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Practical Cryptographic Systems

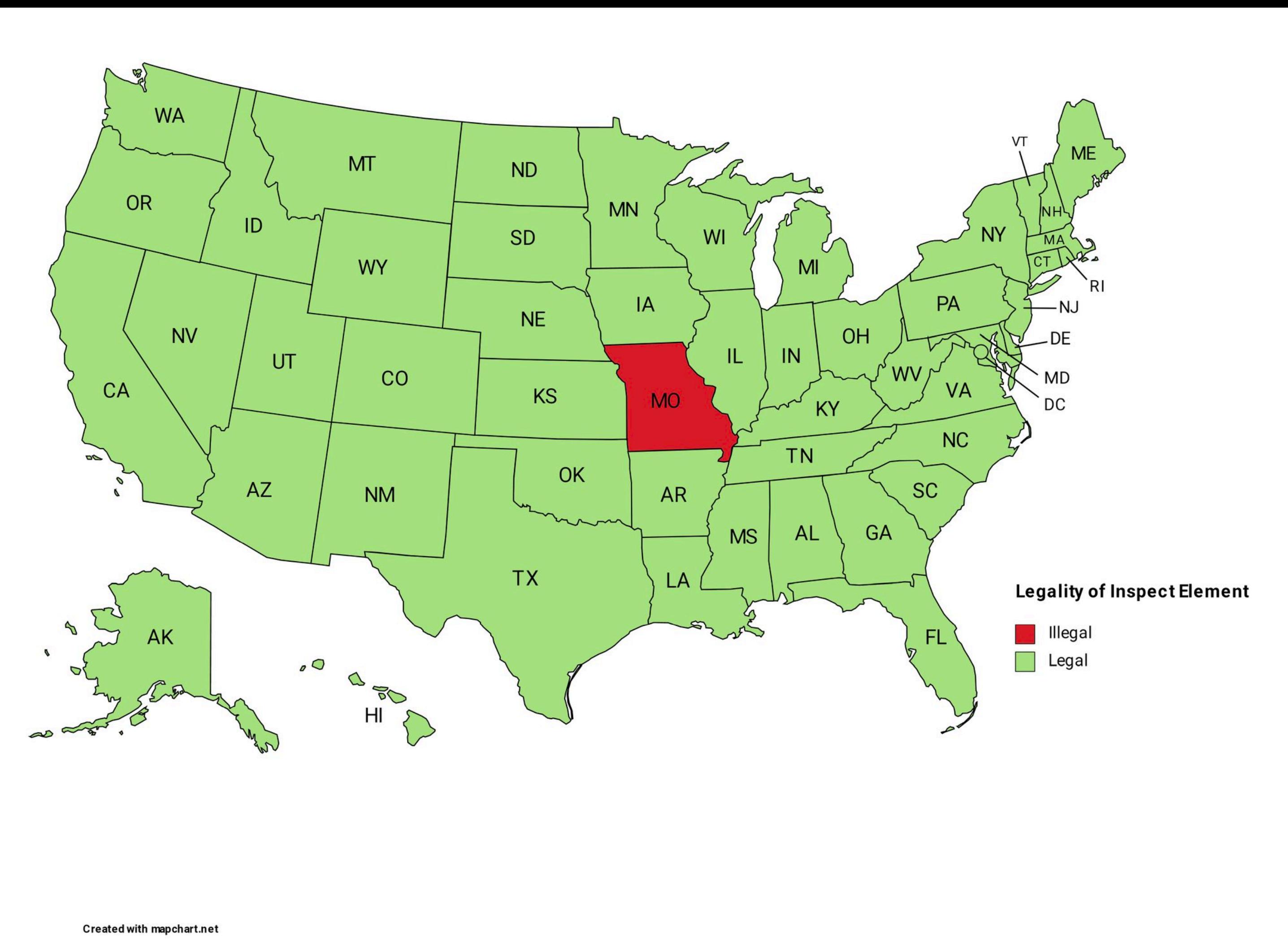
MPC and Private Computation

Instructor: Alishah Chator

Housekeeping

- Assignment 2 due Tuesday 10/26 at 11:59pm
- Weekly HW#3 coming out tonight
- Midterm 11/1
 - Will be covering all lecture and reading material so far

News



NEWS

Minneapolis schools are spying on queer students & outing them to teachers and parents

The software has outed one student and also incorrectly notified a transgender teen's parents after they wrote about their past suicidal thoughts.

By LGBTQ Nation Saturday, October 16, 2021

REvil ransomware shuts down again after Tor sites were hijacked

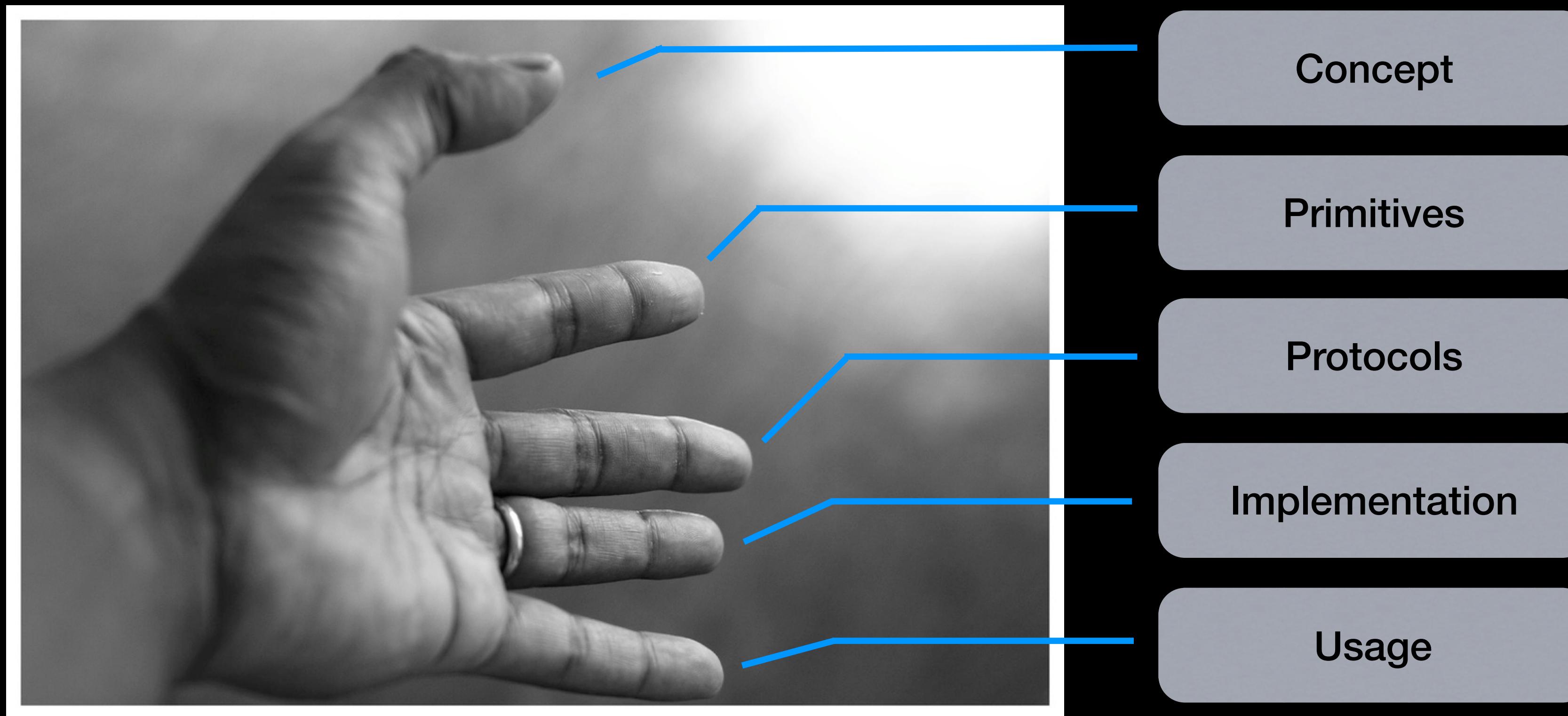
By [Lawrence Abrams](#)

