Reading between the Emails: Gendered Patterns of Communication in Local Government

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In this paper, we study the role of gender in local government organizations. We analyze email data from seventeen county governments in North Carolina to understand the relationship between a department manager's gender and the emails they send and receive. First, we use descriptive statistics to identify aggregate gender-homophilous and gender-heterophilous patterns from the numbers of emails sent and received by all department managers. In contrast to previous research, we find no strong evidence of either gender homophily or heterophily. To investigate this finding, we therefore analyze department-to-department communication patterns. Here, we do find evidence of gender bias, with some departments exhibiting gender homophily and others exhibiting heterophily. Finally, to determine the extent to which these patterns are driven by communication content, we use a recently developed latent variable model to identify topic-specific communication subnetworks for each county. We find differing degrees of gender homophily and heterophily for different topics of communication. From a policy perspective, these findings suggest that a gender-equitable working environment cannot be created by hiring decisions alone, as gender bias in communication still exists independent of the positions held by men and women.

Gender in Organizations

Researchers have observed and documented gender bias in both the public and private sectors. Women often receive lower pay, hold less prestigious positions, have reduced opportunities for advancement, and are excluded from decision-making coalitions [5, 3, 11, 2, 7]. As a result, organizations that aspire to a just, efficient, and sustainable culture strive to provide men and women with equal treatment in the workplace [9]. In practice, however, these organizations and the researchers who study them have found it hard to fully understand the day-to-day causes and extent of gender bias. The limited availability of primary-source data means that most research is based on small-scale observational, ethnographic, or self-reported data [e.g., 6, 1, 8]. Since these data sources are often restricted in scope and can be biased by subjective assessments, their use in understanding gender bias is limited.

In this paper, we take a different approach and instead base our analyses on email communication data. We focus specifically on local government organizations and seek to understand the role of gender in communication at the department manager level. With the increasing use of electronic communication in the workplace, and the rise of transparency initiatives within government, scholars can now use public records requests to gather primary-source data about government organizations. Moreover, for many government organizations, such requests even extend to emails. We draw upon this resource to construct an email data set spanning seventeen county governments in North Carolina. By relying on public records requests, our data collection process is replicable. The resultant data set provides a micro-level view of manager-to-manager communication in these county governments, and a unique opportunity to study the relationship between a department manager's gender and the emails they send and receive.

We start by analyzing aggregate communication patterns from the numbers of emails sent and received by all department managers. In contrast to previous research, we find no strong evidence of the kinds of gender-homophilous or gender-heterophilous patterns that suggest gender bias. To unpack

this finding, we investigate whether different discussion domains exhibit different communication patterns, using the sender's department as a proxy for discussion domain. By analyzing department-to-department communication patterns, we do find evidence of gender bias, with some departments exhibiting homophily and others exhibiting heterophily. Finally, to determine whether these patterns are driven by communication content rather than other factors correlated with man-
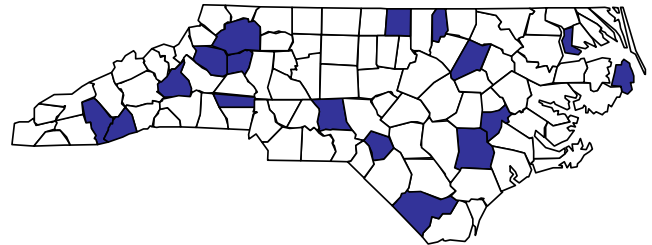

Fig. 1. The seventeen North Carolina counties used in our analysis (shaded).

Table 1. The numbers of male and female department managers for each county, along with the number of manager-to-manager emails sent.

County	Manager Gender		# Emails
	Male	Female	
Alexander	12	9	907
Caldwell	12	8	121
Chowan	12	11	2,027
Columbus	14	10	920
Dare	15	12	2,247
Duplin	13	14	1,914
Hoke	13	11	1,106
Jackson	18	6	1,499
Lenoir	15	5	560
Lincoln	15	7	573
McDowell	12	5	326
Montgomery	8	10	680
Nash	11	8	1,147
Person	12	9	1,491
Transylvania	16	4	1,857
Vance	10	8	185
Wilkes	15	2	303
Total	223	139	17,863

Table 2. Per-manager email statistics.

	Manager Gender	
	Male	Female
Average # emails sent	48.3	51
Average # recipients per email sent	1.45	1.43
Average # emails received	70.8	71.6

agers' departments, we use a recently developed latent variable model to identify topic-specific communication subnetworks for each county. We find differing degrees of gender homophily and heterophily for different topics of communication.

