Let $T : V \to V$ be the scale map $T(v) = kv$ for positive k. Then T has eigenvectors $\vec{v}$ with the eigenvalue k for all nonzero vectors $\vec{v} \in V$.

Since $T(v) = kv$, all $v \in V$ are eigenvectors with eigenvalue k.