Any nonzero element in the kernel of $T : V \to V$ is an eigenvector of T with eigenvalue 0.

Suppose $v \neq 0$ and $v \in \ker T$. Then $T(v) = 0 = 0 \cdot v$. Thus v is an eigenvector with eigenvalue 0.