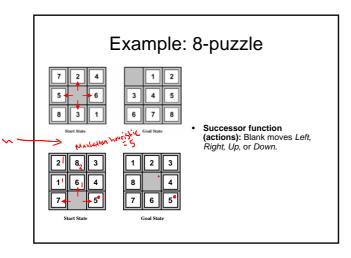
- An initial state, $\theta(0)$
- A list of possible actions, α , for the agent
- A goal test (there can be many goal states)
- A path cost

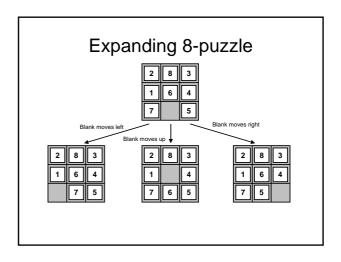
One way to solve this is to search for a path $\theta(0) \to \theta(1) \to \theta(2) \to \dots \to \theta(N)$ such that $\theta(N)$ is a goal state.

This requires that the environment is **observable**, **deterministic**, **static** and **discrete**.









Na Universey Uninformed search

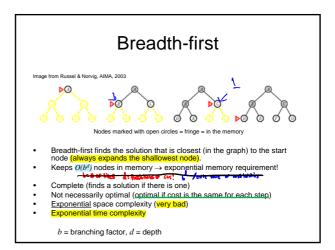
Searching for the goal without knowing in which direction it

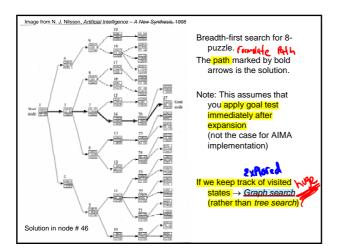
- Breadth-first
- Depth-first
- Iterative deepening

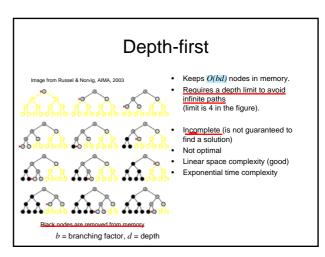
(Depth and breadth refers to the search tree)

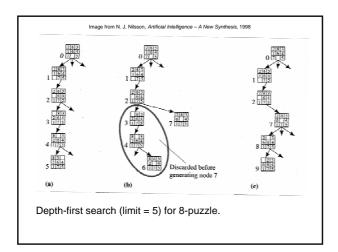
We evaluate the algorithms by their:

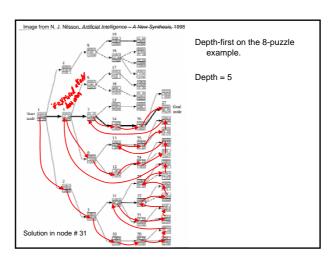
- Completeness (do they explore all possibilities)
 Optimality (if it finds solution with minimum path cost)
- Time complexity (clock cycles)
 Space complexity (memory requirement)

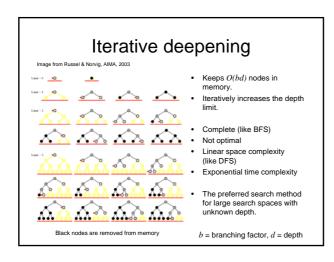


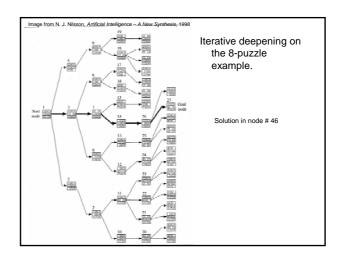






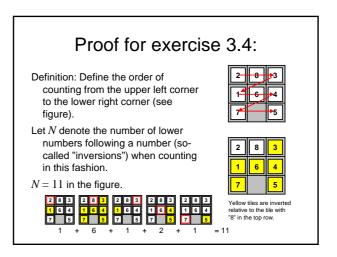






Exercise

Exercise 3.4: Show that the 8-puzzle states are divided into two disjoint sets, such that no state in one set can be transformed into a state in the other set by any number of moves. Devise a procedure that will tell you which class a given state is in, and explain why this is a good thing to have for generating random states.



Proof for exercise 3.4:

Proposition: *N* is either always even or odd (i.e. *N*mod2 is conserved).

Proof:

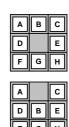
- (1) Sliding the blank along a row does not change the row number and not the internal order of the tiles, i.e. N (and thus also $N \bmod 2$) is conserved.
- (2) Sliding the blank between rows does not change Nmod2 either, as shown on the following slide.

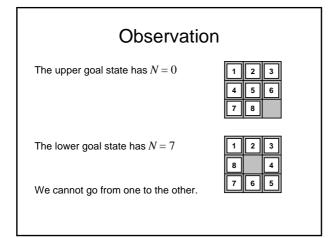
Proof for exercise 3.4:

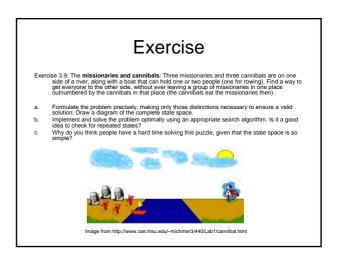
We only need to consider tiles B, C, and D since the relative order of the other tiles remains the same.