Data

We selected the state of North Carolina for our study because its public records laws explicitly mention email data and prevent counties from charging unreasonable fees for fulfilling requests. To construct our email data set, we issued public records requests to the one hundred North Carolina county governments. Our request to each county covered all emails sent and received by the department managers (e.g., health, finance, and elections) over a randomly selected period of three months between January and October in 2013. Twenty-three counties complied with our request, of which seventeen provided sufficient data for our analyses in an electronic format. Figure 1 indicates the seventeen counties. These counties are statistically indistinguishable from the other eighty-three counties in North Carolina along various demographic dimensions, including population, per-capita income, and percentage of the population that is white. In total, these seventeen counties produced over half a million emails, including 17,863 that were sent by a department manager to at least one other department manager in the same county (as well as other recipients, in some cases). We restricted our analyses to these manager-to-manager emails. To augment this data set, we also gathered information on the department affiliation and gender of each of the 362 managers represented in our data set. We provide some descriptive statistics for each county in table 1. Overall, almost 40% of the department managers are women, though there is significant variation across counties.

Descriptive Analysis

We begin our analysis of the relationship between a department manager's gender and the emails they send and receive, by looking for differences in the propensity for department managers to send emails to other managers of the same gender, and managers of the opposite gender. Table 2 provides some basic descriptive statistics including the average number emails sent and received by male and female department managers in our sample. On average, male and female department managers send and receive a comparable number of emails, and emails sent by male and female department managers have a similar number of recipients. Therefore, if we observe gender differences in email communication, they are unlikely to be driven by some innate difference in the propensity for male and female department managers to send or receive emails.

To test whether the gender of an email sender is related to the gender of its recipients, in aggregate, we construct a contingency table of email sending and receiving by gender (see

Table 3. Each cell records the number of times a department manager of gender X was included as a recipient of an email sent by a department manager of gender Y. Statistics provided are calculated for all counties combined. Note that each email may have more than one recipient.

		Recipient		
		Male	Female	Total
Sender	Male	9458	6120	15,578
	Female	6,330	3,833	10,163
	Total	15,788	9,953	

table 3). We then perform a χ^2 test for independence between the rows and columns. The χ^2 test statistic we obtain indicates that the gender of an email sender and its recipients is not independent ($\chi^2 = 6.4, p = 0.011$). However, inspection of the contingency table indicates that the test statistic is actually driven by mild gender heterophily in communication. Furthermore, the gender differences we observe are substantively quite small, as both male and female department managers send emails to recipients of each gender in rough proportion to their overall representation in the sample (60% to men, 40% to women).

Domain-Dependent Gendered Communication

Within large organizations that perform heterogeneous functions, it is of little value to ask whether communication is gender biased in the aggregate. Broad patterns may be dominated by personal communications or mundane professional interactions that are inconsequential to the direction of the organization or the careers of employees. Examining domain specific patterns of communication will build upon limited existing findings, which indicate that gendering patterns depend upon the domain or context of communication. For example, (author?) [5] find a higher degree of male-male homophily in communication network domains that deal with long range strategic planning. We should also expect female managers to be relatively more likely to send heterophilous ties in communication network content partitions that deal with short and medium term coordination and planning, as research has found that female managers tend to preferentially communicate through formal channels [16] and favor gender-heterophilous instrumental connections [11]. The scope and scale of our data present an unprecedented opportunity for understanding whether and how gendering patterns vary with the domain of communication.

We take a two-pronged approach to understanding how the gendering of communication varies with the domain of communication within local government organizations. Our two empirical analyses are complimentary along two dimensions – the use of within versus across-county variation and the operationalization of domain through email content vs the department affiliations of the managers.

Department Affiliation as Domain. Governments, and organizations more generally, spawn subordinate partitions in order to separate tasks according to the domain of organizational function. In the current analysis, we use the departmental affiliations of the managers in our data as proxy measures for the domain of organizational function about which managers communicate (or choose not to communicate) with each other. The use of department affiliation to measure communication domain raises a couple of distinct challenges in our strictly within-county e-mail data, which we solve by combining data across counties. First, aside from a few outlying cases, we only observe one or two managers with a given department affiliation in each county (e.g., one parks department manager). This means that we observe very little within-department communication in our data. Second, within each county, we only observe a handful of across-department dyads of a selected type (e.g., one parks/tax departments pair), which means that we cannot identify gendered patterns within counties that are specific to department pairs (i.e., domain-specific).

