$\LaTeX 2_{\varepsilon}$ Template

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$$u_p^l(r,\phi) \propto r^l L_p^l(2r^2/w^2) e^{-r^2/w^2} \frac{e^{-il\phi}}{e^{-il\phi}}$$
 (1)

1. Low gain.

2.
$$H \sim \int d^3 \mathbf{r} \chi^{(2)}(\mathbf{r}) E_p^{(+)}(\mathbf{r}, t) E_s^{(-)}(\mathbf{r}, t) E_i^{(-)}(\mathbf{r}, t) + H.c.$$

3.
$$H = i\hbar\Gamma \int d\mathbf{q}_s d\mathbf{q}_i F(\mathbf{q}_s, \mathbf{q}_i) a_{\mathbf{q}_s}^{\dagger} a_{\mathbf{q}_i}^{\dagger} + H.c.$$

4.

$$F(\mathbf{q}_s, \mathbf{q}_i) = C \exp\left\{-\sigma^2 \frac{(\mathbf{q}_s + \mathbf{q}_i)^2}{2}\right\} \operatorname{sinc}\left(\frac{L(\mathbf{q}_s - \mathbf{q}_i)^2}{4k_p}\right) \exp\left\{i\frac{L(\mathbf{q}_s - \mathbf{q}_i)^2}{4k_p}\right\}$$

5.
$$|\psi\rangle = \exp\left\{-\frac{i}{\hbar} \int_{-\infty}^{\infty} dt H(t)\right\} |0\rangle \approx -\frac{i}{\hbar} \int_{-\infty}^{\infty} dt H|0\rangle$$

6. Shmidt decomposition

7.
$$F(q_s, q_i, \phi_s - \phi_i) = \sum_{s} \chi_n(q_s, q_i) e^{in(\phi_s - \phi_i)}$$

8.
$$\chi_n(q_s, q_i) = \sum_{m} \sqrt{\lambda_{mn}} \frac{u_{mn}(q_s)}{\sqrt{q_s}} \frac{v_{mn}(q_i)}{\sqrt{q_i}}$$

9.
$$F(\mathbf{q}_s, \mathbf{q}_i) = \sum_{m,n} \sqrt{\lambda_{mn}} \frac{u_{mn}(q_s)}{\sqrt{q_s}} \frac{v_{mn}(q_i)}{\sqrt{q_i}} e^{in(\phi_s - \phi_i)}$$

10. broadband modes and high gain

11.
$$A_{mn}^{\dagger} = \int d\mathbf{q}_s \frac{u_{mn}(q_s)}{\sqrt{q_s}} e^{in\phi_s} a_{\mathbf{q}_s}^{\dagger}$$

12.
$$B_{mn}^{\dagger} = \int d\mathbf{q}_i \frac{v_{mn}(q_i)}{\sqrt{q_i}} e^{-in\phi_i} a_{\mathbf{q}_i}^{\dagger}$$

13.
$$H = i\hbar\Gamma \sum_{m,n} \sqrt{\lambda_{mn}} (A_{mn}^{\dagger} B_{mn}^{\dagger} - A_{mn} B_{mn})$$

14.
$$\frac{dA_{mn}}{dt} = \frac{i}{\hbar}[H, A_{mn}]$$

15.
$$A_{mn}^{out} = A_{mn}^{in} \cosh[G\sqrt{\lambda_{mn}}] + [B_{mn}^{in}]^{\dagger} \sinh[G\sqrt{\lambda_{mn}}]$$

16.
$$B_{mn}^{out} = B_{mn}^{in} \cosh[G\sqrt{\lambda_{mn}}] + [A_{mn}^{in}]^{\dagger} \sinh[G\sqrt{\lambda_{mn}}]$$

17.
$$\frac{da_{\mathbf{q}_{s,i}}}{dt} = \Gamma \sum_{m,n} \sqrt{\lambda_{mn}} \frac{u_{mn}(q_s)}{\sqrt{q_s}} \left[A_{mn}^{\dagger} e^{-in\phi_{s,i}} + B_{mn}^{\dagger} e^{in\phi_{s,i}} \right]$$

