50.039 Theory and Practice of Deep Learning

W5-S1 Introduction to Attacks and Defense on Neural Networks

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About this week (Week 5)

- 1. What are attacks on Neural Networks (NNs)?
- 2. Why are attacks an **important concept** when studying NNs?
- 3. What are the different **types of attacks** and what is the intuition behind basic attacks?
- 4. How to **defend** against such attacks?

5. State-of-the-art of attacks and defense, **open questions** in research.

About this week (Week 8)

- 1. What are attacks on Neural Networks (NNs)?
- 2. Why are attacks an **important concept** when studying NNs?
- 3. What are the different **types of attacks** and what is the intuition behind basic attacks?
- 4. How to defend against such attacks?

5. State-of-the-art of attacks and defense, **open questions** in research.

Attacks: definition

Definition (Attacks on Neural Networks):

Adversarial machine learning, or attacks on Neural Networks, refers to machine learning techniques that attempt to fool models by supplying deceptive input.

The most common reason is to cause a malfunction in a machine learning model.

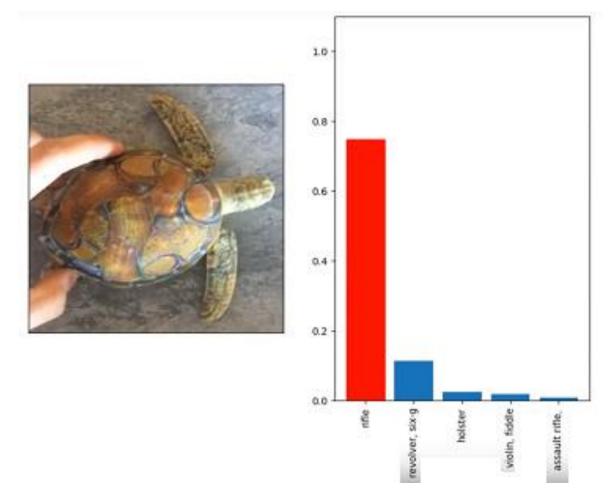


Attack/Adversarial samples: definition

Definition (Attack samples, adversarial samples):

An **input sample** is considered an **attack sample** (or **adversarial sample**) for a given trained model, if and only if, it makes this model malfunction on purpose.

Example: this picture of a turtle has been altered on some of its pixels to be misclassified as a weapon (rifle, revolver, etc.).

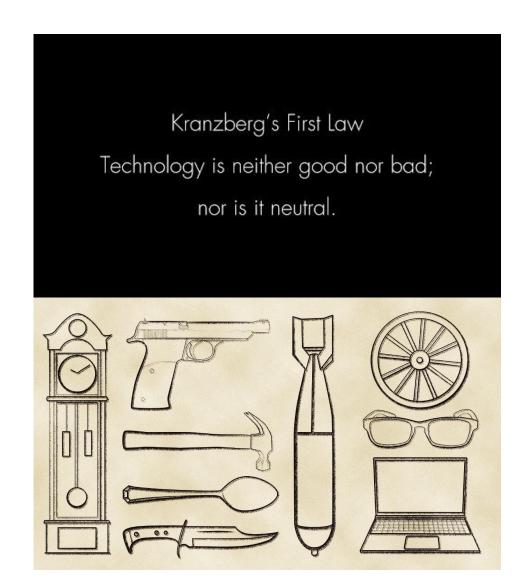


Source: Google's AI thinks this turtle looks like a gun, which is a problem [Verge1].

On the ethics of attacking Neural Networks

This week's lectures and notebooks will introduce techniques, whose objective is to make a trained Neural Network malfunction on purpose.

- These techniques are NOT, so to speak, illegal.
- But let us keep in mind what the consequences of using these attacks could be...



On the ethics of attacking Neural Networks

- Example #1: This stop sign has stickers put in specific locations.
- It is an attack sample as it can no longer be detected as a stop sign, and is instead misclassified as several bottles.

Think: What would be the effect/consequence of such an attack sample on a self-driving car using computer vision?



Source: Slight Street Sign Modifications Can Completely Fool Machine Learning Algorithms [Spectrum1].

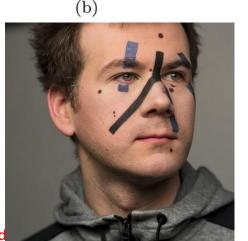
On the ethics of attacking Neural Networks

- Example #2: Covering some areas of your face with paint or glasses with specific patterns can fool facial recognition algorithms.
- These facial recognition Als are no longer able to detect a face, let alone recognize the identity of the person.

Think: Is that a good or a bad discovery for computer vision?











(c)



(d)

Source: These glasses trick facial recognition software into thinking you're someone else [Verge2].

Source: Defeating Facial Recognition [YTB1].

No...?

Okay, yes, fine.

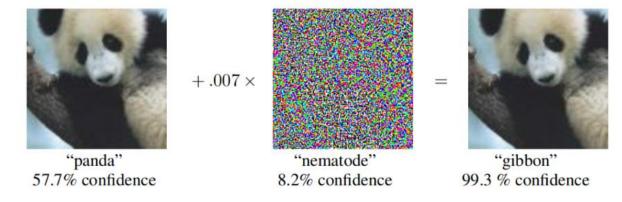
Okay, yes, fine.

But only for two reasons.

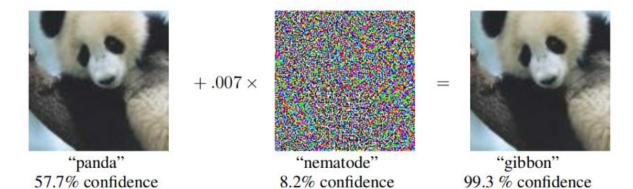
To teach you about limits/vulnerabilities of Neural Networks and how to defend them against such attacks.

- Reason #1: Neural networks are limited and vulnerable, by design.
- They will always be at risk of attacks making them malfunction, no matter how many safeguards you decide to put in place.

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- They will always be at risk of attacks making them malfunction, no matter how many safeguards you decide to put in place.
- For instance, adding noise to an image is often enough to fool any image recognition algorithm.

