

Probabilistic Stereo Egomotion Transform

Hugo Silva, Eduardo Silva

INESC TEC (formerly INESC Porto)

ISEP/IPP - School of Engineering, Polytechnic Institute of Porto

Email: hugo.m.silva, eduardo.silva@inescporto.pt

Alexandre Bernardino

Institute for Systems and Robotics

IST Lisbon, Portugal

Email: alex@isr.ist.utl.pt

Abstract—In this paper we propose a novel fully probabilistic solution to the stereo egomotion estimation problem. We extend the notion of probabilistic correspondence to the stereo case which allow us to compute the whole 6D motion information in a probabilistic way. We compare the developed approach against other known state-of-the-art methods for stereo egomotion estimation, and the obtained results compare favorably both for the linear and angular velocities estimation.

I. INTRODUCTION

The use of mobile robots on modern world tasks is increasing rapidly as well as their application scenarios. One of the robots most complex tasks is navigation where typically GPS-IMU sensor information is used. Some of these scenarios (e.g. urban areas, underwater GPS denied environments) are prone to GPS-IMU failures, making it necessary to use other alternative or complementary sensors such as vision cameras for the robot to perceive and navigate through out the environment. When using visual sensors (cameras), robots must determine motion measuring their displacement relative to static key points in the environment, process which is usually denoted as Visual Odometry (VO). The use of VO methods for obtaining robot motion has been continuously subject of research by the robotics and automotive industry over the past years. One way of performing VO estimation is by determining instantaneous camera displacement on consecutive frames, a process denoted as visual egomotion estimation, and integrating over time the obtained rotational and translational velocities. Monocular egomotion estimation is subject to translation scale ambiguity, i.e. in the absence of other sources of information, only the translational velocity direction can be reliably measured. Therefore, whenever possible, two cameras are used to have a full velocity estimation, usually denoted as stereo egomotion estimation e.g. ([1], [2], [3], [4]).

Most approaches to the stereo egomotion estimation problem rely on non-probabilistic correspondences methods. Common approaches try to detect, match and track key points between images on adjacent time frames, and afterwards use the largest subset of point correspondences that yield a consistent motion. In probabilistic correspondence methods matches are not fully committed during the initial phases of the algorithm and multiple matching hypotheses are accounted for. Our previous work in egomotion estimation (6DP) [1] [2], has shown that the probabilistic correspondence methods

were a viable way to estimate egomotion with advantages in precision over classical feature based methods. Nevertheless 6DP method was unable to estimate the translation scale factor based only on probabilistic approaches, and required a mixed approach to be able to recover all motion parameters.

In this paper, we developed a novel probabilistic stereo egomotion method capable of computing 6-DOF motion parameters solely based on probabilistic correspondence approaches, and without the need to track or commit key point matches between consecutive frames. The use of probabilistic correspondence methods allows to maintain several match hypotheses for each point, which is an advantage when there are ambiguous matches (which is the rule in image feature correspondences problems), because no commitment is made before analyzing all image information. Another advantage is that a full probabilistic distribution of motion provides a better sensor fusion with other sensors, e.g. inertial.

Our proposed approach improves the work conducted in [1], [2] and propose a fully probabilistic algorithm to perform stereo egomotion estimation, which we denote as Probabilistic Stereo Egomotion Transform (PSET). While in 6DP [1], a mixed probabilistic and deterministic approach was used to estimate rotation and translation parameters, PSET only employs probabilistic correspondences. The rotation estimation is achieved the same way as in 6DP (with a 5D search over the motion space based on the notion of epipolar constraint), yet the translation scale factor is obtained by exploiting an accumulator array voting scheme. The obtained results demonstrate a clear performance improvement in the estimation of the linear and angular velocities over current state-of-the-art stereo egomotion estimation methods, when compared to inertial measurement unit ground-truth information. Furthermore, since real-time is a concern in today modern mobile robotics applications the algorithm can be easily implemented using a multi-core system.