We solve the problems raised through using department affiliation to proxy domain by looking across counties for comparable department pairs. The department affiliations are comparable across counties, which means that for most department pairings, we observe a mix of female/female, fe-

male/male and male/female dyads. Using the department pairing to divide potential communication ties into domains, by looking across counties, we're able to observe how the intensity of communication within a given domain varies across different gender combinations. Table 5 gives the gender and department affiliation breakdown of managers in our data. In our first approach to domain-specific analysis of gendering, we construct subsets of data that are specific to department pairings, but span all of the counties in which such pairings are observed. Consider, for example, the pairing of "Human Resources" and "Emergency Services" departments (HR and EMS, respectively). There is at least one HR and one EMS manager in fifteen counties. Across all counties we observe eight male/male pairs of HR/EMS managers, twenty-two mixed gender pairs and two female/female pairs. We construct department-pairing-specific datasets such as this for all of the 300 pairings that can be constructed using the twenty-five departments in our data.

For each of the 130 department-pairing datasets in which there is at least one of each gender pairing type, we fit two Poisson models (the base model and the gendered model) to the frequency of communication between managers. Let $y_{ij} \sim \text{Pois}(\exp(\eta_{ij}))$ be the number of e-mails from i to j. In the base model

$$\eta_{ij} = \beta_0,$$

and in the gendered model

$$\eta_{ij} = \beta_1 g_i g_j + \beta_2 g_i (1-g_j) + \beta_3 (1-g_i) g_j + \beta_4 (1-g_i)(1-g_j),$$

where g_i and g_i are indicators of the genders of the senders and recipients of e-mails, respectively, with males coded 0 and females 1. Since the gendered model reduces to the base model if $\beta_1 = \beta_2 = \ldots = \beta_4$, we use a likelihood-ratio test to evaluate whether the fit of the gendered model, in which separate rates are estimated for each directed gender pairing, is significantly better than the fit of the base (i.e., constant rate) model. We deem a domain, as represented by a pairing of departments, to exhibit gendered communication patterns if the gendered model fits statistically significantly better than the base model, and we use a p value of 0.05 as the threshold for determining statistical significance.
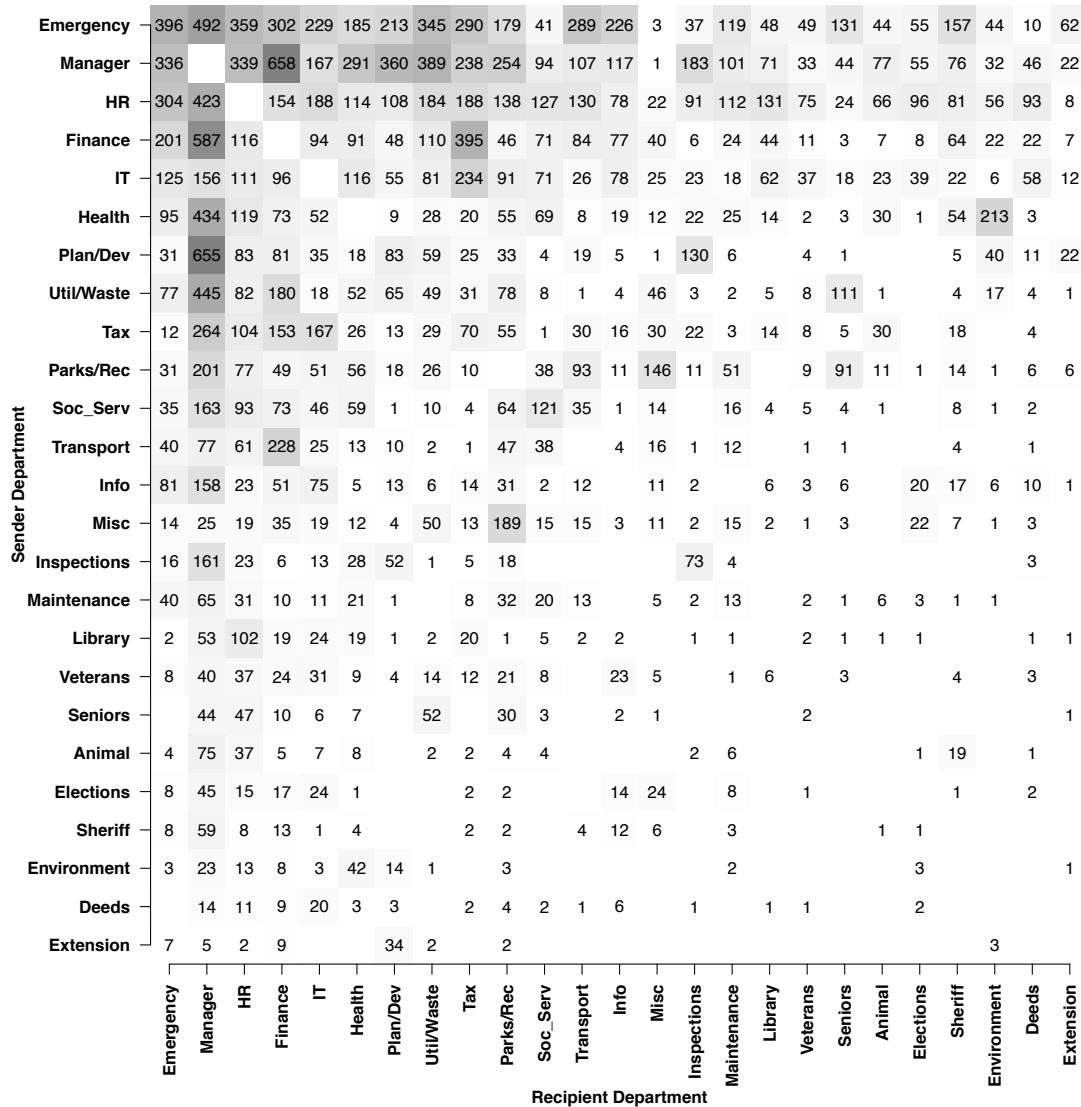
The gendered model fits better in approximately 70% (90 out of 130) of the domains. This result indicates that there is a substantial degree of within-domain gender bias. To summarize domain specific results in those domains in which we find significant gendering, we present lists of domains in which we find a consistent gendering pattern, for the six largest gendering patterns we identify. We take a gendering pattern to be a rank-ordering of the coefficients (β's) in the gendered model. The domains that exhibit the six most prevalent gendering patterns are presented in table 4. The most prevalent gendering pattern, depicted in the first column and first row of Table 4, is characterized by female-centric communication in which both females and males send communications to females at a higher rate than to males, and females send communication at a higher rate than do males. This gendering pattern is dominated by HR departments. The second most prevalent gendering pattern is also female-centric in that senders of both