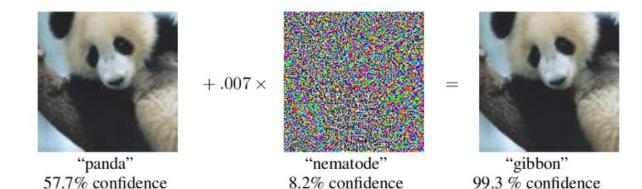


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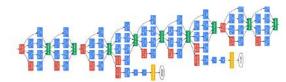
WHO WOULD WIN?

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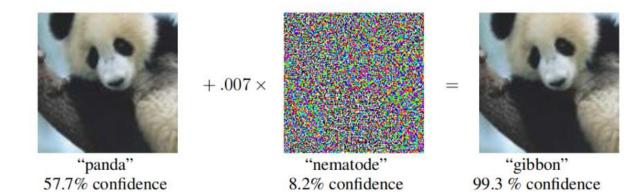


WHO WOULD WIN?

A deep convolutional network with 1 million parameters, trained for days on 64 GPUs, using a dataset consisting of millions of images

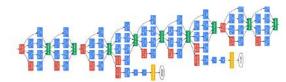


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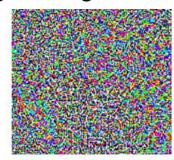


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One small noise image boi, added to an original image



Neural networks are limited and







This raises

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<u>m</u> pւ This raises two questions.

1. Shall we give up on neural networks then?

2. But, wait, how does that even work?!

any image recognition algorithm.



Neural networks are limited and







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This raises two questions.

- 1. Shall we give up on neural networks then?

 No, because of reason #2, defense (more on this later).
- 2. But, wait, how does that even work?!

• Fc im

any image recognition algorithm.



- Please refer to Notebook 1.
 Using Epsilon Noising Attack to Generate Attack Samples.
- All notebooks this week follow the same structure
 - Dataset and Dataloader

Dataset and Dataloader

```
1 # Transform definition
2 # (Basic: only convert image to torch tensor)
3 tf = transforms.Compose([transforms.ToTensor()])
```

- Please refer to Notebook 1.
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 - Dataset and Dataloader
 - Model

```
# Model definition
   class Net(nn.Module):
       def init (self):
            super(Net, self). init ()
            # Conv. 1
            self.conv1 = nn.Conv2d(1, 10, kernel size = 5)
            # Conv. 2
            self.conv2 = nn.Conv2d(10, 20, kernel size = 5)
10
            # Dropout for Conv. layers
            self.conv2 drop = nn.Dropout2d()
11
12
            # FC 1
13
            self.fc1 = nn.Linear(320, 50)
14
            # FC 2
15
            self.fc2 = nn.Linear(50, 10)
16
17
       def forward(self, x):
18
            # Conv. 1 + ReLU + Dropout
19
            x = F.relu(F.max pool2d(self.conv1(x), 2))
20
            # Conv. 2 + ReLU + Dropout
21
            x = F.relu(F.max pool2d(self.conv2 drop(self.conv2(x)), 2))
22
            # Flatten
23
            x = x.view(-1, 320)
24
            # FC 1 + ReLU + Droupout
25
            x = F.relu(self.fcl(x))
26
            x = F.dropout(x, training = self.training)
27
            # FC 2 + Log-Softmax
28
            x = self.fc2(x)
29
            return F.log softmax(x, dim = 1)
```

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            # FC 2 + Log-Softmax
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```

```
# Load the pretrained model
model = Net().to(device)
pretrained_model = "./mnist_model.data"
model.load_state_dict(torch.load(pretrained_model, \
map_location = 'cpu'))
```

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 - Attack function

```
def enm attack(image, epsilon):
        # Generate noise matrix, with same shape as image,
        # and random values in [- epsilon, epsilon]
       img rows = image.shape[-2]
       img cols = image.shape[-1]
       epsilon mat = np.asarray(([[2*(np.random.random() - 0.5)*epsilon
                                    for i in range(img rows)]
                                    for j in range(img cols)]))
11
       # Create the attack image by adjusting each pixel of the input image
       eps image = image.detach().numpy() + epsilon mat
12
13
14
       # Clipping eps image to maintain pixel values into the [0, 1] range
       eps image = torch.from numpy(eps image).float()
15
       eps image = torch.clamp(eps image, 0, 1)
16
17
18
        # Return
19
       return eps image
```

Definition (Epsilon Noising Method):

The **Epsilon Noising Method (ENM)** is the simplest type of attack. It consists of generating an image \tilde{x} , by adding a random noise to each pixel of an image x, with amplitude $[-\epsilon, \epsilon]$.

```
\forall i, j \in Pixel\_Indexes_x
                          \widetilde{\mathbf{x}}_{i,i} = \mathbf{x}_{i,i} + \boldsymbol{\omega}_{i,i}
\omega_{i,j} \to U([-\epsilon, \epsilon]) (Unif. Dist.)
\omega_{i,j} \to N([-\epsilon, \epsilon]) (Normal Dist.)
```

```
def enm attack(image, epsilon):
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15
       eps image = torch.clamp(eps image, 0, 1)
17
18
        # Return
       return eps image
```



"panda" 57.7% confidence



 $+.007 \times$

"nematode" 8.2% confidence



"gibbon" 99.3 % confidence

Generate noise vector with same size as image, and amplitude in $[-\epsilon, \epsilon]$.

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```
\forall i, j \in Pixel\_Indexes_{\chi}
\widetilde{\chi}_{i,j} = \chi_{i,j} + \omega_{i,j}
\left\{ \omega_{i,j} \to U([-\epsilon, \epsilon]) \quad (Unif.Dist.) \right\}
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```

```
def enm attack (image, epsilon):
        # Generate noise matrix, with same shape as image,
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       epsilon mat = np.asarray(([[2*(np.random.random() - 0.5)*epsilon
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11
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12
13
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       eps image = torch.from numpy(eps image).float()
15
       eps image = torch.clamp(eps image, 0, 1)
17
18
        # Return
       return eps image
```



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Add noise to original image.

