

# **650.445: Practical Cryptographic Systems**

## **Side Channel Attacks**

**Instructor: Matthew Green**

# Housekeeping:

- A2 tonight
- Grades for A1 back

# Current Events

A collage of images related to Mozilla Firefox and TLS. It features the Firefox logo, a globe, a hand holding a sword-like object, and a banner with the text "MOZILLA PATCHING FIREFOX CERTIFICATE PINNING VULNERABILITY".

by Michael Mimoso [Follow @mike\\_mimoso](#)

September 19, 2016 , 4:03 pm

# Current Events

[CVE-2016-6309 \(OpenSSL advisory\)](#) [Critical severity] 26th September 2016: 

This issue only affects OpenSSL 1.1.0a, released on 22nd September 2016. The patch applied to address CVE-2016-6307 resulted in an issue where if a message larger than approx 16k is received then the underlying buffer to store the incoming message is reallocated and moved. Unfortunately a dangling pointer to the old location is left which results in an attempt to write to the previously freed location. This is likely to result in a crash, however it could potentially lead to execution of arbitrary code. Reported by Robert Święcki (Google Security Team).

- Fixed in OpenSSL 1.1.0b (Affected 1.1.0a)

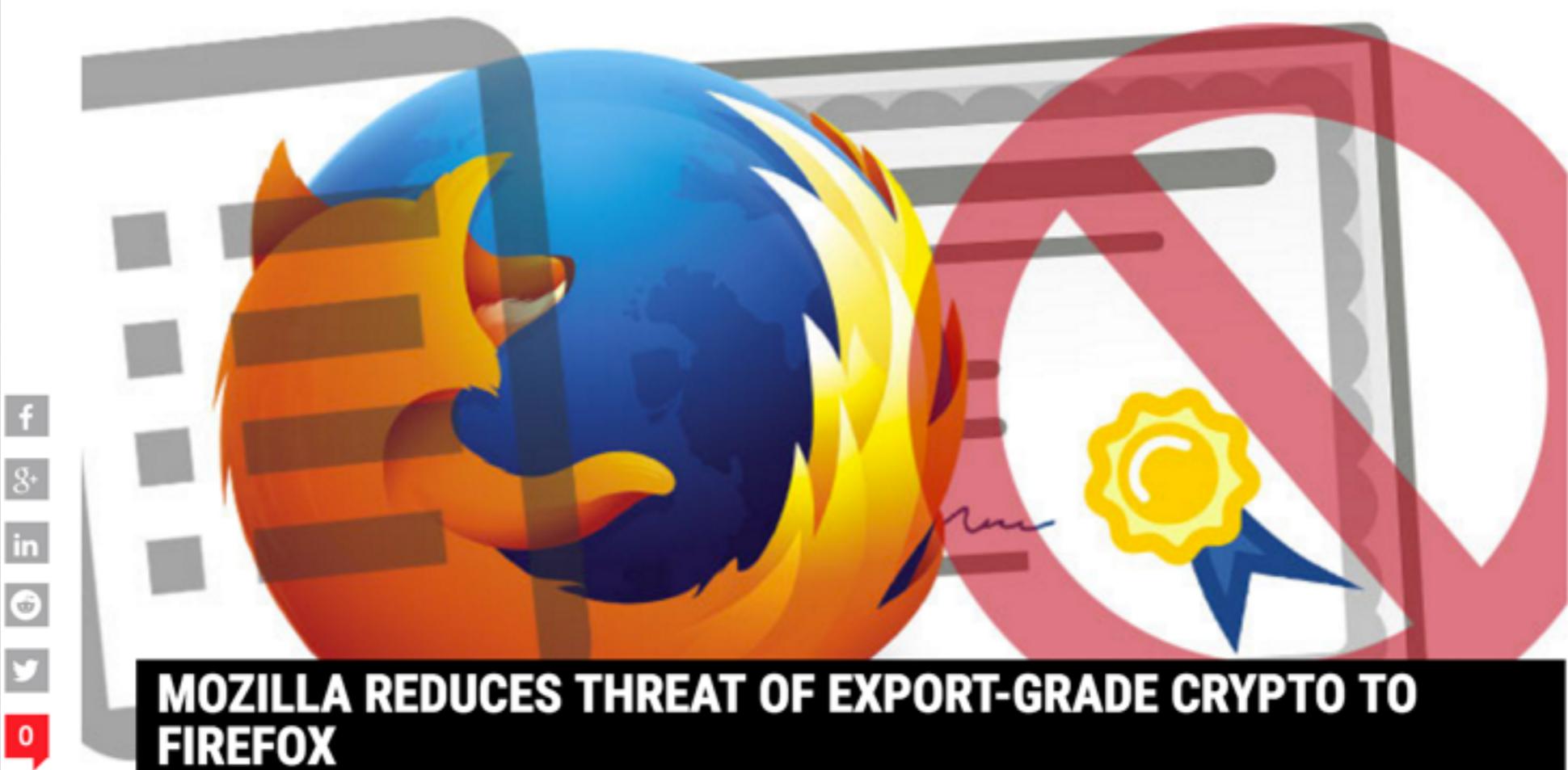
[CVE-2016-7052 \(OpenSSL advisory\)](#) [Moderate severity] 26th September 2016: 

This issue only affects OpenSSL 1.0.2i, released on 22nd September 2016. A bug fix which included a CRL sanity check was added to OpenSSL 1.1.0 but was omitted from OpenSSL 1.0.2i. As a result any attempt to use CRLs in OpenSSL 1.0.2i will crash with a null pointer exception. Reported by Bruce Stephens and Thomas Jakobi.

- Fixed in OpenSSL 1.0.2j (Affected 1.0.2i)

# Current Events

Welcome > Blog Home > Cryptography > Mozilla Reduces Threat of Export-Grade Crypto to Firefox



MOZILLA REDUCES THREAT OF EXPORT-GRADE CRYPTO TO FIREFOX

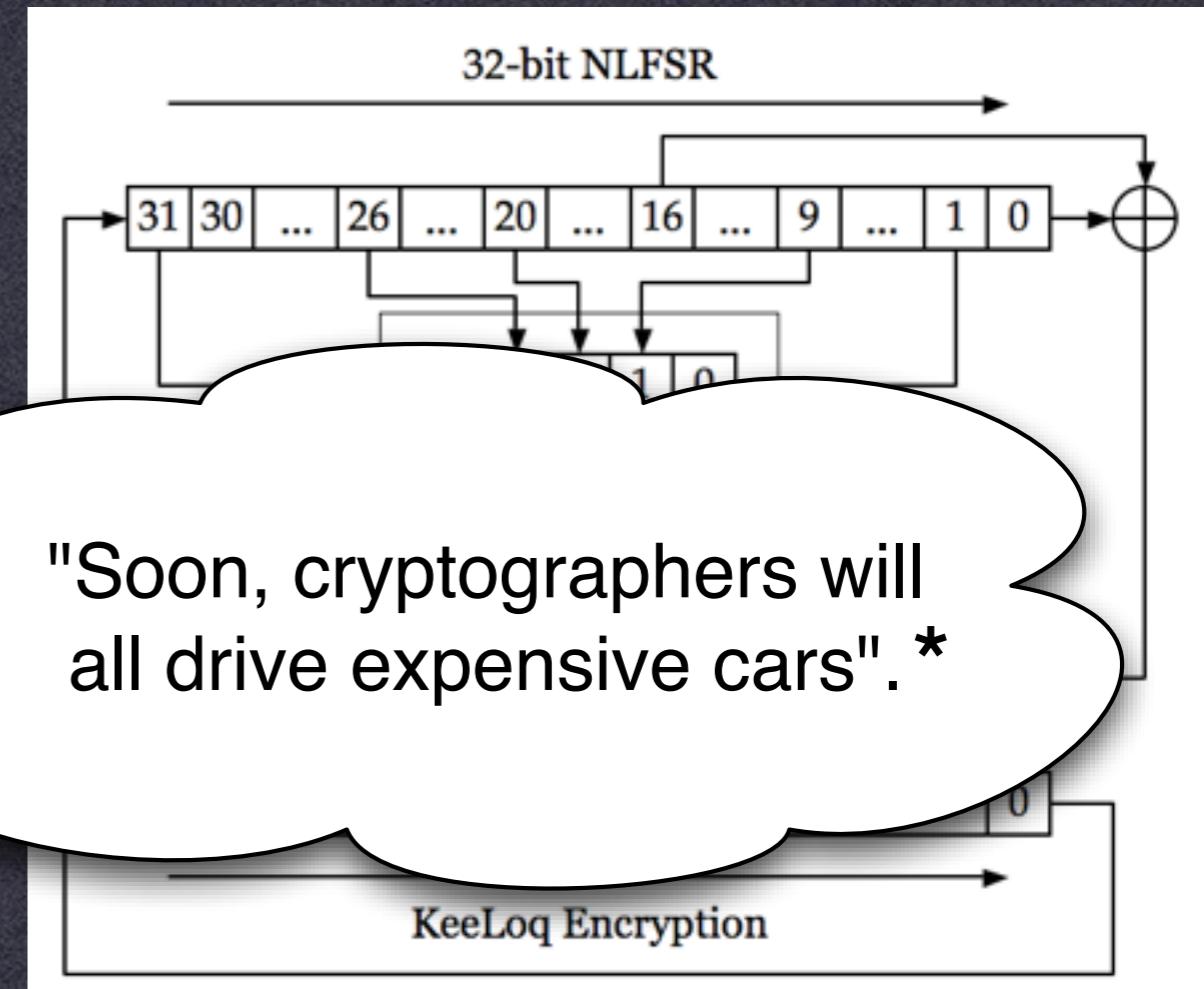
by Michael Mimoso [Follow @mike\\_mimoso](#)

