The linear transformation $T : V \to V$ is injective if and only if zero is not an eigenvalue of T.

The linear transformation $T : V \to V$ is injective if and only if $T(v) = 0$ iff $v = 0$, i.e. if and only if T has no eigenvectors with eigenvalue 0.