

## 1. Friendlier Pacman

1. Assume finite horizon of 8 (so Pacman takes exactly 8 actions) and no discounting ( $\gamma = 1$ ). Now, for each state...

...fill in the optimal policy:

	0	1	2
0	↓	←	←
1	↓	○	←
2	→	↑	↑

(available actions: ↑, ↓, →, ←, ○)

...and fill in the corresponding  $V^*(s)$  value (utility):

	0	1	2
0	8	6	4
1	10	16	14
2	12	14	12

**Hint:** Pacman gets a reward for taking any action while in (1,1), and is not rewarded for the action to enter that state.

1.1.

1.2. Q values:

1.2.1. 4

1.2.2. 14

1.3. No Actions to stay in place:

1.3.1. False

1.3.2. 8

1.4.  $(1/(1-0.5)) * 2 = 4$

## 2. Markov Decision Processes

2.1.

State	A	B	C	D	E
K	4	3	2	1	0

2.2.

State	A	B	C	D	E
K	$\infty$	$\infty$	$\infty$	1	0

(a) Mark **all** of the statements that must be true for any MDP.

- ☐ For no state  $s$  and for all policies  $\pi$ ,  $V^*(s) \geq V^\pi(s)$   
☒ For some state  $s$  and some policy  $\pi$ ,  $V^*(s) \geq V^\pi(s)$   
☒ For all states  $s$  and all policies  $\pi$ ,  $V^*(s) \geq V^\pi(s)$   
☐ None of the above

(b) Mark **all** of the statements that are true for value iteration.

- ☐ Each iteration of value iteration produces a value function that has higher value than the prior value functions **for all states**.  
☒ Value iteration can produce a value function that has higher value than the earlier value functions **for some state**.  
☐ Each iteration of value iteration produces a value function that has lower value than the prior value functions **for all states**.  
☒ Each iteration of value iteration produces a value function that has value at least as high as the prior value functions **for all states**.  
☐ None of the above

2.3.

- (a) ☐  $\frac{1}{2}$  ☐  $\frac{1}{3}$  ☐ 2 ☐ -1 ☐ 3 ☐  $\gamma$  ☒ None
- (b) ☒  $\max_a$  ☐  $\min_a$  ☐ None
- (c) ☐  $T(s', a, s'')$  ☒  $T(s, a, s')$  ☐ None
- (d) ☒  $R(s, a, s') +$  ☐  $R(s, a, s') -$  ☐ None
- (e) ☐  $\max_a$  ☐  $\min_a$  ☐  $\max_{a'}$  ☒  $\min_{a'}$  ☐  $\gamma \max_a$  ☐  $\gamma \min_a$  ☐  $\gamma \max_{a'}$  ☐  $\gamma \min_{a'}$  ☐ None
- (f) ☐  $\sum_{s'}$  ☒  $\sum_{s'} T(s, a, s')$  ☐  $\sum_{s''}$  ☐  $\sum_{s''} T(s', a', s'')$  ☐ None
- (g) ☐  $R(s, a, s') +$  ☐  $R(s, a, s') -$   
☐  $R(s', a', s'') +$  ☐  $R(s', a', s'') -$  ☒ None
- (h) ☐  $\frac{1}{2} V^*(s')$  ☒  $\gamma V^*(s')$  ☐  $V^*(s')$  ☐  $\frac{1}{2} V^*(s'')$   
☐  $\gamma V^*(s'')$  ☐  $V^*(s'')$  ☐ None

2.4.