October 3, 2016 , 8:45 am

Logjam was one of several downgrade attacks discovered in the last 18 months that could theoretically allow a resourced attacker to take advantage of [lingering export-grade cryptography](#) to read and modify data over a supposedly secure connection.

# KeeLoq

- Designed by Kuhn & Smit
  - Block cipher: 64-bit key, 32-bit block
  - 528 rounds
  - Mostly used for door opening
  - Direct attacks\*:
    - A.  $2^{16}$  data &  $2^{51}$  operations
    - B.  $2^{32}$  data &  $2^{27}$  operations
    - C. Indesteege et al.:  
(65 min to get data,  
218 CPU days to process)



Public domain image from Wikipedia

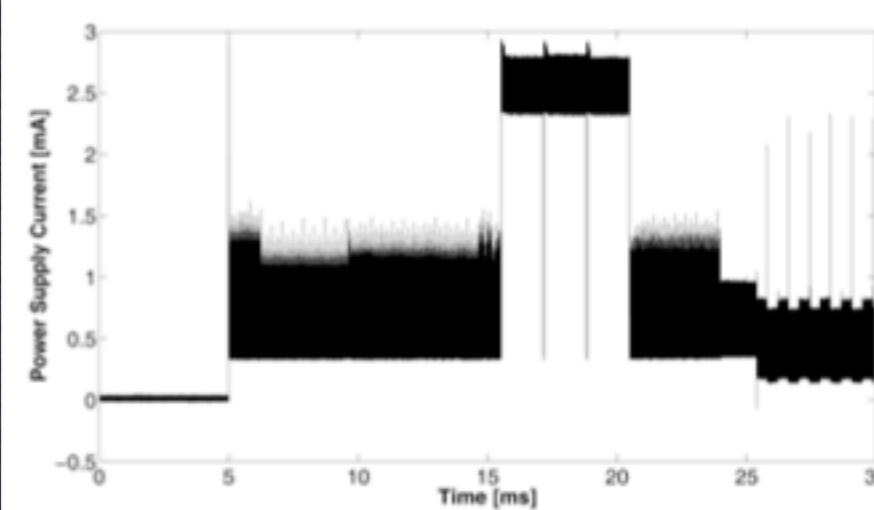
\* Source: Indesteege et al.: <http://www.cosic.esat.kuleuven.be/keeloq/keeloq-slides.pdf>

# KeeLoq

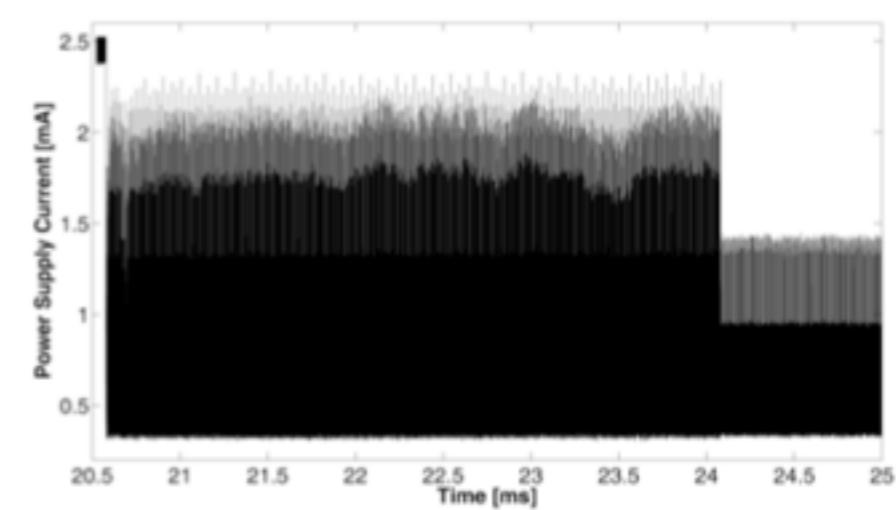
- **Newer attack, CRYPTO 2008**
  - **Requires physical access to device**
  - **Recovers secret key after 10-60 reads**
  - **How?**

# KeyLoq

- CRYPTO 2008
  - Doesn't directly attack the cipher
  - Instead, measures how the cipher works in operation.
  - In this case, use power consumption

