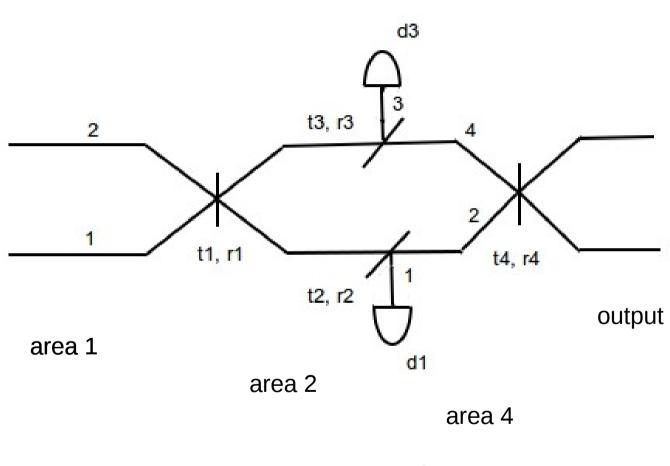
# Setup.



area 3

# Theory.

$$|\psi_{in}\rangle = g(a_1^{\dagger})|0\rangle = \sum_{n=0}^{\infty} g_n(a_1^{\dagger})^n|0\rangle$$

$$|\psi_{in}\rangle = f(a_1^{\dagger})|0\rangle = \sum_{n=0}^{\infty} f_n(a_1^{\dagger})^n|0\rangle$$

$$|\psi_{aux}\rangle = f(a_2^{\dagger})|0\rangle = \sum_{n=0} f_n(a_2^{\dagger})^n|0\rangle$$

1) State in two channels — area 1:

$$|\psi\rangle = |\psi_{in}\rangle \otimes |\psi_{aux}\rangle = \sum_{m,n} \alpha_{m,n} (a_1^{\dagger})^m (a_2^{\dagger})^n |0\rangle^{\otimes 2}$$

2) Mixed at first BS1: 
$$a_1^\dagger \to r_j a_1^\dagger + i t_j a_2^\dagger \\ a_2^\dagger \to r_j a_2^\dagger + i t_j a_1^\dagger \end{cases} \qquad r_j^2 + t_j^2 + a_j^2 = 1$$

3) State in area 2 — after BS1: 
$$|\psi_2\rangle=\sum_{m,n}\alpha_{m,n}^{(2)}(a_1^\dagger)^m(a_2^\dagger)^n|0\rangle^{\otimes 2}$$

$$\sum_{m,n} |\alpha_{m,n}^{(2)}|^2 = 1$$
 For ideal BS (a = 0)

4) State in area 3 (4 channels) — after BS2 and BS3 but before detection:

$$|\psi_3\rangle = \sum_{p_1, p_2, p_3, p_4} \beta_{p_1, p_2, p_3, p_4} (a_1^{\dagger})^{p_1} (a_2^{\dagger})^{p_2} (a_3^{\dagger})^{p_3} (a_4^{\dagger})^{p_4} |0\rangle^{\otimes 4}$$

- 5) State in area 4 (4 channels) after detection:
- 5.1) Only 1st detector was clicked:

Detectors are ideal!

$$|\psi_4\rangle = \sum_{\substack{p_1, p_2, p_4\\p_1 > 0, p_3 = 0}} |\beta_{p_1, p_2, 0, p_4} \sqrt{p_1! p_2! p_4!}|^2 |p_2, p_4\rangle$$

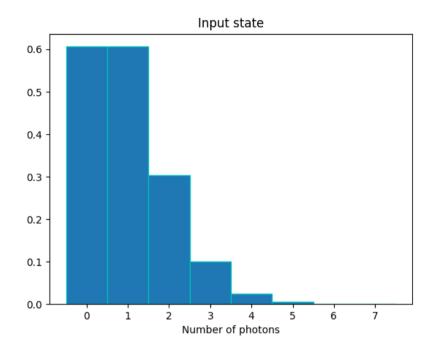
5.2) Both detectors (1st and 3rd) were clicked:

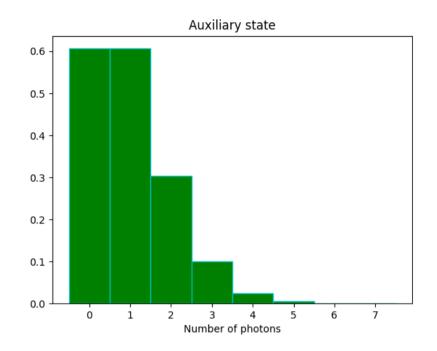
$$|\psi_4\rangle = \sum_{\substack{p_1, p_2, p_3, p_4 \\ p_1 > 0, p_3 > 0}} |\beta_{p_1, p_2, p_3, p_4} \sqrt{p_1! p_2! p_3! p_4!}|^2 |p_2, p_4\rangle$$

