

**601.445/601.645**

# **Practical Cryptographic Systems**

## **Symmetric Cryptography**

Instructor: Matthew Green

# Housekeeping

- Website updated
  - Slides up as we go (<https://github.com/matthewdgreen/practicalcrypto>)
  - Reading assignment today (for Mon)  
Anderson chap 5.7
  - Assignment 1 out this afternoon

# News?

# News?

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( U.S. markets close in 6 hours 15 minutes

S&P 500	Dow 30	Nasdaq	Russell 2000
4,518.53 -1.50 (-0.03%)	35,175.15 +75.15 (+0.21%)	15,325.79 -48.53 (-0.32%)	2,266.43 -9.18 (-0.40%)

Bloomberg

## Juniper Breach Mystery Starts to Clear With New Details on Hackers and U.S. Role



A large image showing the exterior of a Juniper Networks building. The company's name is prominently displayed on the side of the building against a blue sky with some clouds. The image is framed by black bars on the left and right sides, with circular arrows at the bottom corners indicating it's a scrollable image.

# Security/crypto news

- Hacker news: [news.ycombinator.com](https://news.ycombinator.com)
- Ars Technica
- Twitter (e.g., here's a list)  
<https://twitter.com/i/lists/953639568816984064?s=20>

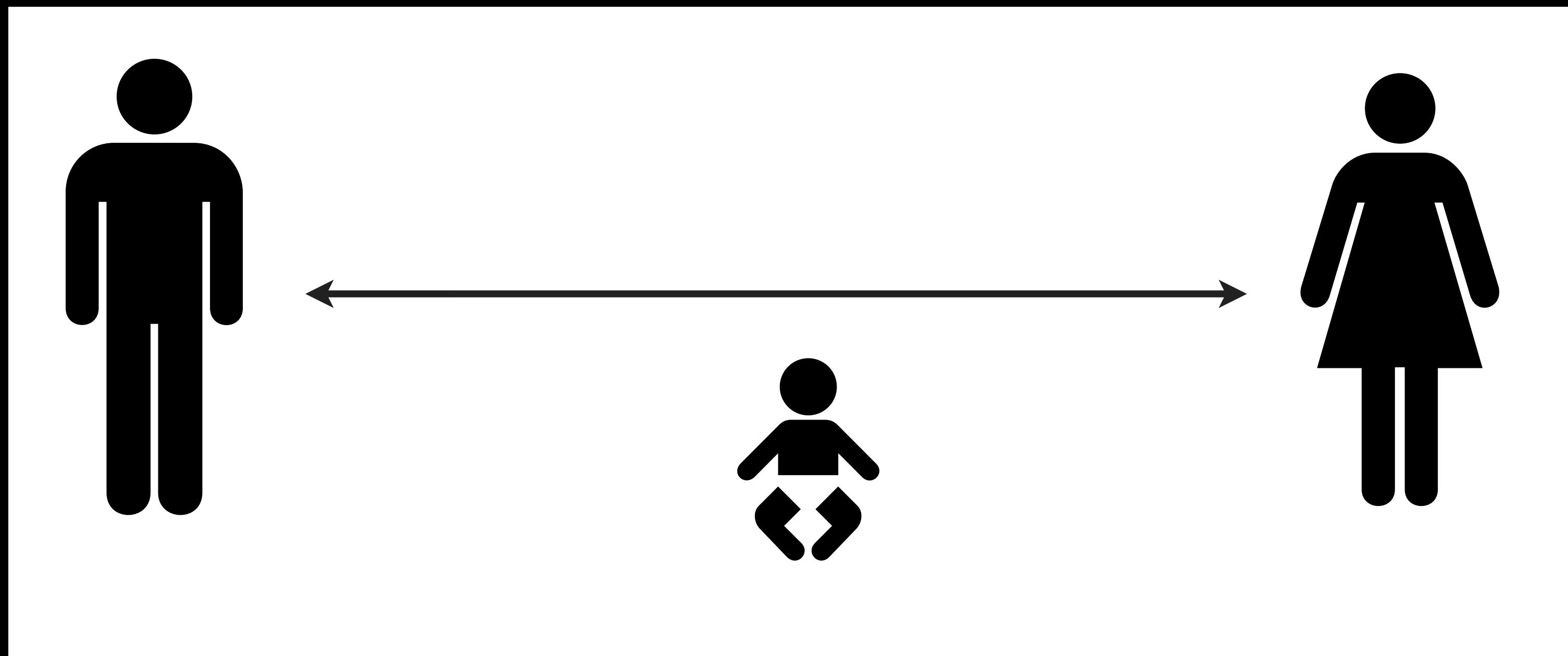
# Review

- Last time:
  - A few examples of how systems break
  - Bad primitives, bad protocols, bad implementation
- Today:
  - A (brief) tour through cryptologic history
  - Starting with symmetric (secret-key) crypto

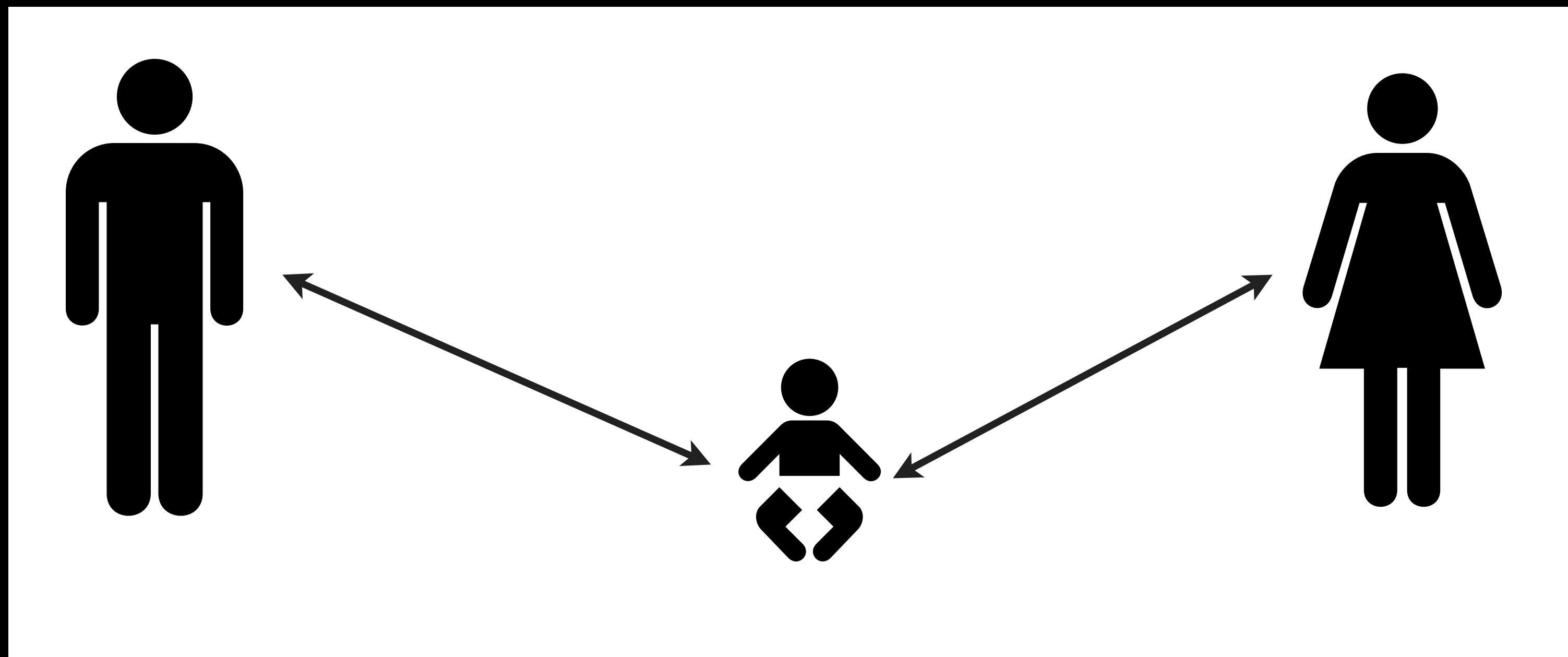
# Communication Model



# Communication Model



# Communication Model



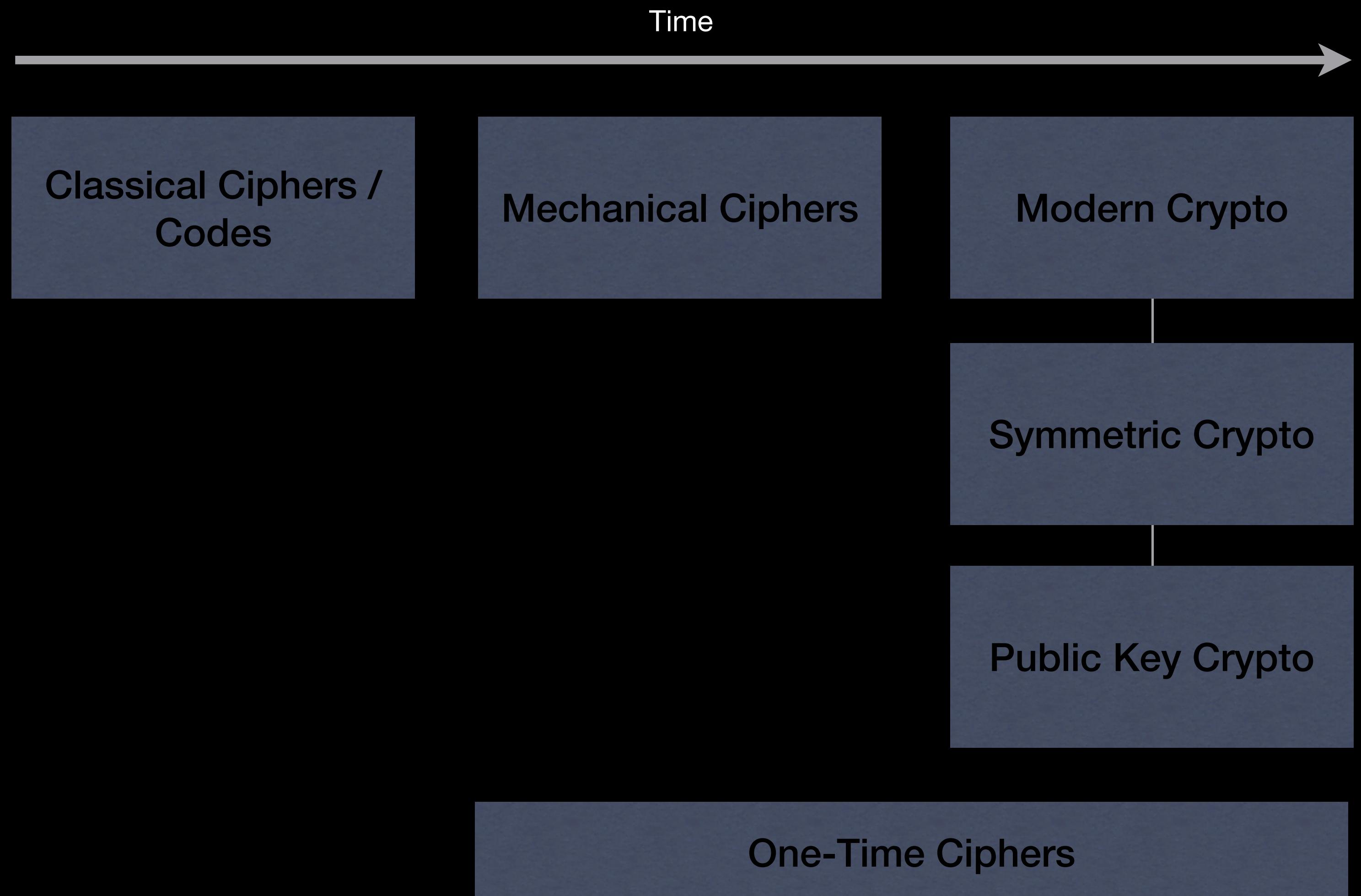
# Secure Communication

- Two basic properties we like to achieve:
  - Data confidentiality
  - Data authenticity (“integrity”)

# Secure Communication

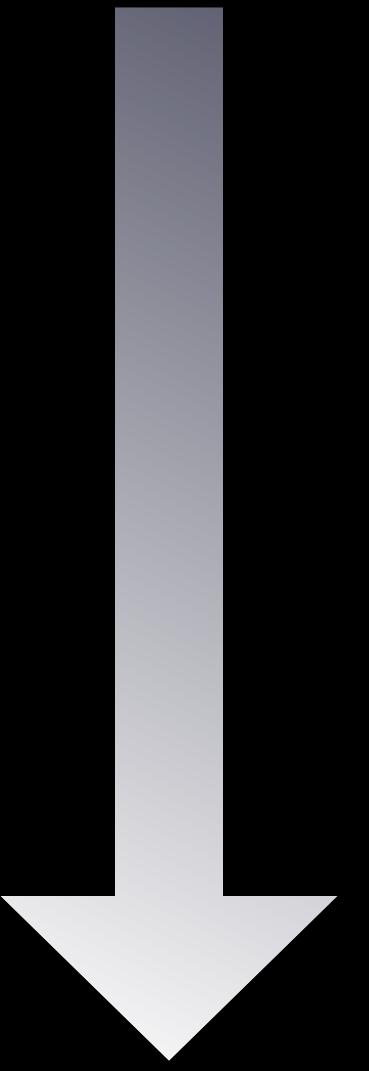
- Two basic properties we like to achieve:
  - Data confidentiality
  - Data authenticity (“integrity”)
- Tools:
  - Encryption / Key exchange
  - Message Authentication Codes (MACs)
  - Digital Signatures

# History of Encryption



# Classical Cryptography

- Beginning of time to 1900s or so
  - Shift (Caesar) cipher
  - Substitution ciphers
  - Polyalphabetic ciphers (Vigenère)
  - Digraph ciphers (Playfair)
  - A multitude of others...