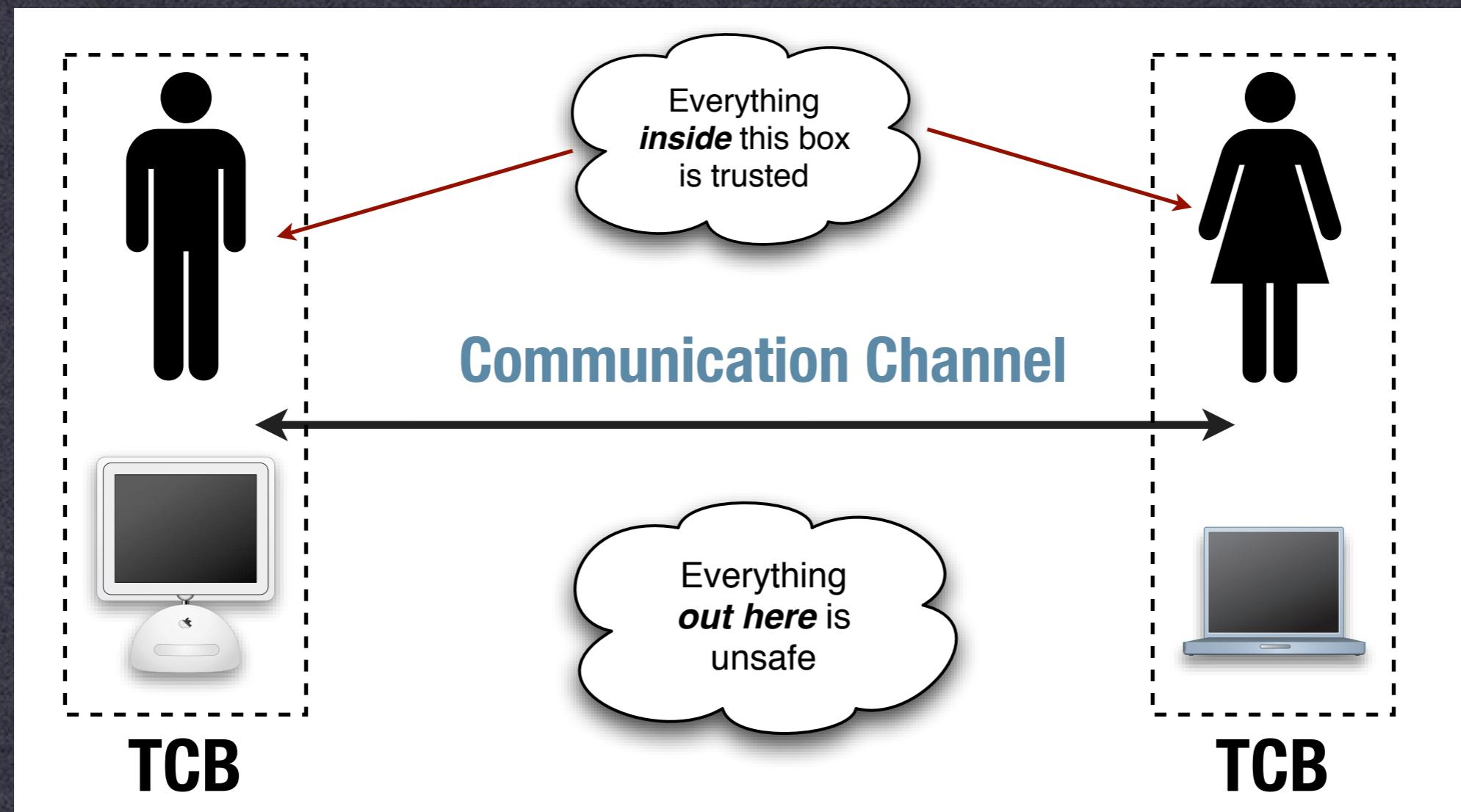


(a) From power up to start sending

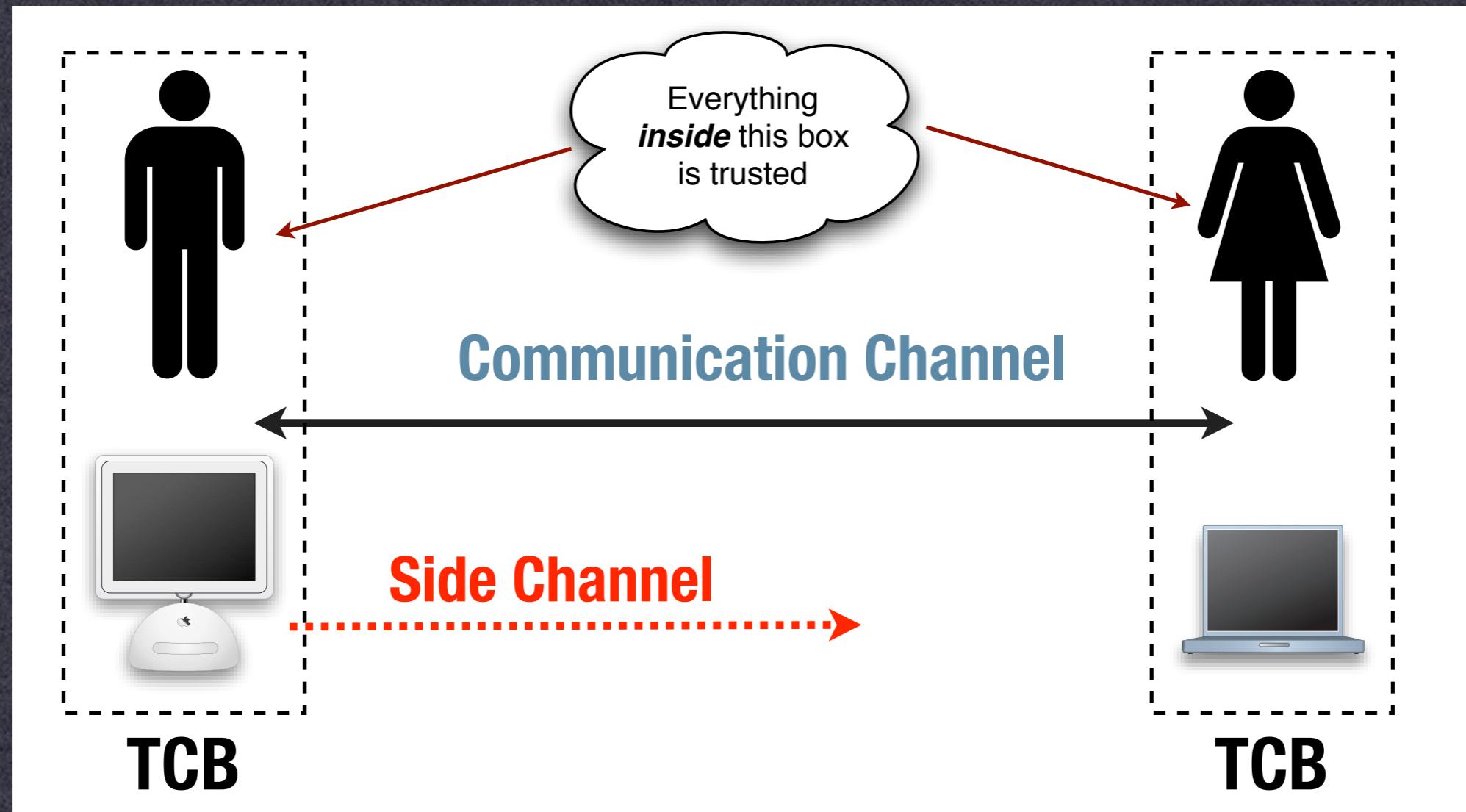


(b) Encryption part

# Review

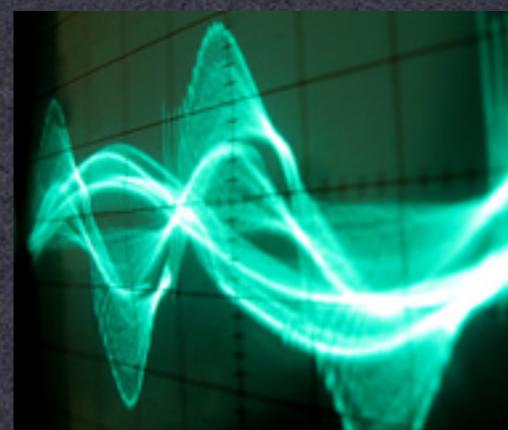


# Side Channels



# Side Channels

- Some history:
  - 1943: Bell engineer detects power spikes from encrypting teletype
  - 1960s: US monitors EM emissions from foreign cipher equipment
  - 1980s: USSR places eavesdropping device inside IBM Selectric typewriters



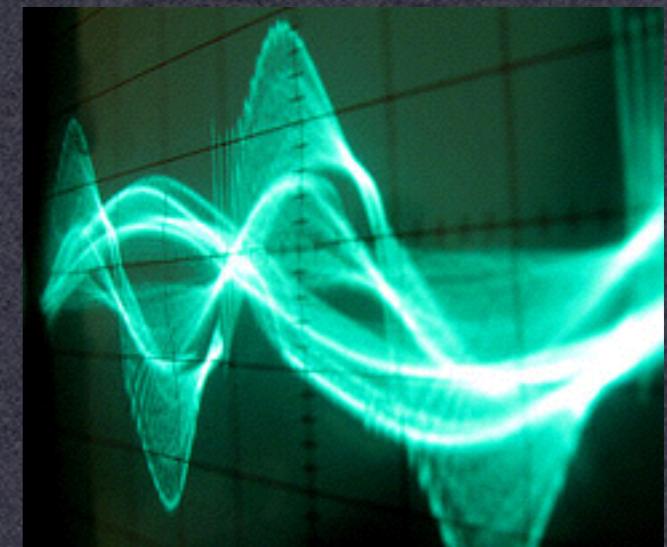
# Side Channels

- Some history:
  - 1990s: Paul Kocher demonstrates timing attacks, power analysis attacks against RSA, Elgamal