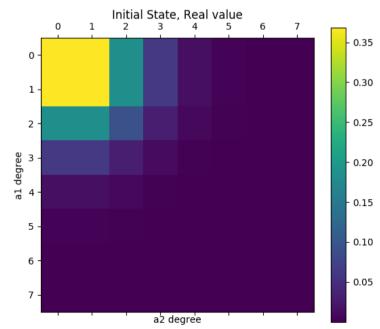
5) State after having been mixed at BS4 (final state):

$$|\psi_{out}\rangle = \sum_{m,n} \alpha_{m,n} (a_1^{\dagger})^m (a_2^{\dagger})^n |0\rangle^{\otimes 2}$$

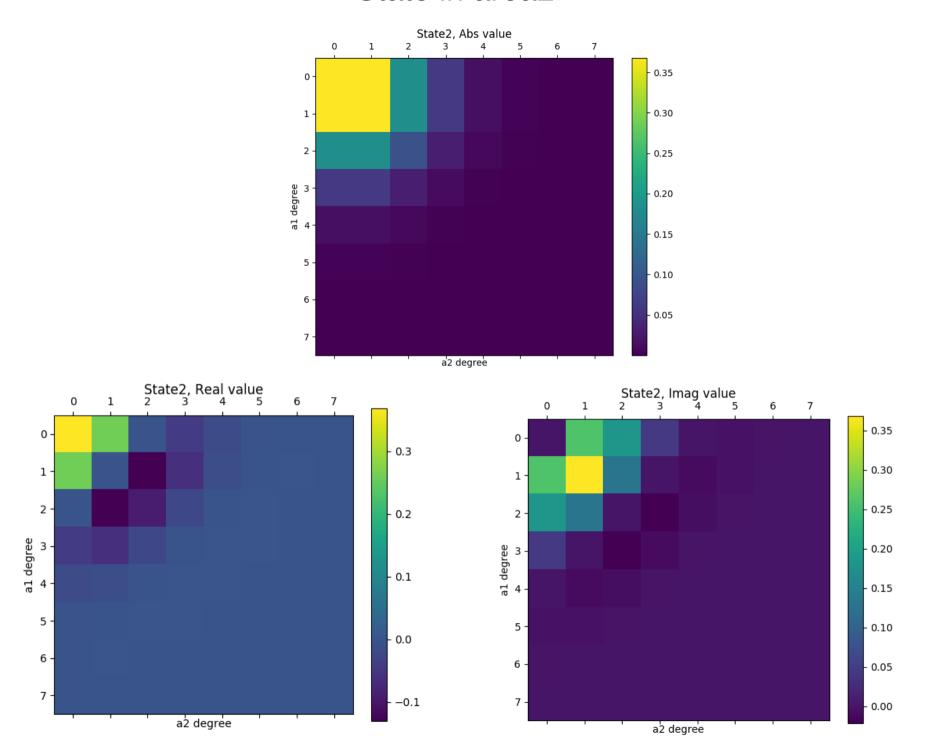
## 1) Input — coherent state. Aux — coherent state.



