The linear transformation  $T:V\to V$  is injective if and only if zero is not an eigenvalue of T.

The linear transformation  $T: V \to V$  is injective if and only if T(v) = 0 iff v = 0, i.e. if and only if T has no eigenvectors with eigenvalue 0.