$$A(X)_{\overline{f}} \stackrel{\sim}{\longrightarrow} A(X)[t]/\left(\overline{f}t - 1\right)$$

$$\downarrow \qquad \qquad \downarrow$$

$$\mathcal{O}_{D(\overline{f})} \stackrel{\sim}{\longrightarrow} \mathcal{O}_{Y}$$