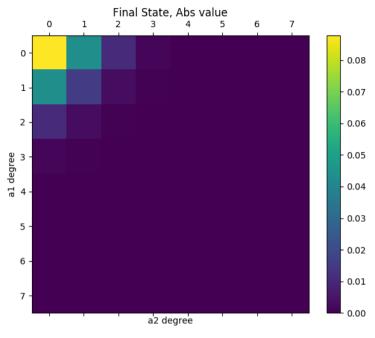


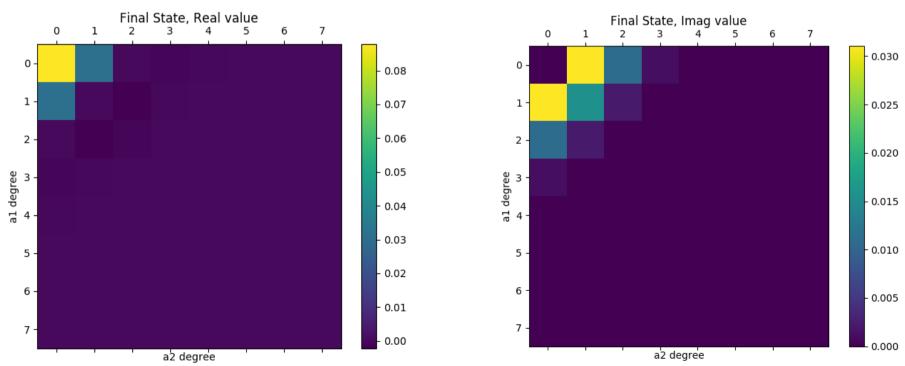


#### State in area2.

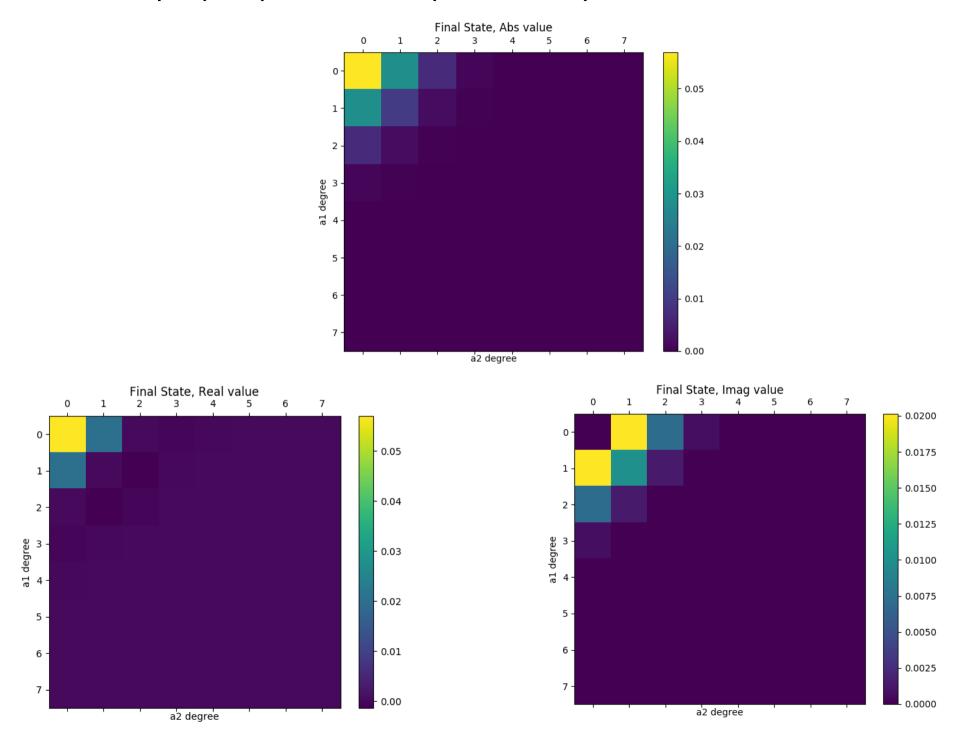


## Output(final) state. First detector was clicked.

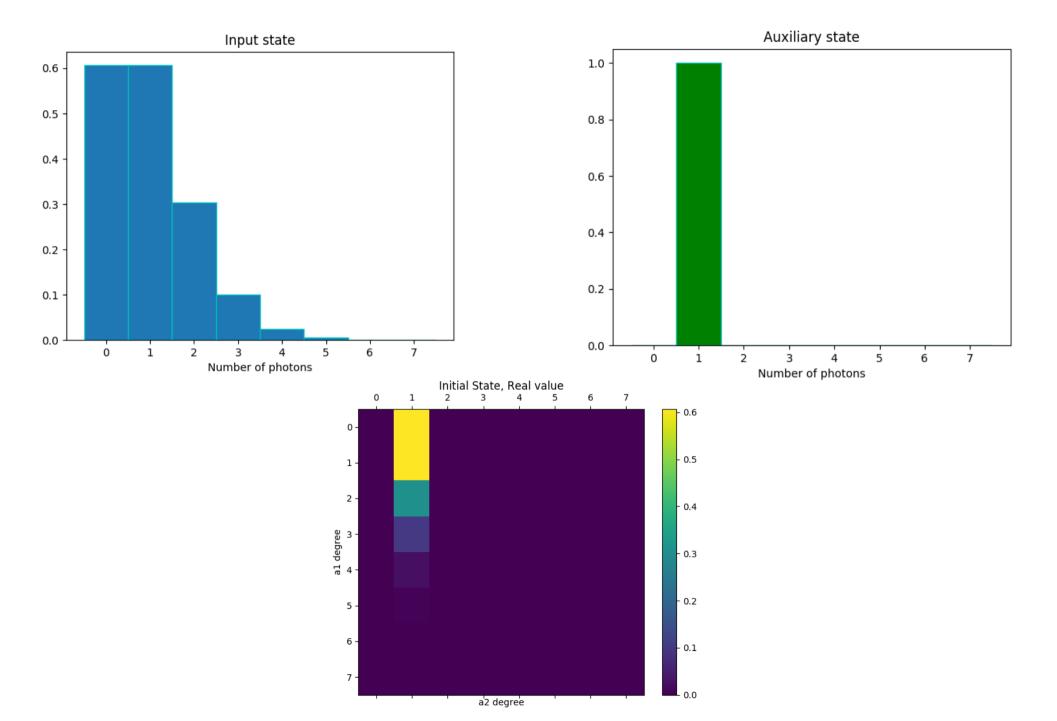




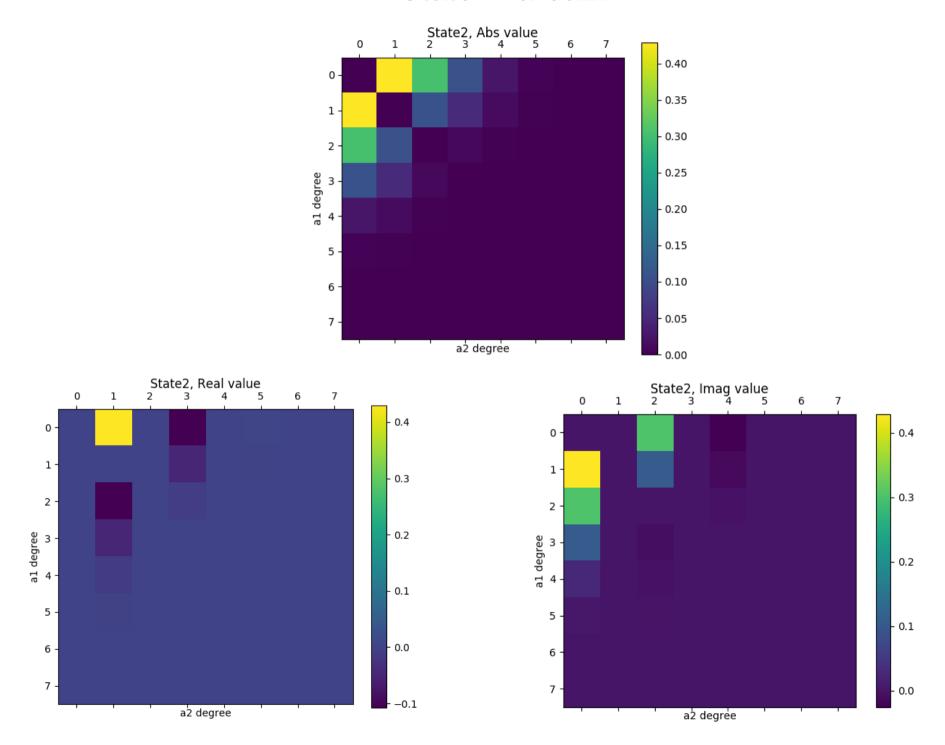
