$$\downarrow^{\mathrm{d}^*} H^{k+1}(M) \longrightarrow H^{k+1}(U) \oplus H^{k+1}(V) \longrightarrow H^{k+1}(U \cap V) \longrightarrow \dots$$

 $\dots \to H^k(M) \to H^k(U) \oplus H^k(V) \to H^k(U \cap V)$