Table 4. Domains in which there is significantly gendered rates of communication grouped by gendering pattern.

FF>FM>MF>MM	FF>MF>FM>MM
HR & Health	Information Technology & Health
HR & Information Technology	HR & Emergency Services
HR & County Manager	Library & County Manager
Planning & HR	Register of Deeds & Information Technology
Register of Deeds & HR	Parks and Recreation & Health
Parks and Recreation & HR	Parks and Recreation & County Manager
Finance & HR	Finance & County Manager
Finance & Parks and Recreation	Finance & Planning
Social Services & HR	Veteran Services & Information Technology
Solid Waste and Recycling & HR	Elections & Emergency Services
Tax Administrator & HR	Elections & Information Technology
Tax Administrator & Library	Elections & County Manager
Tax Administrator & Finance	Animal Control & Emergency Services
Code Enforcement & HR	Soil and Water & Planning
Animal Control & HR	
MM>FM>MF>FF	**FM>MM>MF>FF**
Planning & Information Technology	Social Services & County Manager
Solid Waste and Recycling & Health	Sheriff & Social Services
Sheriff & Health	Tax Administrator & Parks and Recreation
Tax Administrator & Planning	Tax Administrator & Veteran Services
Tax Administrator & Social Services	Animal Control & Tax Administrator
Code Enforcement & Tax Administrator	Animal Control & Code Enforcement
Animal Control & Finance	Soil and Water & HR
Soil and Water & Health	Soil and Water & Finance
Soil and Water & Solid Waste and Recycling	
FF>MM>FM>MF	**MM>MF>FM>FF**
County Manager & Health	Parks and Recreation & Planning
Planning & County Manager	Social Services & Planning
Finance & Emergency Services	Veteran Services & Register of Deeds
Finance & Health	Airport & Health
Social Services & Health	Airport & Tax Administrator
Social Services & Information Technology	County Extension & Planning
Social Services & Parks and Recreation	County Extension & Parks and Recreation

	Emergency	Manager	HR	Finance	IT	Health	Plan/Dev	Util/Waste	Tax	Parks/Rec	Soc_Serv	Transport	Info	Misc	Inspections	Maintenance	Library	Veterans	Seniors	Animal	Elections	Sheriff	Environment	Deeds	Extension
Male	29	15	3	5	11	6	17	15	11	9	8	8	2	5	13	5	3	5	2	9	2	16	9	6	8
Female	3	2	12	12	2	11	6	2	7	5	10	1	6	2	3	1	8	7	6	3	11	1	4	9	5
Total	32	17	15	17	13	17	23	17	18	14	18	9	8	7	16	6	11	12	8	12	13	17	13	15	13