18.
$$\langle N_s(\mathbf{q}_s) \rangle = \sum_{m,n} \frac{|u_{mn}(q_s)|^2}{q_s} (\sinh[G\sqrt{\lambda_{mn}}])^2$$

19. three crystals

20.

$$F(\mathbf{q}_{s}, \mathbf{q}_{i}) = C \exp\left\{-\sigma^{2} \frac{(\mathbf{q}_{s} + \mathbf{q}_{i})^{2}}{2}\right\} \operatorname{sinc}\left(\frac{\Delta \widetilde{q}L}{2}\right) \times \left(\exp\left\{\frac{i\Delta \widetilde{q}L}{2}\right\} + \exp\left\{i(\Delta \widetilde{q}^{air}d_{1} + \frac{3}{2}\Delta \widetilde{q}L)\right\} + \exp\left\{i(\Delta \widetilde{q}^{air}(d_{1} + d_{2}) + \frac{5}{2}\Delta \widetilde{q}L)\right\}\right)$$
(2)

21.

$$\Delta \widetilde{q} = \frac{(\mathbf{q}_s - \mathbf{q}_i)^2}{2k_p}$$

22.

$$\Delta \widetilde{q}^{air} = \frac{(\mathbf{q}_s - \mathbf{q}_i)^2}{2k_p} n_s + \frac{2\delta n^{air} k_s}{n_s}$$

23. splitters

24.

$$|\psi_{in}\rangle = g(a_1^{\dagger})|0\rangle = \sum_{n=0} g_n(a_1^{\dagger})^n|0\rangle$$

25.

$$|\psi_{aux}\rangle = f(a_2^{\dagger})|0\rangle = \sum_{n=0} f_n(a_2^{\dagger})^n|0\rangle$$

26.

$$|\psi\rangle = |\psi_{in}\rangle \otimes |\psi_{aux}\rangle = \sum_{m,n} \alpha_{m,n} (a_1^{\dagger})^m (a_2^{\dagger})^n |0\rangle^{\otimes 2}$$

27. loseless BS

28.

$$\sum_{m,n} |\alpha_{m,n}|^2 = 1$$

29.

$$\sum_{m,n} |\alpha_{m,n}^{(2)}|^2 = 1$$

30.

$$r_i^2 + t_i^2 + a_i^2 = 1$$

31.

$$a_1^{\dagger} \rightarrow r_i a_1^{\dagger} + i t_i a_2^{\dagger}$$

32.

$$a_2^{\dagger} \rightarrow r_j a_2^{\dagger} + i t_j a_1^{\dagger}$$

33. state in area 2 after first BS

34.

$$|\psi_2\rangle = \sum_{m,n} \alpha_{m,n}^{(2)} (a_1^{\dagger})^m (a_2^{\dagger})^n |0\rangle^{\otimes 2}$$

35. 4 channels

36.

$$|\psi_3\rangle = \sum_{p_1, p_2, p_3, p_4} \beta_{p_1, p_2, p_3, p_4} (a_1^{\dagger})^{p_1} (a_2^{\dagger})^{p_2} (a_3^{\dagger})^{p_3} (a_4^{\dagger})^{p_4} |0\rangle^{\otimes 4}$$

37. First and only one ideal detector was clicked

38.

$$|\psi_4\rangle = \sum_{\substack{p_1, p_2, p_4\\p_1 > 0, p_3 = 0}} |\beta_{p_1, p_2, 0, p_4} \sqrt{p_1! p_2! p_4!}|^2 |p_2, p_4\rangle$$

39. First and third detectors were clicked

40.

$$|\psi_4\rangle = \sum_{\substack{p_1, p_2, p_3, p_4\\p_1 > 0, p_3 > 0}} |\beta_{p_1, p_2, p_3, p_4} \sqrt{p_1! p_2! p_3! p_4!}|^2 |p_2, p_4\rangle$$

41. No detection

42.

