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ECEN 326-501

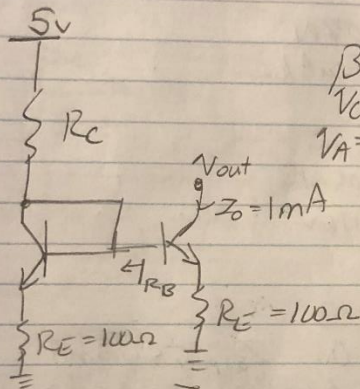
### **Lab 6: Design of Current Mirrors**

#### **Procedure:**

In this lab we constructed several current mirrors with varying designs. Each of these current mirrors have unique properties and to determine them we ran multiple calculations on each.

#### **Calculations:**

# Lab #6



$$\beta = 140$$

$$V_{CE} = 0.2$$

$$V_A = 75V$$

$$\frac{KVL}{-5 + R_C I_O + 0.7 + \frac{R_E (1 + \beta) I_O}{\beta} = 0$$

$$R_C = 4.199 k\Omega$$

$$V_{O, min} = V_{CE, sat} + I_O R_{E2} = 0.3V$$

$$R_O = g_{m2}' r_{O2} R_E' + r_{O2} + R_E'$$

$$g_{m2}' = g_{m2} \frac{r_{\pi 2}}{r_{\pi 2} + R_B}, R_E' = R_{E2} \parallel (r_{\pi 2} + R_B)$$

$$R_B = R_C \parallel (r_{e1} + R_{E1})$$

$$\therefore R_B = 121.21 \Omega, g_{m2}' = 0.03866$$

$$R_E' = 97.31, R_O = 357.247 k\Omega$$

$$g_{m2} = \frac{I_O}{V_T} = 0.04$$

$$r_{\pi 2} = \frac{\beta}{g_{m2}} = 3500$$

$$r_{e1} = \frac{25m}{I_{E1}} = 24.82$$

$$r_{O2} = \frac{V_A}{I_O} = 75000 \Omega$$

$$R_C = 3500 \Omega, V_{O, min} = 0.3$$

$$R_O = g_{m2}' r_{O2} R_E' + r_{O2} + R_E'$$

$$g_{m2}' = g_{m2} \frac{r_{\pi 2}}{r_{\pi 2} + R_B}, R_E' = R_{E2} \parallel (r_{\pi 2} + R_B)$$

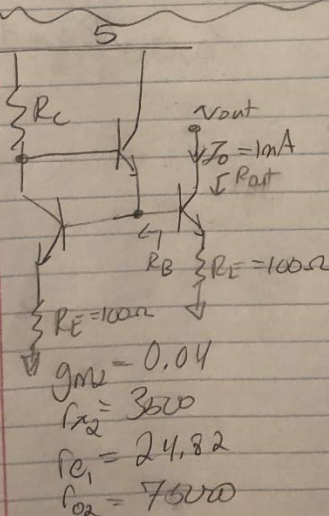
$$R_B = \left( \frac{R_C}{\beta + 1} + \frac{(\beta + 1) r_{e1}}{N} \right) \parallel \left[ \frac{r_{e1} + R_{E1}}{\beta} \left( 1 + \frac{(\beta + 1) R_{E1}}{N R_C} \right) \right]$$

$$\text{Where } N = 2$$

$$1774.03 \parallel 62.84 \parallel 17599.2 (\beta + 1)(r_{e1} + R_{E1})$$

$$\therefore R_B = 60.48 \Omega, R_E' = 97.268 \Omega$$

$$g_{m2}' = 0.039, R_O = 361.944 k\Omega$$



$$g_{m2} = 0.04$$

$$r_{\pi 2} = 3500$$

$$r_{e1} = 24.82$$

$$r_{O2} = 75000$$

## Lab #6

NPN Current mirror w/  $\beta$  helper

$$I_0 = 2 \text{ mA}$$

$$R_{E1} = 100 \Omega \quad R_{E2} = 50 \Omega, Q_2 = 2 \times Q_1 \therefore N = 3$$

$$R_C = 3500 \Omega \quad V_{0, \min} = 0.3 \text{ V}$$

$$R_0 = g_{m2} r_{o2} R_{E2}' + r_{o2} + R_{E2}'$$

$$g_{m2}' = g_{m2} \frac{r_{o2}}{r_{o2} + R_B}, R_{E2}' = R_{E2} \parallel (r_{o2} + R_B)$$

$$R_B = \left( \frac{R_C}{\beta + 1} + \frac{(3+1)r_{o1}}{N} \right) \parallel \left[ \frac{r_{E1} + R_{E1}}{\beta} \left( 1 + \frac{(\beta + 1)^2 r_{o1}}{N R_C} \right) \right] \parallel (\beta + 1)(r_{o1} + R_{E1})$$

$$g_{m2} = 0.08 \quad | R_B = 608 \parallel 19.669 \parallel 15849.81 = 19.03 \Omega$$

$$r_{o2} = 1750 \quad g_{m2}' = 0.079 \quad R_{E2}' = 48.625 \Omega \quad R_0 = 181.602 \text{ k}\Omega$$

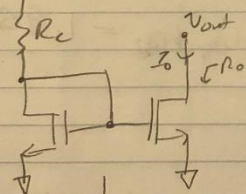
$$r_{E1} = 12.41$$

$$r_{o2} = 37520$$

NMOS simple Current Mirror  $K_n' = 70 \mu\text{A/V}^2 \quad V_{tn} = 1.4$

$$W = 170 \mu\text{m} \quad L = 10 \mu\text{m} \quad \lambda_n = 0.016 \text{ V}^{-1}$$

$$I_0 = 100 \mu\text{A}$$



$$I_{D1} = \frac{5 - V_{GS1}}{R_C} = \frac{K_n' \left( \frac{W}{L} \right)_1 (V_{GS1} - V_{tn})^2}{2}$$

$$I_0 = I_{D1} \quad V_{0, \min} = 0.4 \text{ V} = V_{ov}$$

$$R_C = 31.9 \text{ k}\Omega \quad V_{GS1} = 1.809 \text{ V} \quad R_0 = r_{o2}$$

$$r_{o1} = \frac{1}{\lambda I_0}$$

$$r_{o2} = \frac{1}{\lambda I_0} = 625 \text{ k}\Omega$$

NMOS Simp Current Mirror

$$K_n' = 70 \mu\text{A/V}^2 \quad V_{tn} = 1.4$$

$$I_0 = 200 \mu\text{A}$$

$$V_{GS1} = 1.809$$

$$\left( \frac{W}{L} \right)_1 = 17 \quad \left( \frac{W}{L} \right)_2 = 34$$

$$I_{D1} = 100 \mu\text{A}$$

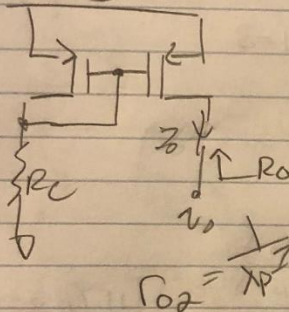
$$V_{0, \min} = 0.409$$

$$r_{o2} = \frac{1}{\lambda I_0} = 312.5 \text{ k}\Omega = R_0$$



## Lab #6

### PMOS Simp Current Mirror



$$K'_p = 15 \mu\text{A/V}^2 \quad V_{tp} = -1.65\text{V} \quad \lambda_p = 0.01\text{V}^{-1}$$

$$\left(\frac{W}{L}\right)_{1,2} = 36$$

$$I_0 = 100 \mu\text{A}$$

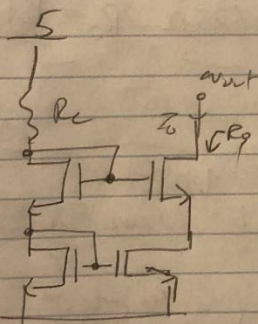
$$I_{D1} = \frac{V_{DD} - V_{SG1}}{R_C} = \frac{K'_p}{2} \left(\frac{W}{L}\right)_1 (V_{SG1} - |V_{tp}|)^2$$

$$I_0 = I_{D1} \quad V_{SG1} = 2.2586\text{V}$$

$$R_C = 27.414 \text{ k}\Omega \quad V_{o, \text{max}} = 4.39\text{V}$$

$$r_{o2} = \frac{1}{\lambda_p I_0} = 1 \text{ M}\Omega$$

### NMOS Cascode Current Mirror



$$K'_n = 70 \mu\text{A/V}^2 \quad V_{tn} = 1.9\text{V} \quad \lambda_n = 0.016\text{V}^{-1}$$

$$\left(\frac{W}{L}\right)_{1,11} = 17$$

$$I_0 = 100 \mu\text{A}$$

$$I_{D1} = \frac{2V_{DD} - 2V_{GS1}}{R_C} = \frac{K'_n}{2} \left(\frac{W}{L}\right)_1 (V_{GS1} - V_{tn})^2$$

$$I_0 = I_{D1} \quad V_{GS1} = 1.809\text{V} \quad R_C = 63.8 \text{ k}\Omega$$

$$V_{o, \text{min}} = -2.782\text{V}$$

$$R_o = g_{m4} r_{o4} r_{o2} + r_{o4} + r_{o2} = 1.96 \text{ M}\Omega$$

$$g_{m4} = \frac{2I_0}{V_{ov}} = 4.89 \times 10^{-4} \text{ S}$$

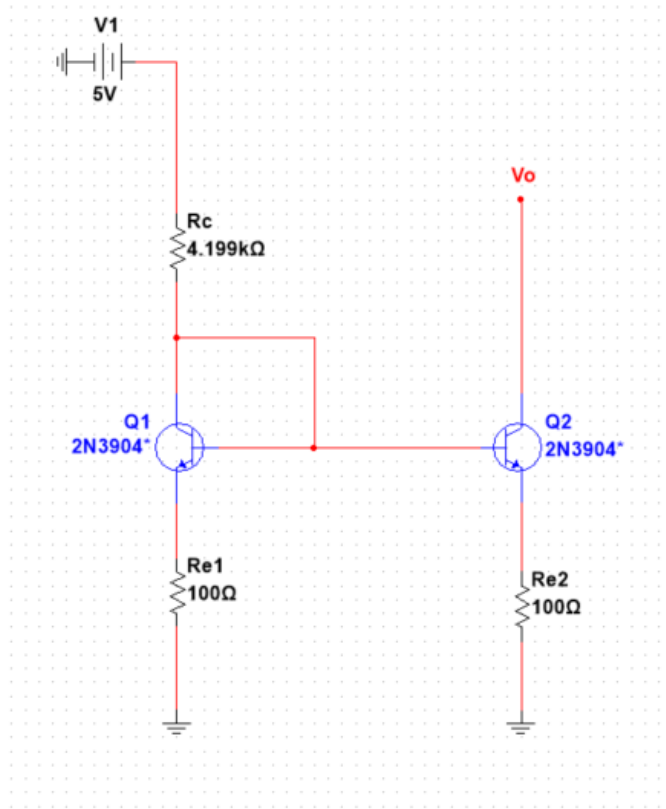
$$r_{o4} = \frac{1}{\lambda_n I_0} = 625 \text{ k}\Omega$$