# Common Examples

- Timing
- Power Consumption
- RF Emissions
- Audio



# RSA Cryptosystem

$$N = p \cdot q$$

$$e \cdot d \equiv 1 \pmod{(p-1)(q-1)}$$

## Encryption

$$c = m^e \pmod{N}$$

## Decryption

$$m = c^d \pmod{N}$$

# RSA Cryptosystem

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## Encryption

$$c = m^e \pmod{N}$$

## Decryption

$$m = c^d \pmod{N}$$

$$m = \underbrace{c * c * c * \cdots * c}_{\text{d times}} \pmod{N}$$

# Modular Exponentiation

$$m = c^d \bmod N$$

$$d = 1010101001110101011001001001001$$



```
modpow(c, d, N) {  
    result = 1;  
  
    for (i = 1 to |d|) {  
        if (the ith bit of d is 1) {  
            result = (result * c) mod N;  
        }  
  
        c = c2 mod N;  
    }  
  
    return result;  
}
```



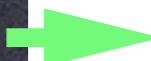
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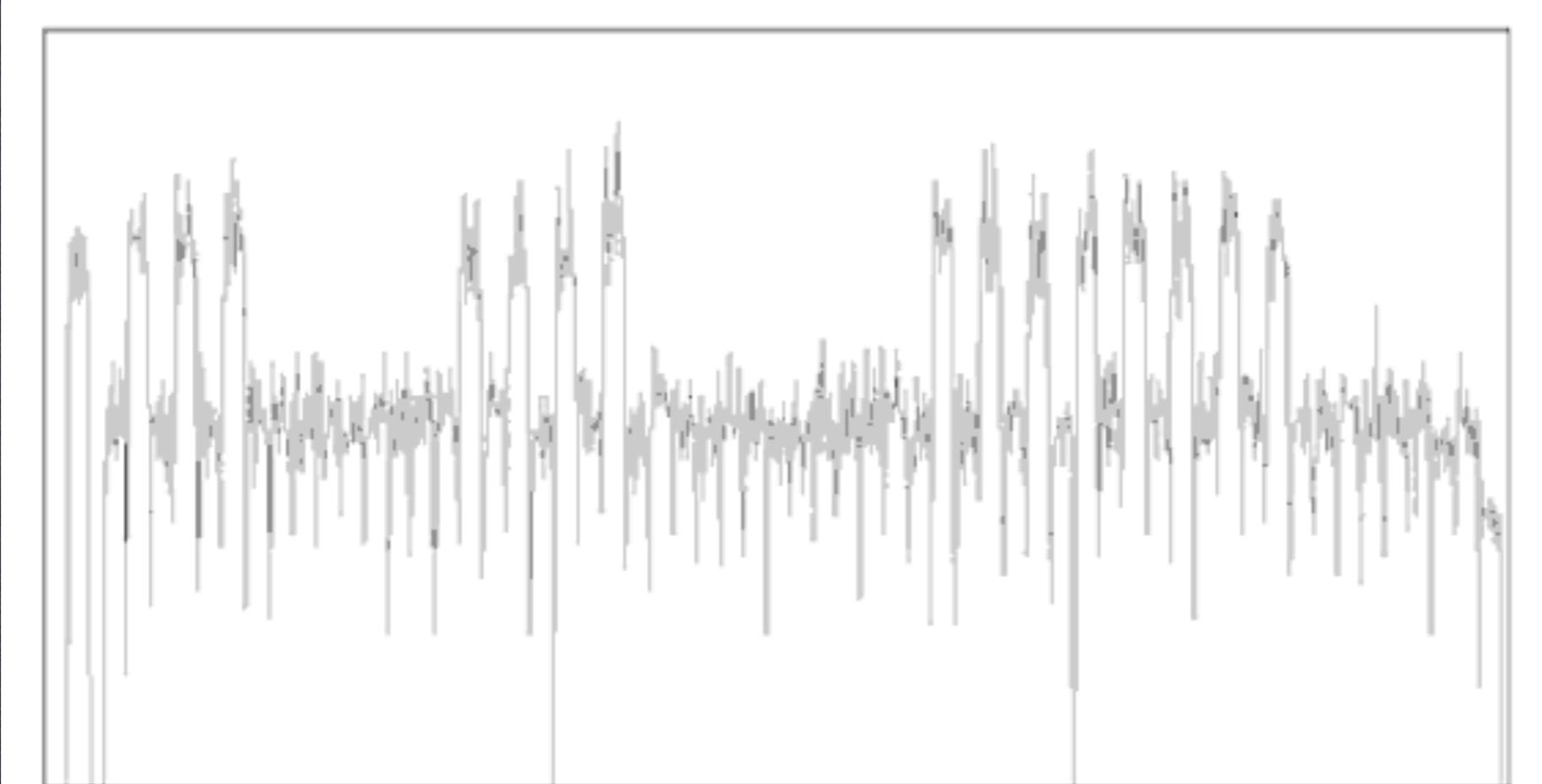
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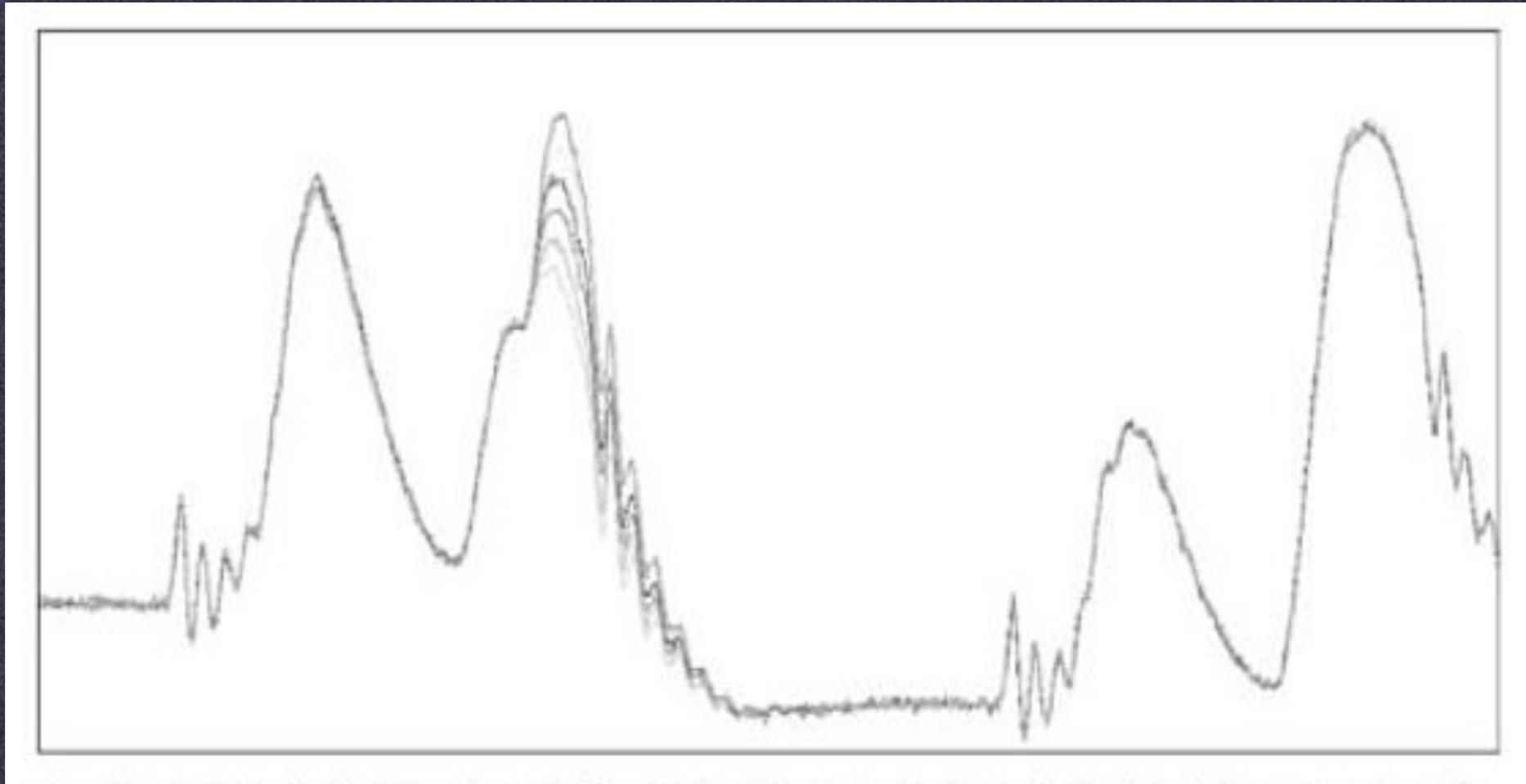
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            result = (result * c) mod N; Expensive Operation  
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```