Increasing  
Complexity

**<- Load New Puzzle**

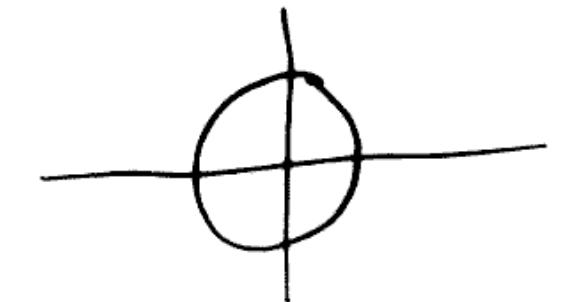
# CRYPTOGRAM

Points 979  
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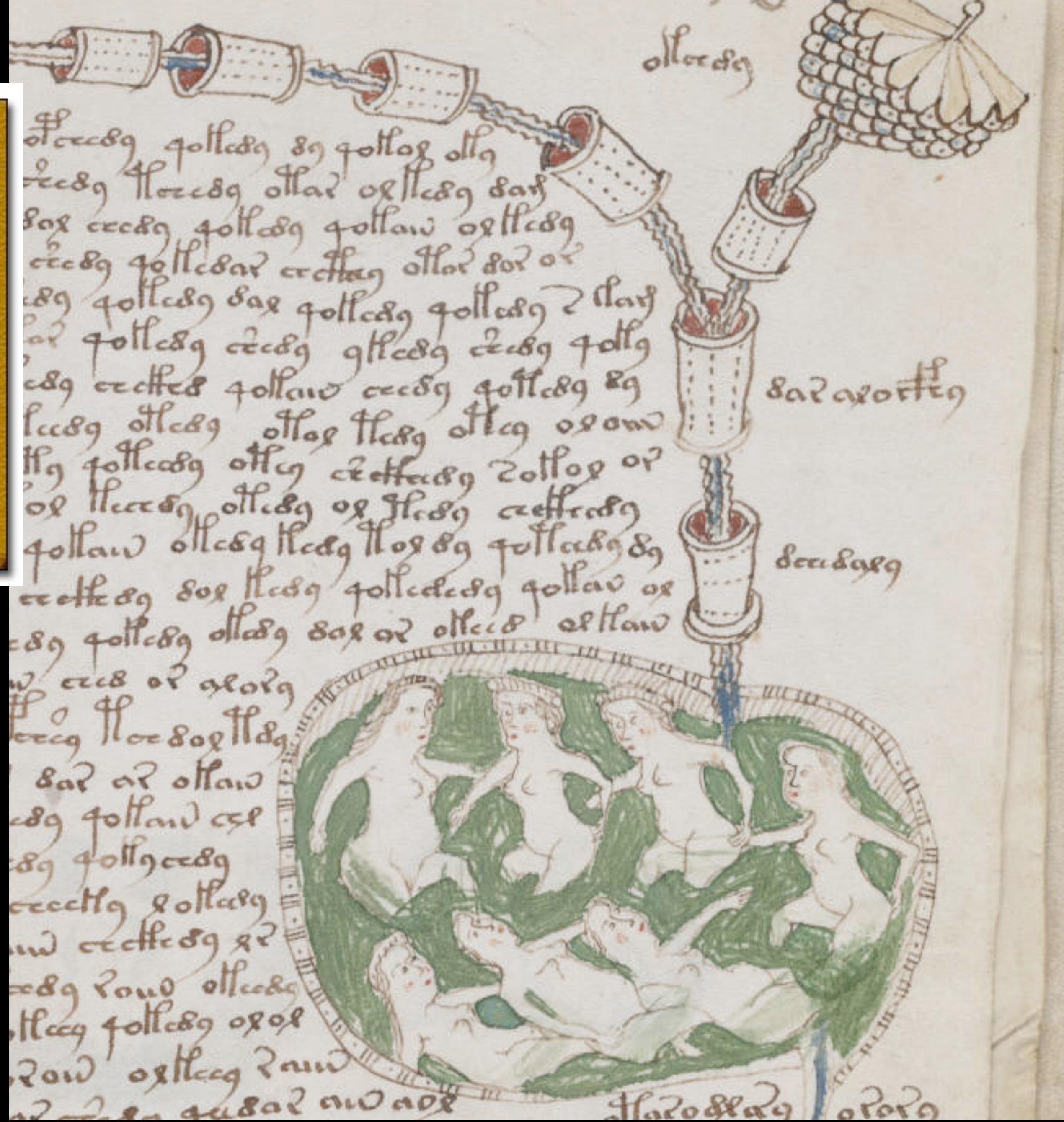
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G	J	H	O

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# Vigenere

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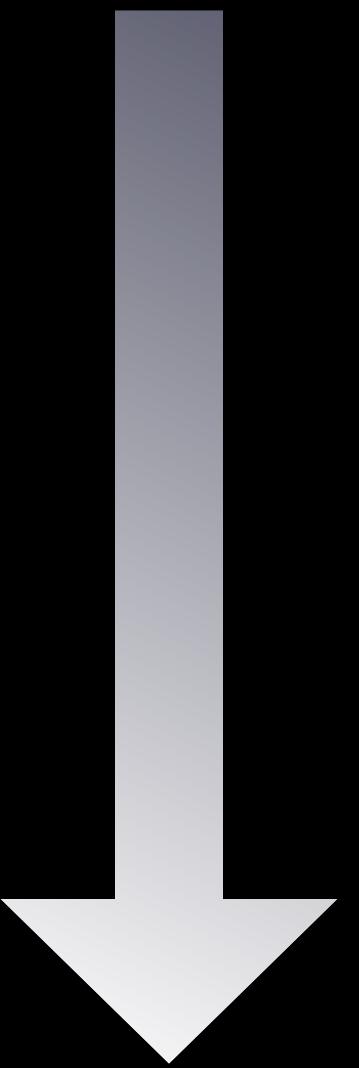
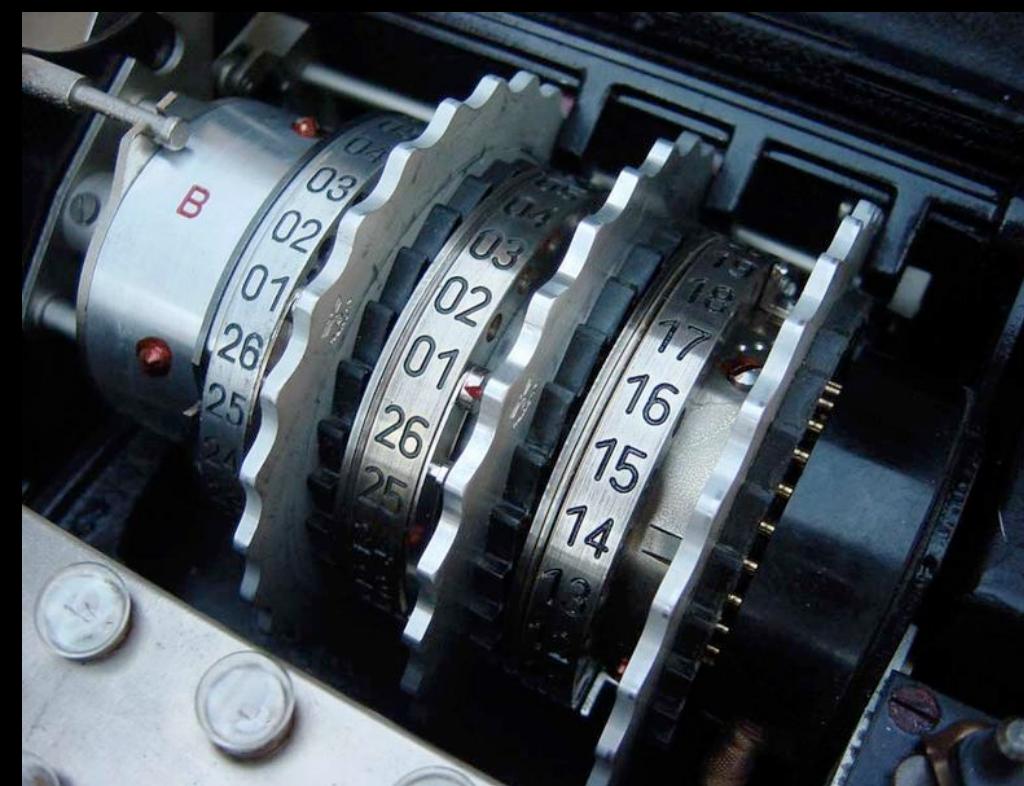
# One-Time Ciphers

- 1900s
  - Vernam & Mauborgne's "Unbreakable" cipher
- Based on Baudot code for Teletypes
- Added (XORed) a random Key (sequence of bits) to a binary message
  - Perfectly secure, provided:
    - key is perfectly random
    - key is at least as long as the message
    - key is never re-used



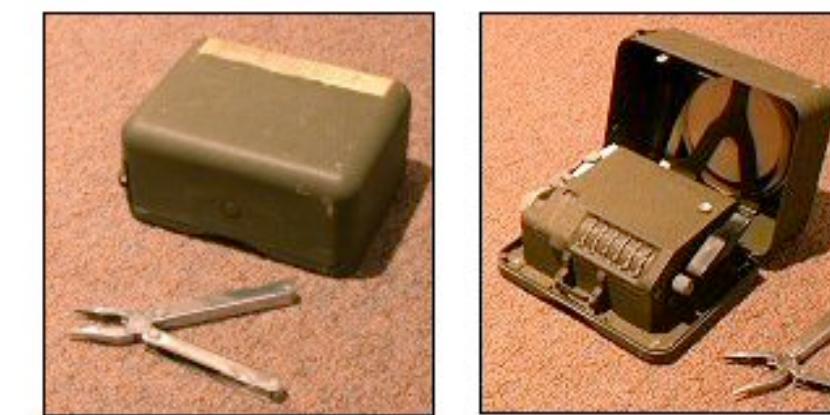
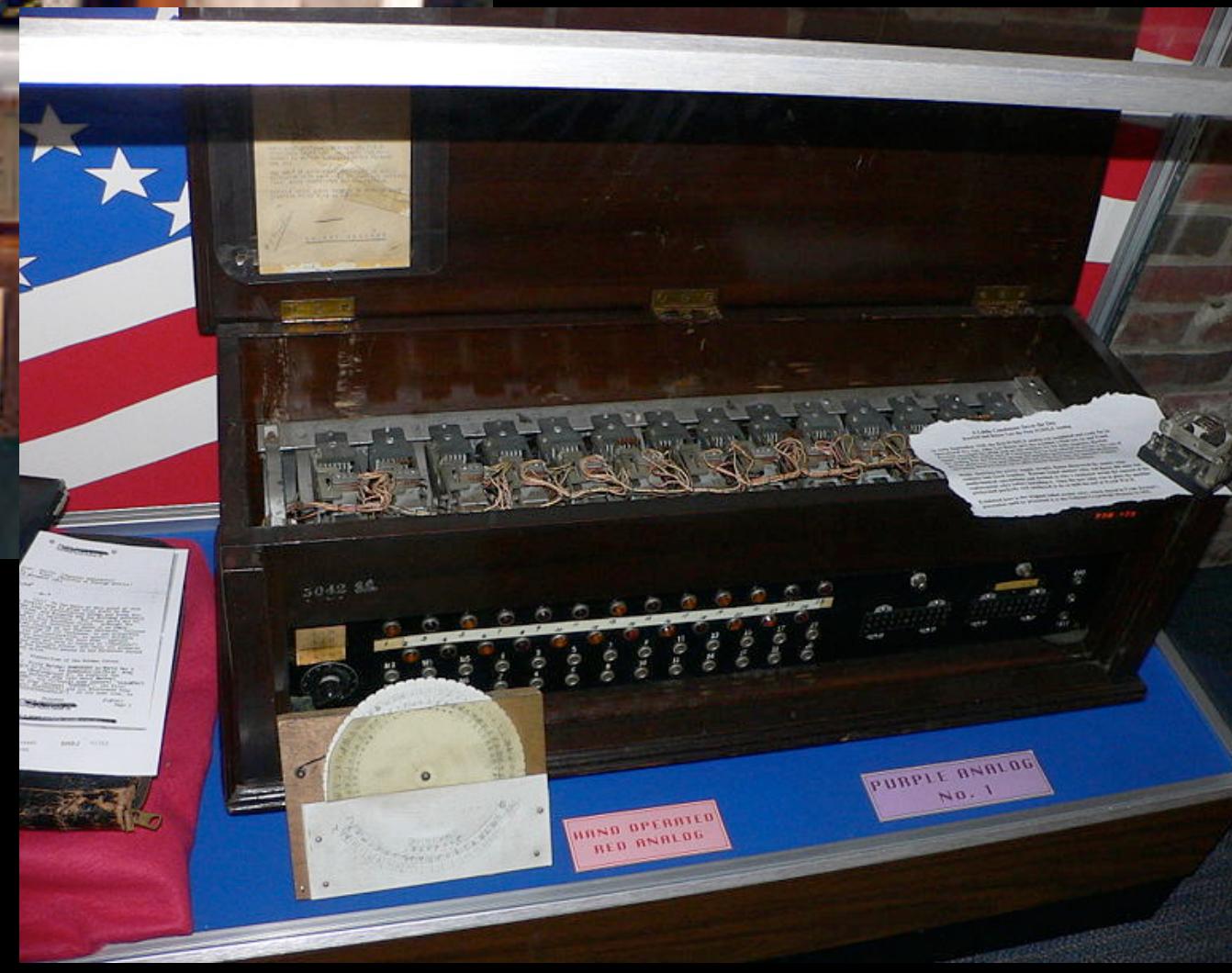
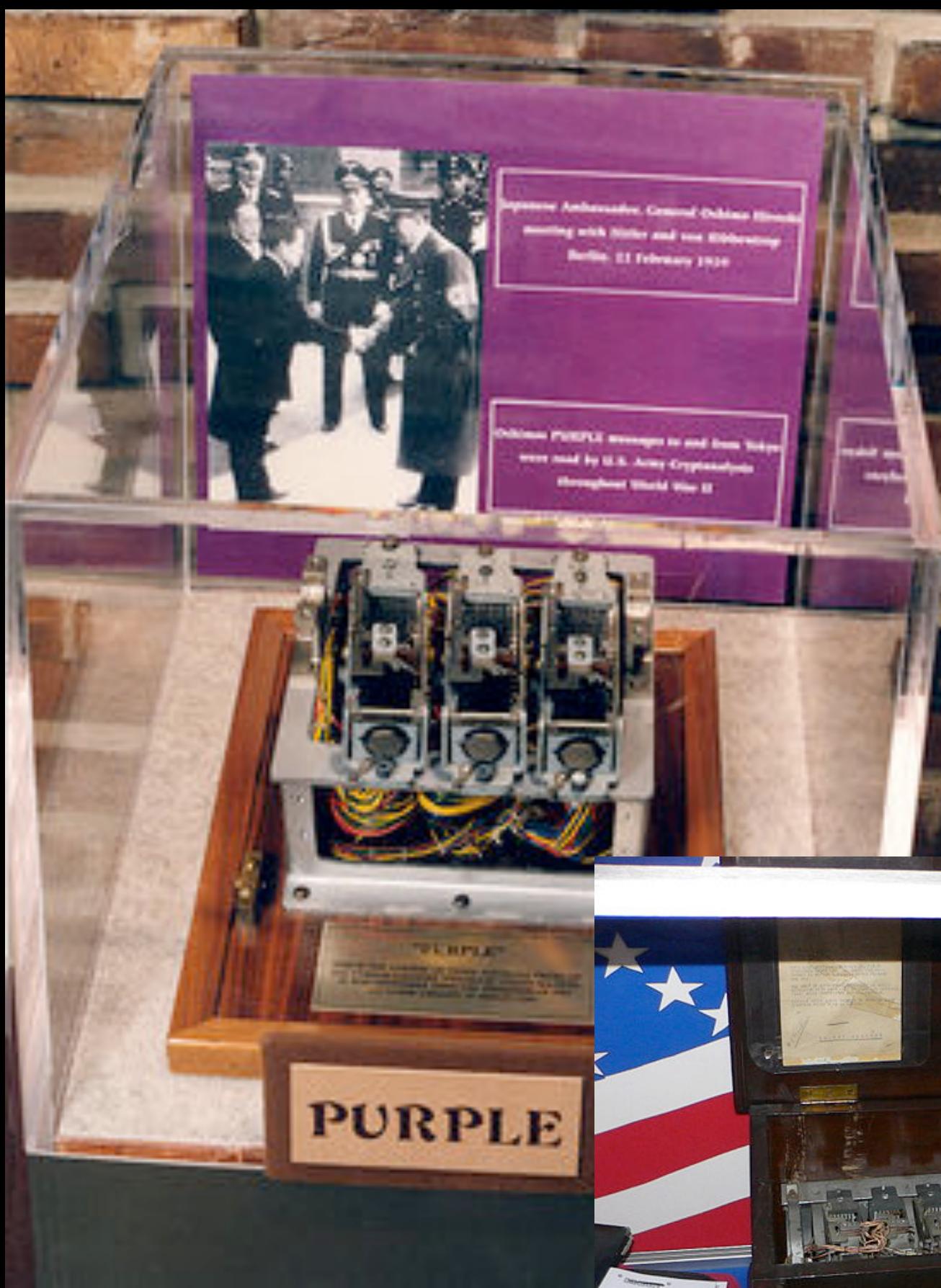
# Mechanical Cryptography