October 17, 2021

07:19 PM

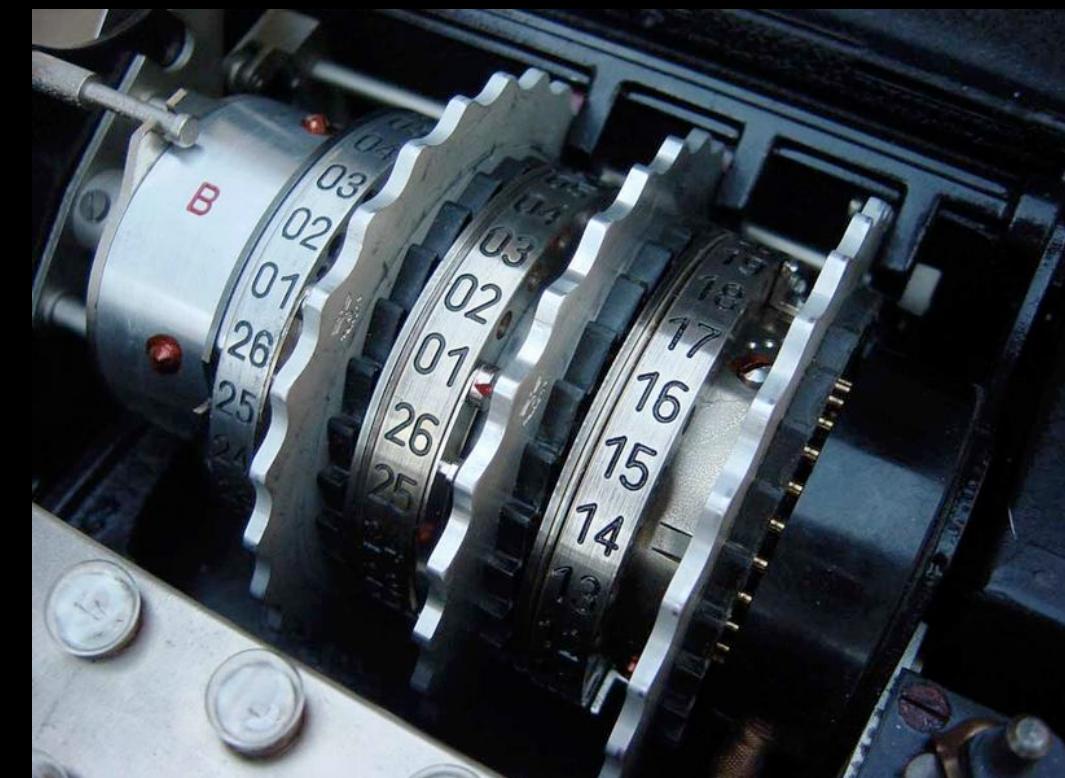
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Part 1

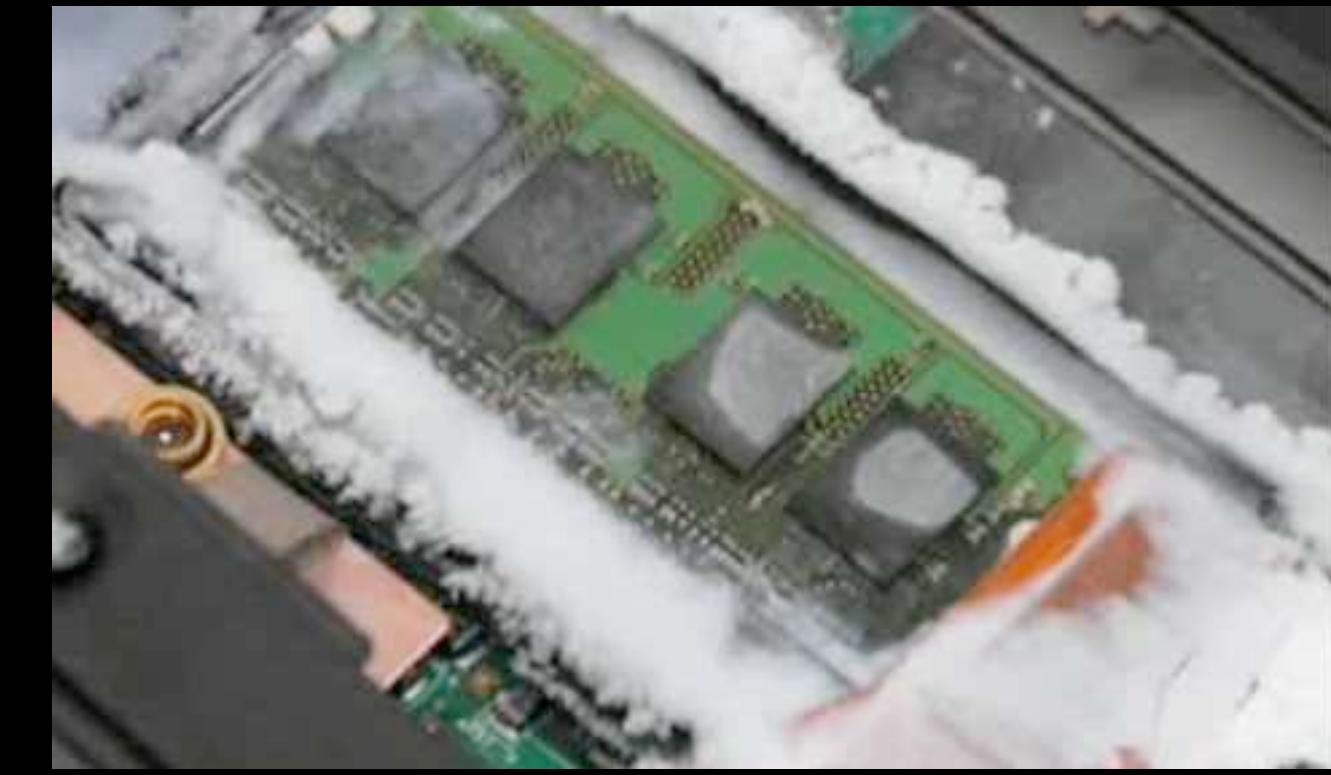
- (Re-)introduction to Crypto... at high speed:
 - Classical cryptography
 - Symmetric-key encryption & block ciphers
 - AES, ChaCha
 - Public-key cryptography
 - Diffie-Hellman, RSA, ECC



Enigma image from Wikipedia, used under GFDL.