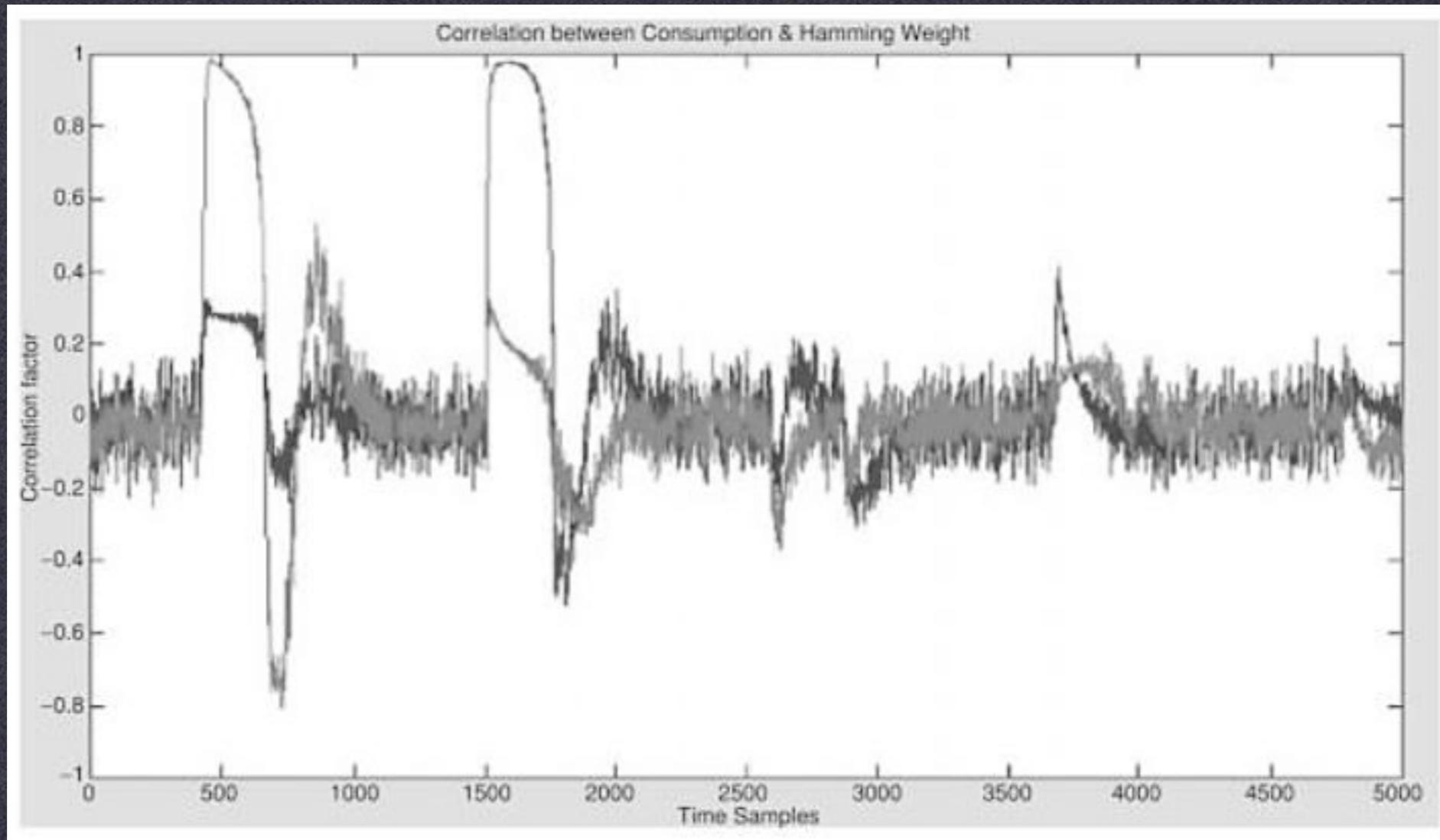
# Simple Power Analysis



# Differential Power Analysis



# Differential Power Analysis



# Modular Exponentiation

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```

Expensive Operation

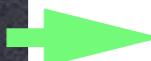
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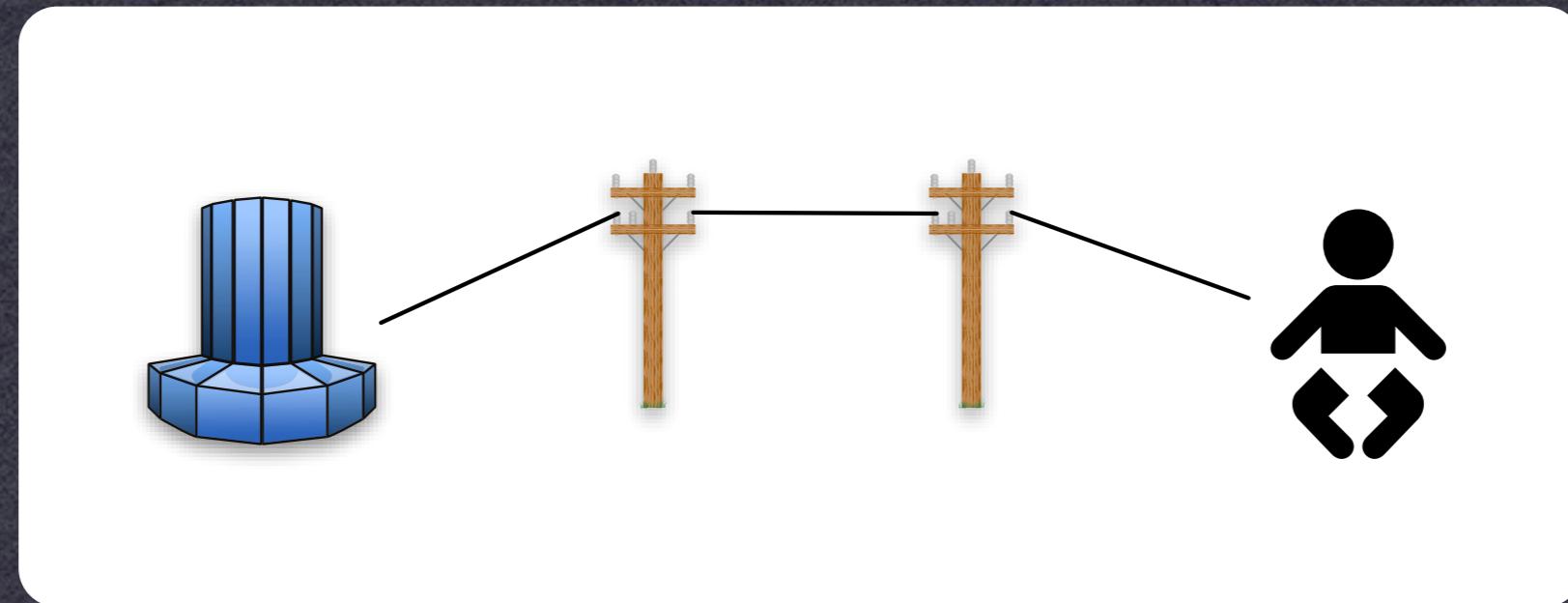


# Kocher's Timing Attack

- Assume that for some values of  $(a * b)$ , multiplication takes unusually long
- Given the first  $b$  bits, compute intermediate value “result” up to that point
- If the next bit of  $d = 1$ , then calc is  $(\text{result} * c)$
- If this is expected to be slow, but response is fast then the next bit of  $d \neq 1$