Definition (Epsilon Noising Method):

The **Epsilon Noising Method (ENM)** is the simplest type of attack. It consists of generating an image \tilde{x} , by **adding a random noise to each pixel of an image** x, with amplitude $[-\epsilon, \epsilon]$.

```
\forall i, j \in Pixel\_Indexes_{x}
\widetilde{x}_{i,j} = x_{i,j} + \omega_{i,j}
\left\{ \omega_{i,j} \to U([-\epsilon, \epsilon]) \quad (Unif.Dist.) \right\}
\left\{ \omega_{i,j} \to N([-\epsilon, \epsilon]) \quad (Normal Dist.) \right\}
```

```
def enm attack(image, epsilon):
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       epsilon mat = np.asarray(([[2*(np.random.random() - 0.5)*epsilon
                                    for i in range(img rows)]
                                    for j in range(img cols)]))
11
        # Create the attack image by adjusting each pixel of the input image
12
       eps image = image.detach().numpy() + epsilon_mat
13
       # Clipping eps image to maintain pixel values into the [0, 1] range
       eps image = torch.from numpy(eps image).float()
       eps image = torch.clamp(eps image, 0, 1)
17
18
        # Return
       return eps image
```



"panda" 57.7% confidence



 $+.007 \times$

"nematode" 8.2% confidence



"gibbon" 99.3 % confidence

Clipping to prevent unwanted pixel values.

Reminder (Clipping a value):

Clipping a value x forces it to remain in an interval [a, b], with $a \le b$.

We define the **clipping function** $\gamma_{a,b}(x)$, as follows.

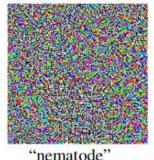
$$\gamma_{a,b}(x) = \max(a, \min(x, b))$$

$$\gamma_{a,b}(x) = \begin{cases} a & \text{if } x \leq a \\ b & \text{if } x \geq b \\ x & \text{otherwise} \end{cases}$$

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Clipping to prevent pixel values to go out of [0, 1].

(Normalization taken into account)

Definition (Epsilon Noising Method):

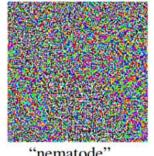
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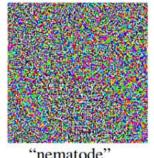
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- All notebooks this week follow the same structure
 - Dataset and Dataloader
 - (Pre-trained) Model
 - Attack function
 - Testing effect of attack on model

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Testing Function

This function attempts to 1) track how an attack with amplitude epsilon, used on the samples in the test_loader will affect our model;

```
1 def test (model, device, test loader, epsilon):
       # Counter for correct values (used for accuracy)
       correct counter = 0
       # List of successful adversarial samples
       adv examples list = []
 9
       # Loop over all examples in test set
10
       for image, label in test loader:
11
12
            # Send the data and label to the device
13
           image, label = image.to(device), label.to(device)
           # Pass the image through the model
           output = model(image)
16
            # Get the index of the max log-probability
17
                                                               52
           init pred = output.max(1, keepdim = True)[1]
18
19
            # If the initial prediction is wrong, do not
20
           # bother attacking, skip current image
           if init pred.item() != label.item():
23
                continue
24
25
            # Calculate the loss
26
           loss = F.nll loss(output, label)
                                                               62
27
           # Zero all existing gradients
           model.zero grad()
            # Backpropagate
31
           loss.backward()
```

```
# Call ENM Attack
    eps image = enm attack(image, epsilon)
    # Re-classify the epsilon image
    output2 = model(eps image)
    # Get the index of the max log-probability
    eps pred = output2.max(1, keepdim = True)[1]
    # Check for successful attack
    # (Successful meaning eps pred label different from init pred)
    if eps pred.item() == label.item():
        correct counter += 1
        # Special case for saving 0 epsilon examples
        # (Maximal number of saved samples is set to 5)
        if (epsilon == 0) and (len(adv examples list) < 5):</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
    else:
        # Save some adv examples for visualization later
        # (Maximal number of saved samples is set to 5)
        if len(adv examples list) < 5:</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
# Calculate final accuracy for this epsilon value
final acc = correct counter/float(len(test loader))
# Display for progress
print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
                                                         correct counter, \
                                                         len(test loader), \
                                                         final acc))
# Return the accuracy and an adversarial example
return final acc, adv examples list
```

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Testing Function

```
This function attempts to 1) track how an attack with amplitude epsilon, used on the samples in the test_loader will affect our model; and 2) return attack samples that worked for later visualization.
```

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                                                         len(test loader), \
                                                         final acc))
# Return the accuracy and an adversarial example
return final acc, adv examples list
```

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Testing Function

```
This will track how many samples were correctly classified despite the attack being performed on the test samples.
```

```
def test (model, device, test loader, epsilon):
       # Counter for correct values (used for accuracy)
       correct counter = 0
       # List of successful adversarial samples
       adv examples list = []
 9
       # Loop over all examples in test set
10
       for image, label in test loader:
11
12
            # Send the data and label to the device
13
           image, label = image.to(device), label.to(device)
           # Pass the image through the model
           output = model(image)
16
           # Get the index of the max log-probability
17
           init pred = output.max(1, keepdim = True)[1]
18
19
            # If the initial prediction is wrong, do not
20
           # bother attacking, skip current image
           if init pred.item() != label.item():
23
                continue
24
25
            # Calculate the loss
26
           loss = F.nll loss(output, label)
27
           # Zero all existing gradients
           model.zero grad()
            # Backpropagate
31
           loss.backward()
```

```
# Call ENM Attack
    eps image = enm attack(image, epsilon)
    # Re-classify the epsilon image
    output2 = model(eps image)
    # Get the index of the max log-probability
    eps pred = output2.max(1, keepdim = True)[1]
    # Check for successful attack
    # (Successful meaning eps pred label different from init pred)
    if eps pred.item() == label.item():
        correct counter += 1
        # Special case for saving 0 epsilon examples
        # (Maximal number of saved samples is set to 5)
        if (epsilon == 0) and (len(adv examples list) < 5):</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
    else:
        # Save some adv examples for visualization later
        # (Maximal number of saved samples is set to 5)
        if len(adv examples list) < 5:</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
# Calculate final accuracy for this epsilon value
final acc = correct counter/float(len(test loader))
# Display for progress
print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
                                                         correct counter, \
                                                         len(test loader), \
                                                         final acc))
# Return the accuracy and an adversarial example
return final acc, adv examples list
```

Testing Function

```
This will store up to 5 attack samples that made the model malfunction (used for visualization later).
```