This paper is organized as follows: In section II some related work is presented. In section III, we discuss the monocular approach to probabilistic egomotion estimation. Afterwards in section IV we extend this approach to the stereo egomotion estimation case. In section V results of the PSET Transform compared with other state of the art stereo egomotion estimation methods are presented. Finally, section VI contains the conclusions with final remarks and future work.

II. RELATED WORK

One way to perform stereo VO is to estimate the instantaneous velocity (egomotion) of the vehicle or robot from a sequence of images acquired using a stereo camera setup, and integrate the velocity measurements in time. The main advantage of a stereo camera configuration setup is the ability to easily recover the translation motion scale. Most of the known stereo VO methods use the 3D position of observed image key points that are computed by triangulating their relative position between stereo images. Afterwards, camera motion can be computed based on the alignment of the same 3D key points between adjacent time steps. The research work on stereo VO estimation started with Olson *et al* [5], when visual sensors became an alternative to the dead reckoning estimation (e.g wheel odometry) that were unable to estimate robot motion over long distances, and accumulated large errors specially due to wheel slip in uneven terrain. However, the main boost in the development of stereo VO methods was given by Cheng *et al* [6] with the Mars Rover Project. The proposed method estimated all 6-DOF motion parameters by tracking image key points between left and right image pairs in consecutive time frames, and determined the change of position and attitude using maximum likelihood estimation.

Currently stereo VO methods are classified according to the employed feature detection scheme or by the way motion estimation is performed [7]. In Alismail *et al* [8], a study for evaluating Absolute Orientation (AO) methods and Perspective-n-Point methods (PnP) for achieving robot pose estimation using only stereo visual odometry is conducted. Their work concluded that PnP methods are more accurate than AO methods, AO methods consist on triangulating 3D key points for every stereo pair. Then motion estimation is solved using key point alignment algorithms such as the Procrustes method [9], used in [1] or Iterative-Closest-Point (ICP) method [10], used in Milella and Siegwart [11] for estimating motion of an all-terrain rover. Nister *et al* [12], developed the first PnP algorithm (3D-2D camera pose estimation), computed in real-time with an outlier rejection scheme, that minimized the re-projection error. In what concerns image information, stereo VO methods may use sparse or dense approaches. One of the most relevant dense stereo VO applications was developed by Howard [13] for ground vehicle applications. The method makes no assumption of prior knowledge over camera motion, and so it can handle very large image translations. However, due to the absence of feature detectors invariant to rotation and scaling, it only works on low-speed applications with high frame-rate. Some authors like Ni *et al* [14], minimize dependencies on feature matching and tracking algorithms by simultaneously using an algorithm that computes feature displacement in both cameras, together with a quadrifocal setting within a RANSAC [15] framework.

More recently the application focus of stereo VO methods has moved from planetary rover application to the development of novel intelligent vehicles by the automotive industry, as the one developed by Kitt *et al* [3]. Their method is available

as an open-source visual odometry library named LIBVISO. Stereo egomotion estimation is based on image triples and the online estimation of the trifocal tensor [16]. It uses rectified stereo image sequences and produces an output 6D vector with estimated linear and angular velocities. Comport *et al* [4] also developed a stereo VO method based on the quadrifocal tensor. By using tensor notation, the authors can compute motion using 2D-2D image pixels matches, thus yielding a more precise motion estimation. Another way of developing stereo VO is to combine with other absolute sensor information. Rehder *et al* [17] developed a stereo visual odometry method that combined visual data with GPS and IMU information. The proposed method consistently fused stereo visual odometry information with inertial measurements and sparse GPS information into a single pose estimate in real-time. Kneip *et al* [18] also proposed an alternative tightly coupled approach with vision and IMU information. Their strategy for continuous robust pose computation is based on the triangulation of frame to frame point clouds when there is sufficient disparity among them.