# Remote Timing Attacks

- Boneh & Brumley
  - Remote attack on RSA-CRT as implemented in OpenSSL
  - Optimization, uses knowledge of  $p, q$



# Solutions

- Quantization:
  - All operations take the same time
  - Hard to do without sacrificing performance
- Blinding:
  - Prevents attacker from selecting ciphertext (that is processed with the secret key)

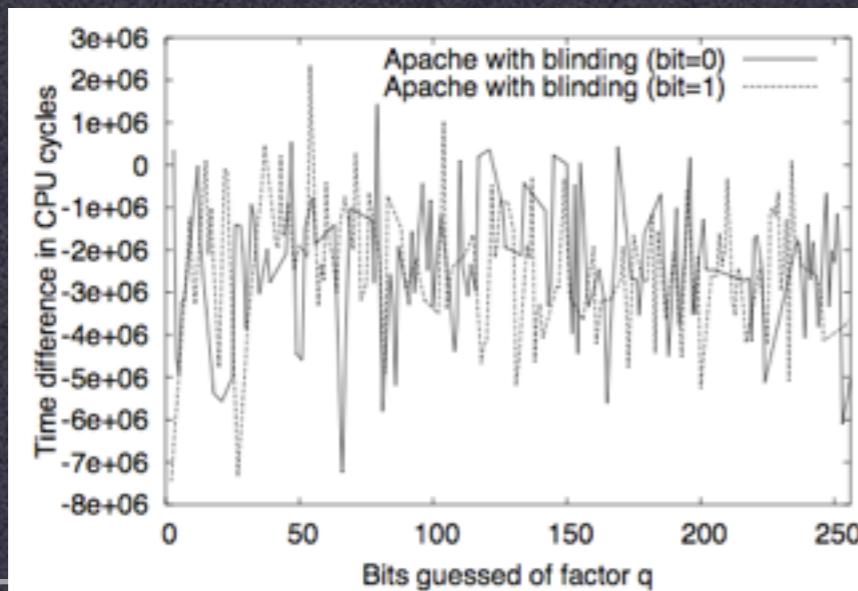
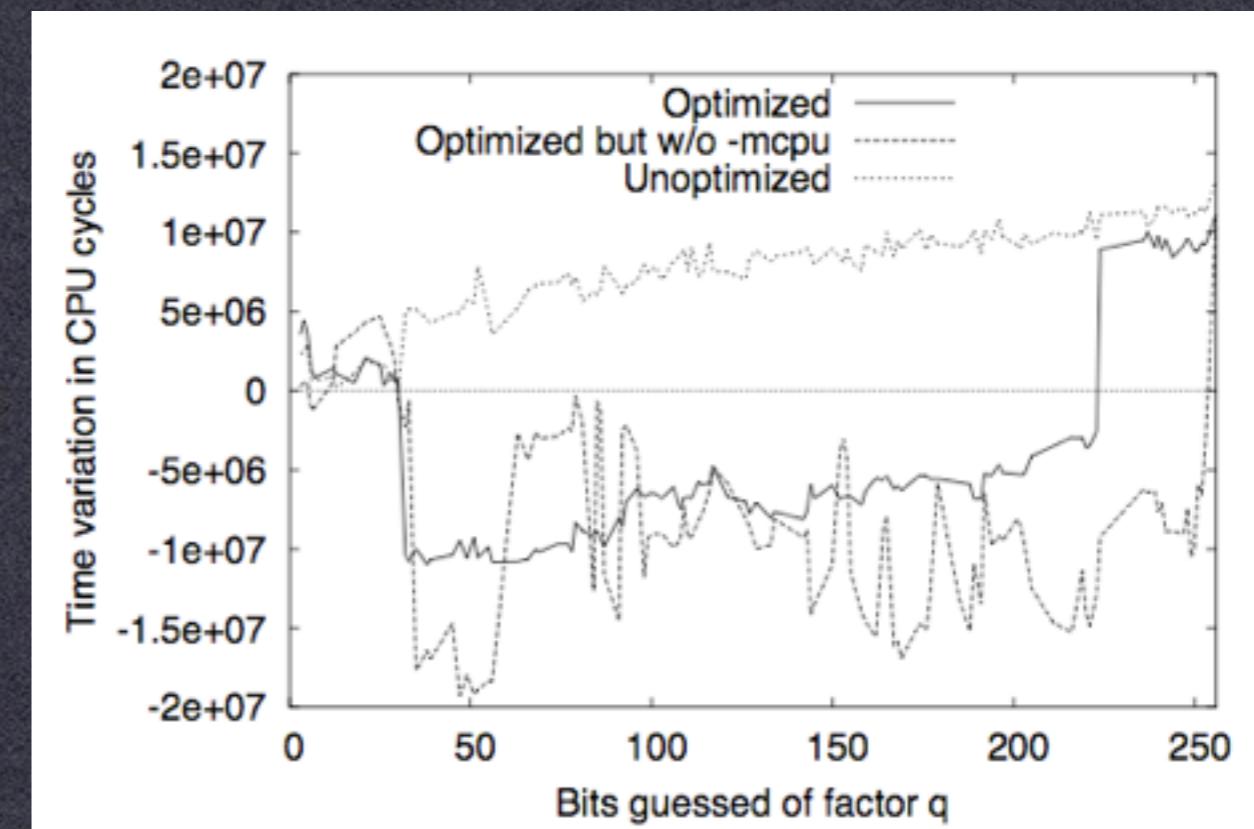
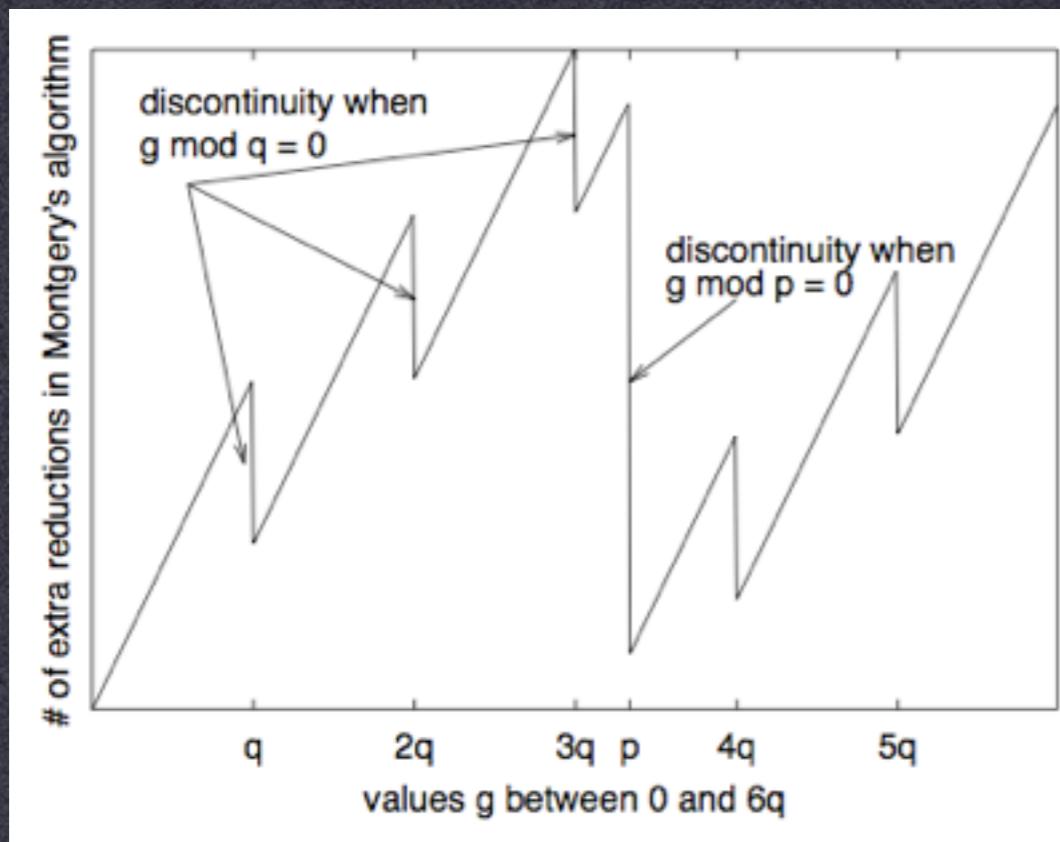