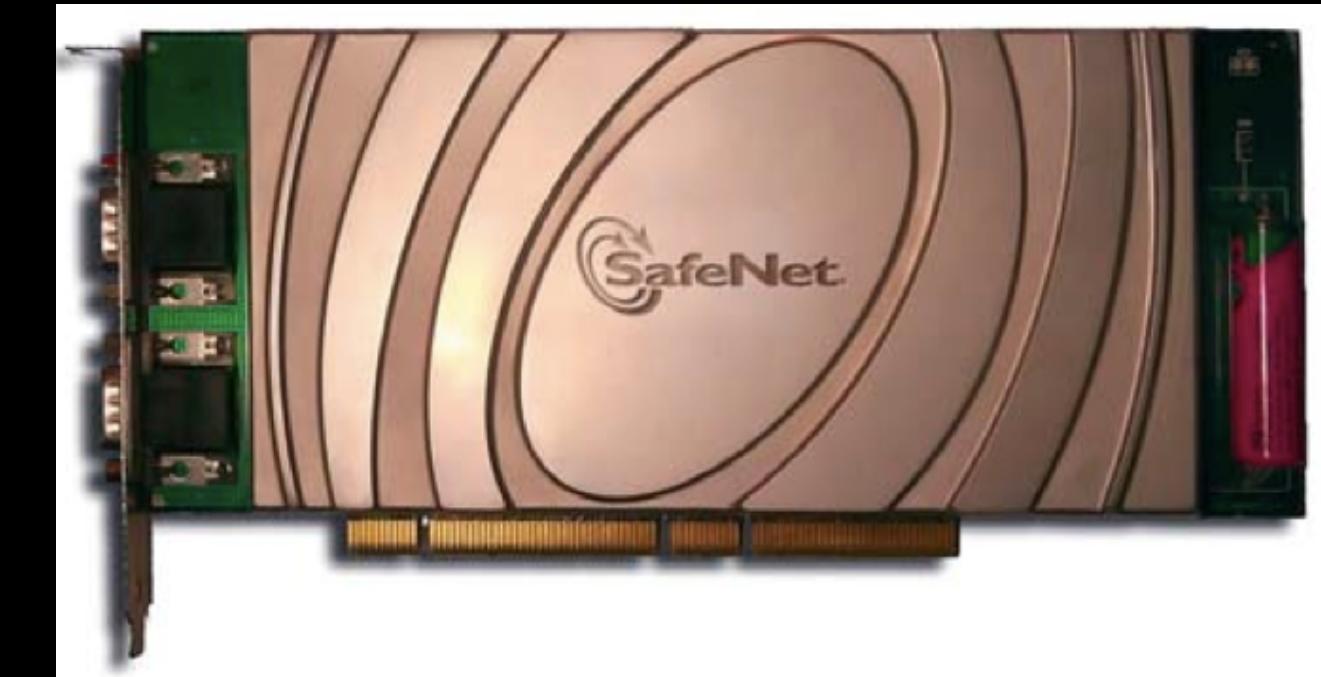
Part 2

- Exploiting Software:
 - Crypto vulnerabilities and where they turn up
- Privacy
 - Multi-party Computation
 - Tor and Anonymity
 - Zero Knowledge Proofs



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Today

- What is Multiparty Computation?
- How can we build an MPC system

MPC: the Classic Example

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I am the richest person around

MPC: the Classic Example



Image credit: Bloomberg

No, I am the richest!



I am the richest person around

MPC: the Classic Example



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No, I am the richest!



I am the richest person around

What if neither party wants to disclose their net worth?

MPC More concretely



Atlas des Plantes de France,
A. Masclef 1891

Pl. 276. *Bette vulgaire.* (*Betterave*). *Beta vulgaris* L.

Technology preview: Private contact discovery for
Signal

A small circular logo in the top right corner of the slide, depicting a white sailboat with a single mast and sail, set against a blue and white background.

MPC Formally

- A Multiparty Computation Protocol involves a set of parties $\{A, B, C, \dots\}$, a private input for each party $\{x_A, x_B, x_C, \dots\}$ and some functionality to jointly compute $f(x_A, x_B, x_C, \dots) = y$
- Each party should learn nothing besides the output y
- Crucially, that means the input of all other parties should be hidden