Heat map (Sender Department = rows, Recipient Department = columns):

Sender \ Recipient	Emergency	Manager	HR	Finance	IT	Health	Plan/Dev	Util/Waste	Tax	Parks/Rec	Soc_Serv	Transport	Info	Misc	Inspections	Maintenance	Library	Veterans	Seniors	Animal	Elections	Sheriff	Environment	Deeds	Extension
Emergency	396	492	359	302	229	185	213	345	290	179	41	289	226	3	37	119	48	49	131	44	55	157	44	10	62
Manager	336		339	658	167	291	360	389	238	254	94	107	117	1	183	101	71	33	44	77	55	76	32	46	22
HR	304	423		154	188	114	108	184	188	138	127	130	78	22	91	112	131	75	24	66	96	81	56	93	8
Finance	201	587	116		94	91	48	110	395	46	71	84	77	40	6	24	44	11	3	7	8	64	22	22	7
IT	125	156	111	96		116	55	81	234	91	71	26	78	25	23	18	62	37	18	23	39	22	6	58	12
Health	95	434	119	73	52		9	28	20	55	69	8	19	12	22	25	14	2	3	30	1	54	213	3	
Plan/Dev	31	655	83	81	35	18		83	59	25	33	4	19	5	1	130	6	4	1			5	40	11	22
Util/Waste	77	445	82	180	18	52	65		49	31	78	8	1	4	46	3	2	5	8	111	1	4	17	4	1
Tax	12	264	104	153	167	26	13	29		70	55	1	30	16	30	22	3	14	8	5	30		18		4
Parks/Rec	31	201	77	49	51	56	18	26	10		38	93	11	146	11	51		9	91	11	1	14	1	6	6
Soc_Serv	35	163	93	73	46	59	1	10	4	64		121	35	1	14		16	4	5	4	1		8	1	2
Transport	40	77	61	228	25	13	10	2	1	47	38		4	16	1	12		1	1		4				1
Info	81	158	23	51	75	5	13	6	14	31	2	12		11	2		6	3	6		20	17	6	10	1
Misc	14	25	19	35	19	12	4	50	13	189	15	15	3		11	2	15	2	1	3		22	7	1	3
Inspections	16	161	23	6	13	28	52	1	5	18						73	4						3		
Maintenance	40	65	31	10	11	21	1		8	32	20	13		5	2		13		2	1	6	3	1	1	
Library	2	53	102	19	24	19	1	2	20	1	5	2	2		1	1		2	1	1	1		1		1
Veterans	8	40	37	24	31	9	4		14	12	21	8		23	5		1		6		3		4		3
Seniors		44	47	10	6	7		52		30	3		2	1		2		2							1
Animal	4	75	37	5	7	8		2	2	4	4				2	6					1	19			1
Elections	8	45	15	17	24	1			2	2		14	24		8		1		1			2			
Sheriff	8	59	8	13	1	4			2	2		4	12	6		3			1	1					
Environment	3	23	13	8	3	42	14	1		3						2					3				1
Deeds		14	11	9	20	3	3		2	4	2	1	6		1		1	1		2					
Extension	7	5	2	9			34	2		2												3			

Fig. 2. Heat map depicting the total number of emails sent from the managers of each department to the managers of each other department, aggregated across counties. Departments are ordered by the total number emails their managers sent.

genders communicate more frequently with females than with males. Both the departments of Elections and Emergency Services are disproportionately represented in this pattern, with Elections appearing in pairs only within this pattern of gendering and Emergency Services appearing only once outside of this pattern. The two gendering patterns in the second row that in the second column of the third row are more male centric, with both females and males exhibiting bias in favor of male recipients. Soil and Water, County Extension, Sheriff, and Social Services departments appear either exclusively or disproportionately within these patterns. Looking across gendering patterns, we see that the forms of bias exhibited in communication with managers of some departments, including Information Technology, Health, Tax Administrator and County Manager, depend upon the affiliation of the

other manager in the dyad, as these departments are relatively evenly spread across gendering patterns.

There are several limitations involved with using the department affiliations of managers to operationalize domain. First, we need to combine dyads across counties to build domain-specific datasets, which involves the questionable assumption that managers from comparably named departments, but very different counties (e.g., urban/rural, wealthy/poor, coastal/Appalachian), perform similar governing functions. Second, this approach does not make use of the textual content in the e-mails, which is likely relevant to understanding the domain of communication. Our second analytical approach addresses the limitations associated with using department affiliation to measure the domain of communication.