Image Source: Boneh, Brumley: Remote Timing Attacks are Practical

# Remote Timing Attacks

- Boneh & Brumley
  - By repeating the timing measurements, they were able to extract a secret key after several million samples



Source: Boneh, Brumley: Remote Timing Attacks are Practical

# Windowed Exponentiation

$$m = c^d \bmod N$$

$$d = 1010101001110101011001001001001$$

- Handles the input in larger “chunks”
  - Fixed or variable sized
  - Can speed up by pre-computing some values
    - e.g.,  $c^2, c^3, \dots, c^{16}$

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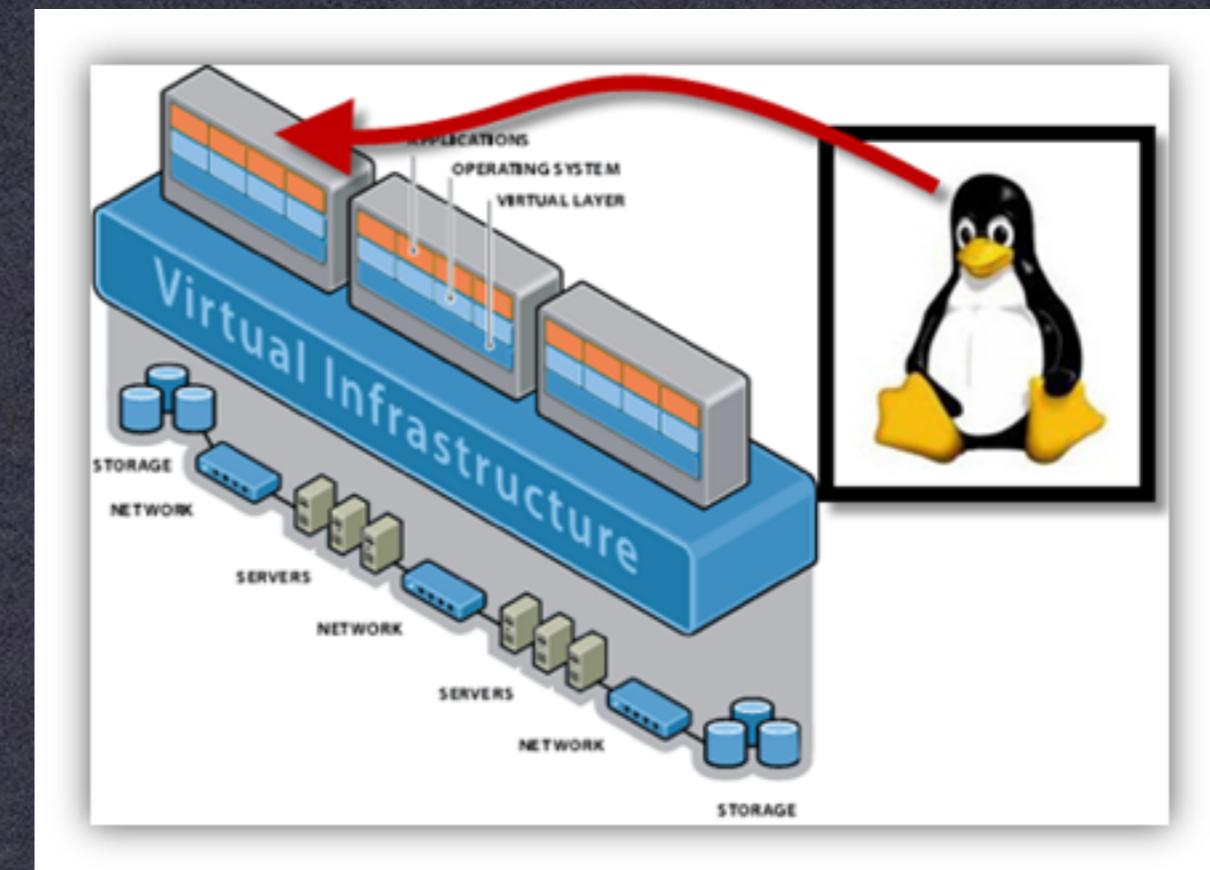
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- Handles the input in larger “chunks”
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# Cache Timing Attacks

- Observation
  - When we use pre-computed tables, this implies a memory access
  - This takes time
  - Unless the data is cached!

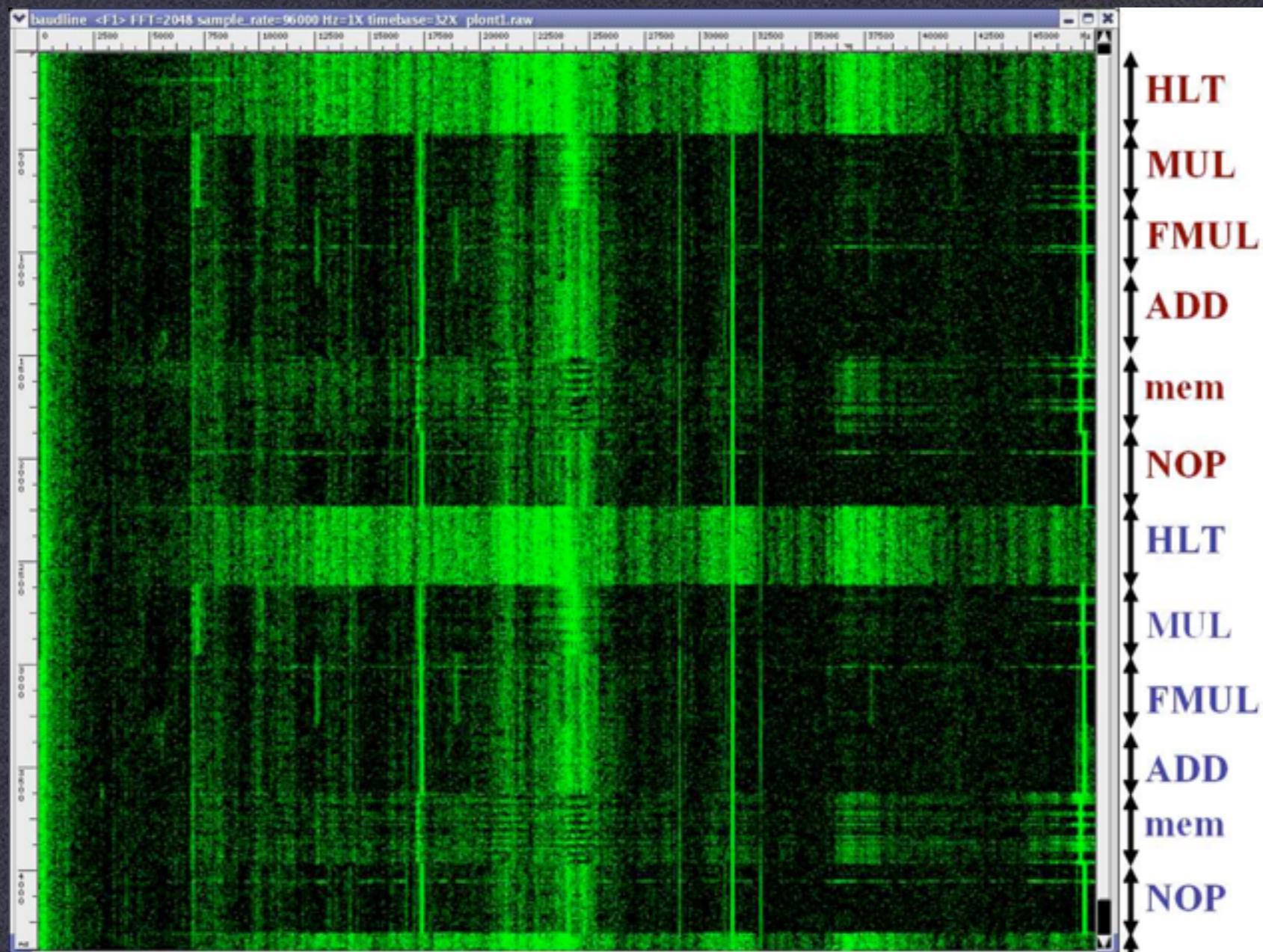


# Hypervisor attacks

- Observation
  - This applies to code too!

```
SquareMult( $x, e, N$ ):  
    let  $e_n, \dots, e_1$  be the bits of  $e$   
     $y \leftarrow 1$   
    for  $i = n$  down to 1 {  
         $y \leftarrow \text{Square}(y)$  (S)  
         $y \leftarrow \text{ModReduce}(y, N)$  (R)  
        if  $e_i = 1$  then {  
             $y \leftarrow \text{Mult}(y, x)$  (M)  
             $y \leftarrow \text{ModReduce}(y, N)$  (R)  
        }  
    }  
    return  $y$ 
```

