If T is an invertible linear transformation, then all eigenvalues of T are non-zero.

Proof. Suppose T is invertible. Then $T(v) \neq 0$ for $v \neq 0$, which is true of eigenvectors. Therefore 0 cannot be an eigenvalue of T, so all eigenvalues of T are nonzero. □