This result contradicts what we know about gender-driven interaction in the workplace, and is possibly a result of the vast majority of e-mails being substantively uninteresting (e.g. meeting reminders sent automatically from a manager's Microsoft Outlook account). Therefore, we need to partition e-mails according to content in order to observe substantively interesting patterns. Our data allow us to use the department of each manager as a rough proxy for the content of their email communication. We begin by looking for aggregate differences in the gender breakdown of department managers for each department, across our sample (see table 5). Departments were hand coded into one of twenty-five different categories based on the title given in the county directory, to group departments that perform a similar function. Note that not all departments are represented in each county.

We can see that some departments are mostly managed by men: the county manager (the supervisor of all other department managers), the sheriff, and the emergency manager, for example. Other departments are mostly managed by women: the HR, finance, and health departments, for example. A a χ^2 test for the independence of department and gender confirms our qualitative finding that there is a strong bias in which departments tend to be managed by women ($\chi^2 = 98.6, p < 0.001$). This result indicates a bias in the gender breakdown of department managers for each department, across our sample, but cannot tell us about differences in email communication by men and women who manage the same department. To answer this question, we need to know whether the gender of an email sender and the gender of its recipients is independent of the their respective departments.

Table 2 displays the aggregate number of times each department manager was a recipient of an email sent by a manager of each other department. We see pronounced differences in email sending an receiving by department, but cannot graphically disentangle the role of gender. Next, we construct a contingency table of department dyad-types (where each "dyad-type" is a unique combination of sender and recipient department, eg. finance $\longrightarrow$ HR) against gender dyad-types (where each "dyad-type" is a unique combination of sender and recipient gender, eg. male $\longrightarrow$ female). We then perform a χ^2 test on this contingency table, which indicates that the gender of an email sender and its recipients is not independent of their respective departments ($\chi^2 = 40,805, p < 0.001$).

This dyadic χ^2 test tells us that there is an association between gender mixing patterns and department mixing patterns. Indeed, when we construct similar contingency tables for each department, we find that email senders in utilities and waste management departments exhibit gender-homophilous behavior ($\chi^2 = 11.61, p < 0.001$), senders in the parks and recreation departments exhibit gender-heterophilous behavior ($\chi^2 = 7.06, p < 0.007$), and senders in the tax departments seem unbiased ($\chi^2 = 0.1, p = 0.75$). However, we can't say

from these results that the form of gender bias depends upon the domain of interaction since factors other than content are likely to vary with department labels, including the county in which the manager is working, the experience of the manager, and the manager's status in the organizational hierarchy. To disentangle these effects, we need explicitly model the topical content of emails. To do this, we extend a recently introduced joint model for communication topical content and network structure [14], and apply it to our email data.

A Model of Email Content

Here we provide a brief overview of our extension to the topic-partitioned multinetwork embedding (TPME) model [14]. In particular, we illustrate how this model lets us make inferences about the gender-specific patterns of communication in organizations, and how these patterns change with the topics of communication. Our model follows Krafft et al. [14] by integrating the latent space network model (LSM) [10] with latent Dirichlet allocation (LDA) [4] to jointly model the content and structure of an email network. This model is designed to be applied to email data where we observe each message sender and its recipients, as well as the email content (the words).

At a high level, our model assumes the following generative process for a message sent across the email network. First, we sample the content of the message following the generative process for LDA. Then, for a given message sender, we draw whether each other actor in the network is a recipient of that message following the LSM. However, different topics are associated with different latent spaces, so how likely each actor is to be a recipient of a particular message is dependent on the topical content of that message. We review this process in greater detail below.

The message content is assumed to be generated via LDA. Under this model, we assume that all unique words in our vocabulary are associated to varying degrees with each of T latent *topics*. Each topic is then a distribution over unique words (or *word types*), $\phi^{(t)}$. For example *doctor*, *virus*, and *medicine* might all have high probability in a topic about hospitals, while *cat* and *music* might have low probability in that topic. We further assume that each topic distribution is drawn from a Dirichlet prior:

$$\phi^{(t)} \sim \text{Dirichlet}(\beta, \boldsymbol{n}) \text{ for } t = \{1, ..., T\} \qquad [\mathbf{1}]$$

where the base measure $\boldsymbol{n}$ is the mean of the distribution, and the concentration parameter β controls how concentrated typical draws are around that mean.