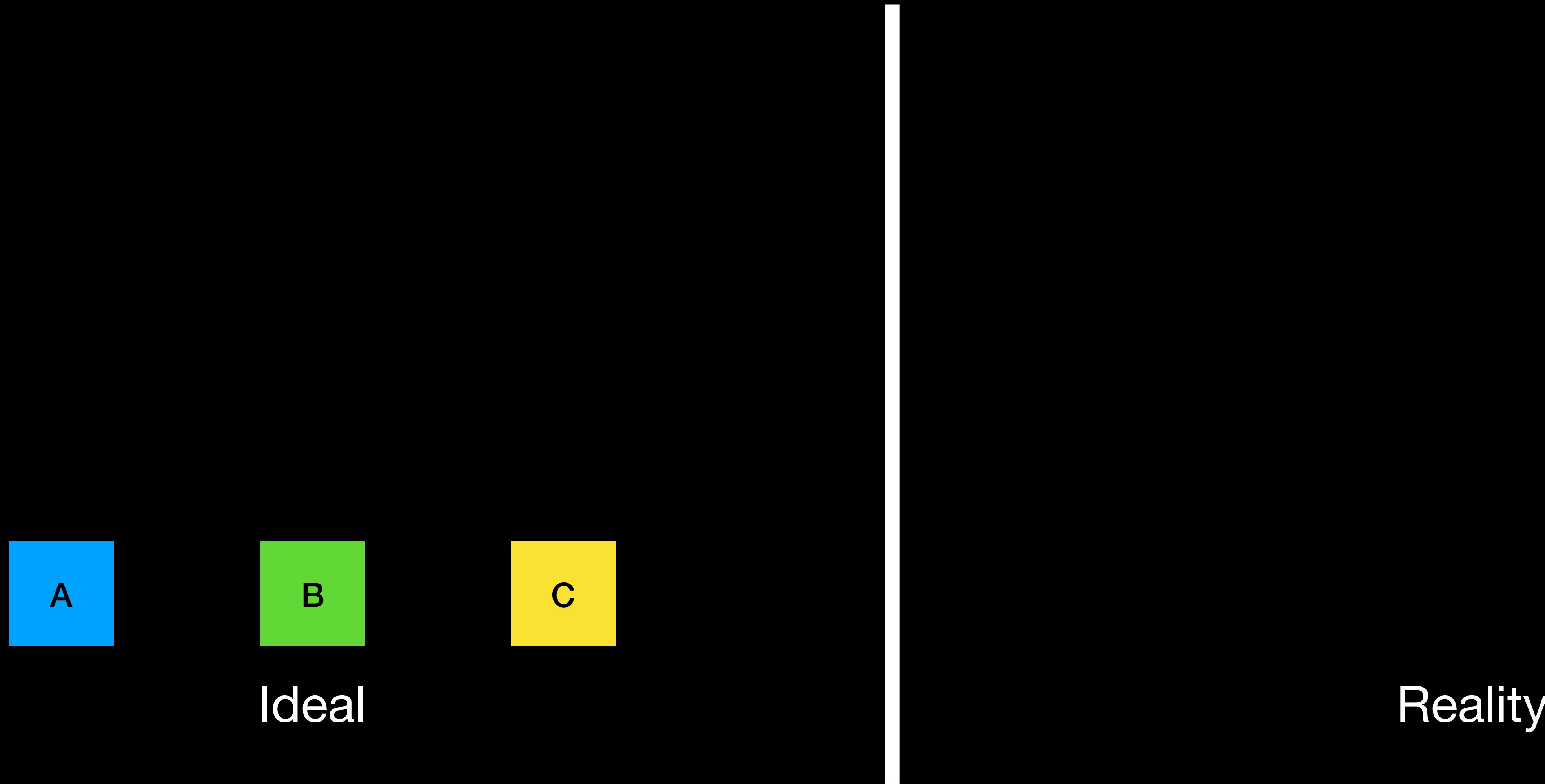
MPC: Ideal vs Reality

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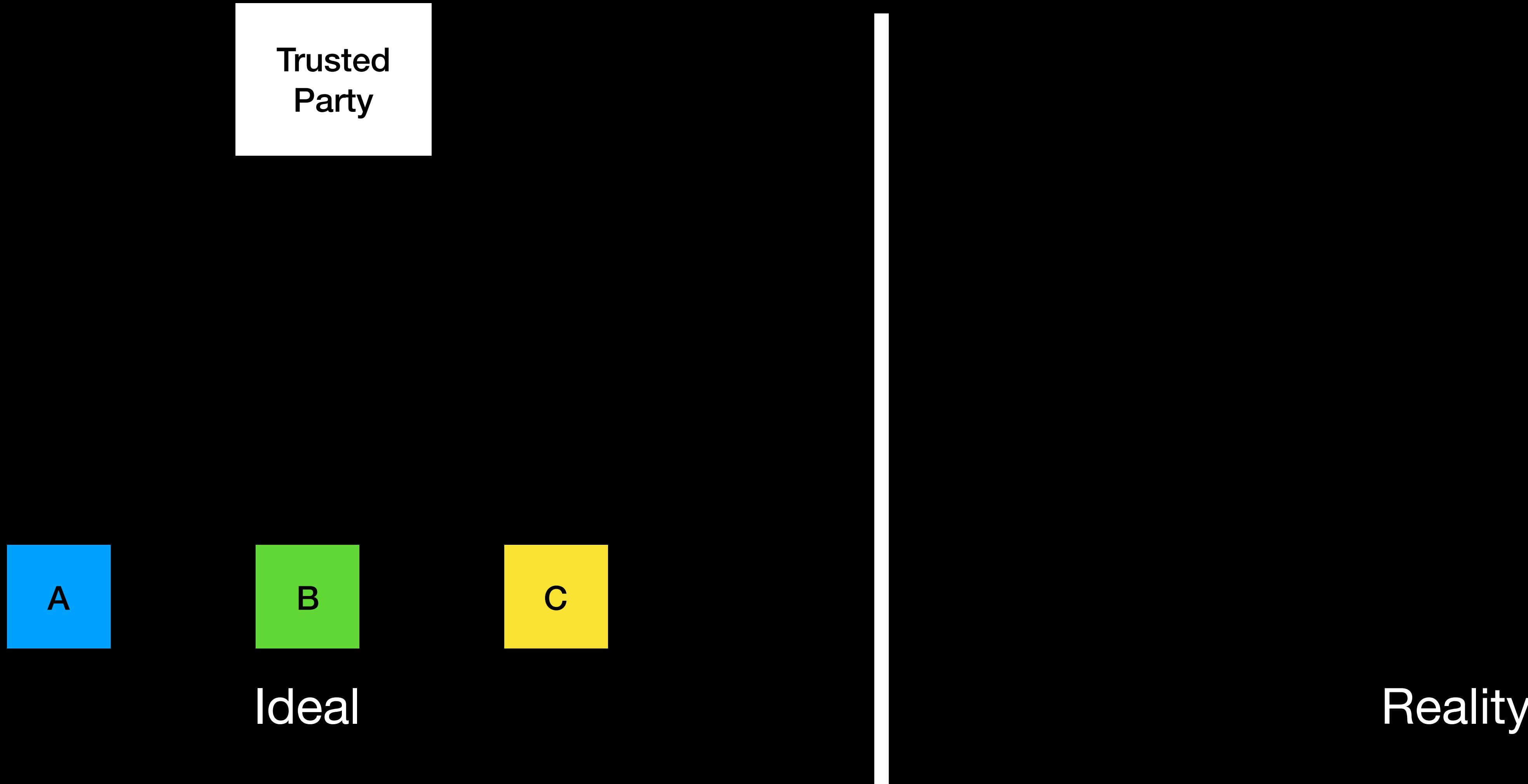
Ideal