In our previous work [1], [2] a probabilistic correspondence method developed by [19] was used to compute the stereo egomotion estimation. The results obtained show an improvement in the angular velocities estimation, but not in the linear velocities estimation where scale was obtained using deterministic matches instead of probabilistic correspondences. In this paper, we will extend the probabilistic correspondence approach to the estimation of the linear velocities.

III. PROBABILISTIC EGOMOTION ESTIMATION

The seminal work of Domke *et al* [19] has introduced the notion of probabilistic correspondence in the context of the egomotion estimation problem. In this section we provide a brief description of their method and introduce the notation required for the remaining sections.

Given two images taken at different times, I_k and I_{k+1} , the probabilistic correspondence between point $s \in R^2$ in image I_k and point $q \in R^2$ in image I_{k+1} , is defined as a belief:

$$\rho_s(q) = \text{match}(s, q)$$

where the function $\text{match}(\cdot)$ outputs a value between 0 and 1 expressing similarity in the appearance of the two points in local neighborhoods. In [19] that function was implemented by the correlation of a Gabor Filter bank response in the two points. In our work we use the zero-mean normalized cross-correlation function (ZNCC) to measure point similarity:

$$ZNCC_{(s,q)} = \frac{\sum_{\delta \in W} [I_k(s + \delta) - \bar{I}_k] [I_{k+1}(q + \delta) - \bar{I}_{k+1}]}{\sqrt{\sum_{\delta \in W} [I_k(s + \delta) - \bar{I}_k]^2} \sqrt{\sum_{\delta \in W} [I_{k+1}(q + \delta) - \bar{I}_{k+1}]^2}}$$

where W denotes a 2D window centered at the origin whose size defines the neighborhood of analysis around points s and q . In practice we use a fast recursive implementation of the ZNCC developed by Huang *et al* [20]. The probabilistic correspondence is then computed as:

$$\rho_s(q) = \frac{ZNCC(s, q) + 1}{2}$$

so that its values range from 0 to 1.

Afterwards, motion hypotheses defined by the incremental rotation matrix R and the translation velocity direction $\hat{t} = t/\|t\|$ are checked by analyzing the probabilistic correspondences $\rho_s(q)$ along the epipolar lines derived from R and \hat{t} [19]. A correspondence q for point s must satisfy the epipolar constraint denoted by:

$$\tilde{s}^T E \tilde{q} = 0 \quad (1)$$

where \tilde{s} and \tilde{q} are the homogeneous representations of s and q , respectively. Matrix E is the so called Essential Matrix [16], a 3×3 matrix of rank 2 and 5 degrees of freedom that encodes the rigid camera motion. In order to obtain the Essential Matrix (E) from the probabilistic correspondences, [19] proposes the computation of a probability distribution over the 5-dimensional space of essential matrices. Each dimension of the space is discretized in 10 bins, thus leading to 100000 hypotheses E_i . For each point s the likelihood of these hypotheses is evaluated by:

$$\rho(E_i|s) \propto \max_{(\tilde{q})^T E_i \tilde{s} = 0} \rho_s(q) \quad (2)$$

Therefore for a single point s in image I_k^L , the likelihood of a motion hypothesis (E_i) is proportional to the likelihood of the best match obtained along the epipolar line generated by the essential matrix. If one assumes statistical independence between the measurements obtained at each point, the overall likelihood of a motion hypothesis is proportional to the product of the likelihoods for all points:

$$\rho(E_i) \propto \prod_s \rho(E_i|s) \quad (3)$$

Finally, given the top ranked motion hypotheses, a Nelder-Mead simplex method [21] is used to refine the motion estimate, and obtain the best motion, up to a scale factor, that represents the image movement between the two frames.

