$$\widehat{H}^{-1}(H, A') \xrightarrow{\sim} \widehat{H}^{0}(H, A) = A^{H}/N_{H}A$$

$$\downarrow^{\text{cores}} \qquad \qquad \downarrow^{\text{cores}}$$

$$\widehat{H}^{-1}(G, A') \xrightarrow{\sim} \widehat{H}^{0}(G, A) = A^{G}/N_{G}A$$