Reality

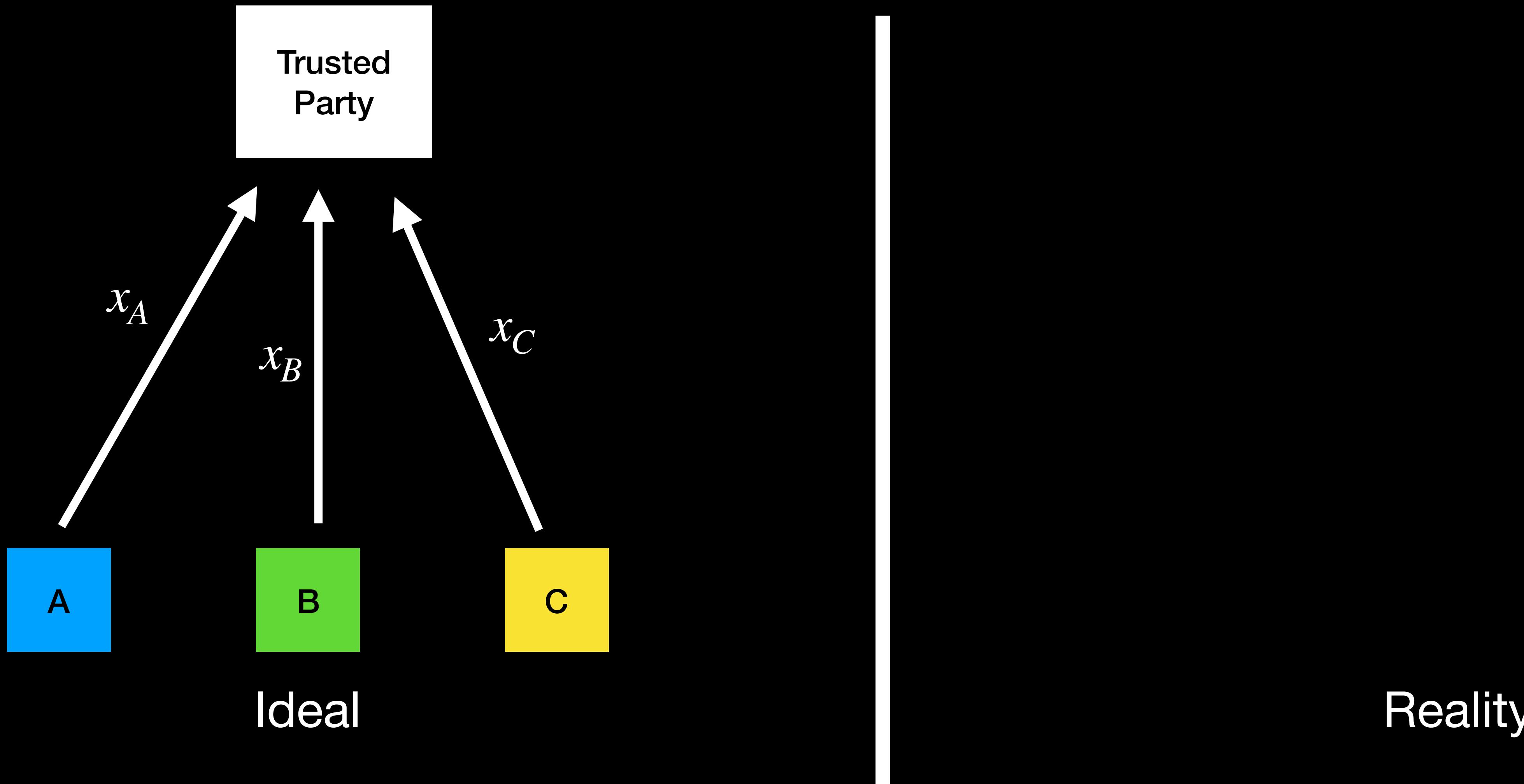
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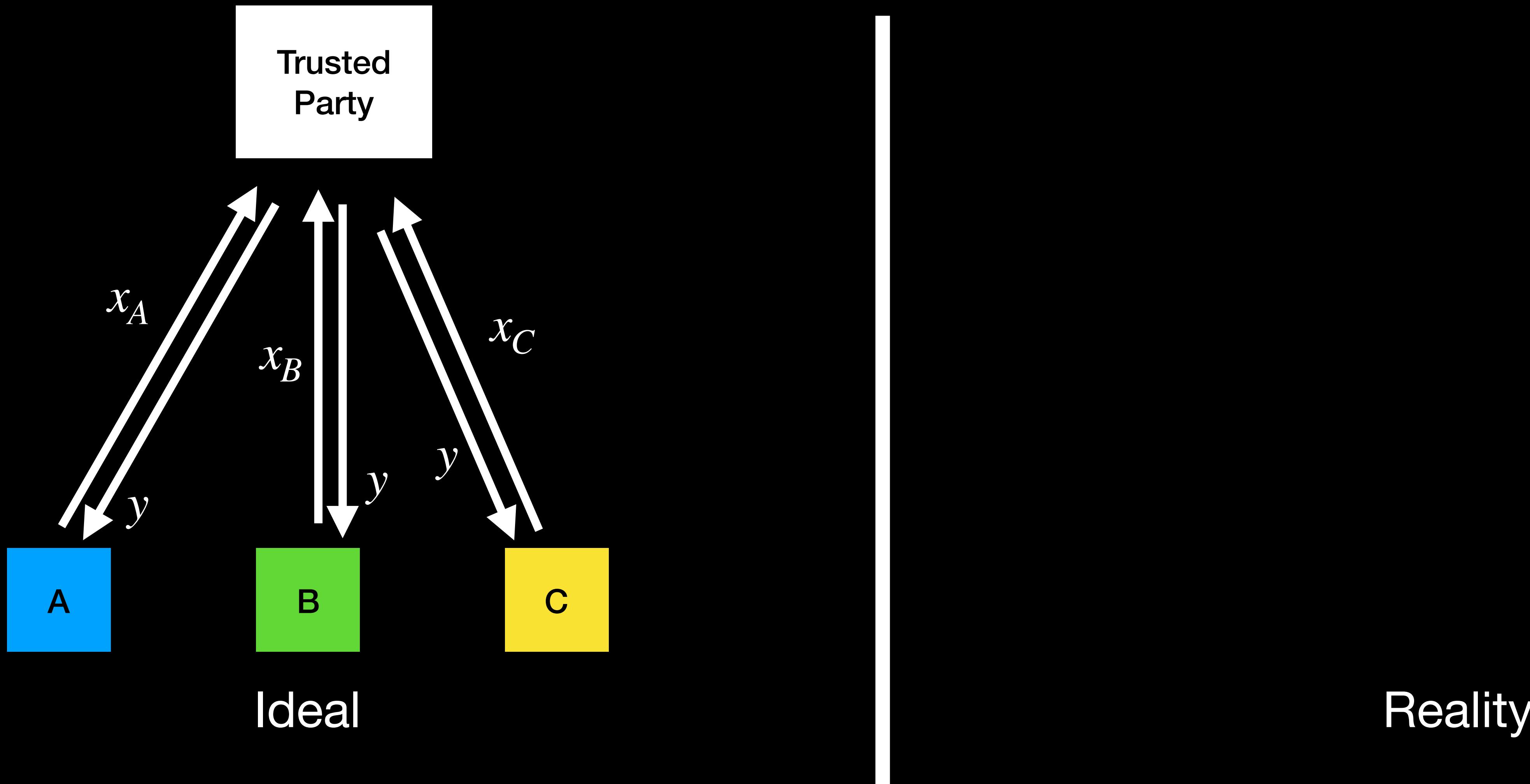
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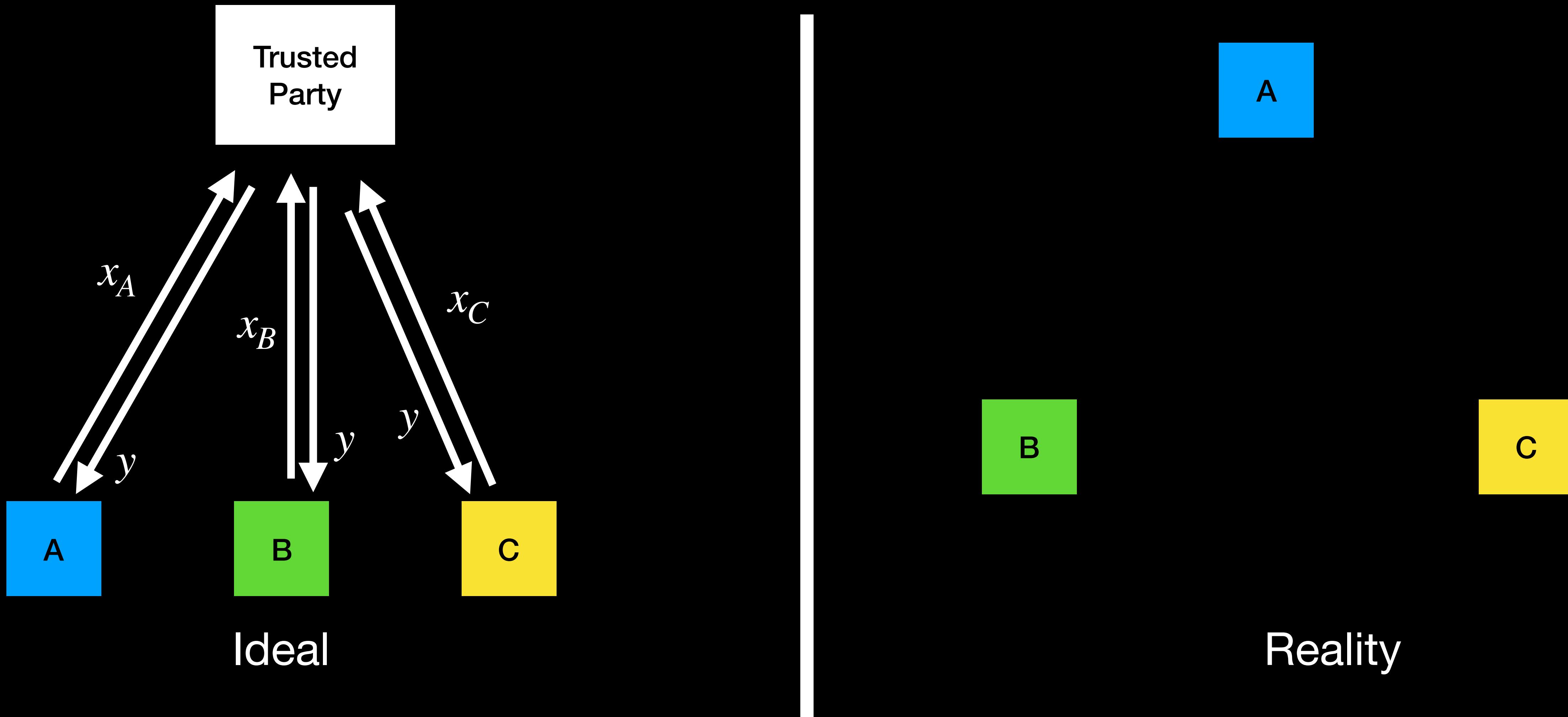