IV. PROBABILISTIC STEREO EGOMOTION ESTIMATION

In this work we extend the notion of probabilistic correspondence to the stereo case which allow us to compute the whole 6D motion information in a probabilistic way. In a stereo setup we consider images I_k^L , I_{k+1}^L , I_k^R and I_{k+1}^R , where superscripts L and R denote respectively the left and right images of the stereo pair. Probabilistic matches of a point s in I_k^L are now computed not only for points q in I_{k+1}^L but also for points r in I_k^R and p in I_{k+1}^R :

$$\rho_s(r) = \frac{ZNCC(s, r) + 1}{2}$$

$$\rho_s(p) = \frac{ZNCC(s, p) + 1}{2}$$

For the sake of computational efficiency, analysis can be limited to sub-regions of the images given prior knowledge about the geometry of the stereo system or the motion given by other sensors like IMU's. In particular, for each point s , coordinates r can be limited to a band around the epipolar lines according to the stereo setup epipolar geometry.

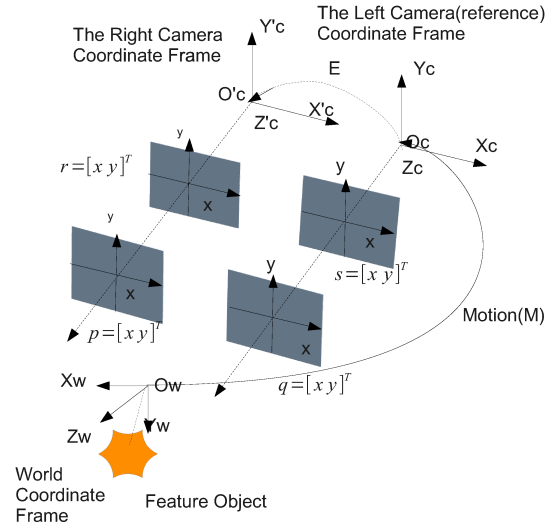


Fig. 1: Stereo Egomotion Geometry

A. The Geometry of Stereo Egomotion

In this section we describe the geometry of the stereo egomotion problem, i.e. will analyze how world points project in the four images acquired from the stereo setup in two consecutive instants of time according to its motion. This analysis is required to derive the expressions to compute the translational scale factor.

Let us consider the 4×4 rototranslations T_L^R and M_k^{k+1} that describe, respectively, the rigid transformation between the left and right cameras of the stereo setup, and the transformation describing the motion of the left camera from time k to $k+1$:

$$T_L^R = \begin{bmatrix} R_L^R & t_L^R \\ 0 & 1 \end{bmatrix} \quad M_k^{k+1} = \begin{bmatrix} R_k^{k+1} & t_k^{k+1} \\ 0 & 1 \end{bmatrix}$$

where R and t denote the rotational and translational components. We factorize the translational motion t_k^{k+1} in its direction \hat{t} and amplitude α :

$$t_k^{k+1} = \alpha \hat{t}$$

Given that rotational motion and translation direction are computed by the method described in the previous section, the computation of α is the objective to pursue.

Let us consider an arbitrary 3D point $X = (X_x, X_y, X_z)^T$ expressed in the reference frame of the left camera at time k . Considering normalized intrinsic parameters (unit focal distance $f = 1$, zero central point $c_x = c_y = 0$, no skew), the homogeneous coordinates of the projection of X in the 4 images is given by:

$$\begin{cases} \tilde{s} = X \\ \tilde{r} = R_L^R X + t_L^R \\ \tilde{q} = R_k^{k+1} X + \alpha \hat{t} \\ \tilde{p} = R_L^R R_k^{k+1} X + \alpha R_L^R \hat{t} + t_L^R \end{cases} \quad (4)$$

To illustrate the solution, let us consider the particular case of parallel stereo. This will allow us to obtain the form of the

solution with simple equations but does not compromise generality because the procedure to obtain the solution in the non parallel case is analogous. In parallel stereo the cameras are displaced laterally with no rotation. The rotation component is the 3×3 identity ($R_L^R = I_{3 \times 3}$) and the translation vector is an offset (baseline b) along the x coordinate, $r_L^R = (b, 0, 0)^T$. In this case, expanding the equations for $s = (s_x, s_y)^T$ and $r = (r_x, r_y)^T$ we obtain:

$$\begin{cases} s_x = \frac{X_x}{X_z} \\ s_y = r_y = \frac{X_y}{X_z} \\ r_x = \frac{(X_x + b)}{X_z} \end{cases}$$