```
def test (model, device, test loader, epsilon):
                                                                 34
                                                                 35
                                                                 36
        # Counter for correct values (used for accuracy)
        correct counter = 0
        # List of successful adversarial samples
                                                                 40
        adv examples list = []
                                                                 41
                                                                 42
 9
        # Loop over all examples in test set
                                                                 43
10
        for image, label in test loader:
                                                                 44
11
                                                                 45
12
            # Send the data and label to the device
                                                                 46
            image, label = image.to(device), label.to(device)
13
                                                                 48
                                                                 49
            # Pass the image through the model
                                                                 50
            output = model(image)
16
                                                                 51
            # Get the index of the max log-probability
17
                                                                 52
            init pred = output.max(1, keepdim = True)[1]
18
                                                                 53
19
                                                                 54
            # If the initial prediction is wrong, do not
20
                                                                 55
            # bother attacking, skip current image
                                                                 56
            if init pred.item() != label.item():
                                                                 57
23
                continue
                                                                 58
                                                                 59
24
                                                                 60
25
            # Calculate the loss
                                                                 61
26
            loss = F.nll loss(output, label)
                                                                 62
27
                                                                 63
            # Zero all existing gradients
                                                                 64
            model.zero grad()
                                                                 65
                                                                 66
            # Backpropagate
31
                                                                 67
            loss.backward()
```

```
# Call ENM Attack
    eps image = enm attack(image, epsilon)
    # Re-classify the epsilon image
    output2 = model(eps image)
    # Get the index of the max log-probability
    eps pred = output2.max(1, keepdim = True)[1]
    # Check for successful attack
    # (Successful meaning eps pred label different from init pred)
    if eps pred.item() == label.item():
        correct counter += 1
        # Special case for saving 0 epsilon examples
        # (Maximal number of saved samples is set to 5)
        if (epsilon == 0) and (len(adv examples list) < 5):</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
    else:
        # Save some adv examples for visualization later
        # (Maximal number of saved samples is set to 5)
        if len(adv examples list) < 5:</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
# Calculate final accuracy for this epsilon value
final acc = correct counter/float(len(test loader))
# Display for progress
print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
                                                         correct counter, \
                                                         len(test loader), \
                                                         final acc))
# Return the accuracy and an adversarial example
return final acc, adv examples list
```

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Testing Function

```
def test (model, device, test loader, epsilon):
       # Counter for correct values (used for accuracy)
       correct counter = 0
       # List of successful adversarial samples
       adv examples list = []
9
       # Loop over all examples in test set
10
       for image, label in test loader:
11
12
            # Send the data and label to the device
13
           image, label = image.to(device), label.to(device) 47
14
            # Pass the image through the model
           output = model(image)
16
            # Get the index of the max log-probability
17
18
           init pred = output.max(1, keepdim = True)[1]
19
20
           # If the initial prediction is wrong, do not
           # bother attacking, skip current image
           if init pred.item() != label.item():
23
                continue
24
25
            # Calculate the loss
26
           loss = F.nll loss(output, label)
27
           # Zero all existing gradients
           model.zero grad()
            # Backpropagate
31
           loss.backward()
```

This is very typical for our test functions so far, just browsing through (normal) test samples and trying those on our model.

```
# Call ENM Attack
    eps image = enm attack(image, epsilon)
    # Re-classify the epsilon image
    output2 = model(eps image)
    # Get the index of the max log-probability
    eps pred = output2.max(1, keepdim = True)[1]
    # Check for successful attack
    # (Successful meaning eps pred label different from init pred)
    if eps pred.item() == label.item():
        correct counter += 1
        # Special case for saving 0 epsilon examples
        # (Maximal number of saved samples is set to 5)
        if (epsilon == 0) and (len(adv examples list) < 5):</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
    else:
        # Save some adv examples for visualization later
        # (Maximal number of saved samples is set to 5)
        if len(adv examples list) < 5:</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
# Calculate final accuracy for this epsilon value
final acc = correct counter/float(len(test loader))
# Display for progress
print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
                                                         correct counter, \
                                                         len(test loader), \
                                                         final acc))
# Return the accuracy and an adversarial example
return final acc, adv examples list
```

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Testing Function

```
def test (model, device, test loader, epsilon):
       # Counter for correct values (used for accuracy)
       correct counter = 0
       # List of successful adversarial samples
       adv examples list = []
 9
       # Loop over all examples in test set
10
       for image, label in test loader:
11
12
           # Send the data and label to the device
           image, label = image.to(device), label.to(device)
13
           # Pass the image through the model
           output = model(image)
16
           # Get the index of the max log-probability
17
18
           init pred = output.max(1, keepdim / True)[1]
19
           # If the initial prediction is wrong, do not
20
           # bother attacking, skip current image
           if init pred.item() != label.item():
23
                continue
24
25
            # Calculate the loss
26
           loss = F.nll loss(output, label)
27
           # Zero all existing gradients
           model.zero grad()
            # Backpropagate
31
           loss.backward()
```

If the model already misclassifies the sample, <u>do not bother attacking</u> (Attack could make the model right!).

```
# Call ENM Attack
    eps image = enm attack(image, epsilon)
    # Re-classify the epsilon image
    output2 = model(eps image)
    # Get the index of the max log-probability
    eps pred = output2.max(1, keepdim = True)[1]
    # Check for successful attack
    # (Successful meaning eps pred label different from init pred)
    if eps pred.item() == label.item():
        correct counter += 1
        # Special case for saving 0 epsilon examples
        # (Maximal number of saved samples is set to 5)
        if (epsilon == 0) and (len(adv examples list) < 5):</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
    else:
        # Save some adv examples for visualization later
        # (Maximal number of saved samples is set to 5)
        if len(adv examples list) < 5:</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
# Calculate final accuracy for this epsilon value
final acc = correct counter/float(len(test loader))
# Display for progress
print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
                                                         correct counter, \
                                                         len(test loader), \
                                                         final acc))
# Return the accuracy and an adversarial example
return final acc, adv examples list
```

Restricted

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Testing Function

This is again very typical. Right now, it does not appear necessary, but more advanced attacks will rely on the gradients of the model, and that would be the way to compute them (more on this later!).