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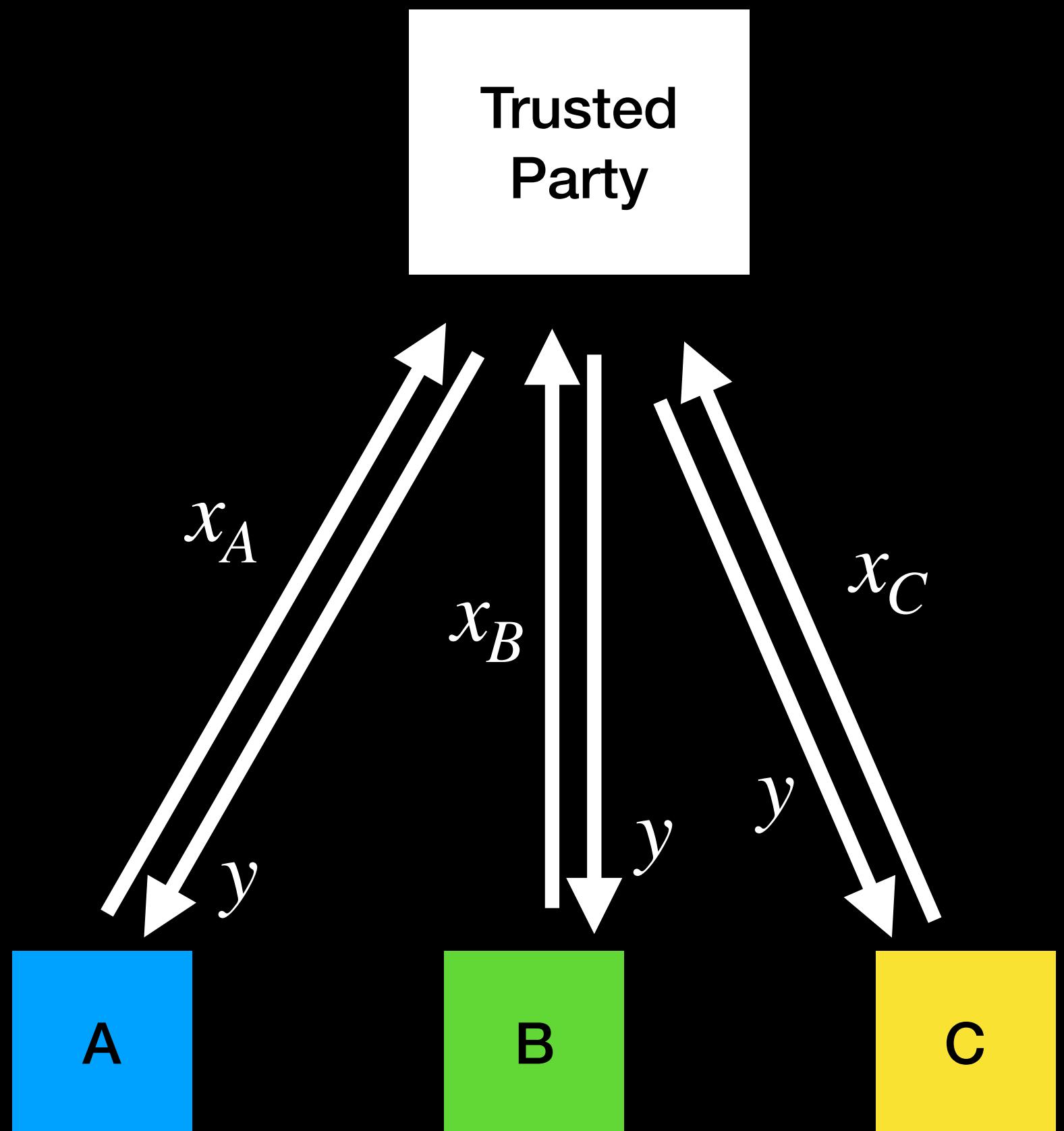
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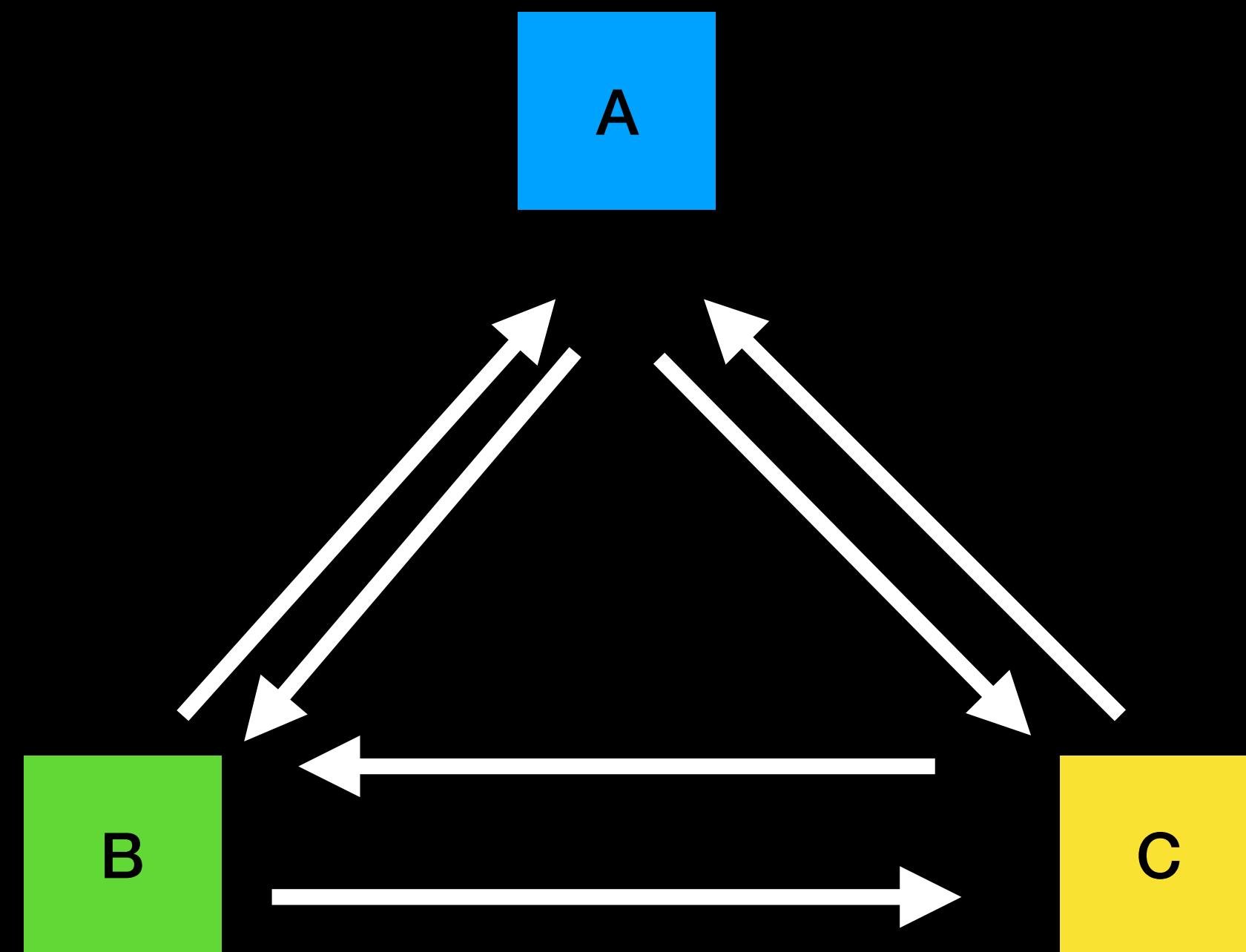
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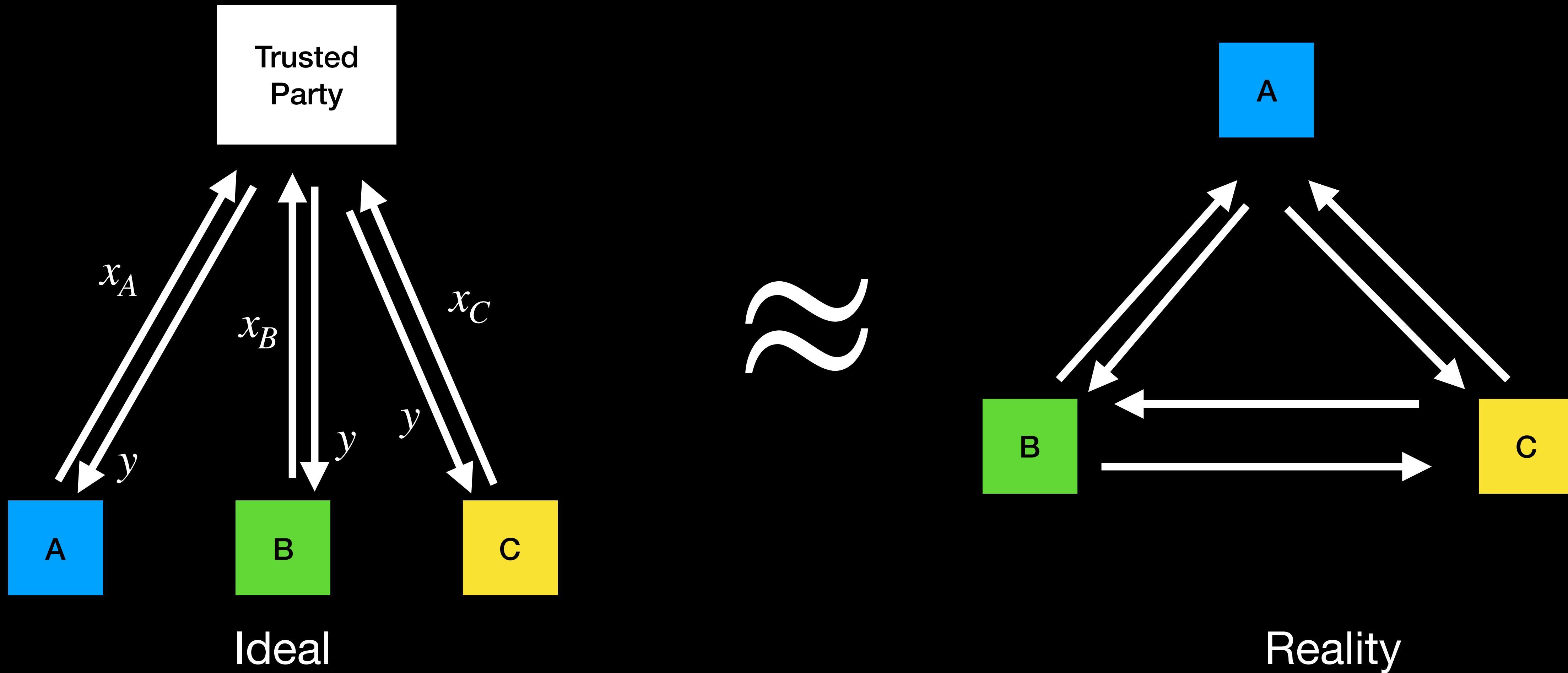