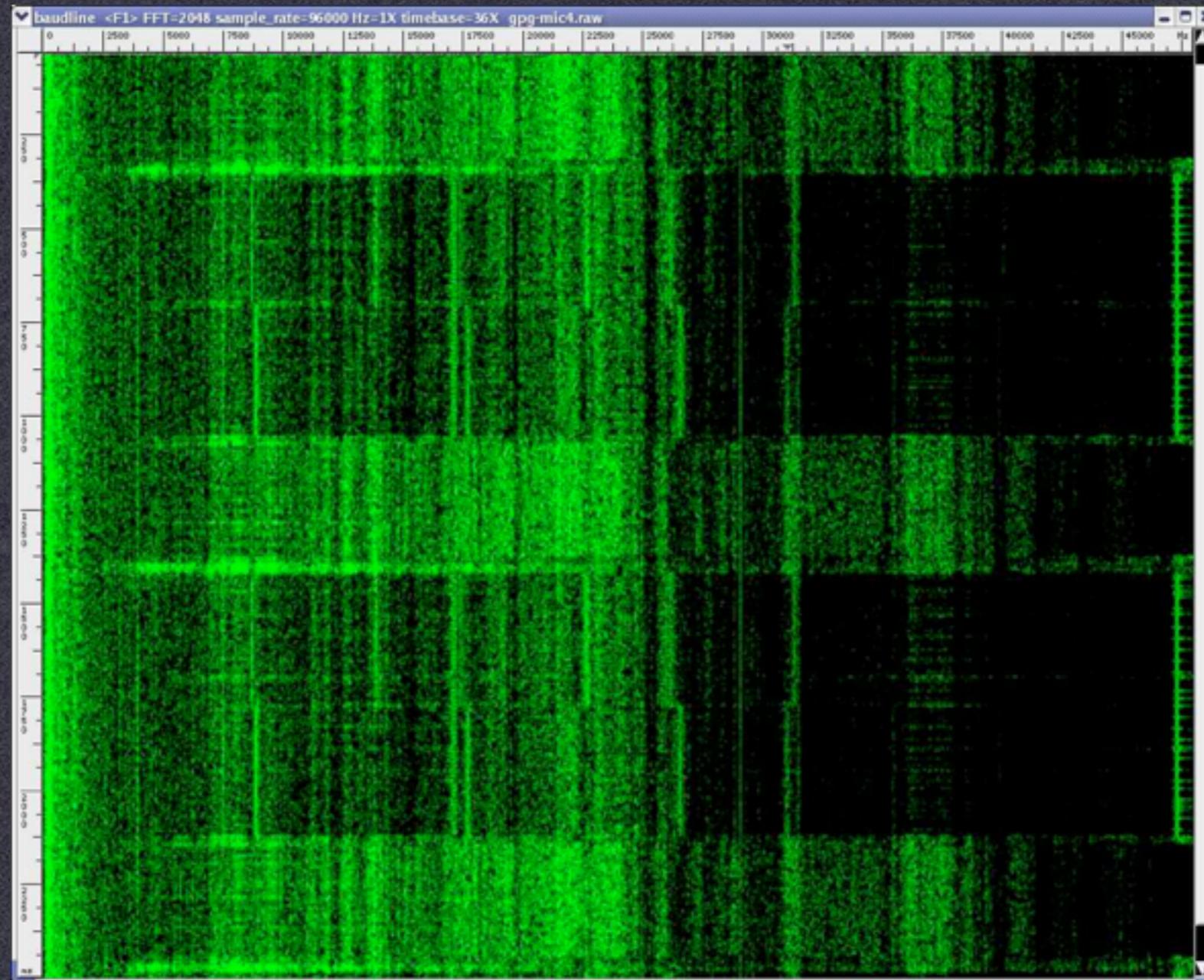
# Acoustic Side Channels



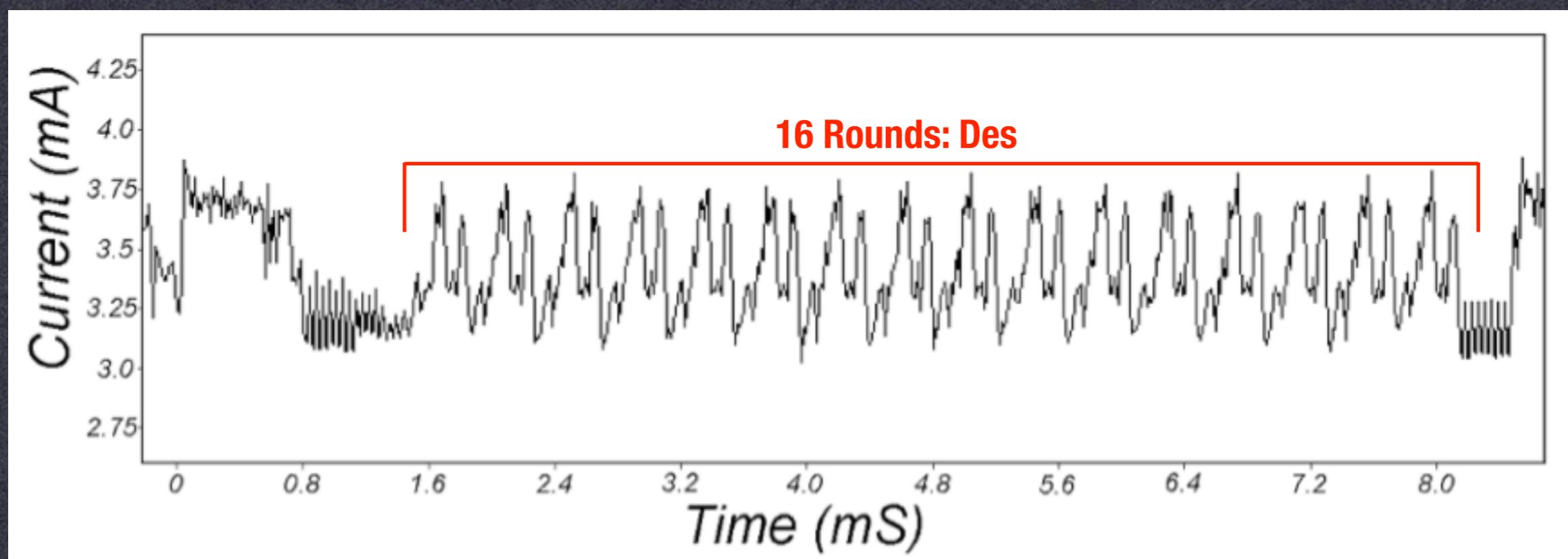
# Acoustic Side-Channels

GPG RSA-CRT  
signature #1:

(repeated)



# Reverse Engineering



Source: Kocher et al. 1999

# Back to KeyLoq

- KeyLoq attack has an unhappy coda:
  - Turns out that all keys for a given manufacturer are derived from the same MK

$$k = \text{pad}(ID, \text{seed}) \oplus MK$$

- Key derivation function based on XOR :(
- By observing 2 interactions between key/car we can derive the MK and thus steal any car