```
def test (model, device, test loader, epsilon):
       # Counter for correct values (used for accuracy)
       correct counter = 0
       # List of successful adversarial samples
       adv examples list = []
 9
       # Loop over all examples in test set
10
       for image, label in test loader:
11
12
            # Send the data and label to the device
           image, label = image.to(device), label.to device)
13
           # Pass the image through the model
           output = model(image)
16
           # Get the index of the max log-probability
17
18
           init pred = output.max(1, keepdim = True)[1]
19
20
           # If the initial prediction is wrong, do not
           # bother attacking, skip current image
           if init pred.item() != label.item():
23
                continue
24
           # Calculate the loss
25
26
           loss = F.nll loss(output, label)
27
           # Zero all existing gradients
           model.zero grad()
           # Backpropagate
31
           loss.backward()
```

```
# Call ENM Attack
    eps image = enm attack(image, epsilon)
    # Re-classify the epsilon image
    output2 = model(eps image)
    # Get the index of the max log-probability
    eps pred = output2.max(1, keepdim = True)[1]
    # Check for successful attack
    # (Successful meaning eps pred label different from init pred)
    if eps pred.item() == label.item():
        correct counter += 1
        # Special case for saving 0 epsilon examples
        # (Maximal number of saved samples is set to 5)
        if (epsilon == 0) and (len(adv examples list) < 5):</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
    else:
        # Save some adv examples for visualization later
        # (Maximal number of saved samples is set to 5)
        if len(adv examples list) < 5:</pre>
            adv ex = eps image.squeeze().detach().cpu().numpy()
            adv examples list.append((init pred.item(), eps pred.item(), adv ex))
# Calculate final accuracy for this epsilon value
final acc = correct counter/float(len(test loader))
# Display for progress
print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
                                                         correct counter, \
                                                         len(test loader), \
                                                         final acc))
# Return the accuracy and an adversarial example
return final acc, adv examples list
```

Generate an attack sample, using our ENM attack function.

```
# Call ENM Attack
   def test (model, device, test loader, epsilon):
                                                                              eps_image = enm_attack(image, epsilon)
                                                                   35
                                                                   36
        # Counter for correct values (used for accuracy)
                                                                   37
                                                                              # Re-classify the epsilon image
        correct counter = 0
                                                                              output2 = model(eps image)
                                                                              # Get the index of the max log-probability
                                                                   39
        # List of successful adversarial samples
                                                                              eps pred = output2.max(1, keepdim = True)[1]
                                                                   40
        adv examples list = []
                                                                   41
                                                                   42
                                                                               # Check for successful attack
 9
        # Loop over all examples in test set
                                                                               # (Successful meaning eps pred label different from init pred)
                                                                   43
10
        for image, label in test loader:
                                                                              if eps pred.item() == label.item():
                                                                   44
11
                                                                                  correct counter += 1
                                                                   45
12
            # Send the data and label to the device
                                                                   46
                                                                                   # Special case for saving 0 epsilon examples
                                                                                   # (Maximal number of saved samples is set to 5)
13
            image, label = image.to(device), label.to(device)
                                                                                  if (epsilon == 0) and (len(adv examples list) < 5):</pre>
                                                                   48
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
                                                                   49
            # Pass the image through the model
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
                                                                   50
            output = model(image)
16
                                                                   51
                                                                              else:
            # Get the index of the max log-probability
17
                                                                   52
                                                                                   # Save some adv examples for visualization later
18
            init pred = output.max(1, keepdim = True)[1]
                                                                   53
                                                                                   # (Maximal number of saved samples is set to 5)
19
                                                                   54
                                                                                  if len(adv examples list) < 5:</pre>
            # If the initial prediction is wrong, do not
20
                                                                   55
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
            # bother attacking, skip current image
                                                                   56
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
            if init pred.item() != label.item():
                                                                   57
23
                 continue
                                                                   58
                                                                           # Calculate final accuracy for this epsilon value
                                                                          final acc = correct counter/float(len(test loader))
                                                                   59
24
                                                                   60
25
            # Calculate the loss
                                                                   61
                                                                           # Display for progress
26
            loss = F.nll loss(output, label)
                                                                   62
                                                                          print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
27
                                                                   63
                                                                                                                                  correct counter, \
            # Zero all existing gradients
                                                                                                                                  len(test loader), \
                                                                   64
            model.zero grad()
                                                                   65
                                                                                                                                  final acc))
                                                                   66
            # Backpropagate
31
                                                                   67
                                                                           # Return the accuracy and an adversarial example
            loss.backward()
                                                                          return final acc, adv examples list
```

Try attack sample on our model.

```
def test (model, device, test loader, epsilon):
                                                                               # Call ENM Attack
                                                                   35
                                                                              eps image = enm attack(image, epsilon)
                                                                   36
        # Counter for correct values (used for accuracy)
                                                                             # Re-classify the epsilon image
                                                                   37
        correct counter = 0
                                                                              output2 = model(eps image)
                                                                              # Get the index of the max log-probability
                                                                   39
        # List of successful adversarial samples
                                                                              eps pred = output2.max(1, keepdim = True)[1]
                                                                   40
        adv examples list = []
                                                                   41
                                                                   42
                                                                               # Check for successful attack
9
        # Loop over all examples in test set
                                                                               # (Successful meaning eps pred label different from init pred)
                                                                   43
10
        for image, label in test loader:
                                                                              if eps pred.item() == label.item():
                                                                   44
11
                                                                                   correct counter += 1
                                                                   45
12
            # Send the data and label to the device
                                                                   46
                                                                                   # Special case for saving 0 epsilon examples
                                                                                   # (Maximal number of saved samples is set to 5)
13
            image, label = image.to(device), label.to(device)
                                                                                  if (epsilon == 0) and (len(adv examples list) < 5):</pre>
                                                                   48
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
                                                                   49
            # Pass the image through the model
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
                                                                   50
            output = model(image)
16
                                                                   51
                                                                               else:
            # Get the index of the max log-probability
17
                                                                   52
                                                                                   # Save some adv examples for visualization later
            init pred = output.max(1, keepdim = True)[1]
18
                                                                   53
                                                                                   # (Maximal number of saved samples is set to 5)
19
                                                                   54
                                                                                  if len(adv examples list) < 5:</pre>
            # If the initial prediction is wrong, do not
20
                                                                   55
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
            # bother attacking, skip current image
                                                                   56
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
            if init pred.item() != label.item():
                                                                   57
23
                 continue
                                                                   58
                                                                           # Calculate final accuracy for this epsilon value
                                                                          final acc = correct counter/float(len(test loader))
                                                                   59
24
                                                                   60
25
            # Calculate the loss
                                                                           # Display for progress
                                                                   61
26
            loss = F.nll loss(output, label)
                                                                   62
                                                                          print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
27
                                                                   63
                                                                                                                                   correct counter, \
            # Zero all existing gradients
                                                                   64
                                                                                                                                  len(test loader), \
            model.zero grad()
                                                                   65
                                                                                                                                   final acc))
                                                                   66
            # Backpropagate
                                                                   67
                                                                           # Return the accuracy and an adversarial example
            loss.backward()
                                                                          return final acc, adv examples list
```

Restricted

If attack sample is correctly classified, the attack is a failure. Increase correct score by one.