$$|\psi_4\rangle = \sum_{\substack{p_2, p_4\\p_1=0, p_2=0}} |\beta_{0, p_2, 0, p_4} \sqrt{p_2! p_4!}|^2 |p_2, p_4\rangle$$

43. final state

44.

$$|\psi_{out}\rangle = \sum_{m,n} \alpha_{m,n}^{out} (a_1^{\dagger})^m (a_2^{\dagger})^n |0\rangle^{\otimes 2}$$

45. example with two coherent states - alpha=1

46.

$$|\psi\rangle = |\alpha\rangle \otimes |\alpha\rangle, \quad \alpha = 1$$

47. two coherent after BS

48.

$$|\psi_2\rangle \approx e^{-1}(1 + \frac{1+i}{\sqrt{2}}a_1^{\dagger} + \frac{1+i}{\sqrt{2}}a_2^{\dagger} + ia_1^{\dagger}a_2^{\dagger} + \frac{i}{2}(a_1^{\dagger})^2 + \frac{i}{2}(a_2^{\dagger})^2 + \frac{i-1}{2\sqrt{2}}a_1^{\dagger}(a_2^{\dagger})^2 + \frac{i-1}{2\sqrt{2}}(a_1^{\dagger})^2a_2^{\dagger} + \dots)$$

49. auto correlation

$$Autocorr_s(q, q') = \langle N_s(q)N_s(q')\rangle - \langle N_s(q)\rangle\langle N_s(q')\rangle =$$

$$= \langle a_s^{\dagger}(q)a_s(q)a_s^{\dagger}(q')a_s(q')\rangle - \langle a_s^{\dagger}(q)a_s(q)\rangle\langle a_s^{\dagger}(q')a_s(q')\rangle$$

50. cross correlation

$$Crosscorr(q, q') = \langle N_s(q)N_i(q')\rangle - \langle N_s(q)\rangle\langle N_i(q')\rangle =$$
$$= \langle a_s^{\dagger}(q)a_s(q)a_i^{\dagger}(q')a_i(q')\rangle - \langle a_s^{\dagger}(q)a_s(q)\rangle\langle a_i^{\dagger}(q')a_i(q')\rangle$$

51. POVM operators

52.

$$\Pi_{no-click} = \sum_{n=0}^{\infty} (1 - \eta_{SPD})^n |n\rangle \langle n|$$

53.

$$\Pi_{click} = 1 - \Pi_{no-click} = \sum_{n=0}^{\infty} [1 - (1 - \eta_{SPD})^n] |n\rangle\langle n|$$

54. After projection

55. Only first clicked

56.

$$|\psi_{out}\rangle = \Pi_{click}^{(1)} |\psi_{in}\rangle$$

57. Two clicked 1st and 3rd

$$|\psi_{out}\rangle = \Pi_{click}^{(1)} \Pi_{click}^{(3)} |\psi_{in}\rangle$$

59. First and only one ideal detector was clicked

60.

$$|\psi_4\rangle = \sum_{\substack{p_1, p_2, p_4\\p_1 \neq 0, p_3 = 0}} \beta_{p_1, p_2, 0, p_4} \sqrt{p_1!} (b_2^{\dagger})^{p_2} (b_4^{\dagger})^{p_4} |0\rangle^{\otimes 2}$$

61. First and third detectors were clicked

62.

$$|\psi_4\rangle = \sum_{\substack{p_1, p_2, p_3, p_4\\p_1 \neq 0, p_3 \neq 0}} \beta_{p_1, p_2, p_3, p_4} \sqrt{p_1! p_3!} (b_2^{\dagger})^{p_2} (b_4^{\dagger})^{p_4} |0\rangle^{\otimes 2}$$

63. No detection

64.

$$|\psi_4\rangle = \sum_{\substack{p_2, p_4\\p_1=0, p_3=0}} \beta_{0, p_2, 0, p_4} (b_2^{\dagger})^{p_2} (b_4^{\dagger})^{p_4} |0\rangle^{\otimes 2}$$

65. Projection operators

66.

$$\hat{\Pi} = \Pi^{(1)} \otimes$$