$$r_{o2} = \leftarrow$$

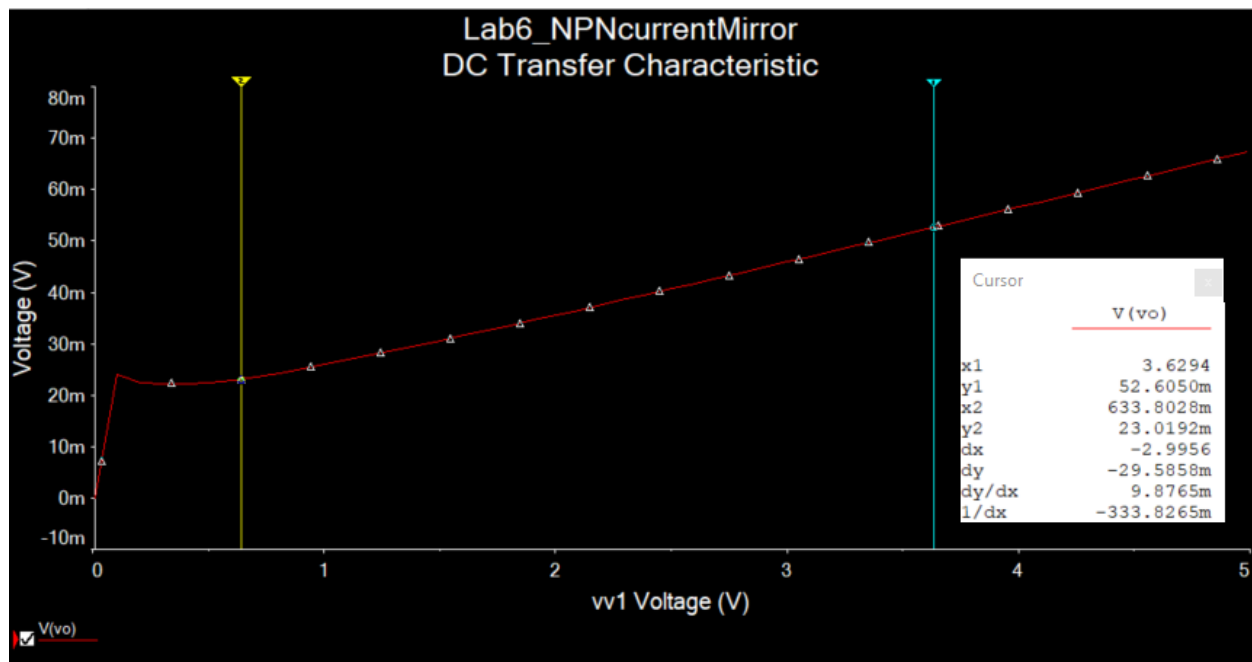
**Data:**

Simple NPN Current Mirror

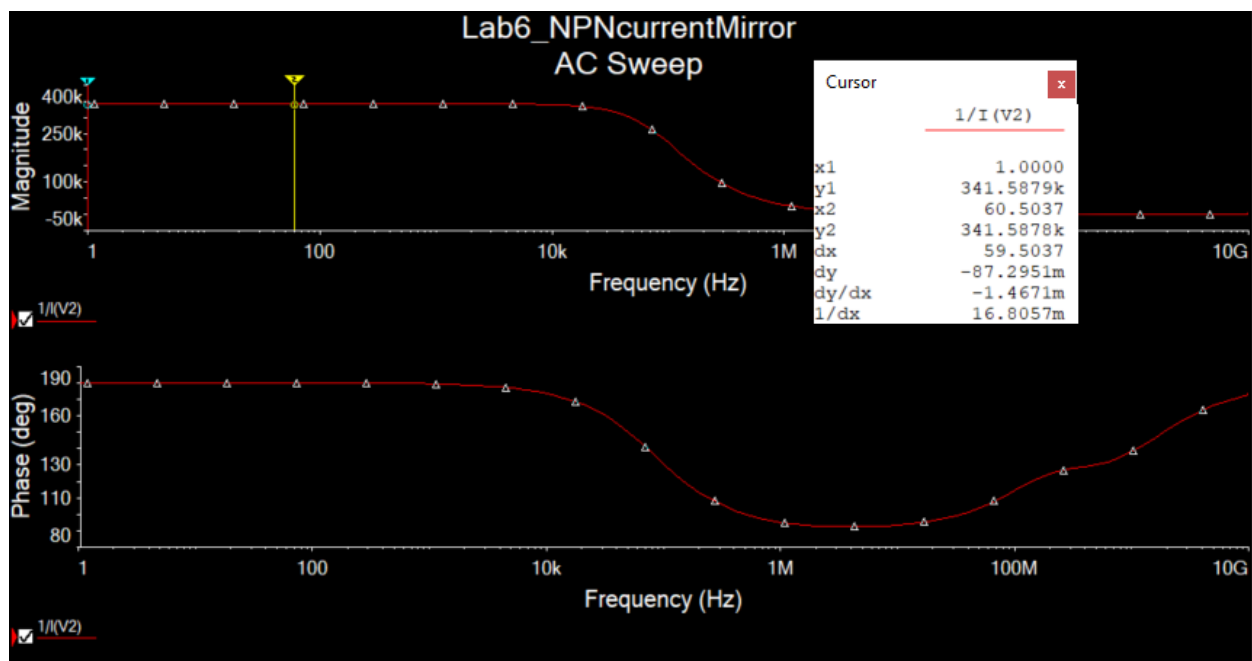
Circuit:



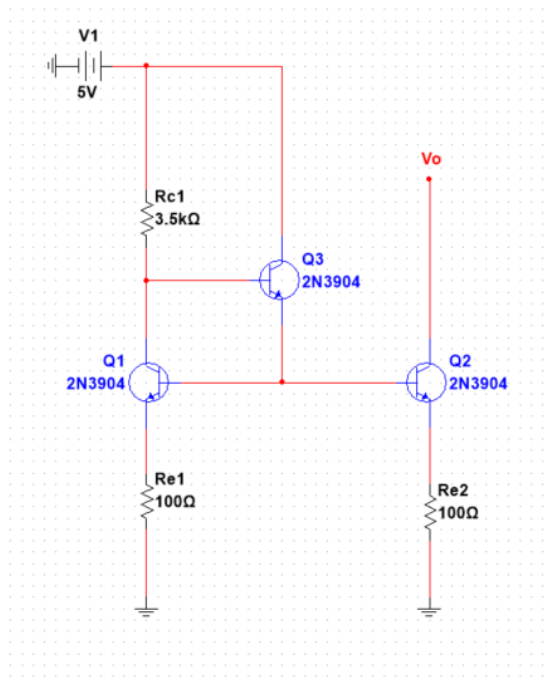
DcSweep:



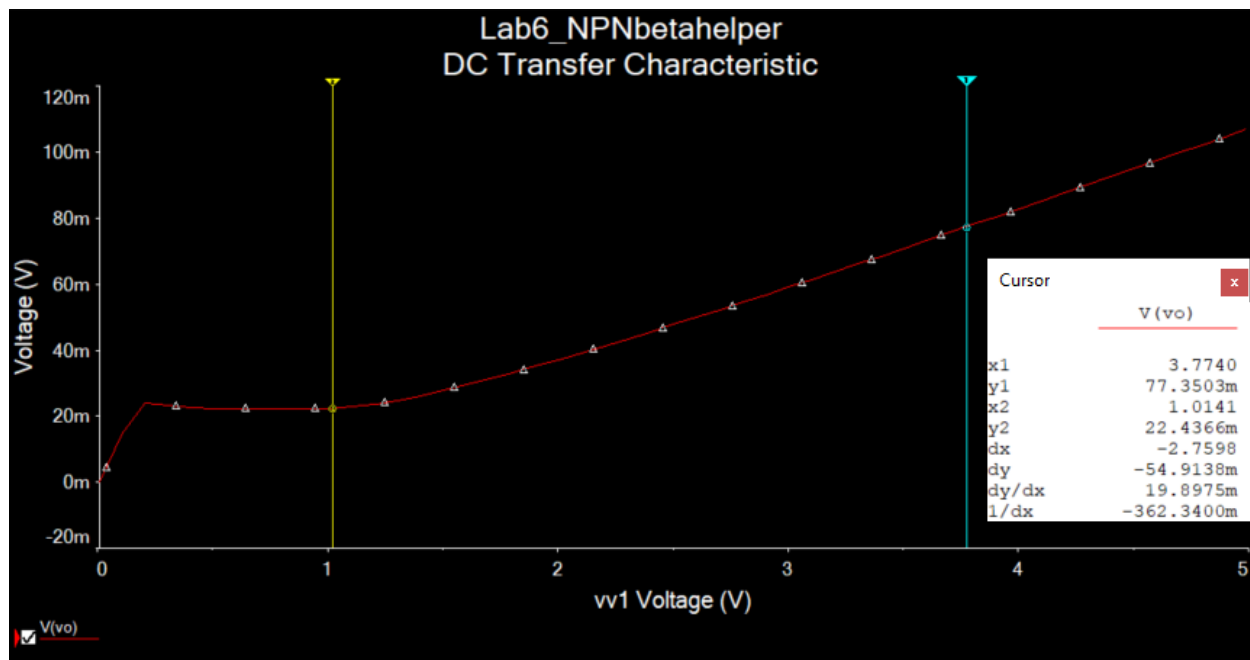
Rout:



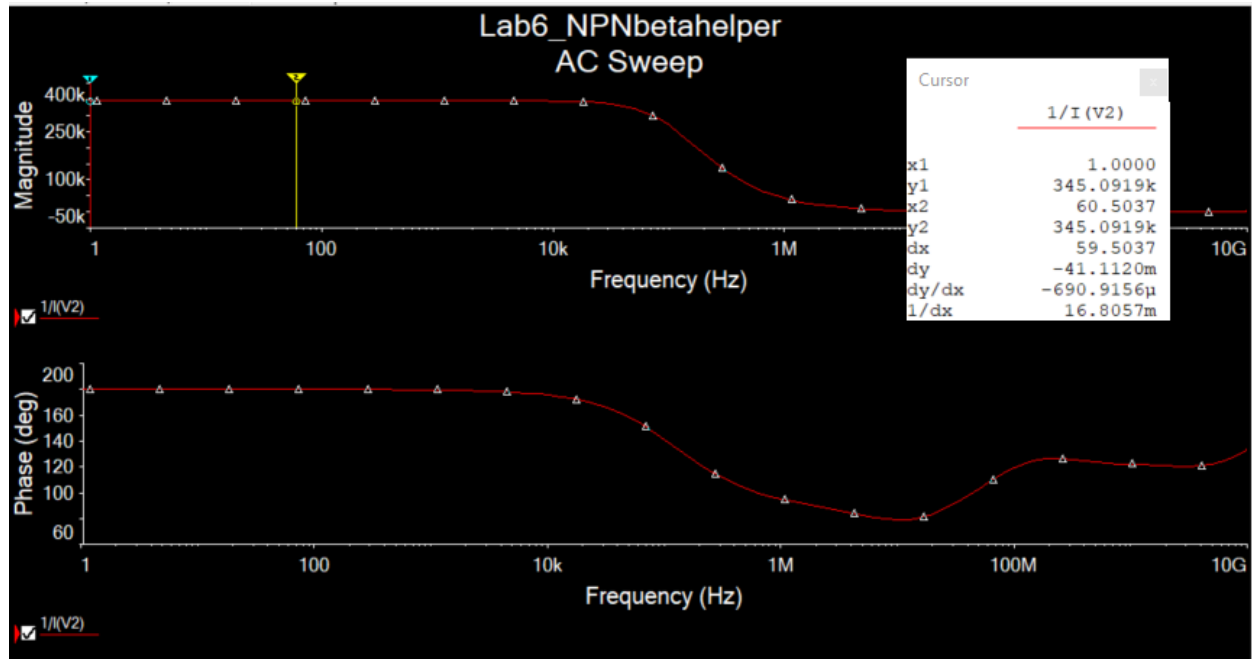
NPN Beta Helper:



DcSweep:

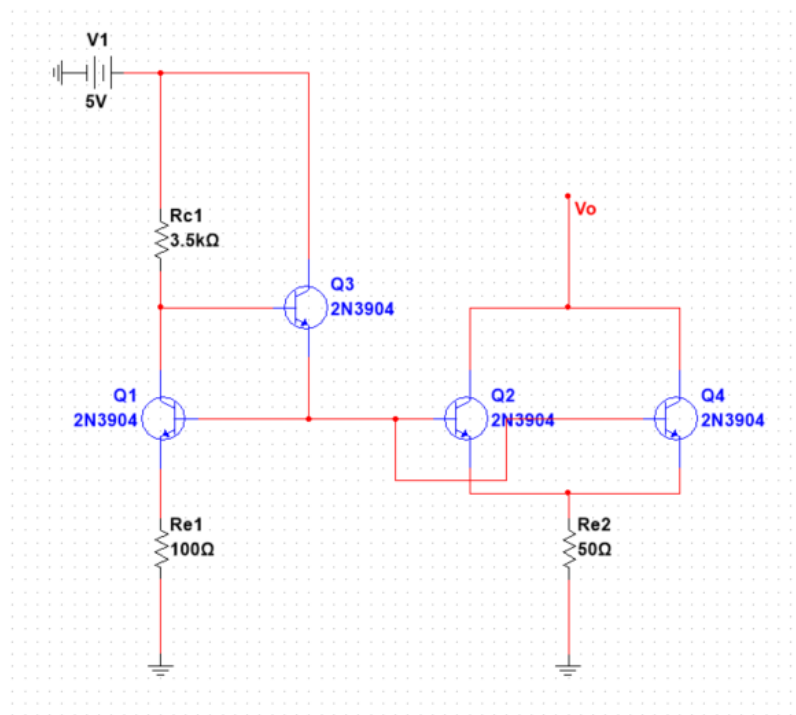


Ro:



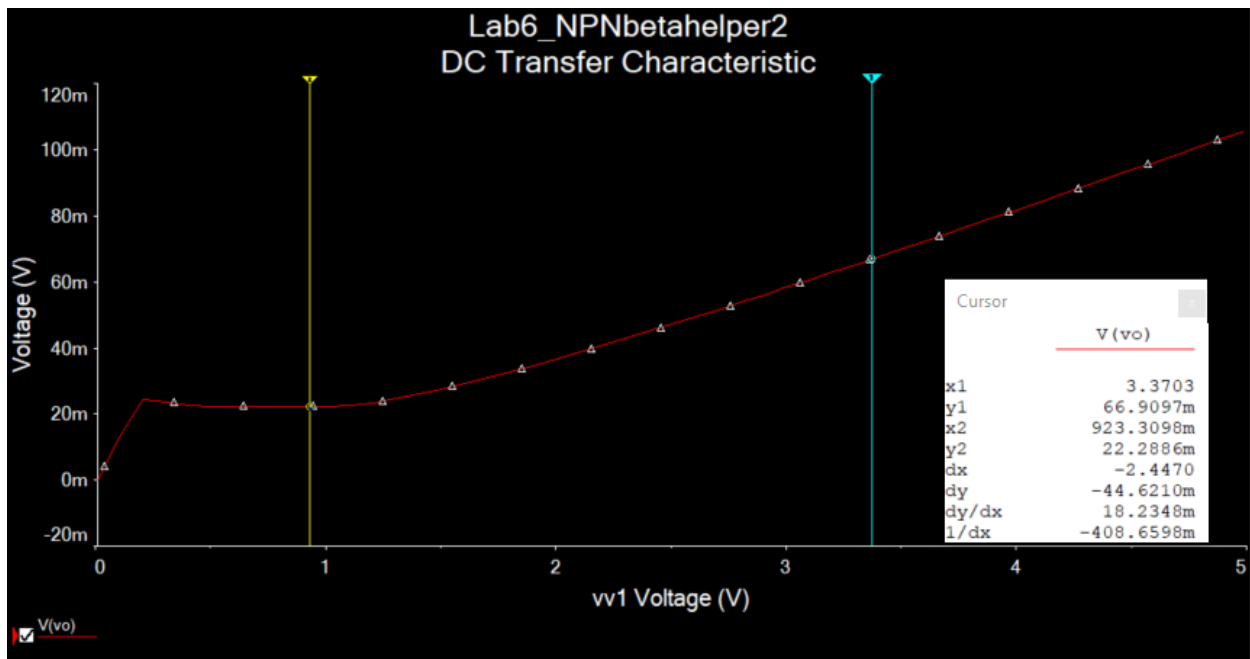
NPN Beta Helper with second stage

Circuit:

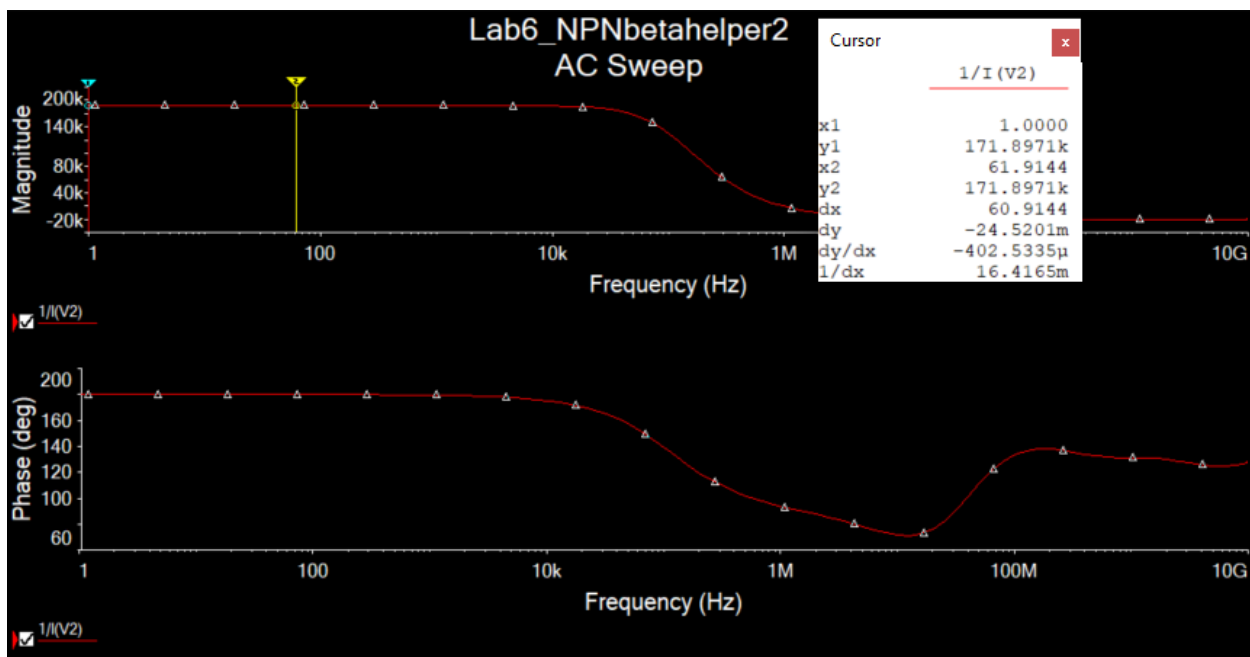


DcSweep:



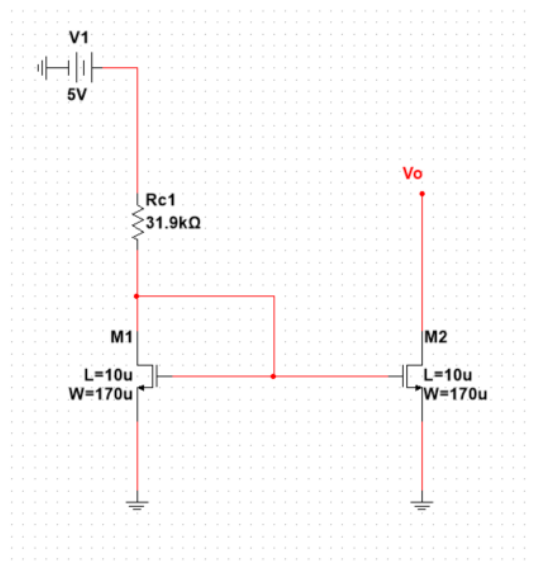


Ro:

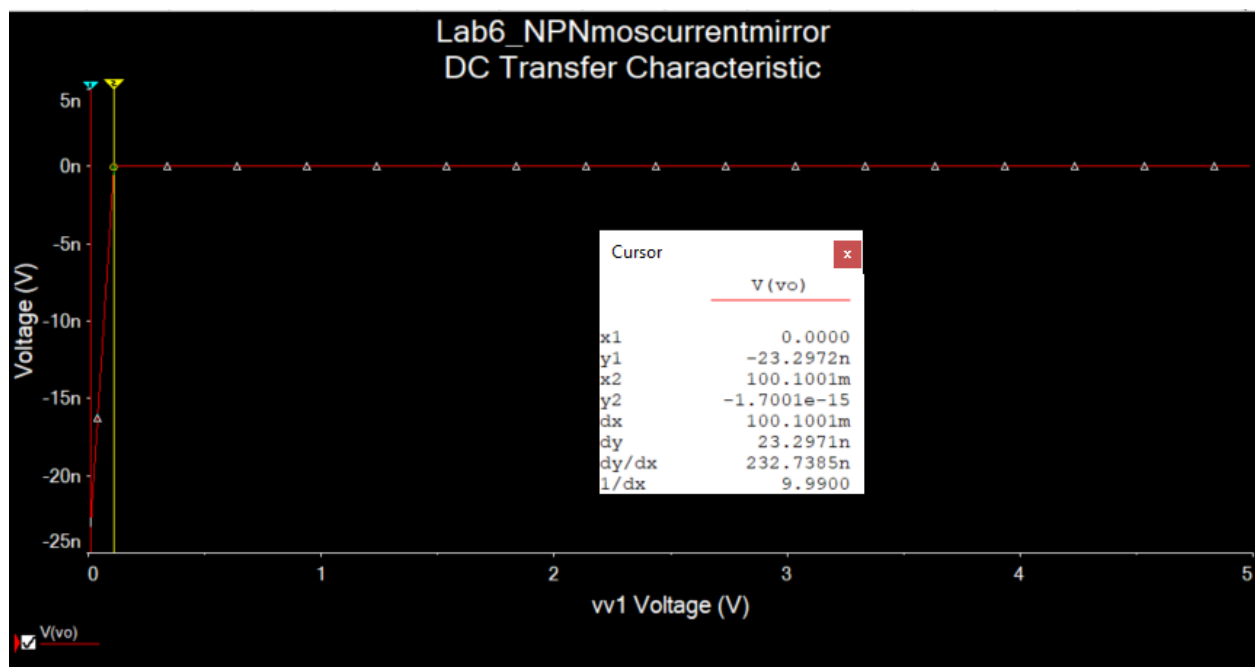


NMOS Simple Current Mirror:

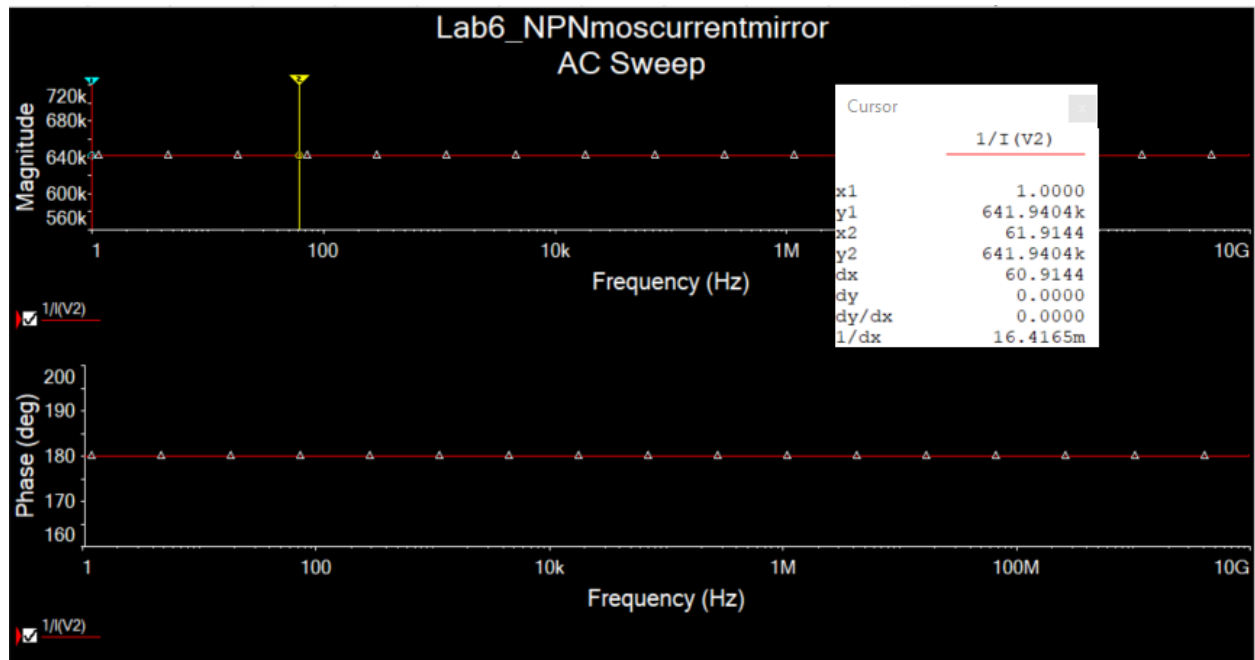
Circuit:



DcSweep:

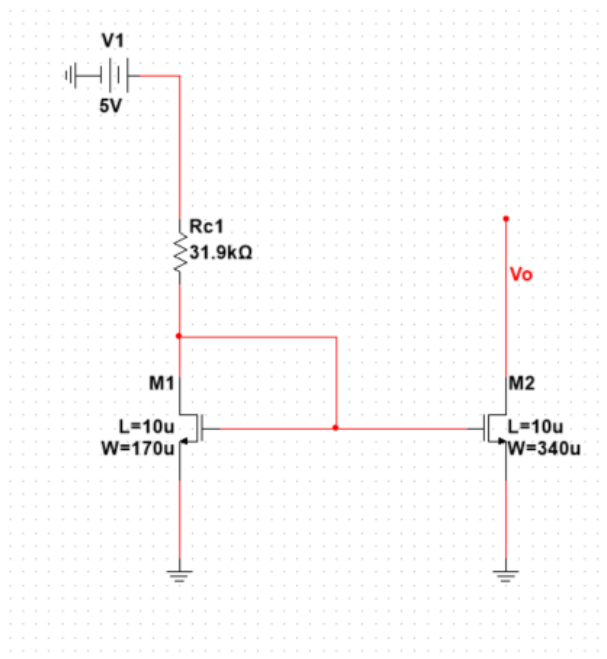


Ro:

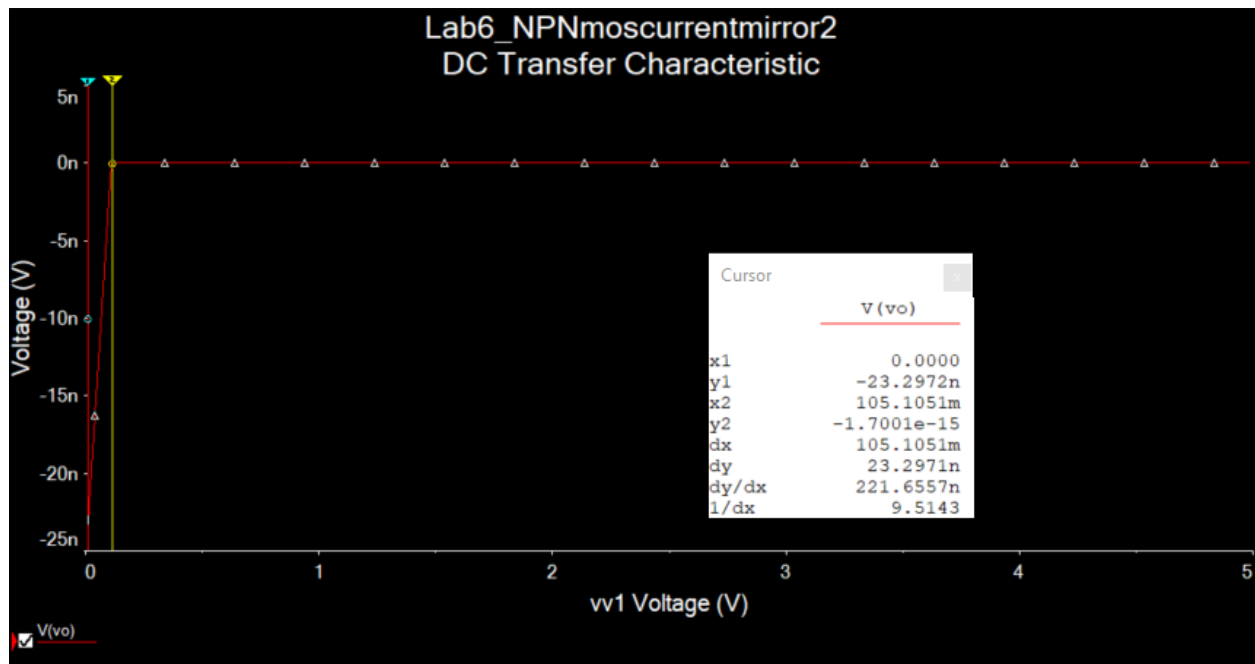


NPN MOS Simple Current Mirror:

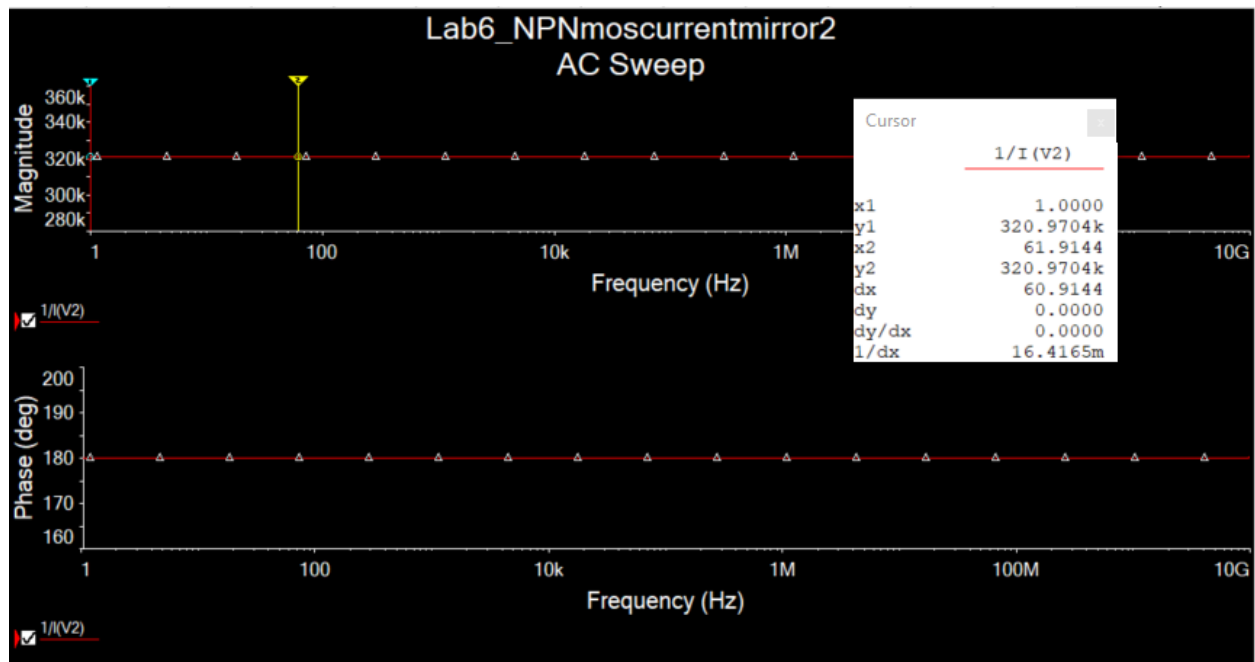
Circuit:



DcSweep:

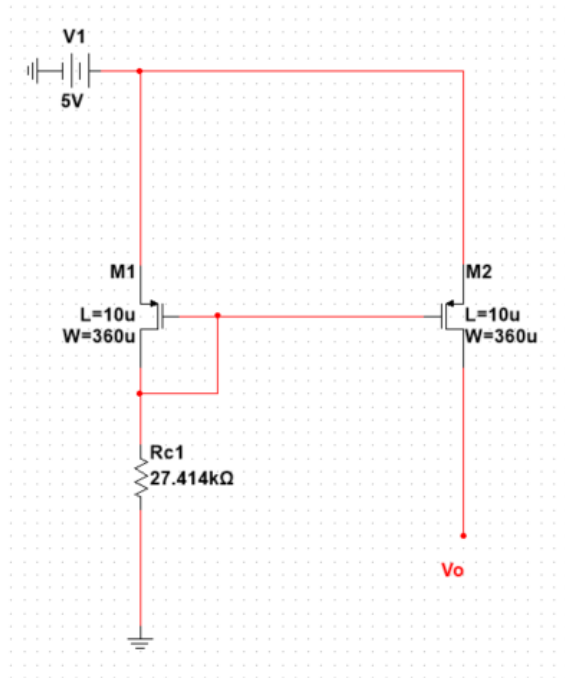


Ro:

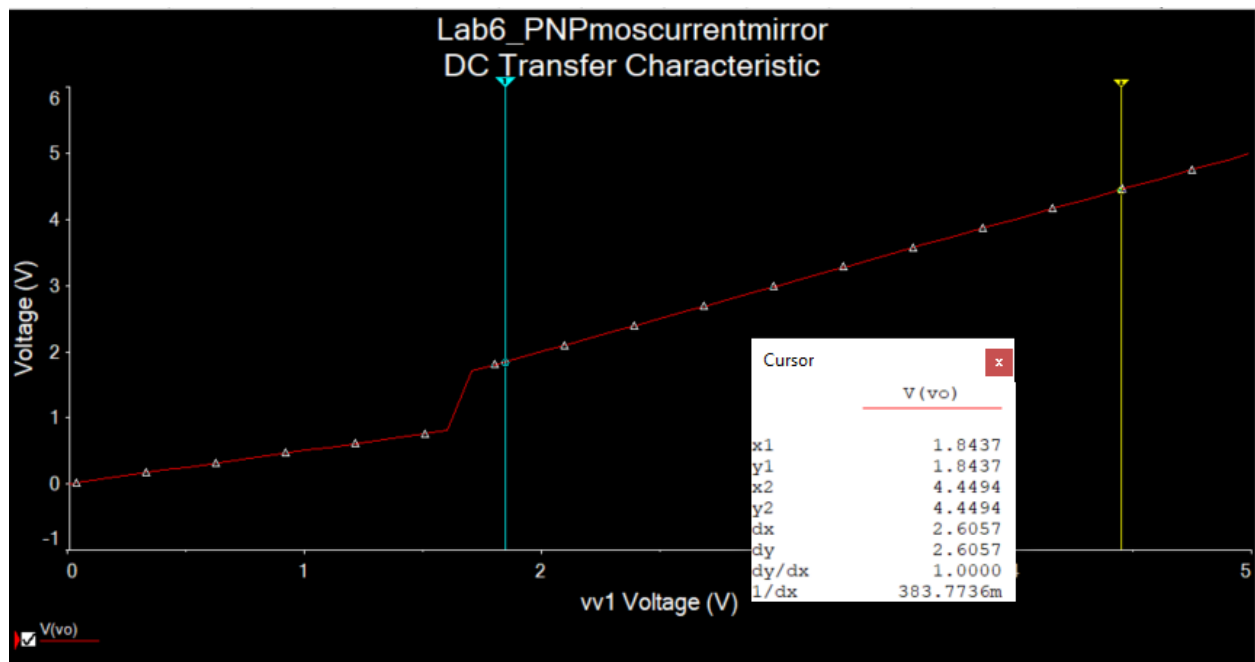


PNP MOS Current Mirror:

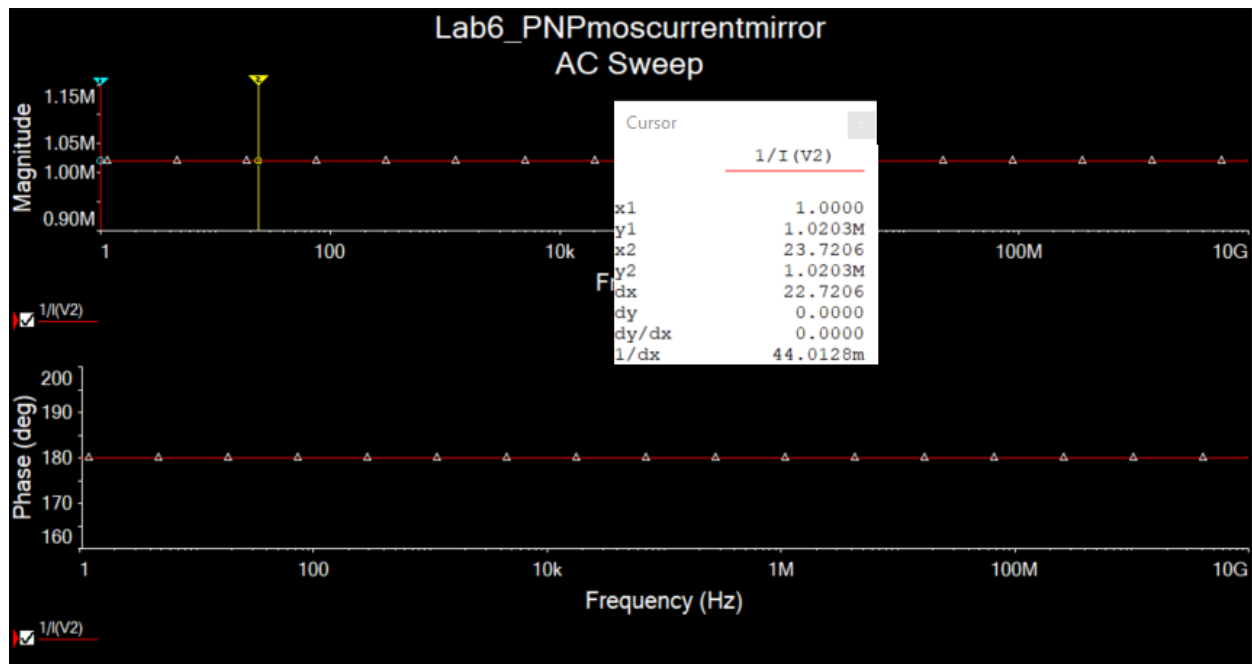




DcSweep:

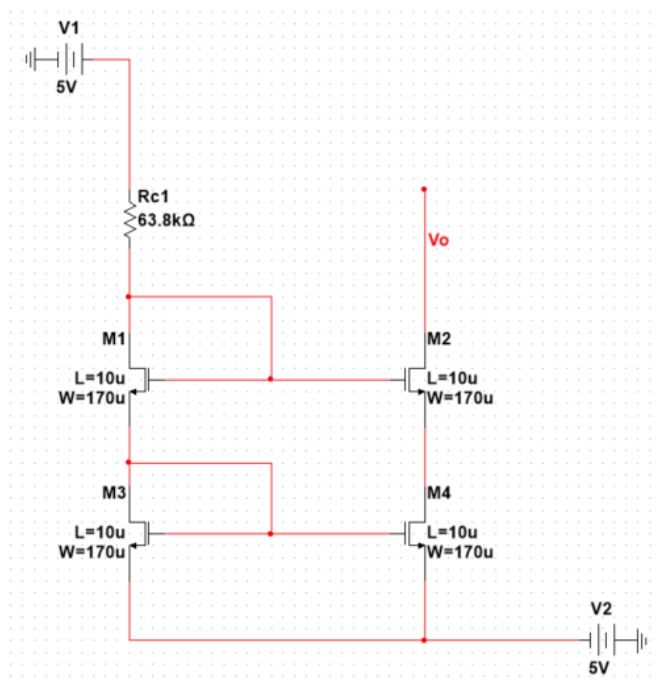


Ro:

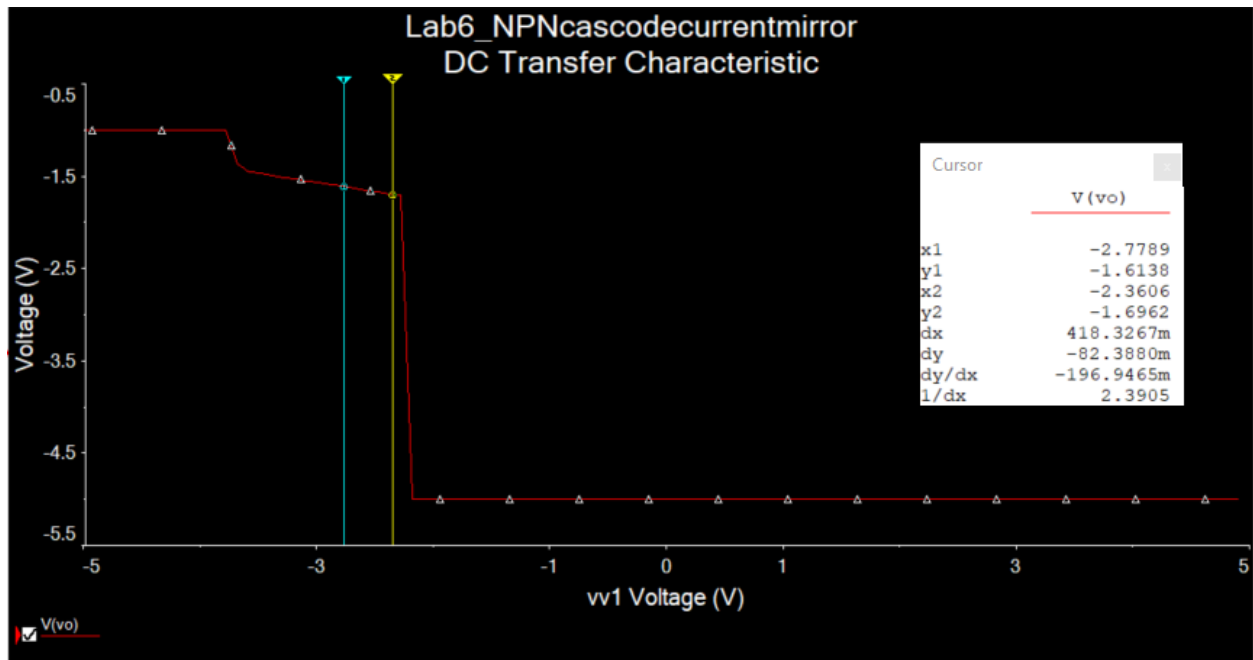


## NMOS Cascode Current Mirror

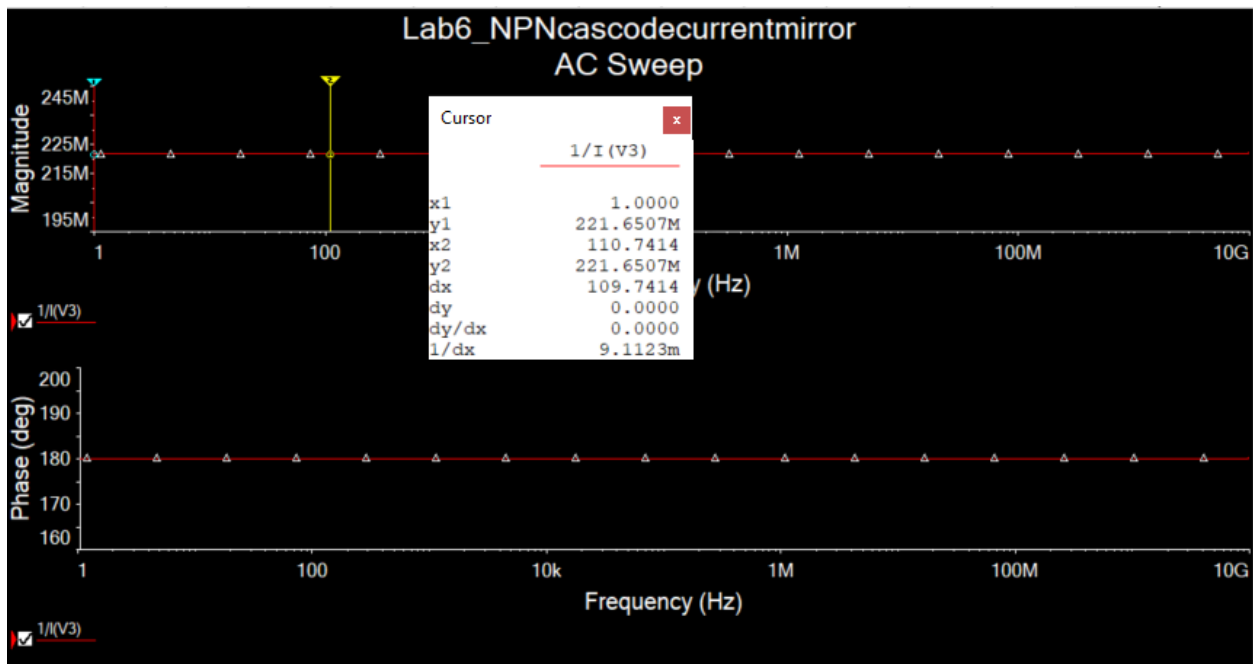
Circuit:



DcSweep:



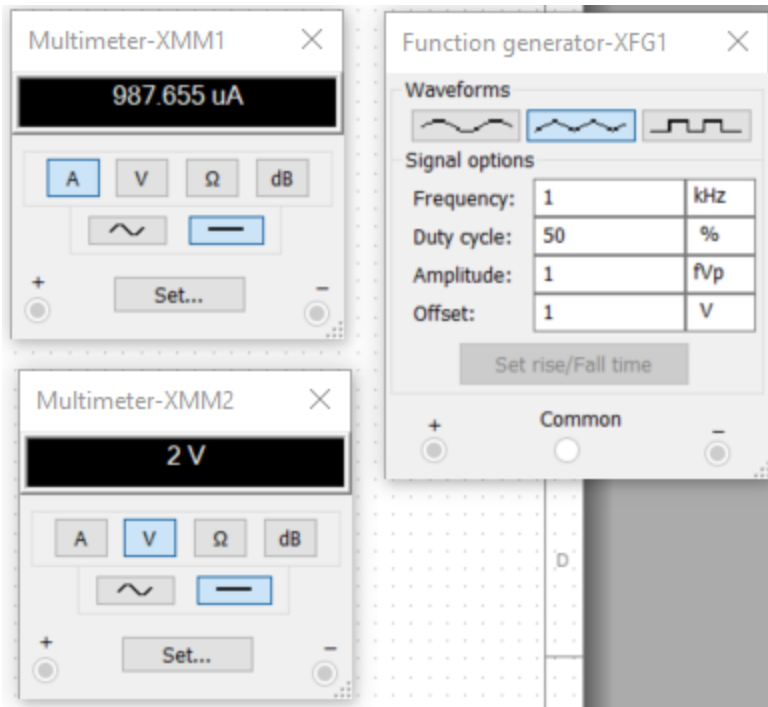
Ro:



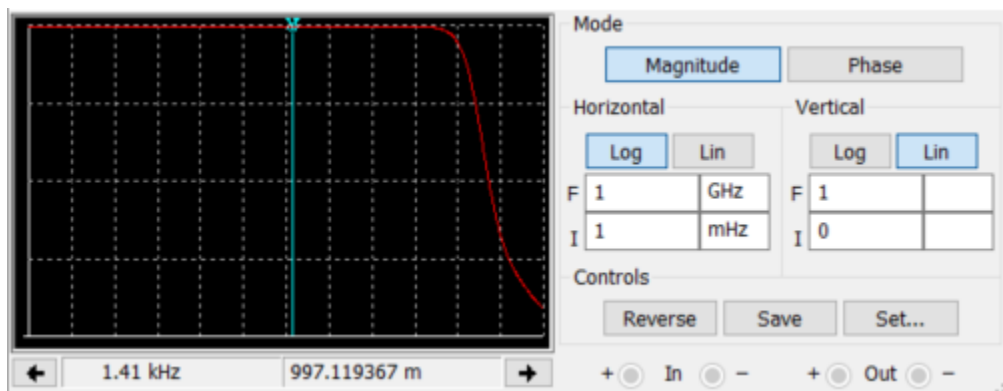
Measurements:

NPN Simple Current Mirror:

Io:



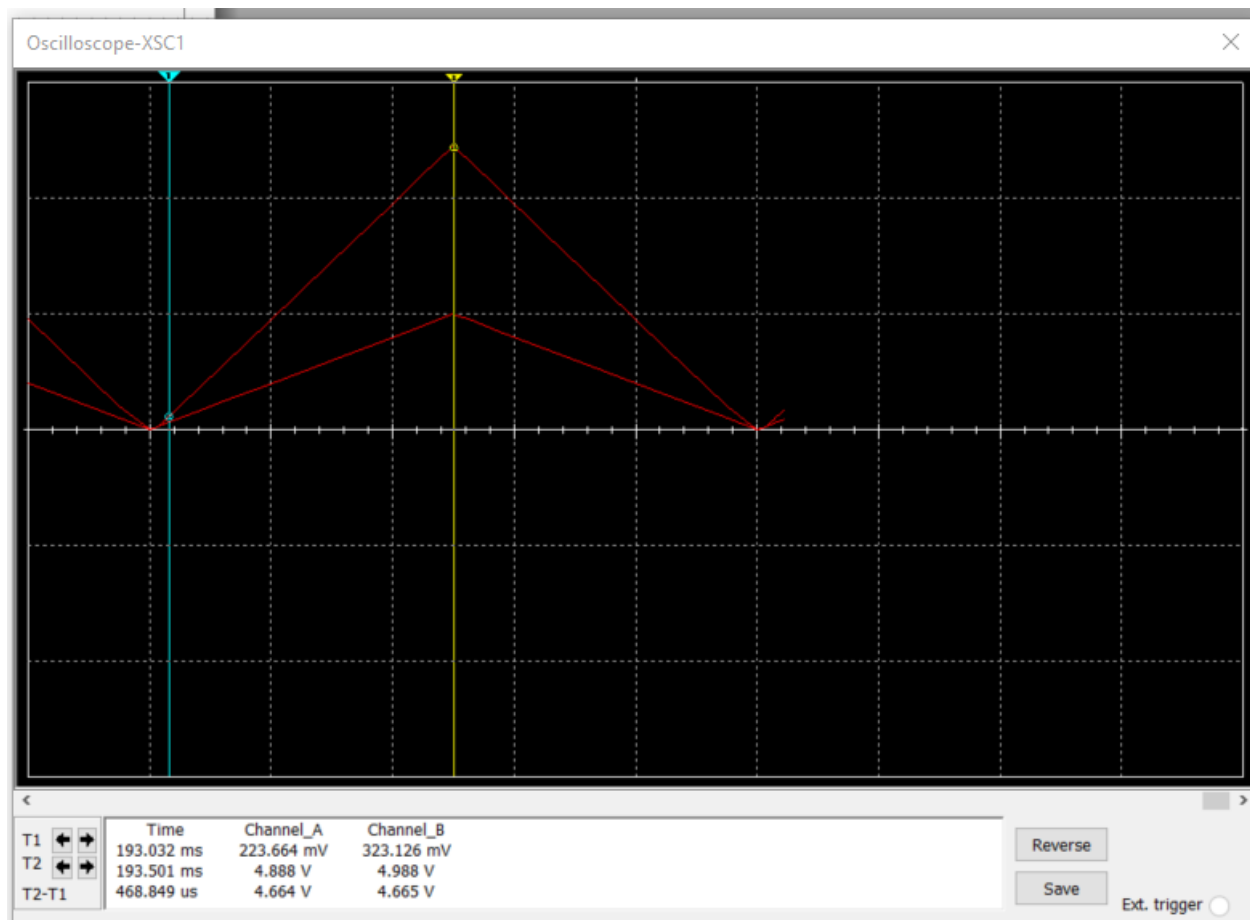
Ro:



$\Rightarrow 332.3 \text{ k}\Omega$

Operation Range

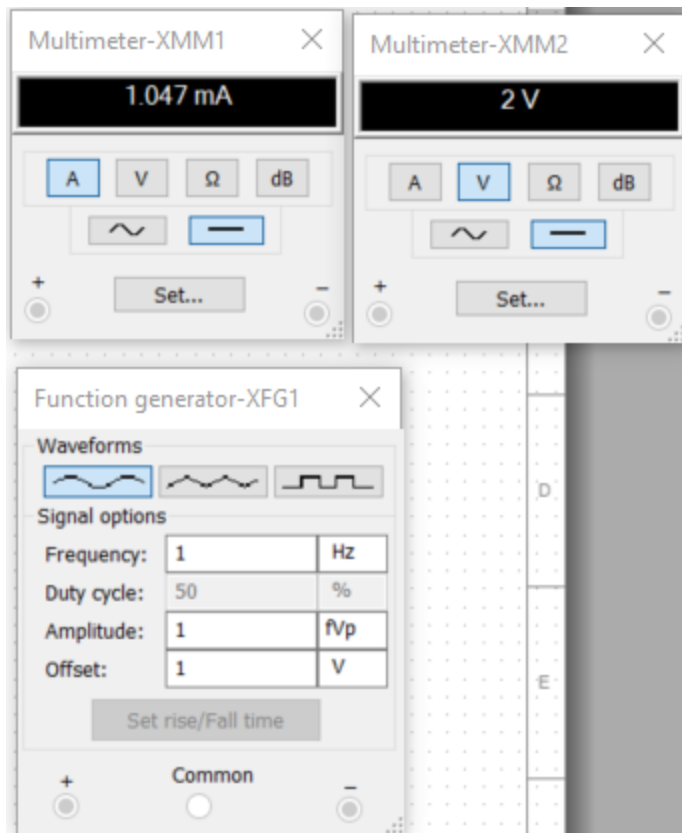




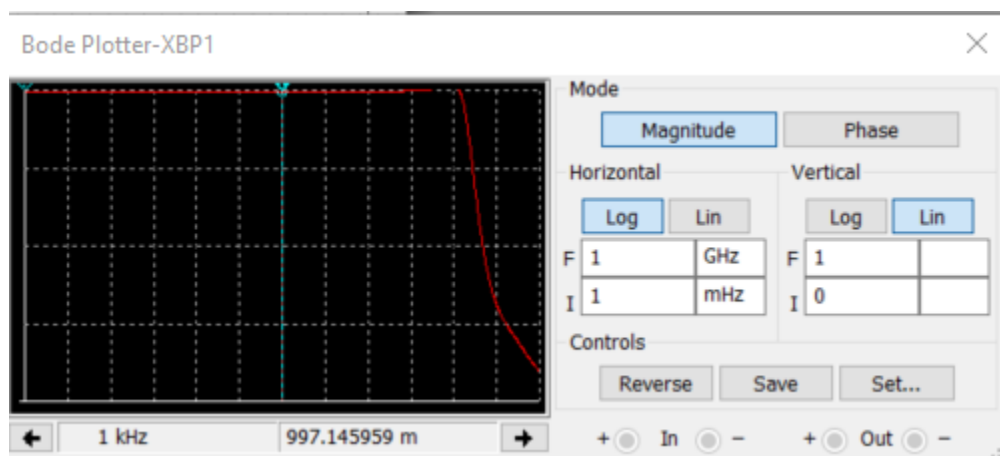
0.323v – 5v

NPN Beta helper single stage

I<sub>out</sub>:

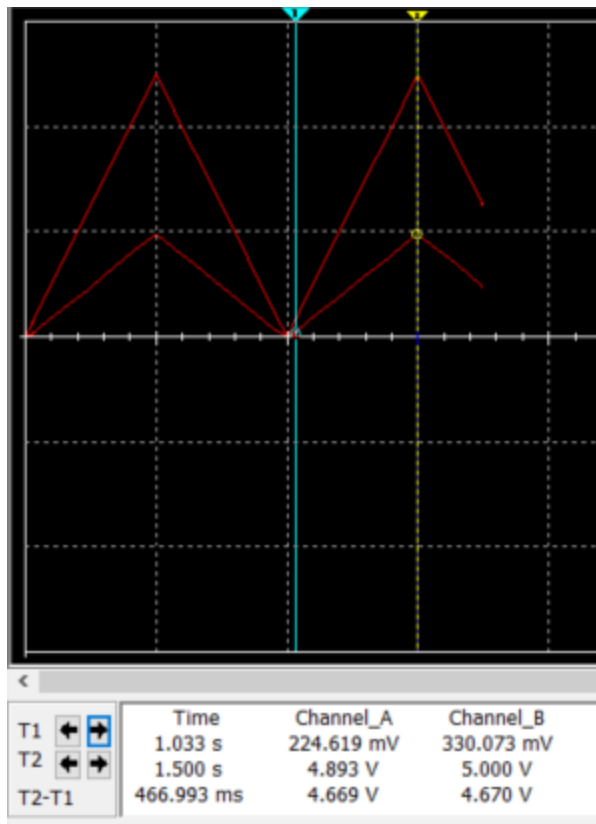


Ro:



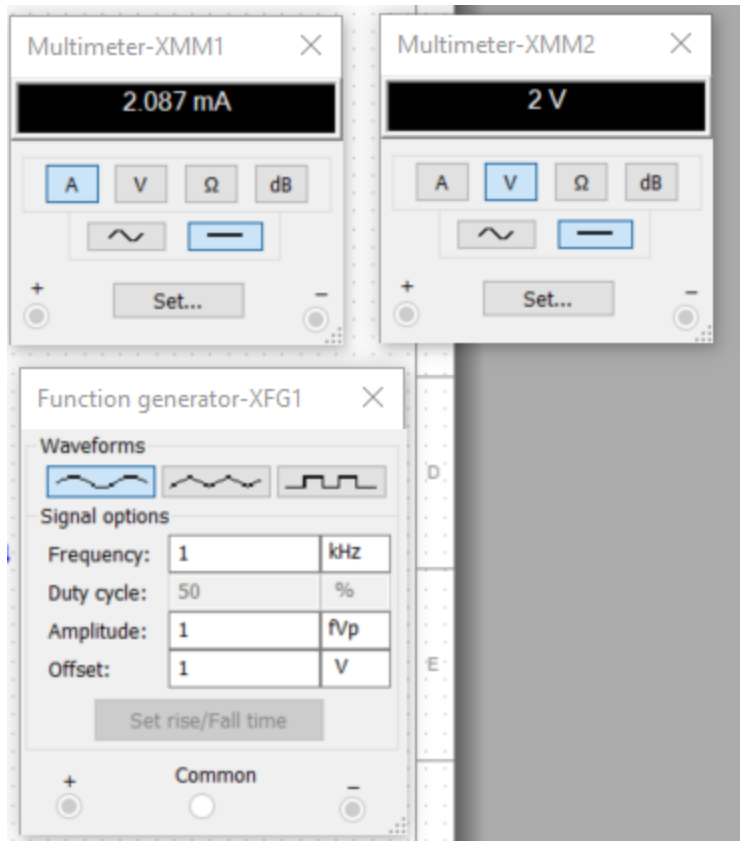
$\Rightarrow 332.3 \text{ k}\Omega$

Operation Range:

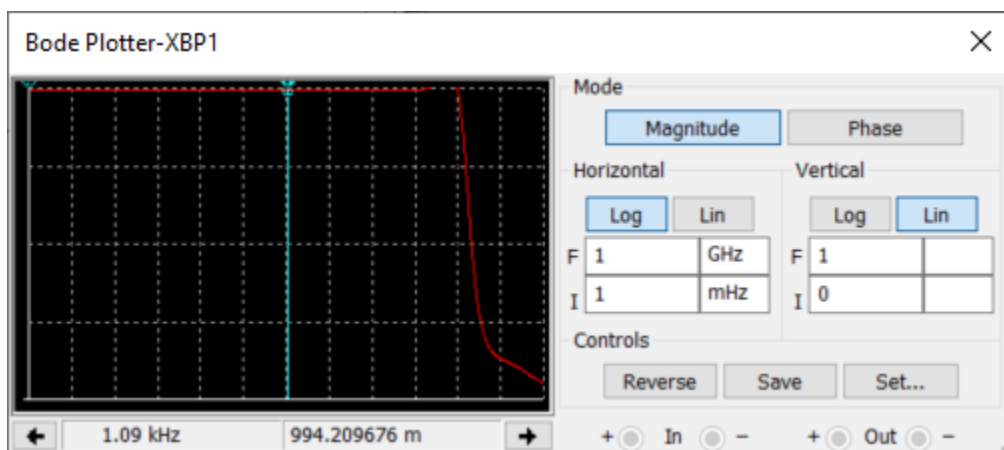


0.330v – 5v

NPN Beta Helper three stage  
Iout:



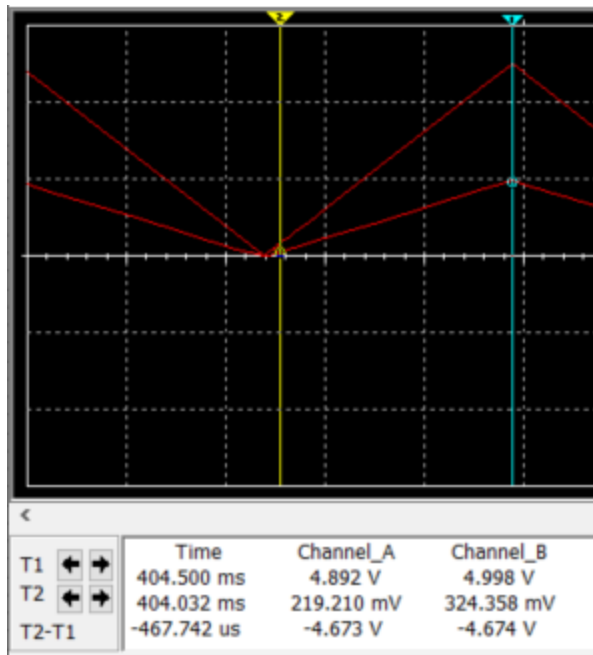
Rout:



=165.66kohm

Operation Range

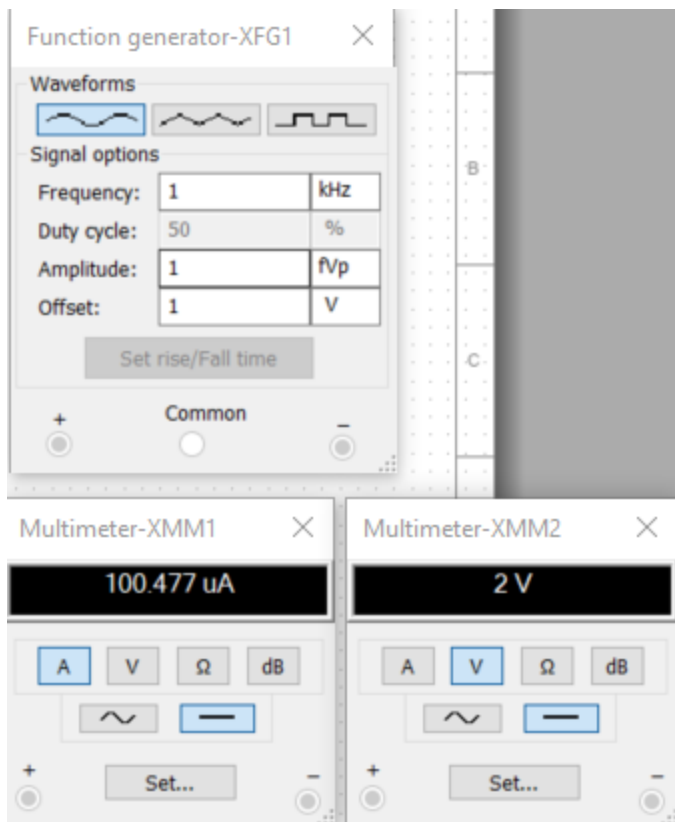




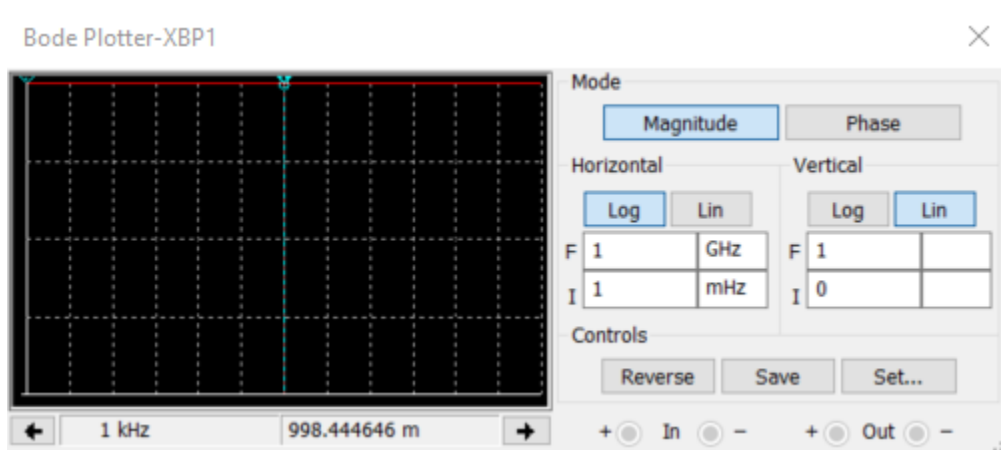
0.324v – 5v

NPN MOS Simple Current Mirror

I<sub>out</sub>:

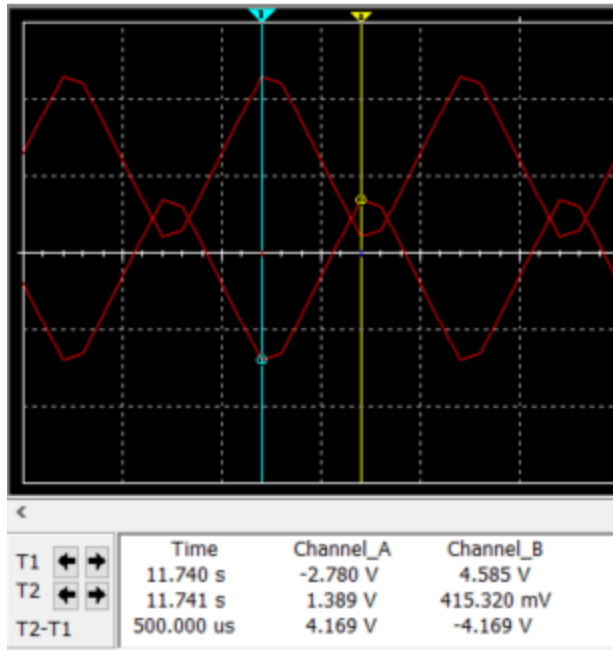


Rout:



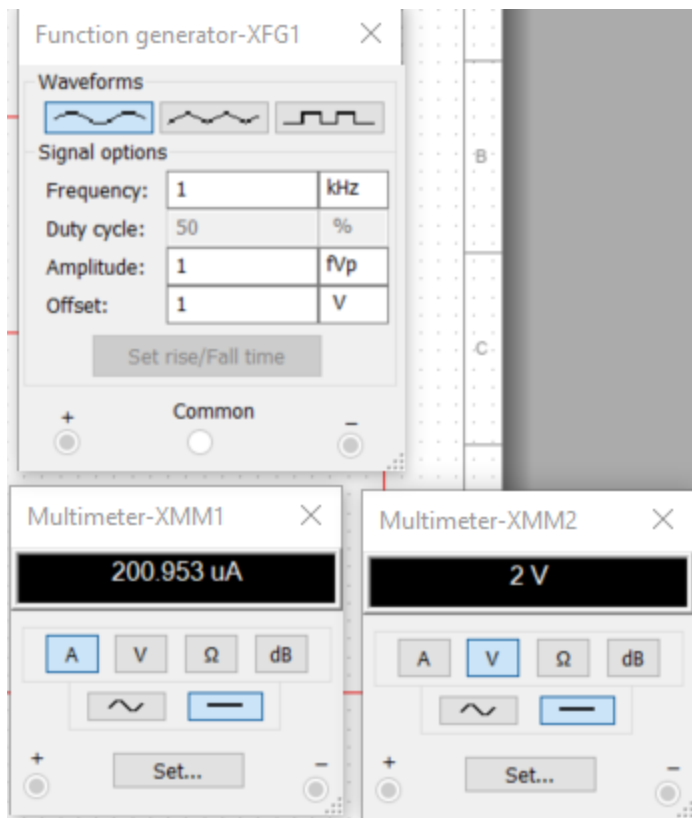
$\approx 641.67 \text{ k}\Omega$

Operation Region:

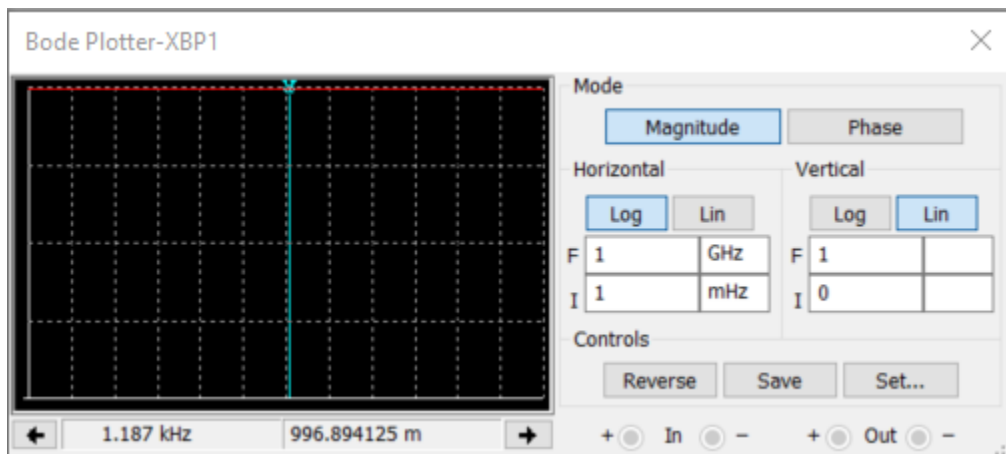


NMOS Simple Current Mirror w/ varying sized MOSFETs

I<sub>out</sub>:

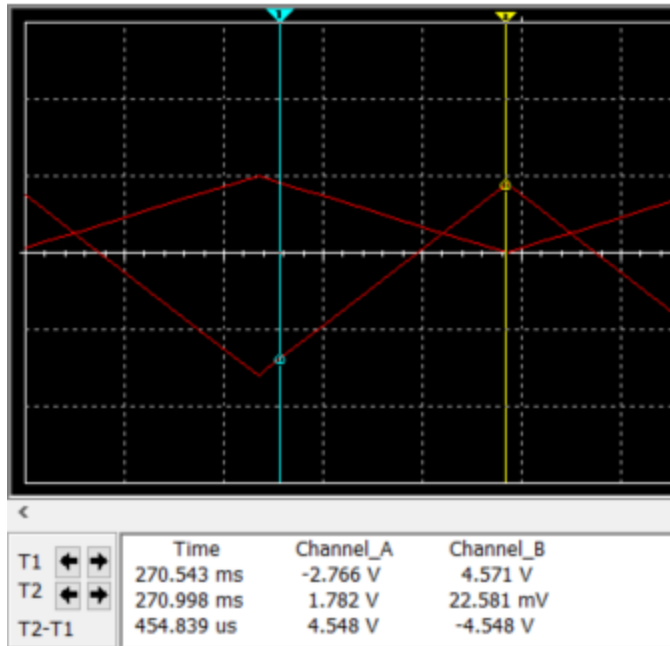


Rout:



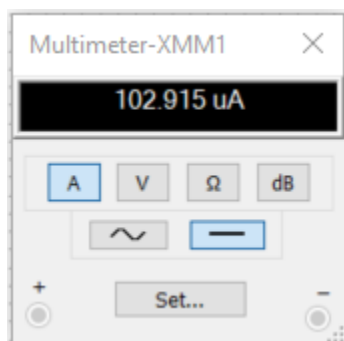
$\approx 320.97 \text{ k}\Omega$

Operation Region:

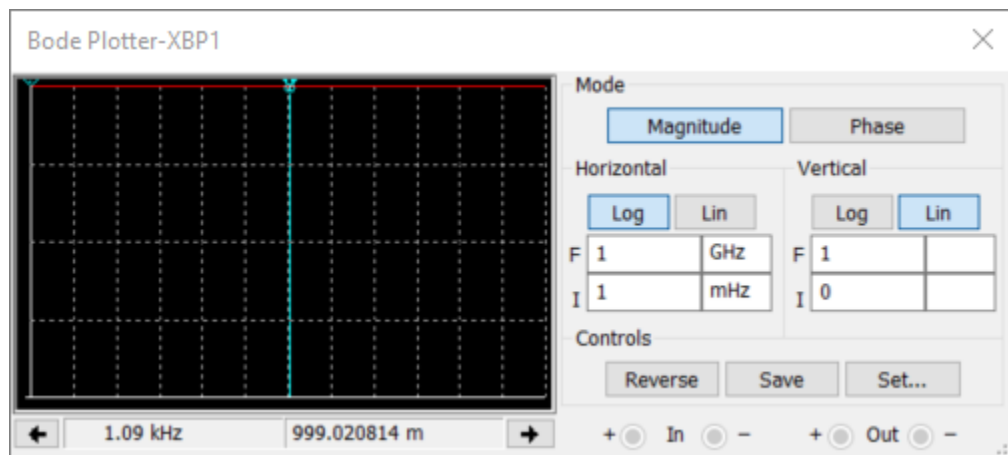


PMOS Simple Current Mirror

I<sub>out</sub>:

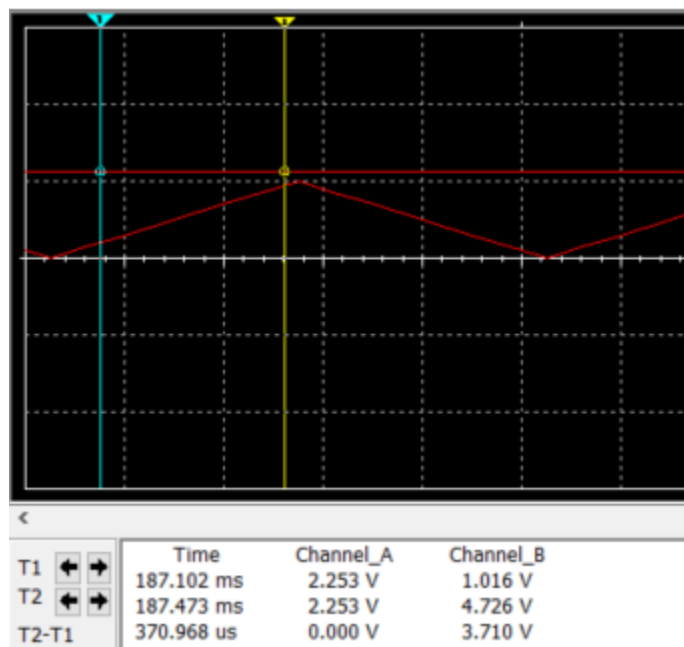


R<sub>out</sub>:



$\approx 1.02 \text{ Mohm}$

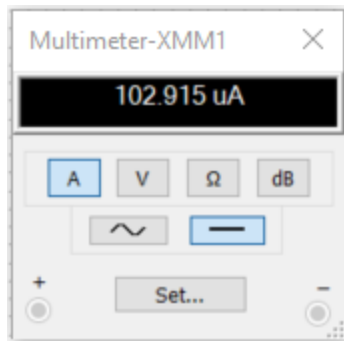
Operation Region:



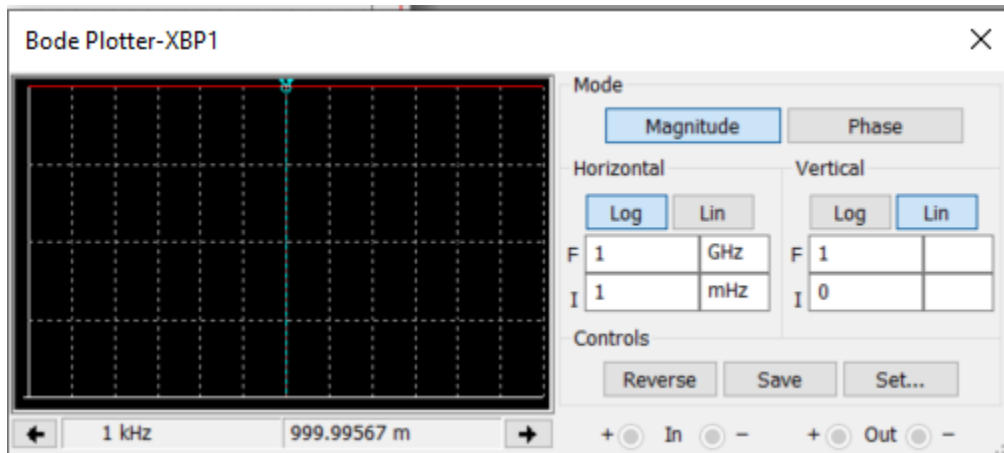
NMOS Cascode Current Mirror

$I_{out}$ :



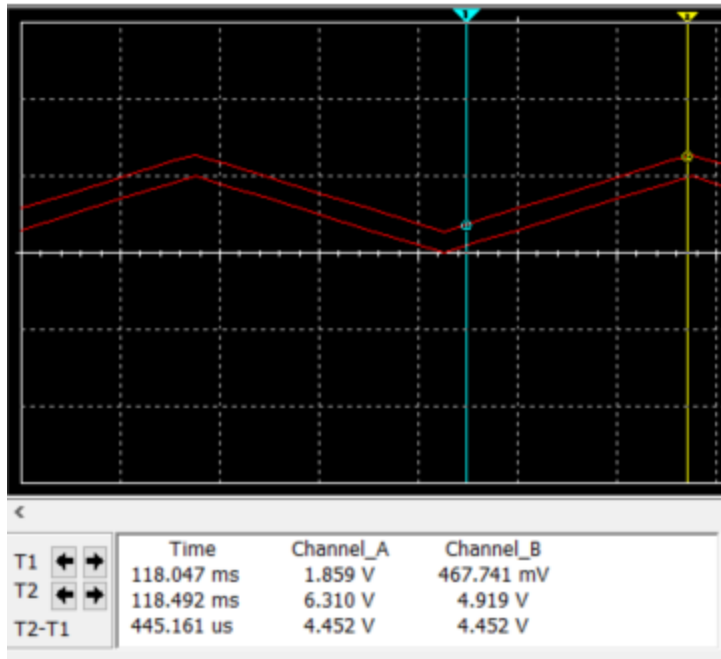


Rout:



= 230Mohm

Active Region:



## Results

### NPN Current Mirror

	Calculated	Simulated	Measured
$I_o$	1mA	9.8mA	0.987mA
$R_o$	357.24k $\Omega$	345k $\Omega$	337k $\Omega$
Active Region	0.3-5	-	0.323-4.988

### NPN Beta Helper

	Calculated	Simulated	Measured
$I_o$	1mA	19.87mA	1.047mA
$R_o$	361.944k $\Omega$	345k $\Omega$	332k $\Omega$
Active Region	0.3-5	-	0.33-5

### NPN Beta Helper with second cascade stage

	Calculated	Simulated	Measured
$I_o$	2mA	19.24mA	2.087mA
$R_o$	181.602k $\Omega$	171k $\Omega$	165.66k $\Omega$
Active Region	0.3-5	-	0.324-4.988

### NMOS Simple Current Mirror

	Calculated	Simulated	Measured
$I_o$	100uA	0.2uA	100.477uA
$R_o$	625k $\Omega$	641k $\Omega$	641k $\Omega$
Active Region	1.4<1.809<5	-	1.4<1.908<4.998

### NMOS Simple Current Mirror Differing Sizes

	Calculated	Simulated	Measured
$I_o$	200uA	0.221uA	200.953uA
$R_o$	312.5k $\Omega$	320k $\Omega$	320.97k $\Omega$
Active Region	1.4<1.809<5	-	1.4<2.015<4.98

### PMOS Simple Current Mirror

	Calculated	Simulated	Measured
$I_o$	100uA	0.2uA	102.3uA
$R_o$	1M $\Omega$	1.02M $\Omega$	1.02M $\Omega$
Active Region	1.65<2.258<4.39	-	1.65<2.456<4.39

### NMOS Cascode Current Mirror

	Calculated	Simulated	Measured
$I_o$	100uA	802uA	102uA
$R_o$	1.9G $\Omega$	221M $\Omega$	230M $\Omega$
Active Region	1.4<1.809<2.5	-	1.406<1.8756<2.489

Some differences in my simulation data comes from my failure to correctly measure the output current on the MOSFET designs. This is most likely a user error as the measured values is all correctly corresponding to the values calculated. Another source of change was from the last cascode mirror and the output resistances. The measured value was simple massive and while the simulated and measured value are large, not the same magnitude as the calculated value. This leads me to believe that the Multisim simulation is unable to register a value that large and caps out where my values are.