```
def test (model, device, test loader, epsilon):
                                                                               # Call ENM Attack
                                                                   35
                                                                              eps image = emm attack(image, epsilon)
                                                                   36
        # Counter for correct values (used for accuracy)
                                                                               # Re-classify the epsilon image
                                                                   37
        correct counter = 0
                                                                              output2 = model(eps image)
                                                                               # Get the index of the max log-probability
                                                                   39
        # List of successful adversarial samples
                                                                              eps pred = output2.max(1, keepdim = True)[1]
                                                                   40
        adv examples list = []
                                                                   41
                                                                               # Check for successful attack
                                                                   42
9
        # Loop over all examples in test set
                                                                               # (Successful meaning eps pred label different from init pred)
                                                                   43
10
        for image, label in test loader:
                                                                              if eps pred.item() == label.item():
                                                                   44
11
                                                                   45
                                                                                   correct counter += 1
12
            # Send the data and label to the device
                                                                   46
                                                                                   # Special case for saving 0 epsilon examples
                                                                                   # (Maximal number of saved samples is set to 5)
13
            image, label = image.to(device), label.to(device)
                                                                   47
                                                                                  if (epsilon == 0) and (len(adv examples list) < 5):</pre>
                                                                   48
14
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
                                                                   49
            # Pass the image through the model
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
                                                                   50
            output = model(image)
16
                                                                   51
                                                                              else:
            # Get the index of the max log-probability
17
                                                                   52
                                                                                   # Save some adv examples for visualization later
18
            init pred = output.max(1, keepdim = True)[1]
                                                                   53
                                                                                   # (Maximal number of saved samples is set to 5)
19
                                                                   54
                                                                                  if len(adv examples list) < 5:</pre>
            # If the initial prediction is wrong, do not
20
                                                                   55
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
            # bother attacking, skip current image
                                                                   56
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
            if init pred.item() != label.item():
                                                                   57
23
                 continue
                                                                   58
                                                                           # Calculate final accuracy for this epsilon value
                                                                          final acc = correct counter/float(len(test loader))
24
                                                                   59
                                                                   60
25
            # Calculate the loss
                                                                   61
                                                                           # Display for progress
26
            loss = F.nll loss(output, label)
                                                                   62
                                                                          print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
27
                                                                   63
                                                                                                                                  correct counter, \
            # Zero all existing gradients
                                                                   64
                                                                                                                                  len(test loader), \
            model.zero grad()
                                                                   65
                                                                                                                                   final acc))
                                                                   66
            # Backpropagate
31
                                                                   67
                                                                           # Return the accuracy and an adversarial example
            loss.backward()
                                                                          return final acc, adv examples list
```

Testing Function

Add sample to adversarial samples list if epsilon = 0 and list not full (attacking with epsilon = 0 will always fail as it will not modify the image). This gives the baseline accuracy of the model before attacks.

```
def test (model, device, test loader, epsilon):
                                                                   34
                                                                               # Call ENM Attank
                                                                   35
                                                                              eps image = enm attack(image, epsilon)
                                                                   36
        # Counter for correct values (used for accuracy)
                                                                              # Re-classify the epsilon image
                                                                   37
        correct counter = 0
                                                                              output2 = model(eps image)
                                                                              # Get the index of the max log-probability
                                                                   39
        # List of successful adversarial samples
                                                                              eps pred = output2 max(1, keepdim = True)[1]
                                                                   40
        adv examples list = []
                                                                   41
                                                                               # Check for successful attack
                                                                   42
9
        # Loop over all examples in test set
                                                                              # (Successful meaning eps pred label different from init pred)
                                                                   43
10
        for image, label in test loader:
                                                                              if eps pred.item() == label.item():
                                                                   44
11
                                                                                  correct counter += 1
                                                                   45
                                                                                   # Special case for saving 0 epsilon examples
12
            # Send the data and label to the device
                                                                   46
                                                                                   # (Maximal number of saved samples is set to 5)
            image, label = image.to(device), label.to(device)
13
                                                                  47
                                                                                  if (epsilon == 0) and (len(adv examples list) < 5):</pre>
                                                                   48
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
                                                                   49
            # Pass the image through the model
                                                                   50
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
            output = model(image)
16
                                                                   51
                                                                              else:
            # Get the index of the max log-probability
17
                                                                   52
                                                                                  # Save some adv examples for visualization later
18
            init pred = output.max(1, keepdim = True)[1]
                                                                   53
                                                                                  # (Maximal number of saved samples is set to 5)
19
                                                                   54
                                                                                  if len(adv examples list) < 5:</pre>
20
            # If the initial prediction is wrong, do not
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
                                                                   55
            # bother attacking, skip current image
                                                                   56
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
            if init pred.item() != label.item():
                                                                   57
                                                                   58
                                                                           # Calculate final accuracy for this epsilon value
23
                continue
                                                                          final acc = correct counter/float(len(test loader))
24
                                                                   59
                                                                   60
25
            # Calculate the loss
                                                                   61
                                                                           # Display for progress
26
            loss = F.nll loss(output, label)
                                                                   62
                                                                          print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
27
                                                                   63
                                                                                                                                  correct counter, \
            # Zero all existing gradients
                                                                                                                                  len(test loader), \
                                                                   64
            model.zero grad()
                                                                   65
                                                                                                                                  final acc))
                                                                   66
            # Backpropagate
31
                                                                           # Return the accuracy and an adversarial example
                                                                   67
            loss.backward()
                                                                          return final acc, adv examples list
```

Testing Function

If attack sample makes the model misclassify, it is a successful attack. Do not increase correct_counter, and store sample in adversarial samples list if not already full.