Introducing the disparity d as $d = r_x - s_x$ we have $d = \frac{b}{X_z}$ and we can reconstruct the 3D coordinates of point X as a function of the image coordinates r and s and the known baseline value b :

$$X = \left(\frac{s_x b}{d} \quad \frac{s_y b}{d} \quad \frac{b}{d} \right)^T$$

Replacing this value now in (4) we obtain:

$$r = \begin{bmatrix} \frac{(s_x b + b)d}{b} \\ s_y \end{bmatrix} \quad (5)$$

$$q = \begin{bmatrix} \frac{r11s_x b + r12s_y b + r13b + \alpha t_x d}{r31s_x b + r32s_y b + r33b + \alpha t_z d} \\ \frac{r21s_x b + r22s_y b + r23b + \alpha t_y d}{r31s_x b + r32s_y b + r33b + \alpha t_z d} \end{bmatrix} \quad (6)$$

$$p = \begin{bmatrix} \frac{r11s_x b + r12s_y b + r13b + \alpha t_x d + b d}{r31s_x b + r32s_y b + r33b + \alpha t_z d} \\ \frac{r21s_x b + r22s_y b + r23b + \alpha t_y d}{r31s_x b + r32s_y b + r33b + \alpha t_z d} \end{bmatrix} \quad (7)$$

We determine the translation scale factor α using (6) by:

$$q_x = \frac{\overbrace{r11s_x b + r12s_y b + r13b}^A + \alpha t_x d}{\underbrace{r31s_x b + r32s_y b + r33b}_{C} + \alpha t_z d} \quad (8)$$

being α given by:

$$\alpha = \frac{A - q_x C}{q_x t_z d - t_x d} \quad (9)$$

The same procedure is applied to q_y :

$$q_y = \frac{\overbrace{r21s_x b + r22s_y b + r23b}^B + \alpha t_y d}{\underbrace{r31s_x b + r32s_y b + r33b}_{C} + \alpha t_z d} \quad (10)$$

being α given by:

$$\alpha = \frac{B - q_y C}{q_y t_z d - t_y d} \quad (11)$$

The translation scale factor α , can also be determined using the same procedure applied to (7). Therefore, being α an over-determined parameter since there are four equations to one

unknown, we choose the α with the highest denominator to minimize the effect of numerical errors. In case both denominators are low due to very low disparity or degenerate motions, this particular point can not be used for the estimation.

B. Translational Scale Estimation

In the previous section we have seen that it is possible to estimate the translational scale α from the observation of a single static point s , if its point correspondences r , q and p are known and there are no degeneracies. In practice, two major problems arise: (i) it is hard to determine what are the static points in the environment given that the cameras are also moving; and (ii) it is very hard to obtain reliable matches due to the noise and ambiguities present in natural images. Therefore using a single point to perform this estimation is doomed to failure. We must therefore use multiple points and apply robust methodologies to discard outliers.

In our previous work [1], this was achieved by computing the rigid transformation between point clouds obtained from stereo reconstruction at times k and $k+1$ with a robust method RANSAC [15]. Point correspondences were deterministically assigned by searching for the best matches along epipolar lines in space (from camera L to camera R) and time (from time k to time $k+1$). In the current work, we extend the probabilistic notion of correspondence to the stereo case. Instead of deterministically committing to matches in space and time, we create a probabilistic observation model for possible matches:

$$P_{match}(s, r, p, q) = \rho_s(r) \rho_s(q) \rho_s(p)$$

where we assume statistical independence in the measurements obtained in the pairwise probabilistic correspondence functions $\rho_s(\cdot)$. Then, because each possible match (s, r, p, q) will correspond to a value of α , we will create an accumulator of α hypotheses, weighted by $P_{match}(s, r, p, q)$. Searching for peaks in the accumulator will provide us the best (most agreed) hypothesis for α given all the information in the images.

