

If T is an orthogonal transformation, then the only possible eigenvalues are 1 or -1 .

Proof. Since orthogonal transformations preserve lengths, if v is an eigenvector of T , $\|v\| = \|\lambda v\|$, which holds precisely when $\lambda = \pm 1$. \square