To generate each of the D documents (messages) in our corpus, we first draw a document-specific distribution over topics:

$$\theta^{(d)} \sim \text{Dirichlet}(\alpha, \boldsymbol{m}) \text{ for } d = \{1, ..., D\} \qquad [\mathbf{2}]$$

Once we have drawn our document-specific distribution over topics we can then generate each of N tokens (words) in the document via a two step process. First we draw the latent topic assignment for that token from the document specific distribution over topics.

$$z_n^{(d)} \sim \theta^{(d)} \text{ for } n = \{1, ..., N\} \qquad [\mathbf{3}]$$

Then we draw the word type of that token from the topic specific distribution over word types.

$$w_n^{(d)} \sim \phi^{(z_n^{(d)})} \text{ for } n = \{1, ..., N\} \qquad [\mathbf{4}]$$

We proceed in this manner for all tokens in all documents.

In our extension of TPME, we further assume each topic is uniquely associated with one of C clusters, drawn from a discrete uniform distribution.

$$C_t \sim \text{U}(1, ..., C) \text{ for } t = \{1, ..., T\} \qquad [\mathbf{5}]$$

The intuition is that different broad content areas of communication (e.g. *planning*, *sports*, *meeting planning*) -each of which is a collection of more specific topics- will imply a different pattern of communication. Importantly, under this model, a message can be about a number of topics, and these topics can be associated with different clusters. Since each cluster is associated with a different pattern of communication, the probability that any actor is a recipient of that particular message depends on an admixture of their probabilities of being a recipient under those different communication patterns. For example, if a department manager in an organization sent an email message to schedule a budget meeting, they would likely include both staff whose job includes setting up meetings, and staff who needed to provide input on the budget as recipients.

Finally, for a given cluster c, the probability that an actor is selected as a recipient of a particular message is specified by the LSM [10]. Under this model, we assume there is some baseline propensity to include message recipients on any email, which is governed by a scalar intercept parameter.

$$b^{(c)} \sim \text{Normal}(\mu, \tau^2) \qquad [6]$$

For example, messages about sensitive HR matters will probably include fewer recipients than messages announcing a department party. Second, some attributes X, of the sender and potential recipient (which we assume are observed) may also affect the probability of that actor being a recipient. The effects that each of these L different attributes have on the probability of an actor being included as a message recipient can then be parameterized by a vector:

$$\gamma_l^{(c)} \sim \text{M. V. Normal}(\lambda, \eta^2) \text{ for } l = \{1, ..., L\} \qquad [7]$$

These covariate effect parameter vectors may vary in size depending on whether the effect is only associated with the attribute of the email sender (only requiring a single parameter), or with the combination of covariate values for the sender and recipient. For example, there is a great deal of social science literature demonstrating gender homophily in communication. Our model could generate a gender-homophilous email communication pattern by drawing positive parameters for male–male and female–female sender–recipient dyads, and negative parameters for female–male and male–female sender–recipient dyads.

The additional variation in the probability that a message is sent between two actors is governed by how close they are in a k dimensional *latent social space*. To generate these latent positions, each actor a is assumed to have some position in the k-dimensional latent space

$$\mathbf{s}_a^{(c)} \sim \text{M. V. Normal}(0, \sigma^2) \text{ for } a = \{1, ..., A\} \qquad [8]$$

and the probability that they send a message to a recipient $r \neq a$ is decreasing in their latent distance from r. Thus the probability of actor r being a recipient of a message from actor a under this model is:

$$P(y_{a,r}^{(c)} = 1) = \text{logisitic sigmoid} \left(b^{(c)} + \sum_L \left[\mathbf{X}_{a,r} \gamma_l^{(c)} \right] - |\mathbf{s}_a^{(c)} - \mathbf{s}_r^{(c)}| \right) \qquad [9]$$

Edge values for an individual message are then drawn from a Bernoulli distribution. However, the probability that $y_{a,r} = 1$ for a given message d may be dependent on multiple latent spaces (because documents can be about multiple topics). The weight given to $P(y_{a,r}^{(c)})$ for each cluster is determined by the proportion of tokens in the message that are assigned to topics associated with cluster c.

$$P(y_{a,r}^{(d)} = 1) = \sum_C P(y_{a,r}^{(c)} = 1) \times * \qquad [10]$$

where $*$ is the proportion of tokens in document d assigned to topics associated with cluster c. In this way, we condition the probability that any given actor r is a recipient of an email (document) from actor a on the content of that email, thus linking LDA and the LSM in the generative process.

