$$H_{n}\left(D_{\alpha}^{n},\partial D_{\alpha}^{n}\right) \xrightarrow{\partial} \widetilde{H}_{n-1}\left(\partial D_{\alpha}^{n}\right) \xrightarrow{\Delta_{\alpha\beta}} \widetilde{H}_{n-1}\left(S_{\beta}^{n-1}\right)$$

$$\downarrow^{\Phi_{\alpha_{*}}} \qquad \qquad \downarrow^{\varphi_{\alpha_{*}}} \qquad \qquad \downarrow^{q_{\beta_{*}}}$$

$$H_{n}\left(X^{n},X^{n-1}\right) \xrightarrow{\partial_{n}} \widetilde{H}_{n-1}\left(X^{n-1}\right) \xrightarrow{q_{*}} \widetilde{H}_{n-1}\left(X^{n-1}/X^{n-2}\right)$$

$$\downarrow^{j_{n-1}} \qquad \qquad \downarrow^{j_{n-1}} \qquad \qquad \downarrow^{\cong}$$

$$H_{n-1}\left(X^{n-1},X^{n-2}\right) \xrightarrow{\cong} H_{n-1}\left(X^{n-2}/X^{n-2},X^{n-2}/X^{n-2}\right)$$