- 1900s
  - Mass production and usage of cipher devices
  - Rotor ciphers
  - Elec

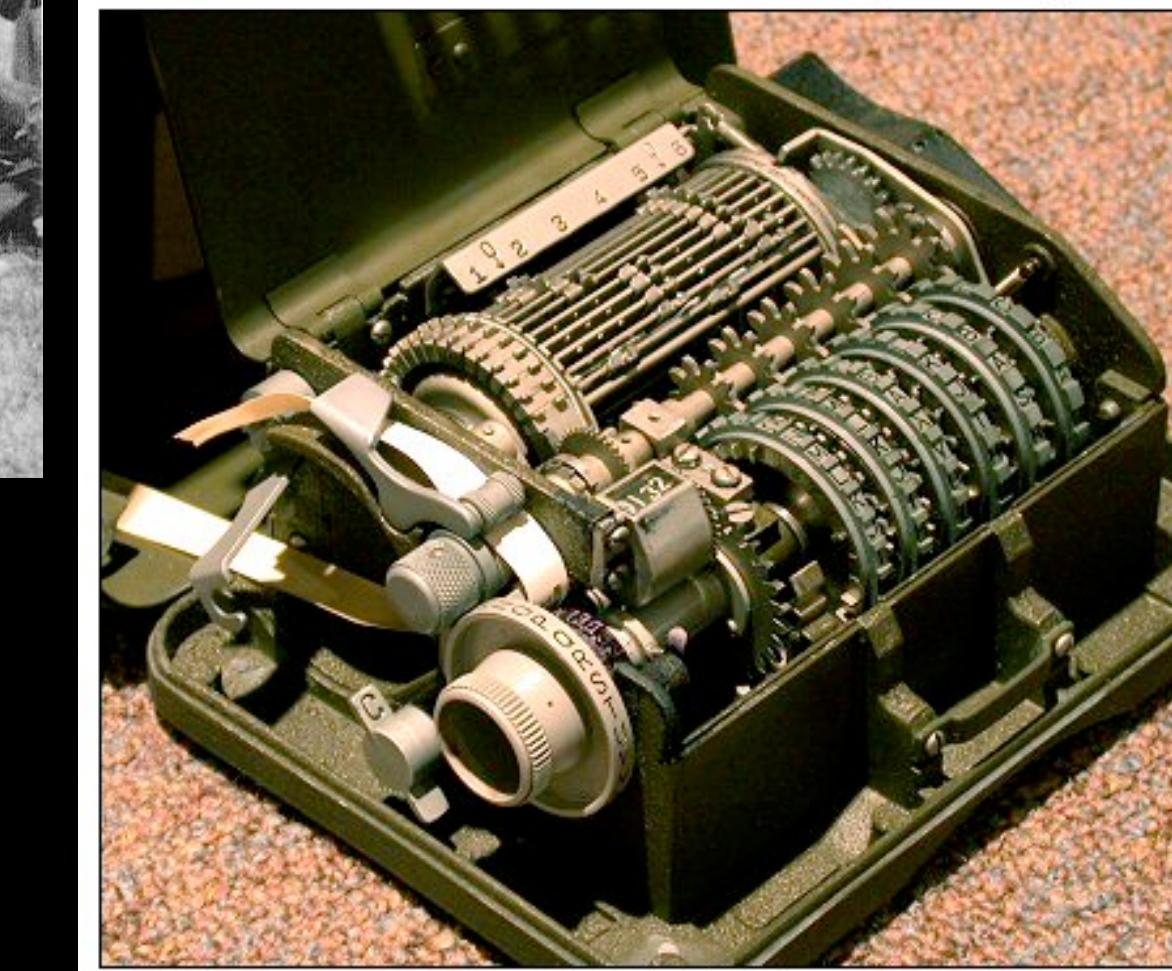


Increasing  
Complexity

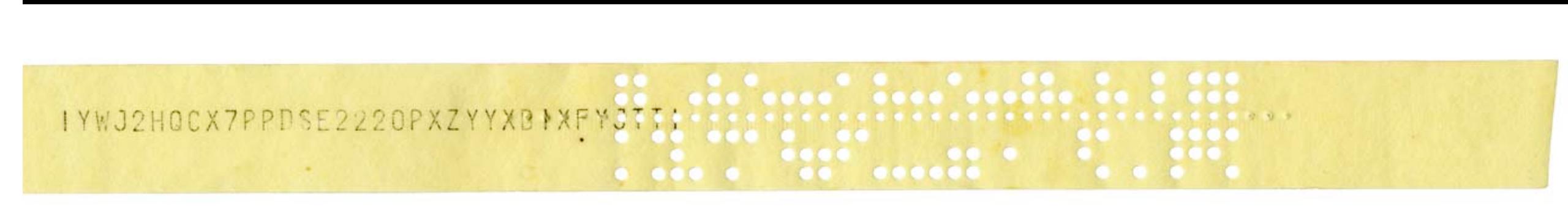
M-94 Cipher Wheel image by Bob Lord, used under a Creative Commons license.  
Remaining images: Wikipedia [M-94, Enigma] used under GFDL.



HAGELIN M-209 CIPHER MACHINE (GVG / PD)



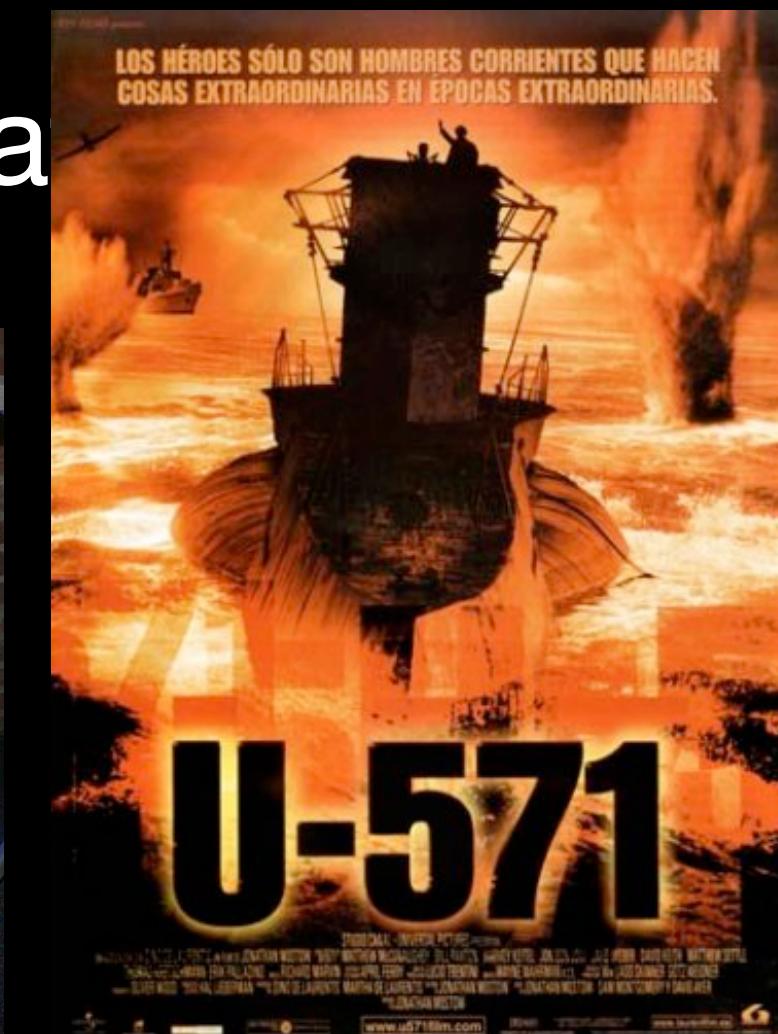
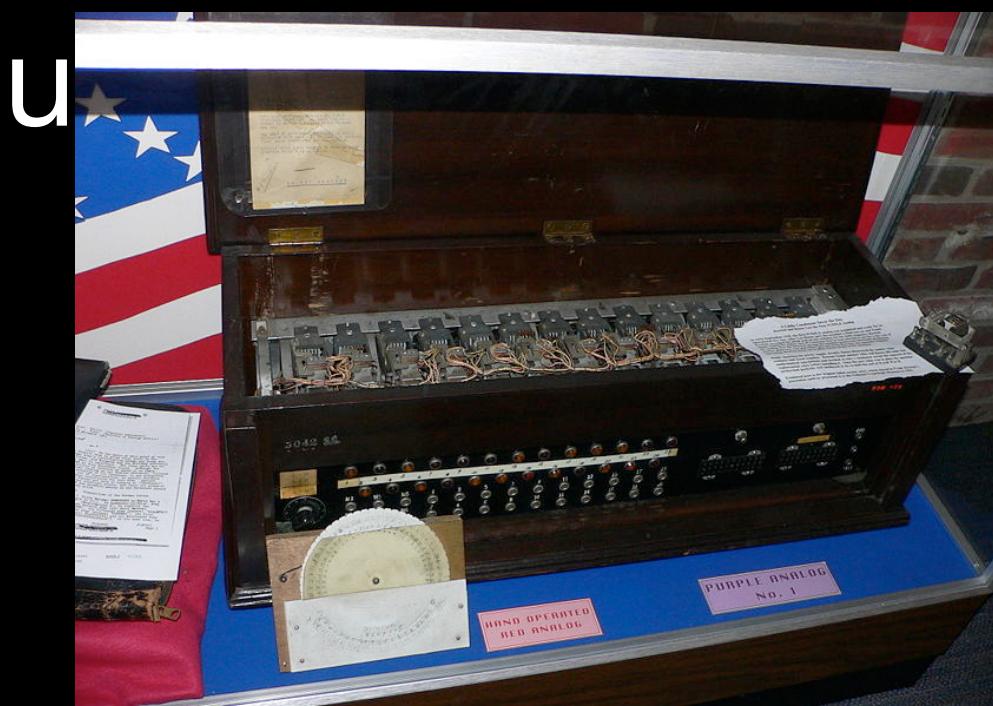
Purple Machine (top left) courtesy NSA, US Purple Replica (center) & M-209 images: Wikipedia used under GFDL/CC License.



Russian Fialka device and tape by Bob Lord, used under a Creative Commons license.  
HC-9 Image: Wikipedia, used under GFDL.

# Summary

- Most cryptosystems ultimately broken
  - Sophistication of the attackers outpaces that of the cryptosystem
  - Security relies on secrecy of design
  - Not evaluated for chosen plaintext, known plaintext attacks
  - Key generation/distribution procedures
  - It's an arms race...