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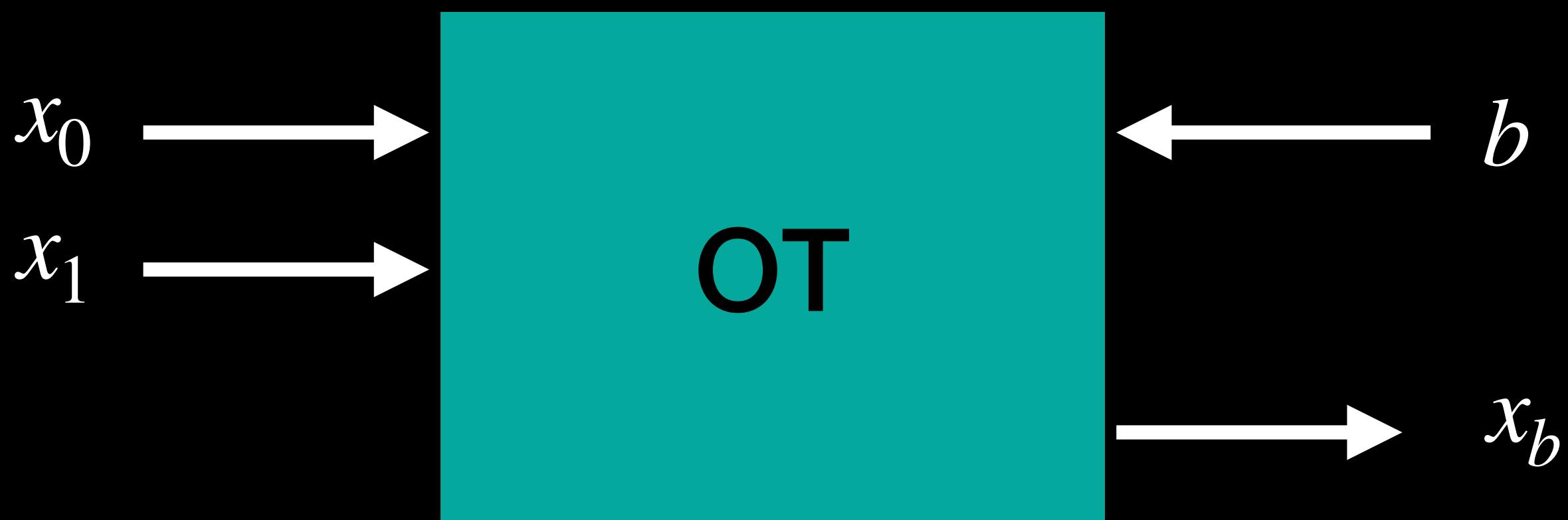
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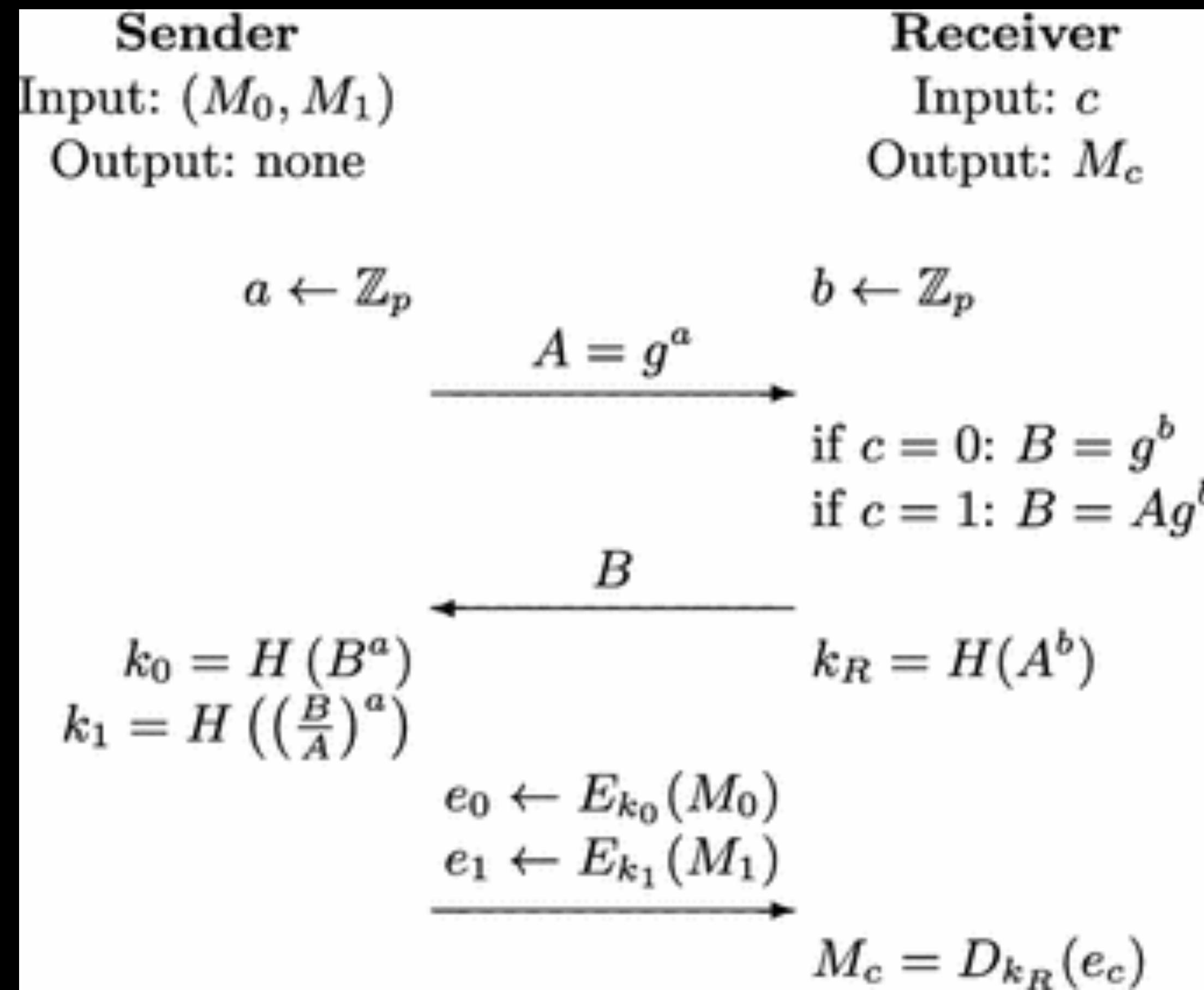
Building Block

