

Formule RMS

$$rms_e = \sqrt{\frac{1}{n} \sum_{i=1}^n (o_{i,e} - d_i)^2}$$
$$rms\ proportion_e = \frac{rms_e}{\max(rms_e, \forall e \in epochs)}$$

with  $\begin{cases} n : \text{number of neurons on the output layer} \\ o_{i,e} : \text{value obtained for the } i^{th} \text{ neuron at the } e^{th} \text{ epoch} \\ d_i : \text{value desired for the } i^{th} \text{ neuron} \end{cases}$

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function DISCRETIZE(hiddenNeuron[], piece)
    result  $\leftarrow$  0
    for  $i = 0 \rightarrow \text{hiddenNeuron.length}$  do
        result  $\leftarrow$  result +  $\text{piece}^i \times \text{cutting}(\text{hiddenNeuron}[i], \text{piece})$ 
         $i \leftarrow i + 1$ 
    end for
    return result
end function

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first_order.calc_hidden_layer(samples.inputs)
high_order.calc_output_layer(first_order.hidden_layer)
first_order.calc_output_layer(first_order.hidden_layer, [0, ..., 0])

h_output  $\leftarrow$  ampli(high_order.output_layer)
right_houtput  $\leftarrow$  [0, 0]
if good_answer(first_order) then
    right_houtput[1]  $\leftarrow$  1
else
    right_houtput[0]  $\leftarrow$  1
end if
first_order.calc_output_layer(first_order.hidden_layer, h_output)

calc_stats()

high_order.train(first_order.hidden_layer, right_houtput)
first_order.train(samples.inputs, samples.outputs, h_output)

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function train(inputs, outputs, add)
  for  $i = 0 \rightarrow \text{output\_neurons.length}$  do
     $y_{\text{output}}[i] \leftarrow g'(\text{output\_neurons}[i].a) \times (\text{outputs}[i] - \text{output\_neurons.state})$ 
  end for

  for  $i = 0 \rightarrow \text{hidden\_neurons.length}$  do
     $w\_sum \leftarrow \sum_{j=0}^{\text{output\_neurons.length}} \text{output\_neurons}[j].\text{weights}[i] \times y_{\text{output}}[j]$ 
     $y_{\text{hidden}}[i] \leftarrow g'(\text{hidden\_neurons}[i].a) \times w\_sum$ 
  end for
  update_weights_hidden_layer( $y_{\text{hidden}}$ )

  for  $i = 0 \rightarrow \text{output\_neurons.length}$  do
    output_neurons[ $i$ ].update_weights_gradient( $y_{\text{output}}[i]$ , hidden_neurons, add)
    output_neurons[ $i$ ].update_weights_perceptron(outputs[ $i$ ], hidden_neurons, add)
  end for
end function

function update_weights_gradient(error, intputs, add)
  calc_output(inputs + add)

  for  $j = 0 \rightarrow \text{inputs.length}$  do
     $dw \leftarrow \text{weights}[j] - \text{last\_weights}[j]$ 
     $p \leftarrow \text{error} \times \text{inputs}[j]$ 
     $\text{weights}[j] \leftarrow \text{weights}[j] + \text{learning\_rate} \times p + \text{momentum} \times dw$ 
  end for
end function

function update_weights_perceptron(goal, intputs, add)
  calc_output(inputs + add)

  for  $j = \text{inputs.length} \rightarrow \text{inputs.length} + \text{add.length}$  do
     $dw \leftarrow \text{weights}[j] - \text{last\_weights}[j]$ 
     $p \leftarrow (\text{goal} - \text{state}) \times \text{add}[\text{inputs.length} - j]$ 
     $\text{weights}[j] \leftarrow \text{weights}[j] + \frac{\text{learning\_rate} \times p + \text{momentum} \times dw}{\text{add.length}}$ 
  end for
end function

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