# Kerckhoffs' Principle

2. It must not be required to be secret, and it must be able to fall into the hands of the enemy without inconvenience:



“The enemy knows the System”  
-- Claude Shannon’s Maxim

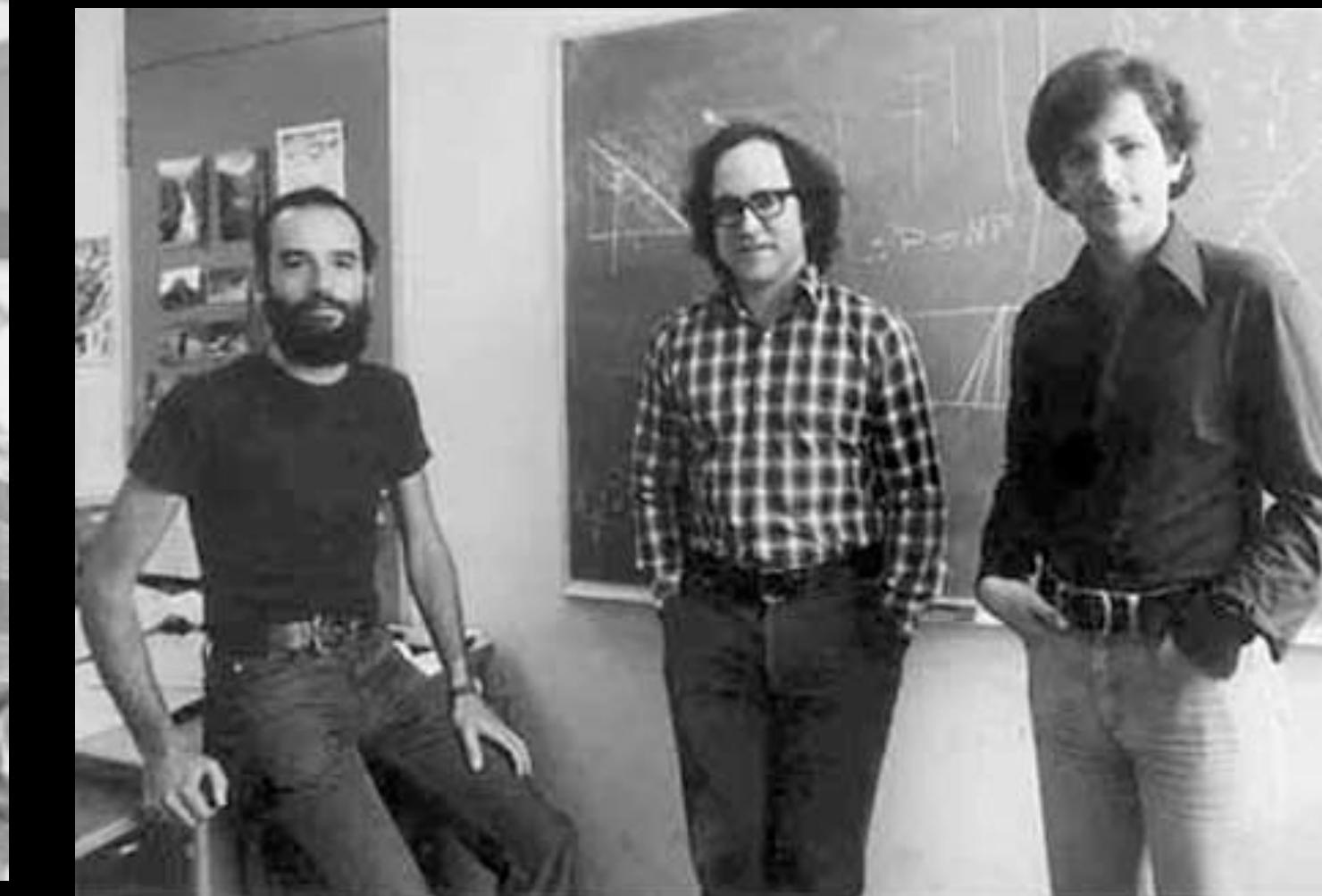
# The 1970s



1972



1976  
(1974)



1977  
(1973)

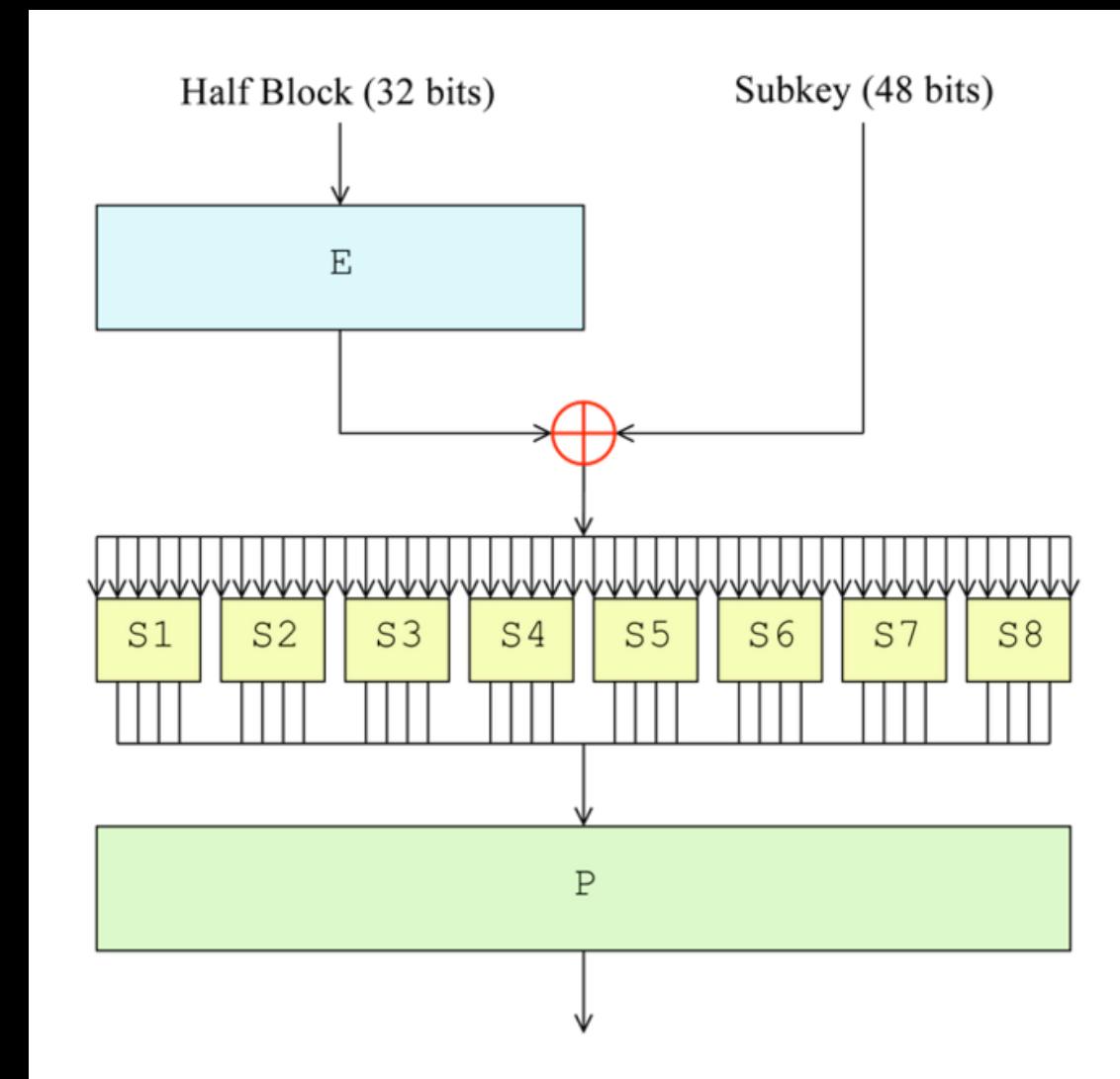
← U.K. GCHQ →

# The Implications

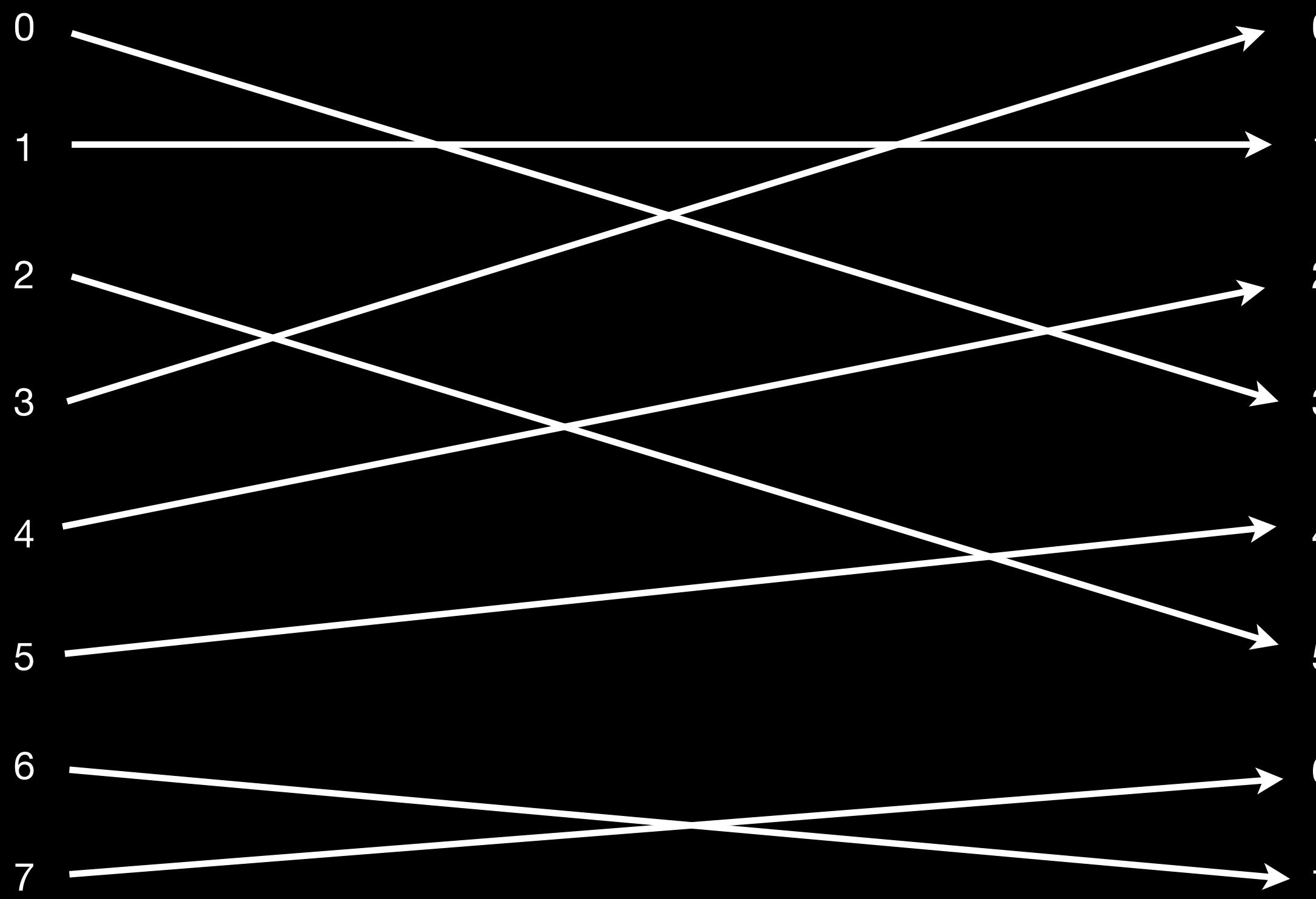
- Exponential increase in study & usage of cryptography in industry, academia
- Wide-scale deployment of cryptographic systems
- Provable Security
  - Cryptographic Systems can be reduced to some hard mathematical problem

# Data Encryption Standard

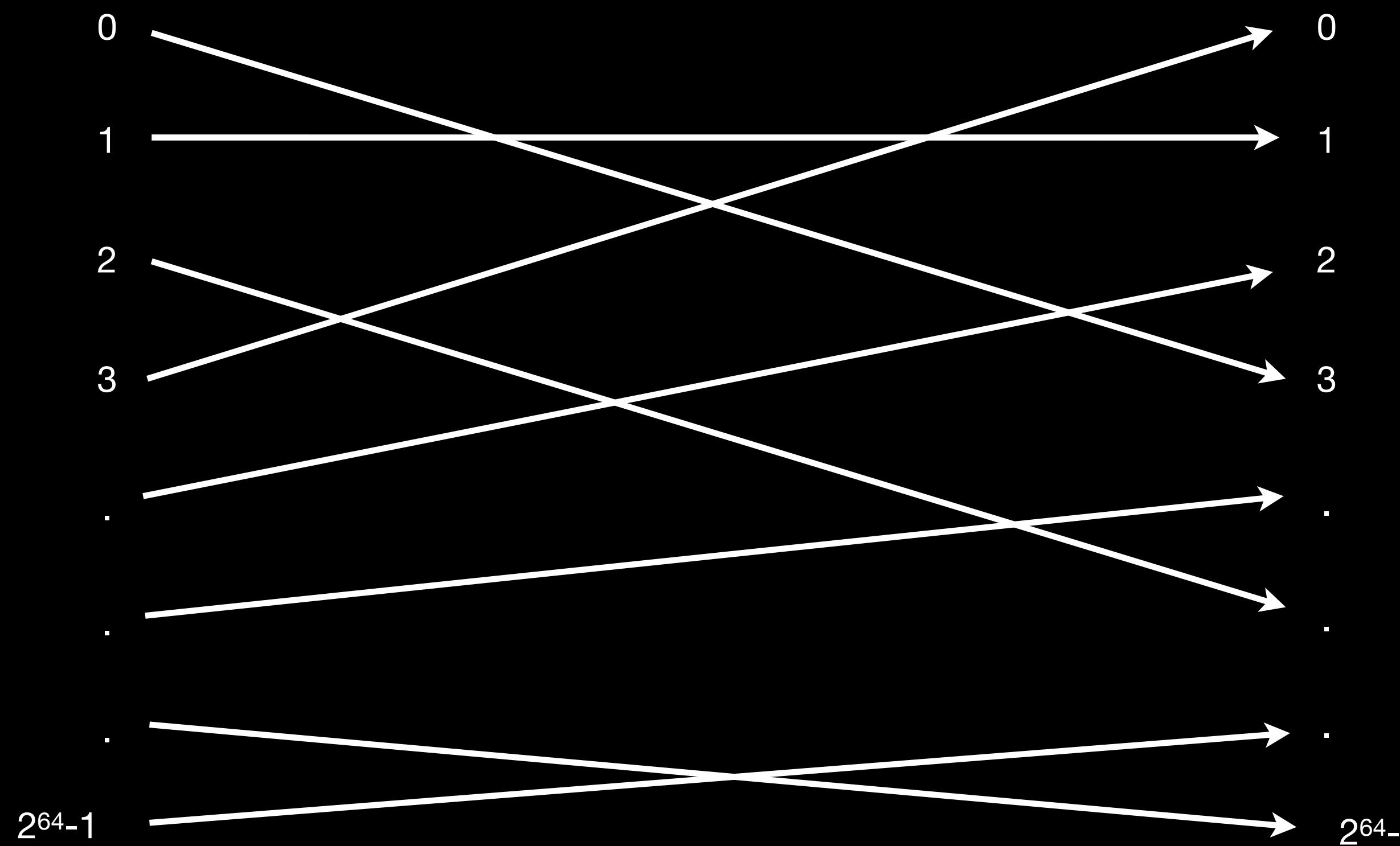
- Commercial-grade Block Cipher
  - 64-bit block size
  - 56 bit key (+ 8 bits parity)
  - “Feistel Network” Construction



# Permutation



# Permutation



# Permutation Families

- Can't have just one permutation
  - Alice & Bob know the permutation  
Adversary doesn't
  - Permutation is “random” (ish)
  - But there are  $2^{64!}$  possible permutations
  - DES has a 56 bit key...