#### Output(final) state. Both (1st and 3rd) detectors were clicked.



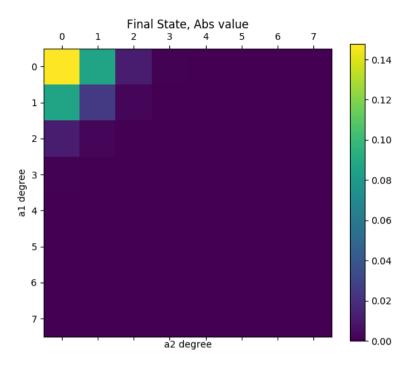
# 2) Input — coherent state. Aux — single photon.

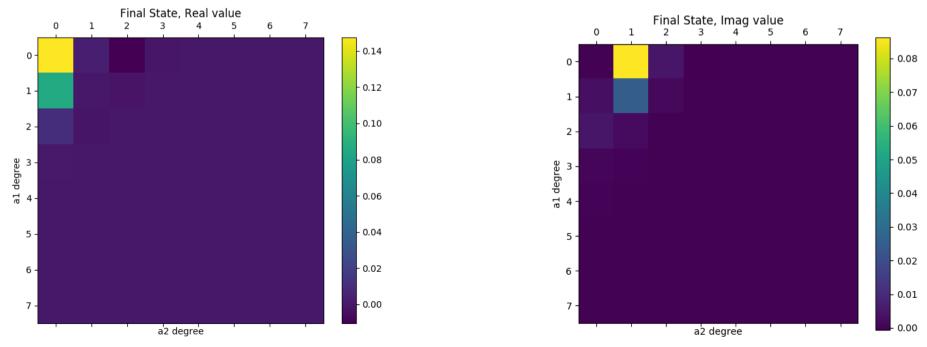


#### State in area2.



## Output(final) state. First detector was clicked.





#### Output(final) state. Both (1st and 3rd) detectors were clicked.