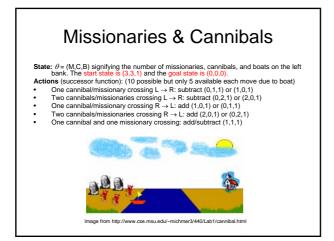
- If B > C and B > D, then the move removes two inversions.
- If B > C and B < D, then the move adds one inversion and removes one (sum = 0).
- If B < C and B < D, then the move adds two inversions.

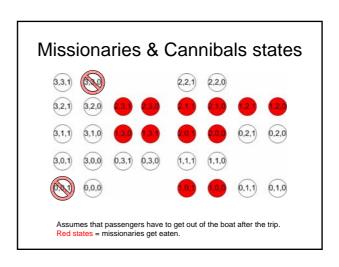
The number of inversions changes in steps of 2.











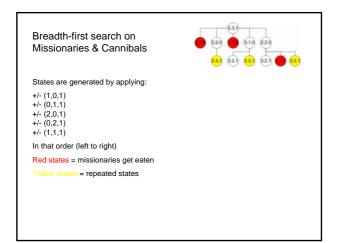
Breadth-first search on Missionaries & Cannibals

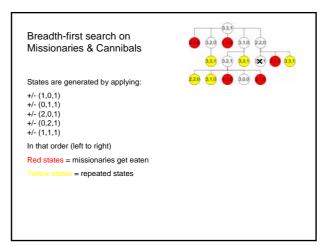
Breadth-first search on Missionaries & Cannibals

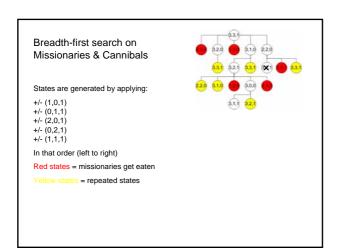
States are generated by applying:

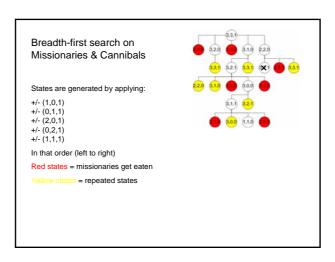
+/- (1,0,1)
+/- (0,1,1)
+/- (0,2,1)
+/- (0,2,1)
+/- (1,1,1)
In that order (left to right)

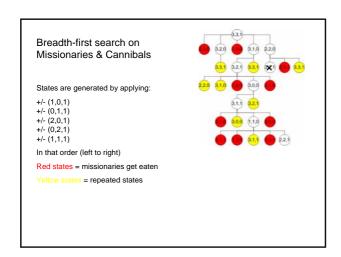
Red states = missionaries get eaten

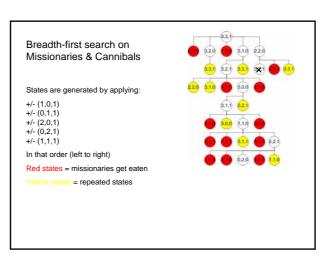


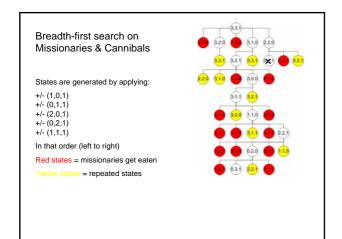


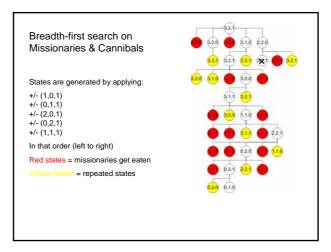


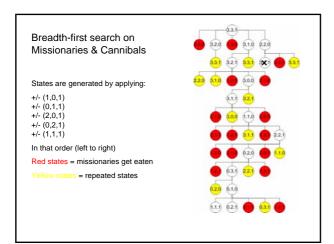


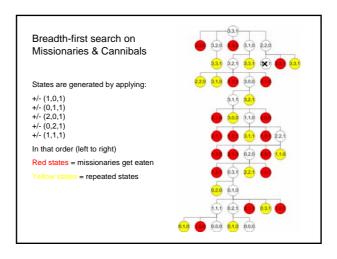


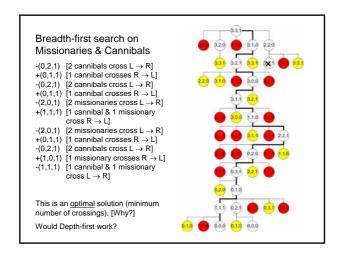


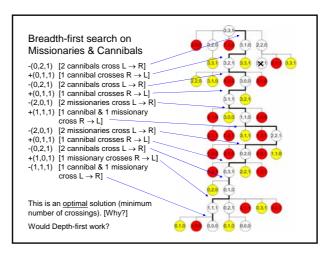












Breadth-first search on Missionaries & Cannibals
Expanded 48 nodes

Depth-first search on Missionaries & Cannibals
Expanded 30 nodes

(if repeated states are checked, otherwise we end up in an endless loop)

An example of a real search application

• Finding interesting web pages (expanding from links). Breadth-first works very nicely and quickly finds pages with high PageRank *R*(*p*). PageRank is the scoring measure used by Google.

$$R(p) = \frac{d}{T} + (1 - d) \sum_{k=1}^{K} \frac{R(k)}{C(k)}$$

k is an index over all pages that link to page p; C(k) is the total number of links out of k; R(k) is the PageRank for page k; T is the total number of web pages on the internet; d is a number 0 < d < 1.