# Block Cipher

- Block cipher is a family of permutations
  - Indexed by a key (DES = 56 bit key)
  - “Pseudo-random”

# Block Cipher

- Block cipher is a family of permutations
  - Indexed by a key (DES = 56 bit key)
  - Ideally: “Pseudo-random permutation (PRP)”

(i.e., attacker who does not know the key  
can't determine whether you're using a  
random permutation, or a PRP)

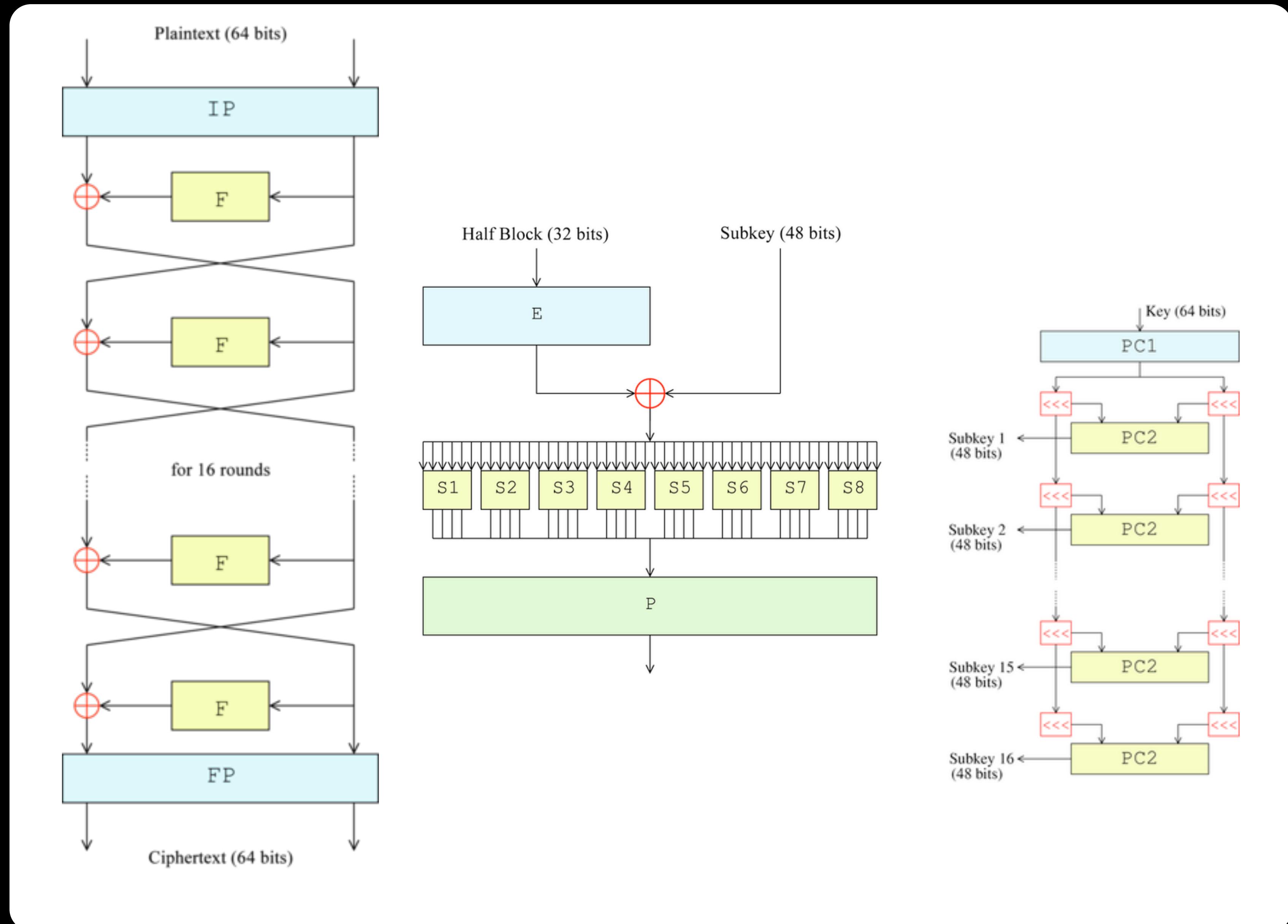
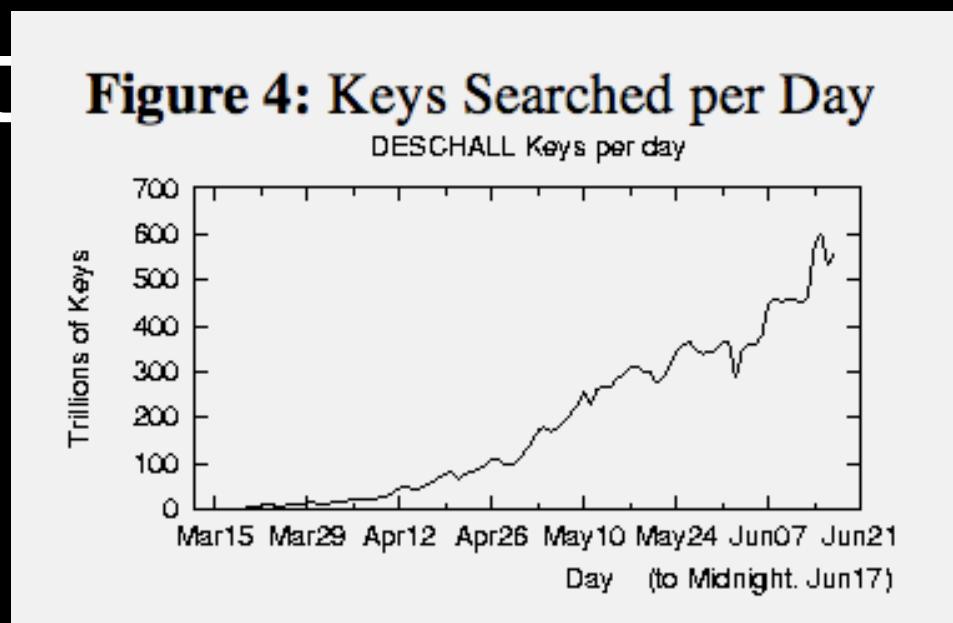


Image from Wikipedia, used under GFDL

# DES

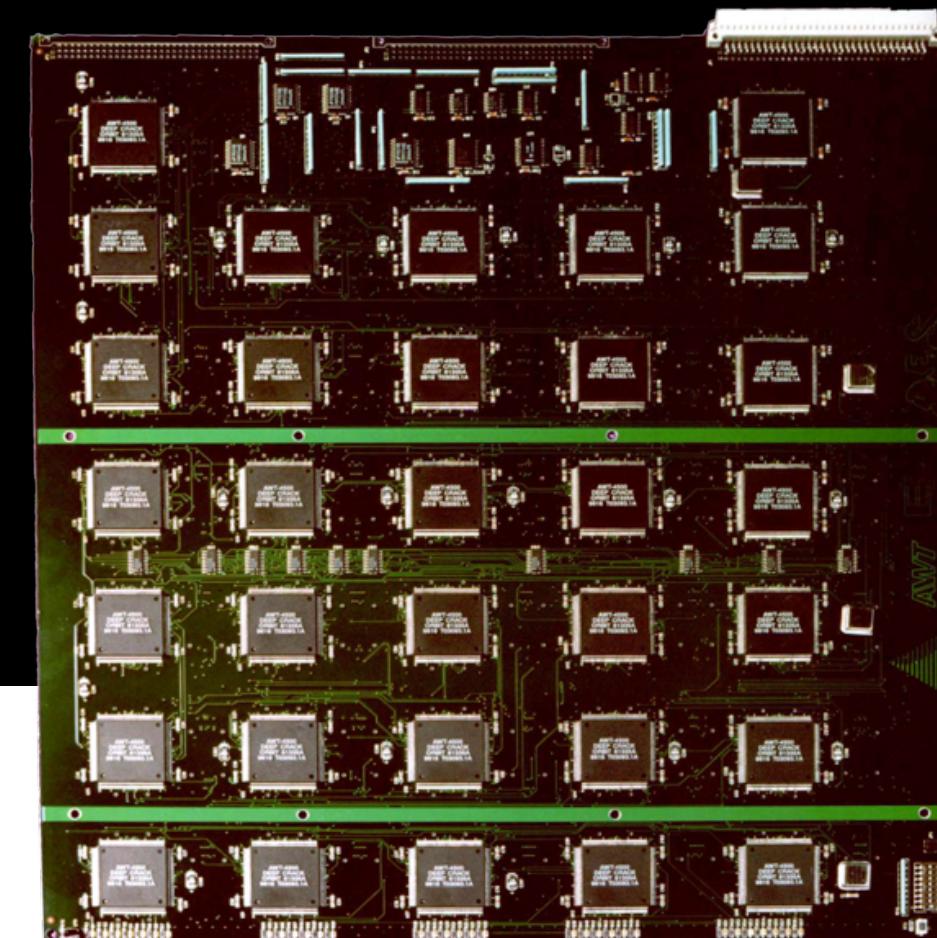
- Some “clever” attacks on DES
- However: practical weakness = 56 bit key size
- Practical attack on DES (now being deprecated)



## U.S. Data-Scrambling Code Cracked With Homemade Equipment

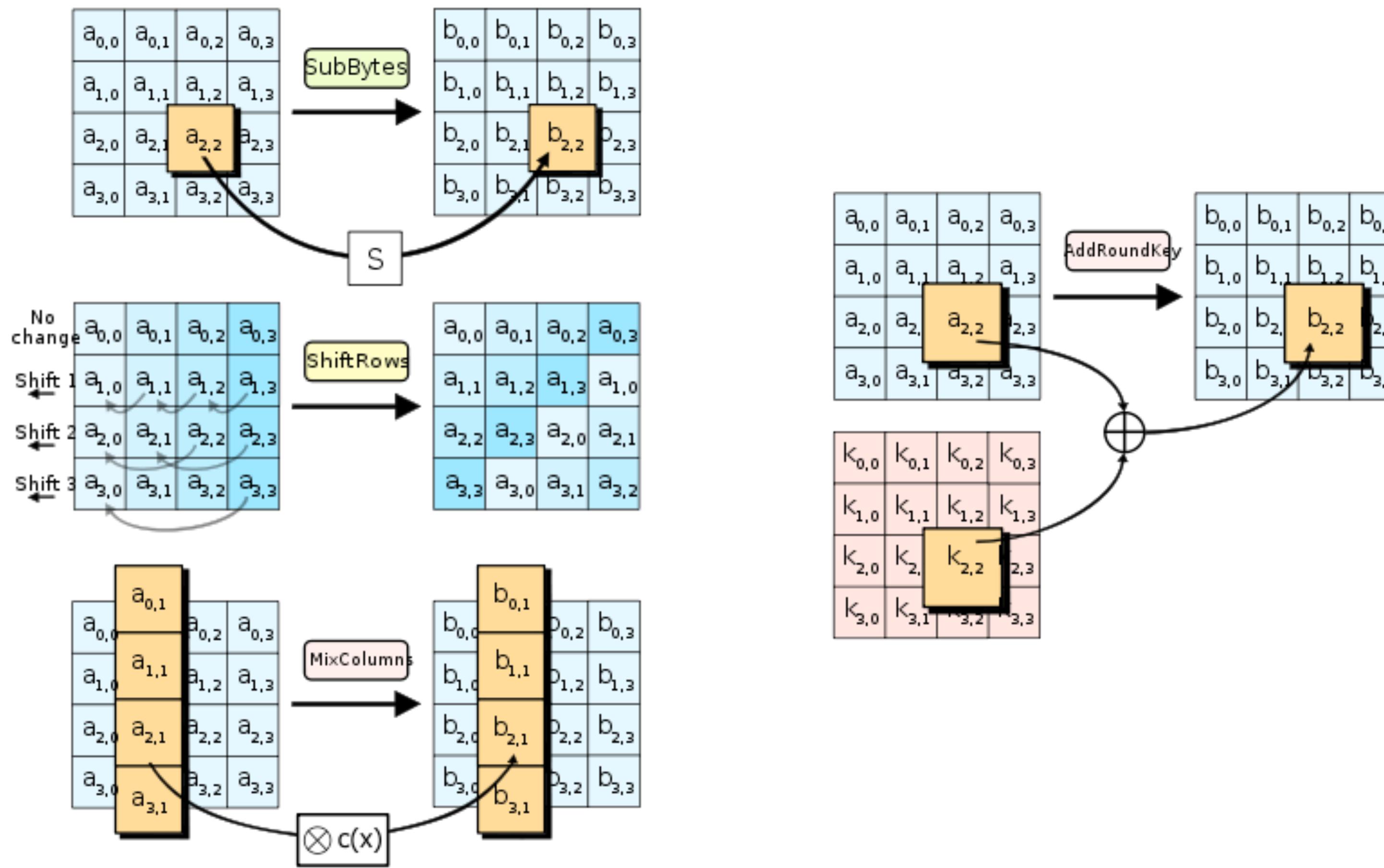
By JOHN MARKOFF

**S**AN FRANCISCO -- In a 1990s variant of a John Henry-style competition between man and machine, researchers using a homemade supercomputer have cracked the government's standard data-scrambling code in record time -- and have done it by out-calculating a team that had harnessed thousands of computers, including some of the world's most powerful.



