

The identity map I_V has eigenvectors \vec{v} with the eigenvalue 1 for all nonzero vectors $\vec{v} \in V$.

The identity map $V \rightarrow V$ is $I(v) = v = 1 \cdot v$ for all $v \in V$. Thus all $v \in V$ are eigenvectors with eigenvalue 1.