C. The Probabilistic Stereo Egomotion Transform

Here we detail how the method is implemented computationally. We assume E has been computed by the methods described previously and the system calibration is known. First a large set of points $s_j, j = 1 \dots J$ is selected. Selection can be random, uniform or based on key points, e.g. Harris corners [22] or Scale-Invariant features [23]. In our current implementation SIFT features are used to detect salient points.

For each point s_j , the epipolar lines $E_{calib} = \tilde{s}_j^T S$ and $E_{sq} = \tilde{s}_j^T E$ are sampled at points r_l and q_m , in images I_k^R and I_{k+1}^L , respectively. Again sample point selection can be random along the epipolar lines or based on match quality. In our implementation we compute local maxima of match quality over the epipolar lines. At this point we create tables that associate to each triplet (s_j, r_l, q_m) a disparity value d_{jl} and a scale value α_{jlm} , determined by either (9) or (11). Given this information the value of p becomes uniquely determined

by (7) and is stored as p_{jlm} . The likelihood of this triplet is then computed by:

$$\lambda_{jlm} = \rho_{s_j}(r_l) \rho_{s_j}(q_m) \rho_{s_j}(p_{jlm})$$

Finally, all computed α_{jlm} values and associated weights λ_{jlm} are fit using a robust (weighted) kernel density estimation with a gaussian smoother [24]. The final estimate of α is computed as the value of the sample α that has the highest smoothed probability density estimate.

D. Dealing with calibration errors

A common source of errors in a stereo setup is uncertainty in the calibration parameters. Both intrinsic and extrinsic parameter errors will deviate the epipolar lines from their nominal values and influence the computed correspondence probability values. To minimize these effects we modify the correspondence probability function when evaluating sample points such that a neighborhood of the point is analyzed and not only the exact same coordinate:

$$\rho'_s(q) = \max_{q' \in \mathcal{N}(q)} \left[\rho_s(q') \exp \frac{(q - q')^2}{2\sigma^2} \right]$$

where $\mathcal{N}(q)$ denotes a neighborhood of the sample point q which, in our experiments, is a 7×7 window.

E. EKF Linear and Angular velocities estimation

Having determined the translation scale factor (α), and the results of the rotation (R) and translation (\hat{t}), is possible to compute the linear and angular velocities (V, Ω) between T_k and T_{k+1} . In order to achieve a more robust estimation and, therefore, disregard erroneous instantaneous measurements, an Extended Kalman filter, with a constant velocity model was used to integrate the velocity estimates, for more detail see [2].

V. RESULTS

A. Experimental Setup

In order to evaluate the PSET algorithm, we utilized one of the sequences of the Karlsruhe dataset [3], and compared performance against LIBVISO, and with our previous implementation of the 6DP [1]. We take the Inertial Measurement Unit (RTK-GPS information) as ground-truth information.

1) *Computational requirements:* The code used to compute the PSET transform was written in MATLAB as a proof of concept, without using any kind of optimization. The experiments conducted to compute the PSET transform were performed using an Intel I5 Dual Core 3.2 GHz. The dataset images have resolution of 1344×391 , which consumes a considerable amount of computational and memory resources making unfeasible the computation of all image points using standard CPU hardware. The PSET transform results were obtained using only 1000 points to estimate the motion. It computes at around 20 sec per image pair. Most of time is consumed in the first stage of the implementation, with the dense probabilistic correspondences and the computation of the motion up to a scale factor. Even so, the approach is

