$$\begin{array}{c} \ddots \\ \uparrow \\ H_c^{k+1}(M) \longleftarrow H_c^{k+1}(U) \oplus H_c^{k+1}(V) \longleftarrow H_c^{k+1}(U \cap V) \\ \\ \text{d}^* \\ \uparrow \\ H_c^k(M) \longleftarrow H_c^k(U) \oplus H_c^k(V) \longleftarrow H_c^k(U \cap V) \end{array}$$