- Consider a simple protocol for retrieving one of two values from a party

1-out-of-2 Oblivious Transfer



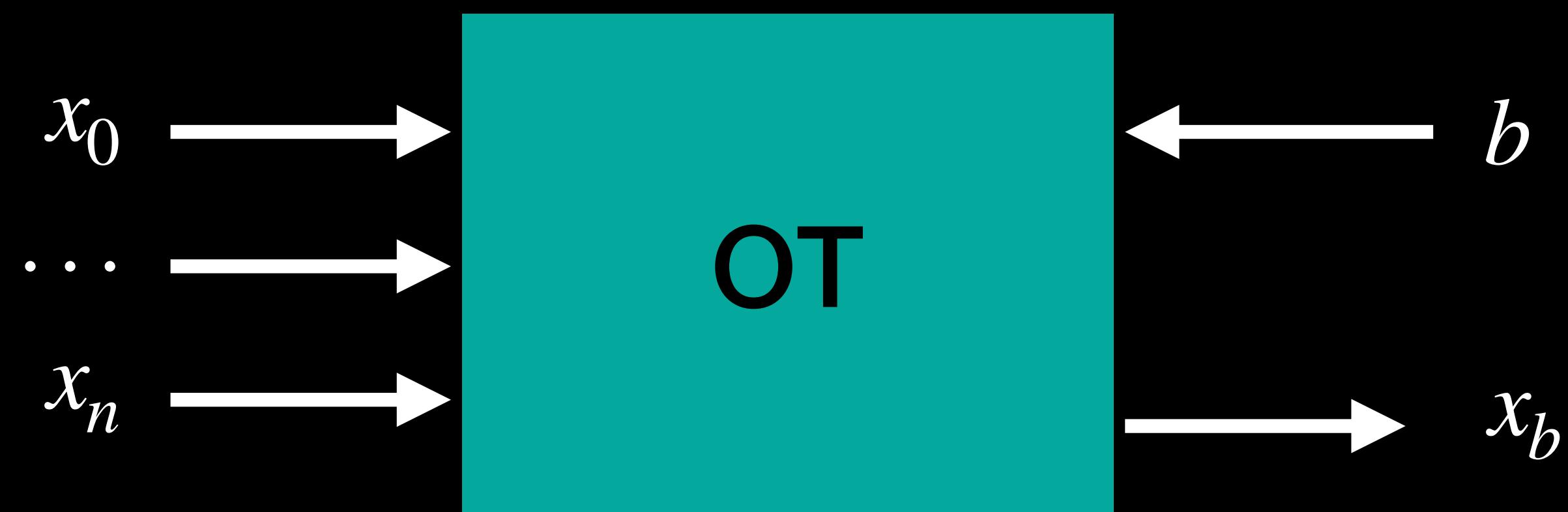
Oblivious Transfer



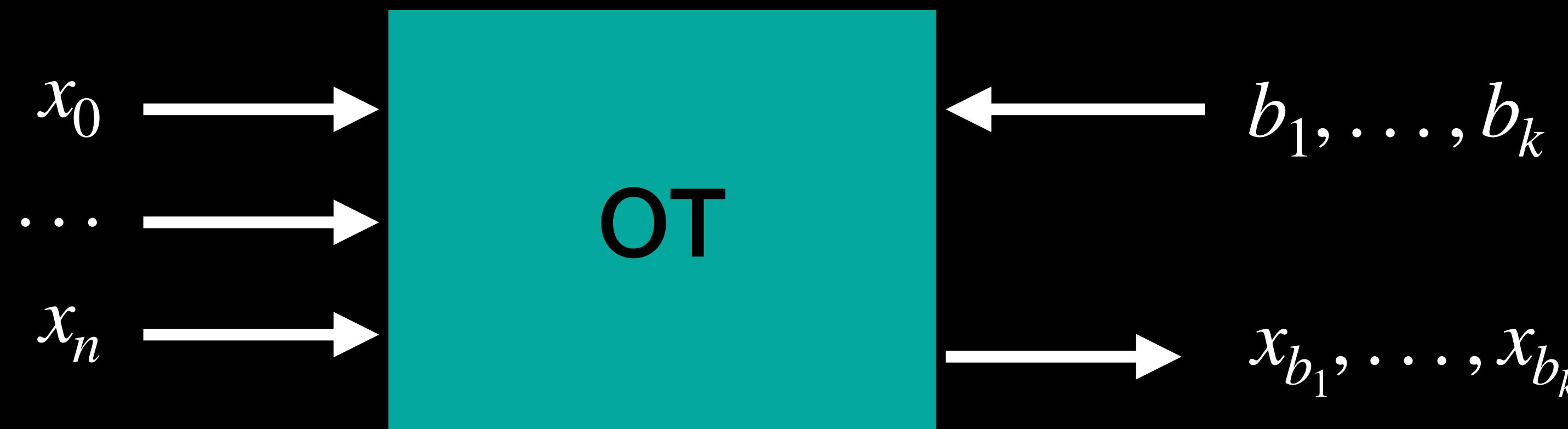
Oblivious Transfer and MPC

- Oblivious Transfer is complete for MPC!
- Note: the protocol we showed is only **semi-honest secure**: It only is secure against an adversary that may try to learn additional information but otherwise follows the protocol
 - Stronger security is possible but difficult so we will focus on semi-honest for now
- We saw 1-out-of-2 OT but we could also have 1-out-of-n OT or k-out-of-n OT

1-out-of-n Oblivious Transfer



k-out-of-n Oblivious Transfer



Private Information Retrieval (PIR)

- Goal: Query a server's database without:
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- How might we do this naively?
- Can we use OT to build this?