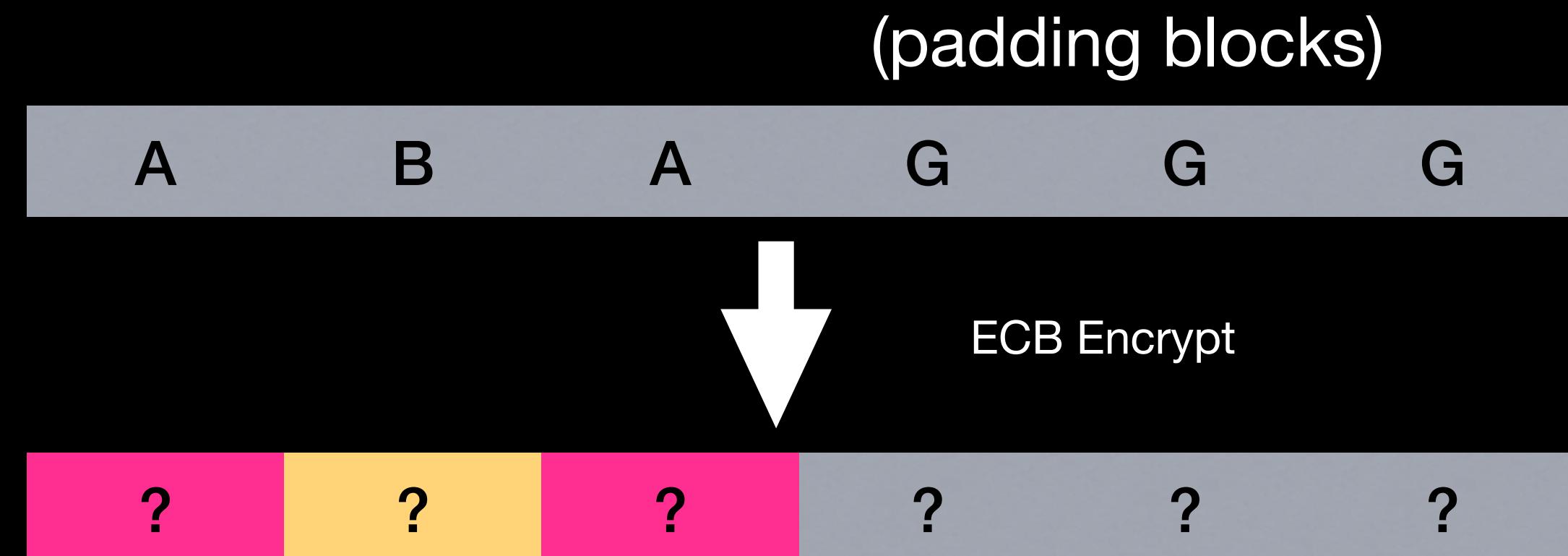
# AES

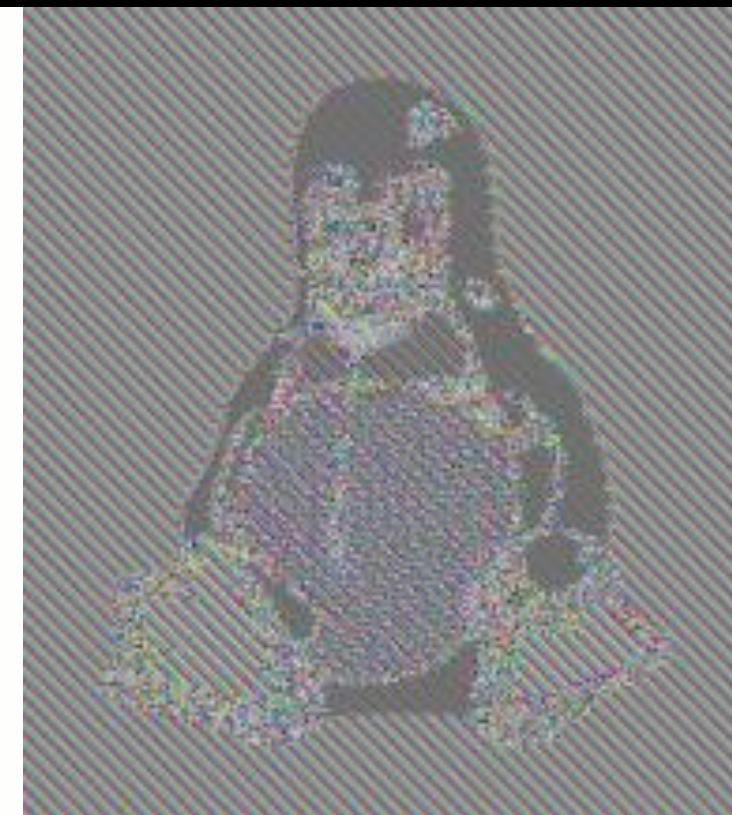
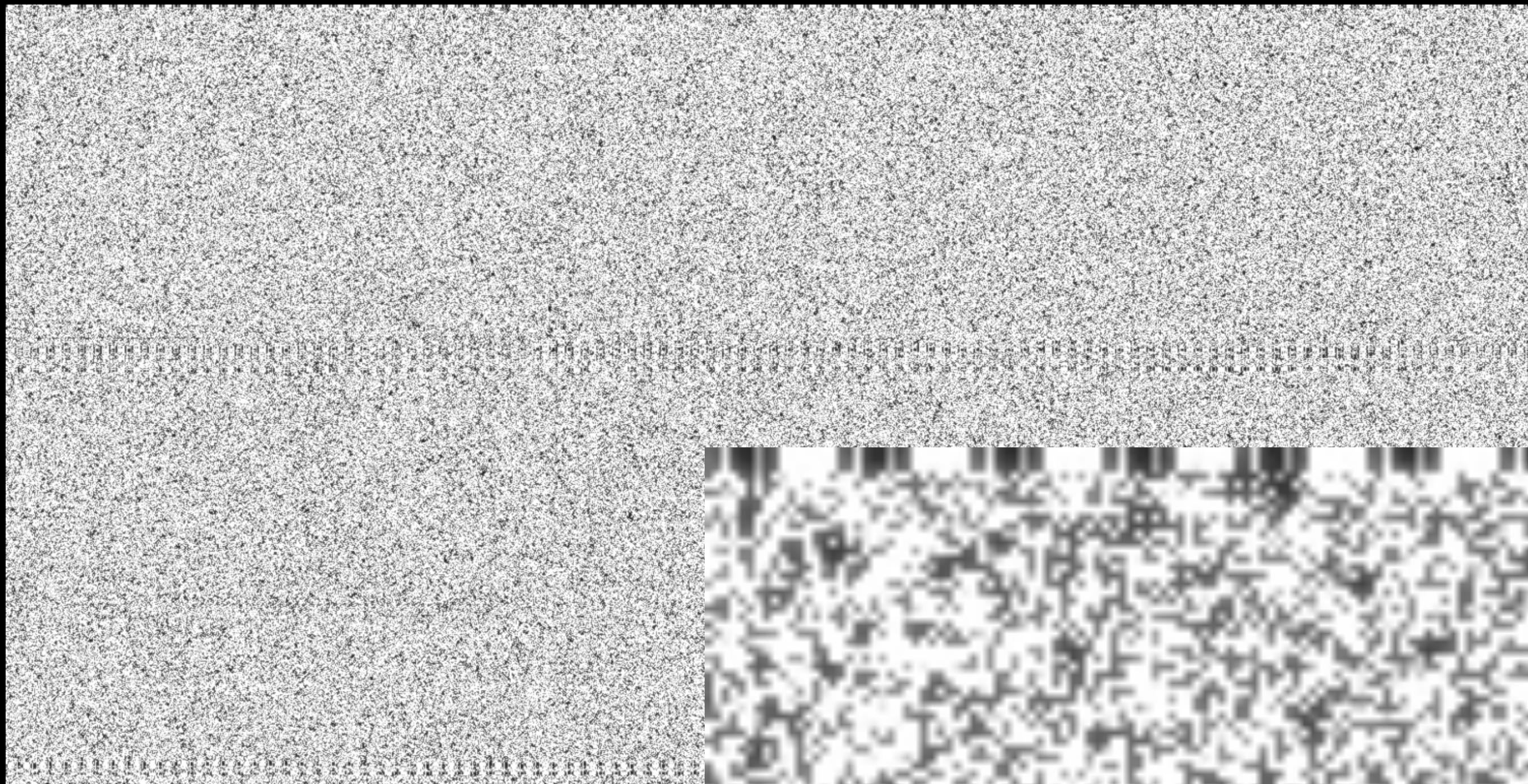
- NIST open competition (200s):
  - Fast in software & hardware
  - Larger block size (128 bit)
  - Longer keys (128/192/256-bit)
- 5 finalists:
  - MARS, RC6, Rijndael, Serpent, and Twofish



# How to use a block cipher?

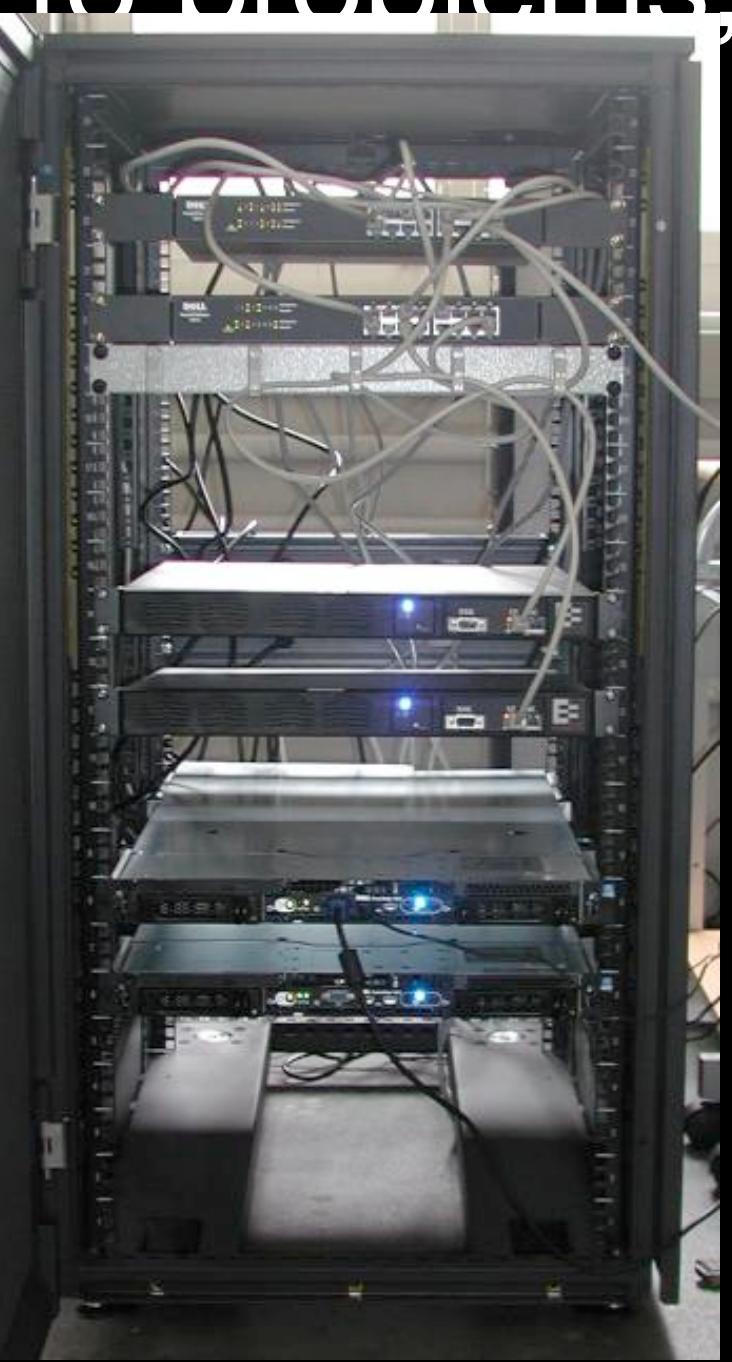
- ECB Mode: Encrypt each block separately
  - Problems?





# ECB Mode

- ECB is deterministic
- Leads to problems, e.g.:



E(Attack Monster)  
←—————→  
E(Monster Attacks)

Game server



Game client

# Definitions

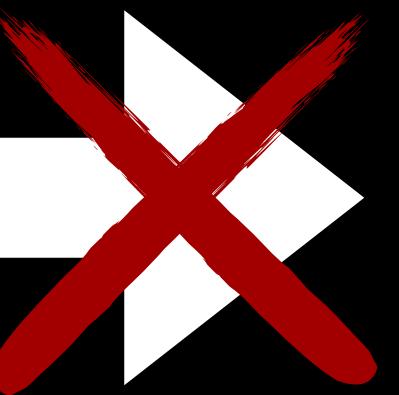
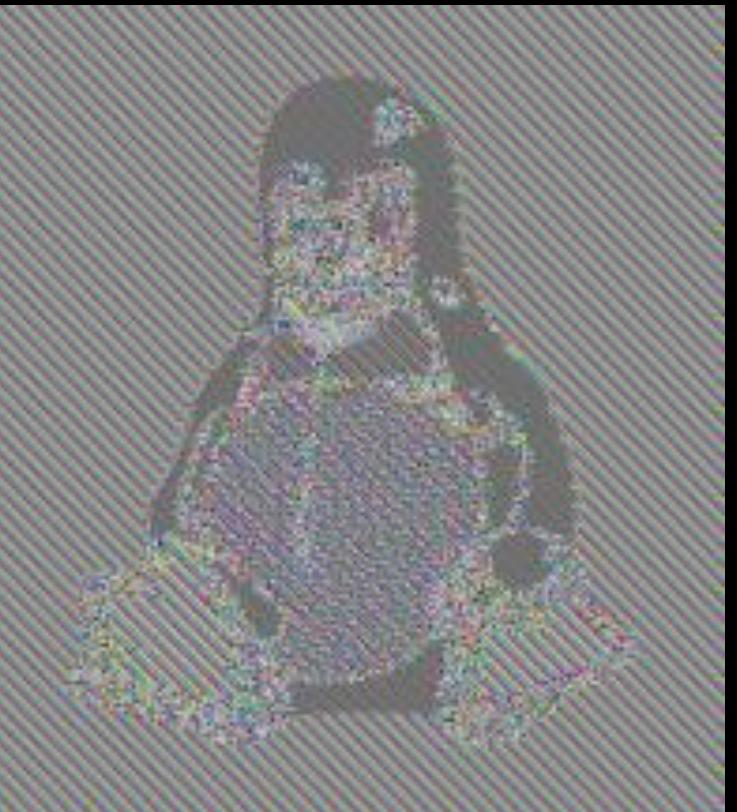
- What does it mean to securely encrypt something?

# Historical attempts

- Given a ciphertext, can't recover the plaintext

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# Security of Encryption

- Semantic Security
  - Due to Goldwasser & Micali (1980s)
  - Informally: An encryption scheme is secure if adversary who sees ciphertext “learns as much” as adversary who doesn’t see ciphertext.
- Even if adversary can request chosen plaintexts
  - How do we state this formally?

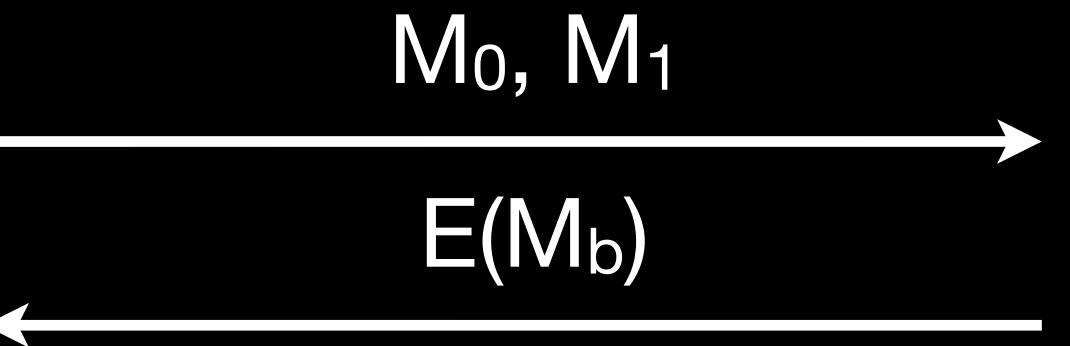
# Semantic security

- Semantic Security (IND-CPA)

$$b \xleftarrow{\$} \{0, 1\}$$



Adversary



b?