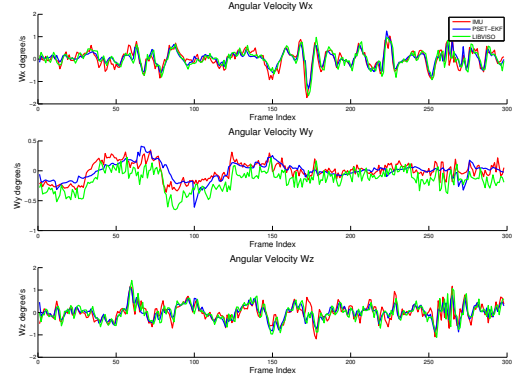


Fig. 2: Results for the angular velocities estimation of 300 frames: ground truth (GPS-IMU information), filtered PSET measurements (PST-EKF) and 6D Visual Odometry Library (LIBVISO). Even though all exhibit similar behaviors the filtered implementation PSET-EKF is the one which is closer to GT (GPS-IMU) (see also table 1).

feasible and can be implemented in real-time for use on mobile robotics applications. The main option is to develop a GPGPU version of the PSET transform implementation since the method copes with multiple hypothesis of correspondences, as well as generated motion hypothesis, making it suitable to be implemented into parallel hardware.

B. Stereo Egomotion results

In this section stereo egomotion estimation results are presented. We compared the PSET estimation results with other state-of-the-art estimation results namely 6DP [1] and LIBVISO [3]. In Fig. 2, PSET and LIBVISO estimation of the angular velocities are presented together with IMU ground-truth information. The 6DP results are not presented in the linear and angular velocities figures, due to the fact that, for angular velocities PSET and 6DP use the same method of computation and thus obtain identical results. One can observe that PSET is closer performance to IMU than LIBVISO. This is quantitatively assessed in Table 1, where the RMS error for the LIBVISO method is about twice the error of the PSET/6DP method.

In Fig. 3, one can observe the behavior of both methods in the linear velocity estimation case. Both LIBVISO and PSET present similar results for the linear velocity estimation case, but PSET has about 50 % less overall RMS error, as can be checked in Table 1. The results confirm that estimating the translation scale using probabilistic approaches produces better results than using deterministic correspondences.

VI. CONCLUSIONS AND FUTURE WORKS

The PSET methodology described in this paper has proven to be an accurate method of computing stereo egomotion. The proposed approach is very interesting because no explicit matching or feature tracking is necessary to compute the vehicle motion. To the best of our knowledge this is the

TABLE I: Comparison of the standard mean squared error between IMU and stereo egomotion estimation methods (LIBVISO, 6DP, and PSET).

	V_x	V_y	V_z	Ω_x	Ω_y	Ω_z	$\ V\ $	$\ \Omega\ $
LIBVISO	0.0674	0.7353	0.3186	0.0127	0.0059	0.0117	1.1213	0.0303
6DP	0.0884	0.0748	0.7789	0.0049	0.0021	0.0056	0.9421	0.0126
PSET	0.0700	0.0703	0.3686	0.0034	0.0019	0.0055	0.5089	0.0108

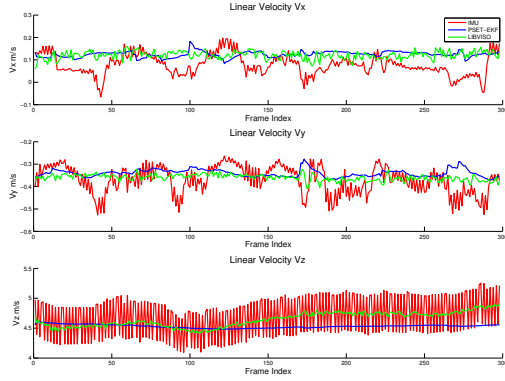


Fig. 3: Estimated linear velocities 300 frames. The PSET transform exhibits a better performance than LIBVISO (see table 1).

first implementation of a full dense probabilistic method to compute stereo egomotion. The results demonstrate that PSET is more accurate than other SOA 3D egomotion estimation methods, improving the overall accuracy in about 50 % over LIBVISO. In future work the main task will be to develop a GPGPU implementation of the PSET transform and test it on difficult and image structure repetitive scenarios where common feature based approaches are more prone to failures. A fused implementation with inertial measurements will also be developed, in order to use the inertial information as motion prior reducing the number of motion hypotheses needed to find the most probable motion.

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