```
def test (model, device, test loader, epsilon):
                                                                   34
                                                                               # Call ENM Attack
                                                                   35
                                                                              eps image = enn attack(image, epsilon)
                                                                   36
        # Counter for correct values (used for accuracy)
                                                                               # Re-classify the epsilon image
                                                                   37
        correct counter = 0
                                                                              output2 = model eps image)
                                                                               # Get the index of the max log-probability
                                                                   39
        # List of successful adversarial samples
                                                                              eps pred = output2.max(1, keepdim = True)[1]
                                                                   40
        adv examples list = []
                                                                   41
                                                                               # Check for successful attack
                                                                   42
9
        # Loop over all examples in test set
                                                                               # (Successful meaning eps pred label different from init pred)
                                                                   43
10
        for image, label in test loader:
                                                                              if eps pred.item() == label.item():
                                                                   44
11
                                                                                  correct counter += 1
                                                                   45
                                                                                   # Special case for saving 0 epsilon examples
12
            # Send the data and label to the device
                                                                   46
                                                                                   # (Maximal number of saved samples is set to 5)
            image, label = image.to(device), label.to(device)
13
                                                                                  if (epsilon == 0) and (len(adv examples list) < 5):</pre>
                                                                   48
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
                                                                   49
            # Pass the image through the model
                                                                   50
                                                                                      adv examples list append((init pred.item(), eps pred.item(), adv ex))
            output = model(image)
16
                                                                   51
                                                                              else:
            # Get the index of the max log-probability
17
                                                                   52
                                                                                   # Save some adv examples for visualization later
18
            init pred = output.max(1, keepdim = True)[1]
                                                                   53
                                                                                   # (Maximal number of saved samples is set to 5)
19
                                                                   54
                                                                                  if len(adv examples list) < 5:</pre>
            # If the initial prediction is wrong, do not
20
                                                                   55
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
            # bother attacking, skip current image
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
                                                                   56
            if init pred.item() != label.item():
                                                                   57
23
                 continue
                                                                   58
                                                                           # Calculate final accuracy for this epsilon value
                                                                          final acc = correct counter/float(len(test loader))
24
                                                                   59
                                                                   60
25
            # Calculate the loss
                                                                   61
                                                                           # Display for progress
26
            loss = F.nll loss(output, label)
                                                                   62
                                                                          print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
27
                                                                                                                                  correct counter, \
                                                                   63
            # Zero all existing gradients
                                                                   64
                                                                                                                                  len(test loader), \
            model.zero grad()
                                                                   65
                                                                                                                                   final acc))
                                                                   66
            # Backpropagate
31
                                                                   67
                                                                           # Return the accuracy and an adversarial example
            loss.backward()
                                                                   68
                                                                          return final acc, adv examples list
```

After the for loop, compute accuracy of model after attack.

```
def test (model, device, test loader, epsilon):
                                                                               # Call ENM Attack
                                                                   35
                                                                              eps image = enm attack(image, epsilon)
                                                                   36
        # Counter for correct values (used for accuracy)
                                                                               # Re-classify the epsilon image
                                                                   37
        correct counter = 0
                                                                              output2 = model(eps image)
                                                                               # Get the index of the max log-probability
                                                                   39
        # List of successful adversarial samples
                                                                              eps pred = output 2.max(1, keepdim = True)[1]
                                                                   40
        adv examples list = []
                                                                   41
                                                                               # Check for successful attack
                                                                   42
9
        # Loop over all examples in test set
                                                                               # (Successful meaning eps pred label different from init pred)
                                                                   43
10
        for image, label in test loader:
                                                                              if eps pred.item() == label.item():
                                                                   44
11
                                                                                   correct counter += 1
                                                                   45
12
            # Send the data and label to the device
                                                                   46
                                                                                   # Special case for saving 0 epsilon examples
                                                                                   # (Maximal number of saved samples is set to 5)
13
            image, label = image.to(device), label.to(device)
                                                                                  if (epsilon == 0) and (len(adv examples list) < 5):</pre>
                                                                   48
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
                                                                   49
            # Pass the image through the model
                                                                                      adv examples liat.append((init pred.item(), eps pred.item(), adv ex))
                                                                   50
            output = model(image)
16
                                                                   51
                                                                               else:
            # Get the index of the max log-probability
17
                                                                   52
                                                                                   # Save some adv examples for visualization later
            init pred = output.max(1, keepdim = True)[1]
18
                                                                   53
                                                                                   # (Maximal number of saved samples is set to 5)
19
                                                                   54
                                                                                  if len(adv examples list) < 5:</pre>
            # If the initial prediction is wrong, do not
20
                                                                   55
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
            # bother attacking, skip current image
                                                                   56
                                                                                      adv_examples_list.appand((init_pred.item(), eps_pred.item(), adv_ex))
            if init pred.item() != label.item():
                                                                   57
                                                                         # Calculate final accuracy for this epsilon value
23
                 continue
                                                                   58
                                                                          final acc = correct counter/float(len(test loader))
                                                                   59
24
                                                                   60
25
            # Calculate the loss
                                                                           # Display for progress
                                                                   61
26
            loss = F.nll loss(output, label)
                                                                   62
                                                                          print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
27
                                                                   63
                                                                                                                                   correct counter, \
            # Zero all existing gradients
                                                                   64
                                                                                                                                  len(test loader), \
            model.zero grad()
                                                                   65
                                                                                                                                   final acc))
                                                                   66
            # Backpropagate
                                                                   67
                                                                           # Return the accuracy and an adversarial example
            loss.backward()
                                                                          return final acc, adv examples list
```

Testing Function

Display accuracy for given epsilon value. Return accuracy score and the list of five adversarial samples.

