

Suppose  $a, b \in \mathbb{R}$ . Then  $a^2 + b^2 \neq (a + b)^2$  if and only if  $a \neq 0$  and  $b \neq 0$ .

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*Proof.* Observe that  $(a + b)^2 = a^2 + 2ab + b^2$ . If  $a \neq 0$  and  $b \neq 0$ ,  $2ab \neq 0$ , so  $a^2 + 2ab + b^2 \neq a^2 + b^2$ . Conversely, if  $a = 0$  or  $b = 0$ ,  $2ab = 0$ , so  $a^2 + 2ab + b^2 = a^2 + b^2$ .  $\square$