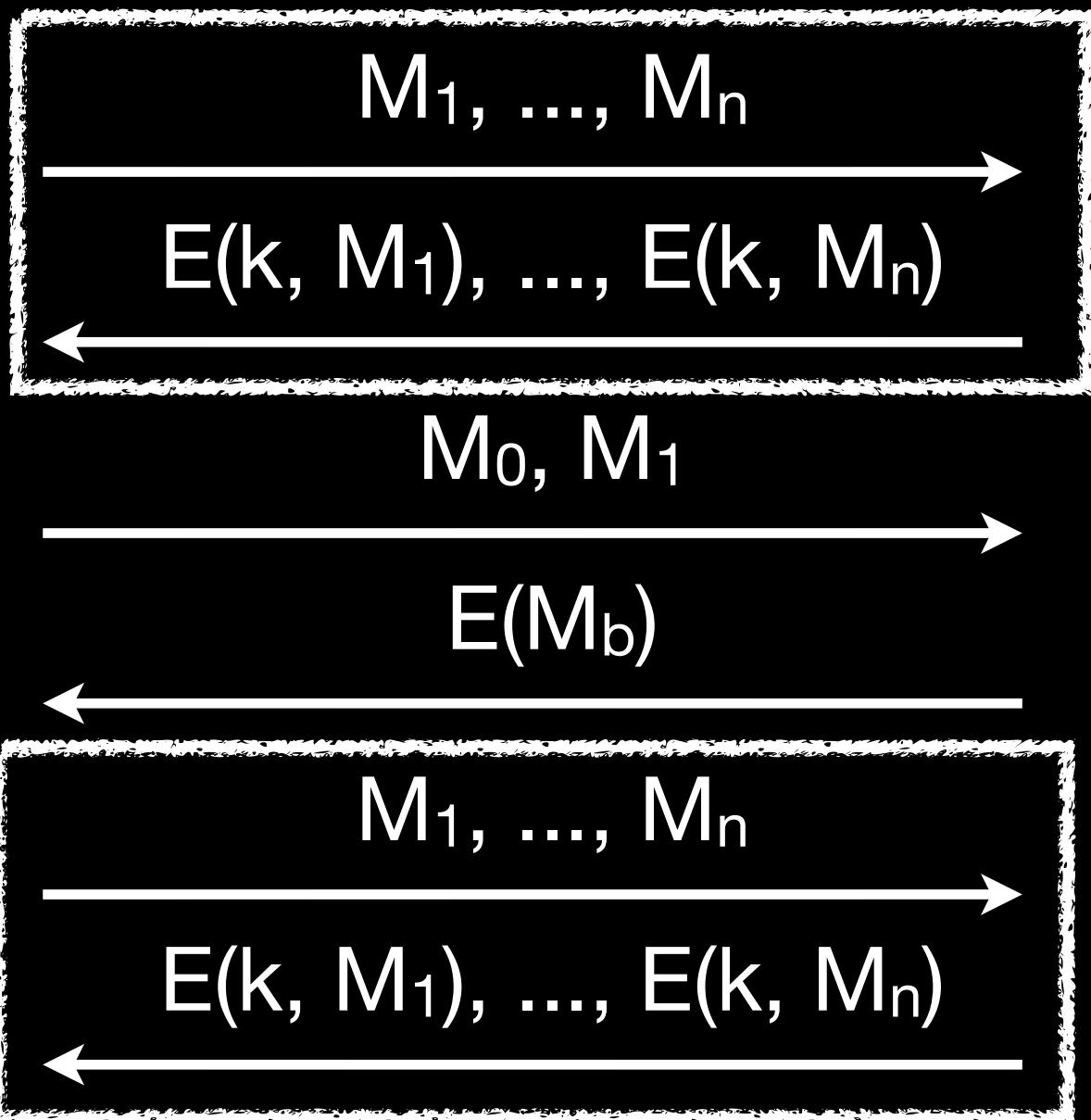
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Adversary



b?

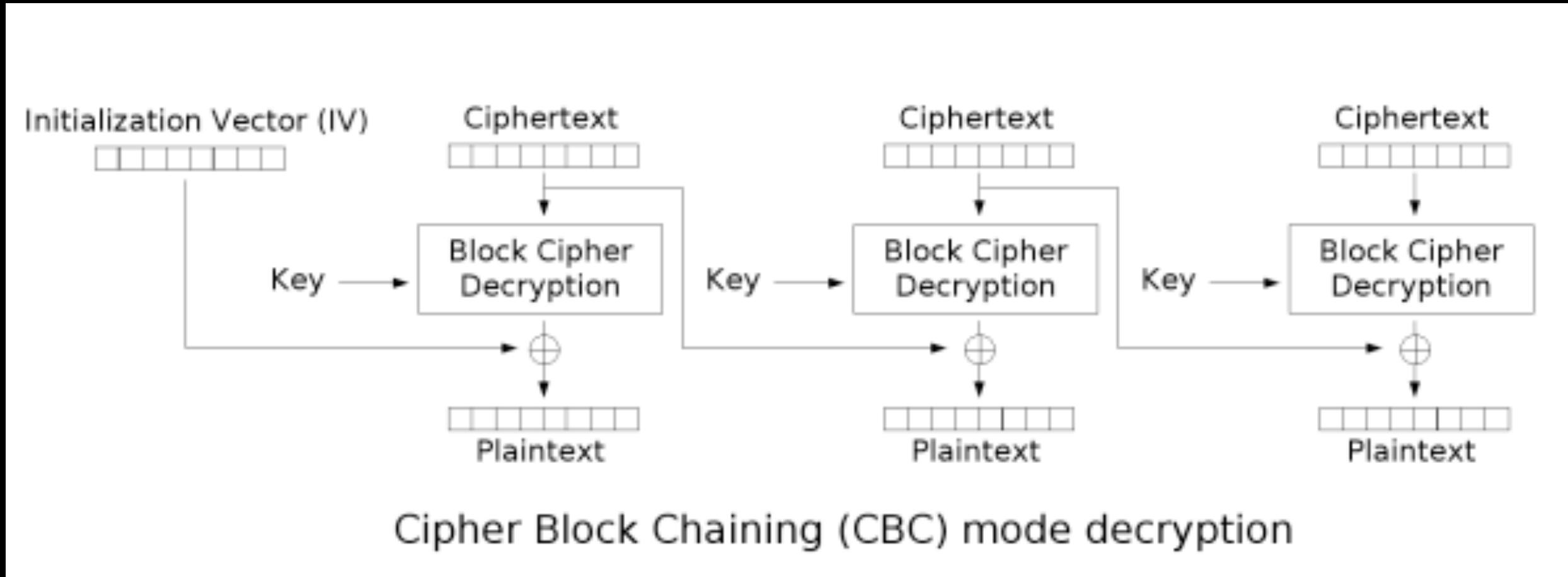
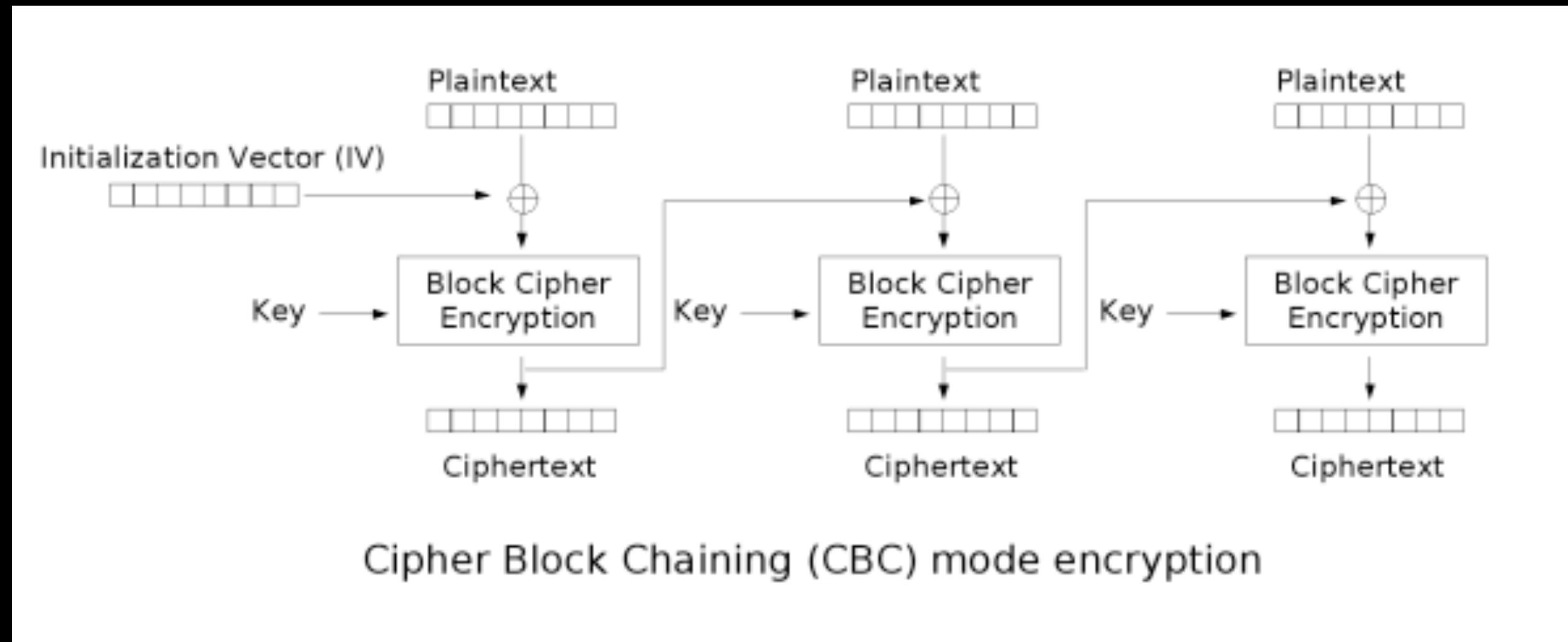


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# Using Block Ciphers

- ECB is not semantically secure, hence we use a “mode of operation”
  - e.g., CBC, CTR, CFB, OFB (and others)
- These provide:
  - Security for multi-block messages
  - Randomization (through an Initialization Vector)

# CBC Mode



# Security of CBC

- Is CBC a secure encryption scheme?
  - Yes, assuming a secure block cipher
  - Correct (random) IV generation
  - Can prove this under assumption that block cipher = Pseudo-Random Permutation (PRP)
- Bellare, Desai, Jokipii & Rogaway (2000)
  - Easy to use wrong...
  - Most important: use a unique & random IV!

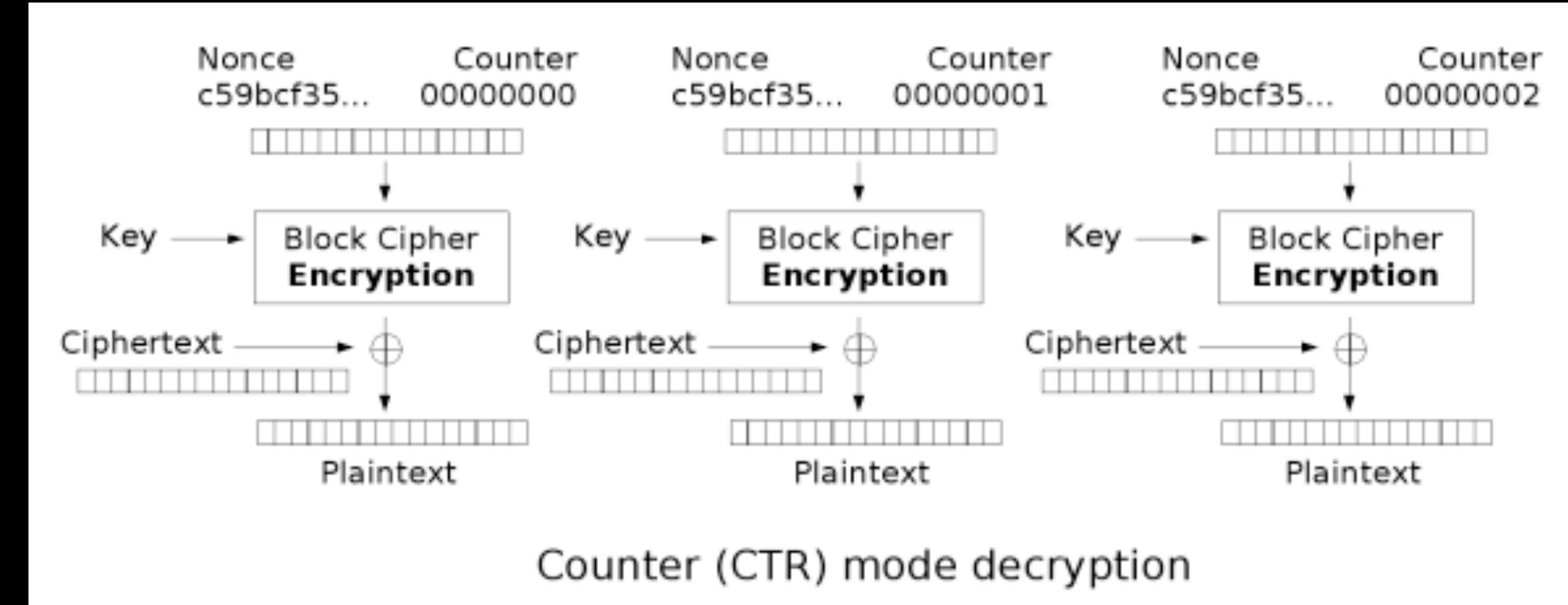
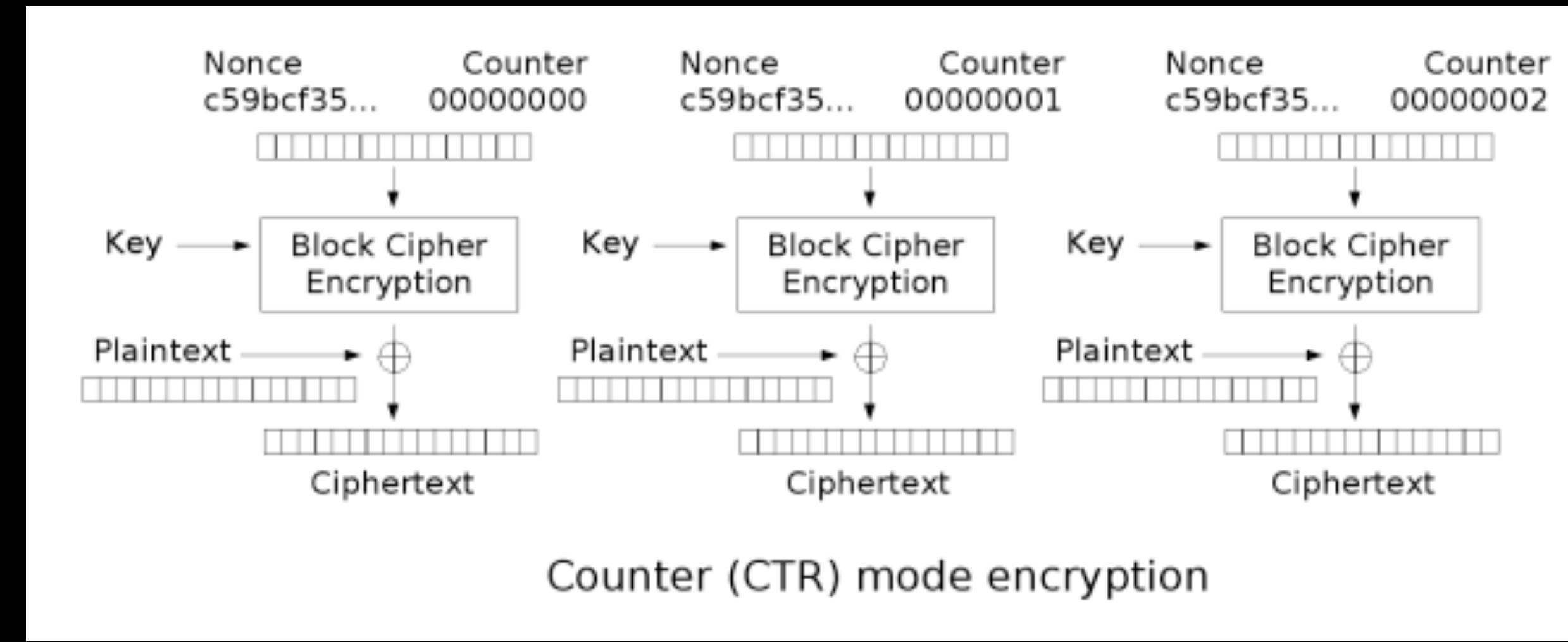
The size of the frame of data to be encrypted or decrypted (i.e. how often a new CBC chain is started) depends on the particular application, and is defined for each in the corresponding format specific books of this specification. Unless otherwise specified, the Initialization Vector used at the beginning of a CBC encryption or decryption chain is a constant,  $iv_0$ , which is:

0BA0F8DDFEA61FB3D8DF9F566A050F78<sub>16</sub>

## Advanced Access Content System (AACS)

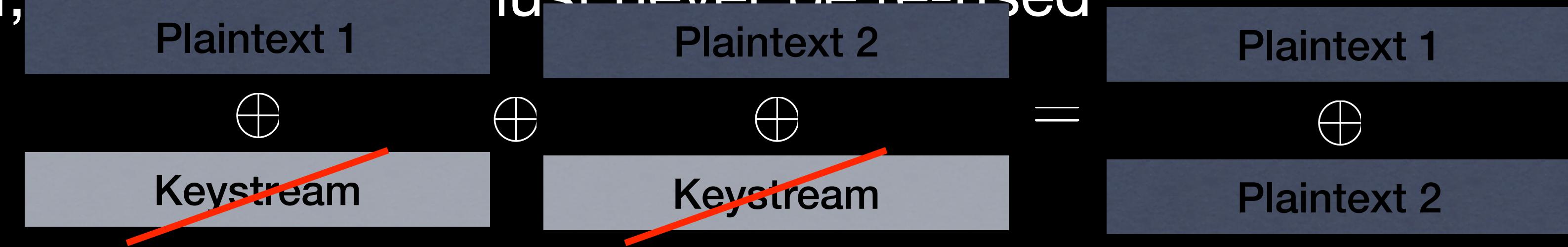
*Introduction and  
Common Cryptographic Elements*

# CTR Mode



# Security of CTR

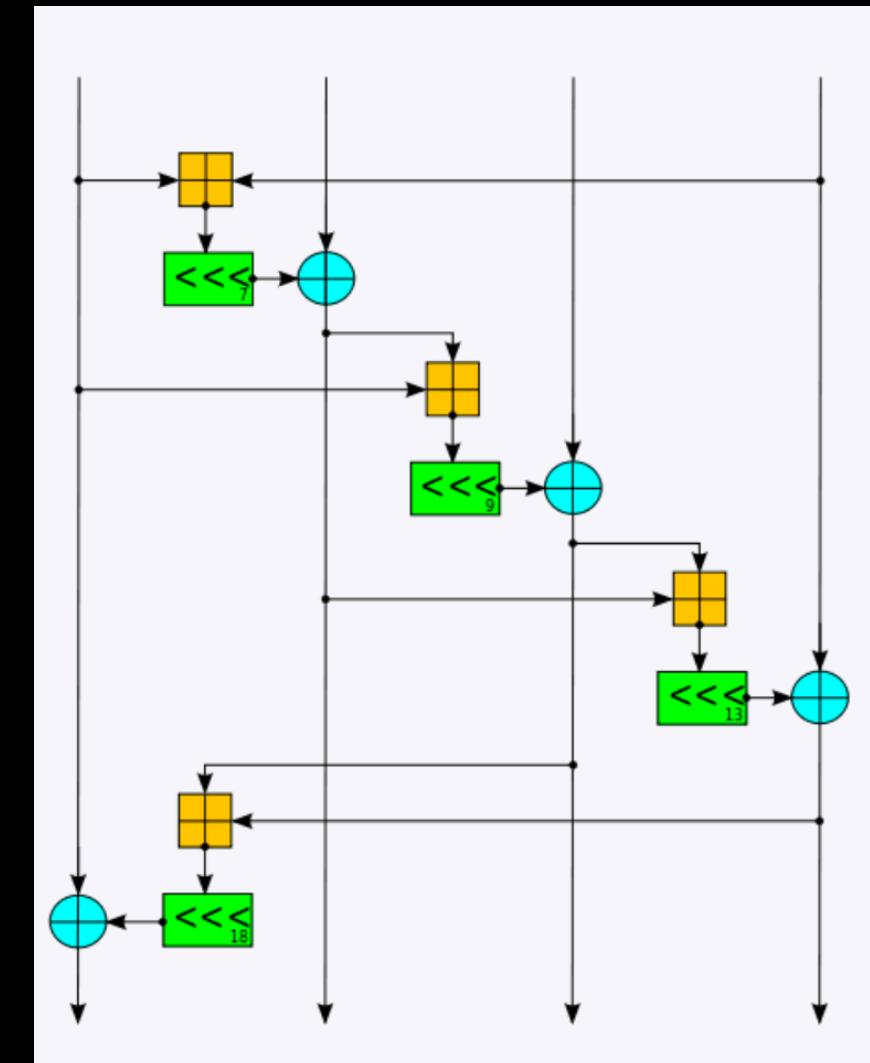
- Yes, assuming secure block cipher (PRP)
- However, counter range must never be re-used



- Similar example: MS Word 2003
  - (they used RC4, but same problem)

# Alternative ciphers

- Salsa20, ChaCha (Bernstein)
  - These are not block ciphers
  - Designed as *non-invertible pseudorandom* functions
  - $\text{Salsa20}(k, n) \rightarrow \{\text{output}\}$
  - Can use these to implement a stream cipher (i.e. CTR mode)



# Point of order

- Proofs of security:
  - We don't know how to prove that DES or AES or Salsa20 are secure block ciphers
  - But if we assume that the block ciphers are secure PRPs (resp PRFs) then:
    - We can prove that CBC & CTR & OFB & CFB etc. are secure encryption modes.

<http://www.cs.ucdavis.edu/~rogaway/papers/sym-enc-abstract.html>

# Point of order

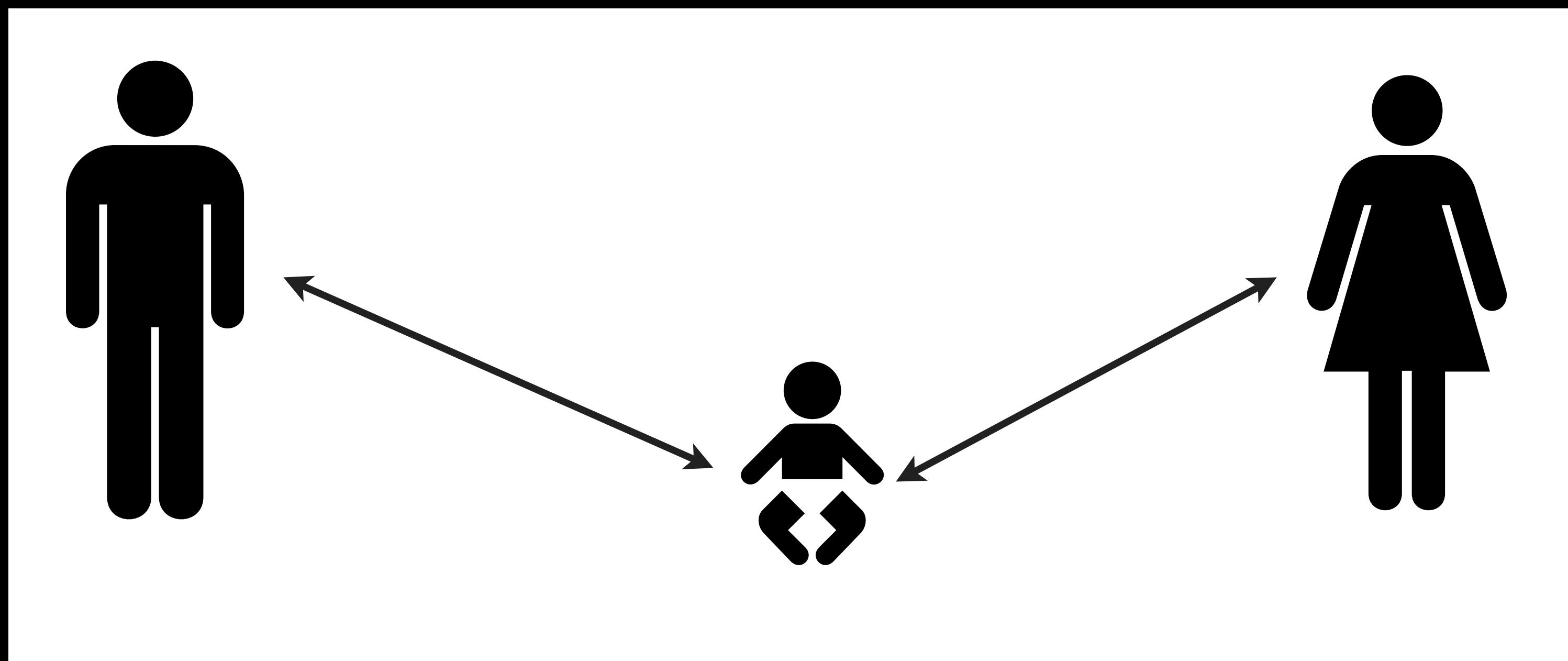
- Proofs of security for ChaCha, achieving slightly better performance.<sup>[17]</sup> The Aumasson et al. paper also attacks ChaCha, achieving one round fewer: for 256 bits ChaCha6 with complexity  $2^{139}$  and ChaCha7 with complexity  $2^{248}$ . 128 bits ChaCha6 within  $2^{107}$ , but claims that the attack fails to break 128 bits ChaCha7.<sup>[3]</sup>
- But if we assume that the block ciphers are secure PRPs (resp PRFs) then:
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# Malleability

- The ability to modify a ciphertext
  - Such that the plaintext is meaningfully altered
  - CTR Mode (bad)
  - CBC Mode (somewhat bad)

# Authenticated Encryption



# MACs

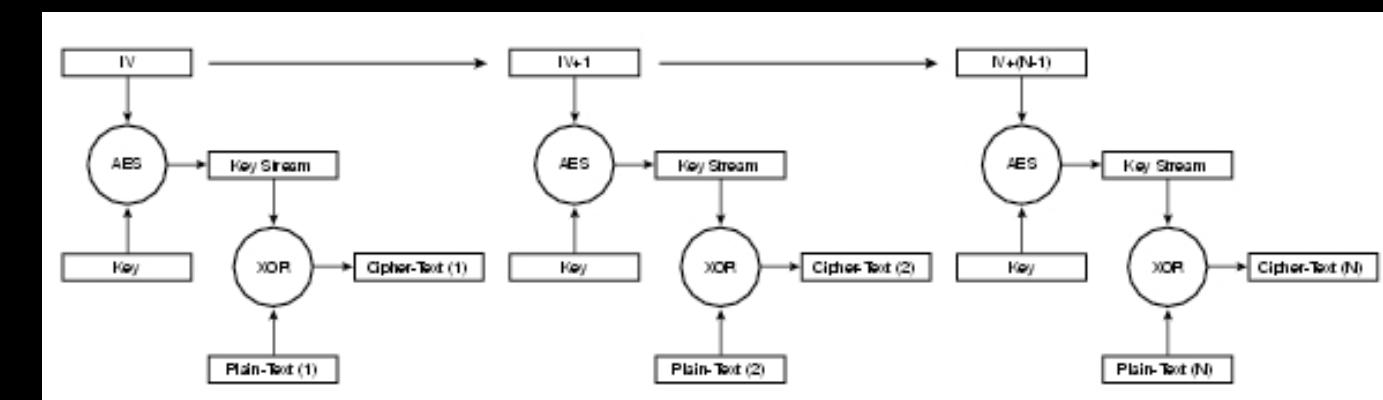
- Symmetric-key primitive
  - Given a key and a message, compute a “tag”
  - Tag can be verified using the same key
  - Any changes to the message detectable
- To prevent malleability:
  - Encrypt then MAC
  - Under separate keys

# MACs

- Definitions of Security
  - Existential Unforgeability under Chosen Message Attack (EU-CMA)
- Examples:
  - HMAC (based on hash functions)
  - CMAC/CBC-MAC (block ciphers)

# Authenticated Encryption

- Two ways to get there:
  - Generic composition  
Encrypt (e.g., CBC mode) then MAC
- two different keys, multiple primitives
  - Authenticated mode of operation
- Integrates both encryption & authentication
- Single key, typically uses only one primitive (e.g., block cipher)
- Ex: CCM, OCB, GCM modes



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