Inference. Given that we do not directly observe the generative process, we have to perform inference for the posterior distribution of our model parameters given the data. We do this by *inverting* the generative process. This problem is analytically intractable, so we must approximate the posterior distribution via Markov chain Monte Carlo (MCMC) methods. We perform inference for this model via block Metropolis within Gibbs sampling[1]. A further discussion of this model is beyond the scope of this paper, but it provides a powerful and flexible framework to investigate the gender-specific patterns of communication in organizations.

However, it is important to briefly discuss the interpretation of the LSM parameters inferred using our model, as their meaning is somewhat counter-intuitive. Durring inference, the latent positions of actors capture all un-modeled factors associated with the propensity for any two actors to form a tie. In a typical social network this might include difficult or impossible to measure quantities like how nice a person is, or whether two people have *chemistry*. Additionally, it may capture observable traits that the researcher was unable to collect data on (e.g. sexual orientation, or ethnicity). This makes the latent positions difficult to interpret when including covariates in the model (because some characteristics that would otherwise be considered latent are fixed by the covariate data), so great care should be taken when doing so. In the analysis that follows, we refrain from interpreting the inferred latent positions of actors.

We apply our model separately to the email data from each county and then pool our model results. To perform inference on real data, we must first select a number of model hyper-parameters. In particular, we must select the number topics, number of clusters, and topic model hyper-parameters[2] to be used by our model, which we hold constant across counties. We choose to include manager gender as the only covariate in our specification, and include the full complment of gender mixing parameters in our model[3]. In addition, we fix the male-male mixing parameter at zero for our analysis, to aid in directly interpreting the other gender mixing parameters. We select 40 topics and 4 clusters, to provide reasonable granularity in capturing variation in the content of communication, while improving the interpretability of the latent space model results by constraining the number of possible patterns of communication. This choice has a practical advantage of ensuring that enough data will be available to fit each clusters latent space with reasonably low uncertainty in the parameter estimates.

To perform inference, we must also select a number of iterations for our MCMC sampler. In the first step of inference, we alternate between one iteration of Gibbs sampling for the LDA parameters, and 1,000 iterations of Metropolis Hastings sampling for the LSM parameters, as the Metropolis Hastings algorithm explores the parameter space much more slowly than Gibbs sampling. We did this for a total of 4,000 iterations of Gibbs sampling, until Geweke statistics indicated convergence

[1] The inference algorithm is currently implemented in a beta version as an R package, and is available here: github.com/matthewjdenny/ContentStructure

[2] We use uniform base measures **m** and **n**, and set $\alpha = 1$ and β equal to 0.01 times the length of the vocabulary for each county. This is standard practice in the literature using LDA, and provides good performance.

[3] male–male, male–female, female–male, and female–female

Table 6. Most common exclusive words in topic clusters associated with three gender mixing patterns.

MM = MF = FM = FF	MM > MF/FM > FF	FF > MF/FM > MM
message, recipient, system, state, requisition, munis, approval, confidential, error, pending, washington, program, general, days, documents, fiscal, accompanying, prohibited, user, notify, entered, delete, commodity, required, sgt, junk, deputy, summary, october, attachments, latest, emails, court, services, directory, dashboard, jail	**finance, budget, manager,** read, password, east, work, report, review, request, emergency, fyi, cell, transportation, electronic, administrator, contact, zee, worker, comp, main, ipad, debt, learn, officer, change, great, actions, call, check, center, day, inspire	**planning, board, library, mail, wrote, insurance, church, suite, third, parties, water,** class, benefits, operations, electronic, jail, fort, project, employees, pool, plan, april, full, center, cashiers, book, ext, enrollment, books, cpa, property, including, story, works
(10/64 Topic Clusters)	(11/64 Topic Clusters)	(11/64 Topic Clusters)

in the un-normalized LDA model log likelihood for all counties. We then ran the LSM component of our model for an additional 10,000,000 iterations, holding the LDA parameters fixed, to ensure that all latent space parameter estimates had converged.

Gender Mixing

Our model is informed by two types of data; the gender of the mangers and the content of e-mails. In each county we use our model to infer topics of communication and cluster topics according to their underlying patterns of manager-to-manager interaction. In each county, we find that gender mixing patterns help differentiate the cross-cluster patterns of social interactions. Take X County, for example. In this county we find a cluster in which there is strong gender homophily, its about A; a cluster that exhibits strong heterophily, its about B; and a cluster in which there is little gender bias, its about C. Unlike with the department-based assessment of mixing patterns, we can be confident that inferences drawn from our model are driven by e-mail content.

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