

$$\begin{array}{ccc}
 A/I_H A & \longleftarrow & \ker N_H/I_H A \\
 \text{cores} \downarrow & & \downarrow \text{cores} \\
 A/I_G A & \longleftarrow & \ker N_G/I_G A
 \end{array}$$