$$\widehat{H}^{-1}(H;A) \longrightarrow \widehat{H}^{0}(H;X) \longrightarrow \widehat{H}^{0}(H;A_{*} \oplus \mathbb{Z}) \stackrel{\sim}{\longrightarrow} \widehat{H}^{0}(H;A) \stackrel{\delta}{\longrightarrow} \widehat{H}^{1}(H;X) \longrightarrow \widehat{H}^{1}(H;A_{*} \oplus \mathbb{Z})$$

$$0 \longrightarrow \widehat{H}^{0}(H;X) \longrightarrow \mathbb{Z}/|H|\mathbb{Z} \stackrel{\sim}{\longrightarrow} A^{H}/N_{H}A \longrightarrow \widehat{H}^{1}(H;X) \longrightarrow 0$$