```
def test (model, device, test loader, epsilon):
                                                                               # Call ENM Attack
                                                                   35
                                                                              eps image = enn attack(image, epsilon)
                                                                   36
        # Counter for correct values (used for accuracy)
                                                                               # Re-classify the epsilon image
                                                                   37
        correct counter = 0
                                                                              output2 = model (eps image)
                                                                               # Get the index of the max log-probability
                                                                   39
        # List of successful adversarial samples
                                                                              eps pred = output2.max(1, keepdim = True)[1]
                                                                   40
        adv examples list = []
                                                                   41
                                                                   42
                                                                               # Check for successful attack
9
        # Loop over all examples in test set
                                                                               # (Successful meaning eps pred label different from init pred)
                                                                   43
10
        for image, label in test loader:
                                                                              if eps pred.item() == label.item():
                                                                   44
11
                                                                                   correct counter += 1
                                                                   45
12
            # Send the data and label to the device
                                                                   46
                                                                                   # Special case for saving 0 epsilon examples
                                                                                   # (Maximal number of saved samples is set to 5)
13
            image, label = image.to(device), label.to(device)
                                                                                  if (epsilon == 0) and (len(adv examples list) < 5):</pre>
                                                                   48
                                                                                      adv ex = eps image.squeeze().detach().cpu().numpy()
                                                                   49
            # Pass the image through the model
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
                                                                   50
            output = model(image)
16
                                                                   51
                                                                               else:
            # Get the index of the max log-probability
17
                                                                                   # Save some adv examples for visualization later
                                                                   52
18
            init pred = output.max(1, keepdim = True)[1]
                                                                   53
                                                                                   # (Maximal number of vaved samples is set to 5)
19
                                                                   54
                                                                                  if len(adv examples list) < 5:</pre>
20
            # If the initial prediction is wrong, do not
                                                                                      adv ex = eps image.queeze().detach().cpu().numpy()
                                                                   55
            # bother attacking, skip current image
                                                                   56
                                                                                      adv examples list.append((init pred.item(), eps pred.item(), adv ex))
            if init pred.item() != label.item():
                                                                   57
                                                                           # Calculate final accuracy for this epsilon value
23
                 continue
                                                                   58
                                                                          final acc = correct counter/float(lan(test loader))
24
                                                                   59
                                                                   60
25
            # Calculate the loss
                                                                   61
                                                                          # Display for progress
26
            loss = F.nll loss(output, label)
                                                                   62
                                                                          print("Epsilon: {} - Test Accuracy = {}/{} = {}".format(epsilon, \
27
                                                                   63
                                                                                                                                  correct counter, \
            # Zero all existing gradients
                                                                                                                                  len(test loader), \
                                                                   64
            model.zero grad()
                                                                   65
                                                                                                                                   final acc))
                                                                   66
            # Backpropagate
31
                                                                           # Return the accuracy and an adversarial example
                                                                   67
            loss.backward()
                                                                   68
                                                                          return final acc, adv examples list
```

- Please refer to Notebook 1.
 Using Epsilon Noising Attack to Generate Attack Samples.
- All notebooks this week follow the same structure
 - Dataset and Dataloader
 - (Pre-trained) Model
 - Attack function
 - Testing effect of attack on model

```
epsilons = [0, .1, .2, .5, 1, 2, 5, 10]
accuracies = []
examples = []

# Run test() function for each epsilon
for eps in epsilons:
    acc, ex = test(model, device, test_loader, eps)
accuracies.append(acc)
examples.append(ex)
```

```
Epsilon: 0 - Test Accuracy = 9810/10000 = 0.981

Epsilon: 0.1 - Test Accuracy = 9792/10000 = 0.9792

Epsilon: 0.2 - Test Accuracy = 9775/10000 = 0.9775

Epsilon: 0.5 - Test Accuracy = 9578/10000 = 0.9578

Epsilon: 1 - Test Accuracy = 6367/10000 = 0.6367

Epsilon: 2 - Test Accuracy = 2203/10000 = 0.2203

Epsilon: 5 - Test Accuracy = 1162/10000 = 0.1162

Epsilon: 10 - Test Accuracy = 1074/10000 = 0.1074
```

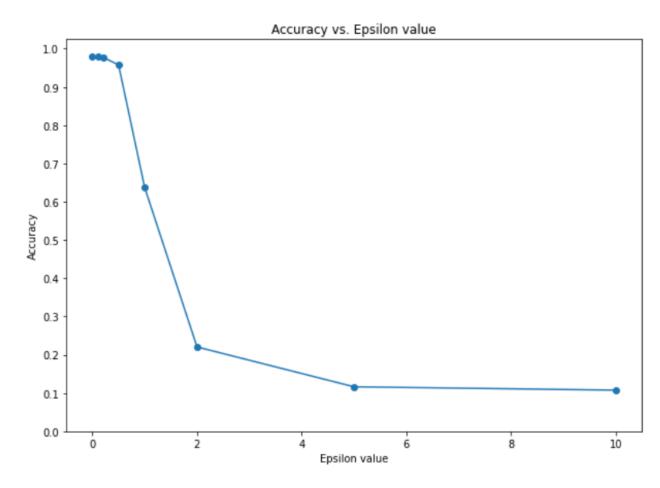
- Please refer to Notebook 1.
 Using Epsilon Noising Attack to Generate Attack Samples.
- All notebooks this week follow the same structure
 - Dataset and Dataloader
 - (Pre-trained) Model
 - Attack function
 - Testing effect of attack on model
 - Accuracy drop and attack samples visualization

Display a simple plot of accuracy vs. epsilon value for our given attack and model.

```
# Initialize figure
   plt.figure(figsize = (7, 10))
   # Display accuracy vs. Epsilon values plot
   plt.plot(epsilons, accuracies, "o-")
   # Adjust x-axis and y-axis labels and ticks
   plt.yticks(np.arange(0, 1.1, step = 0.1))
   \#plt.xticks(np.arange(0, .35, step = 0.05))
   plt.title("Accuracy vs. Epsilon value")
   plt.xlabel("Epsilon value")
   plt.ylabel("Accuracy")
13
   # Display
  plt.show()
```

- Please refer to Notebook 1.
 Using Epsilon Noising Attack to Generate Attack Samples.
- All notebooks this week follow the same structure
 - Dataset and Dataloader
 - (Pre-trained) Model
 - Attack function
 - Testing effect of attack on model
 - Accuracy drop and attack samples visualization

Display a simple plot of accuracy vs. epsilon value for our given attack and model.



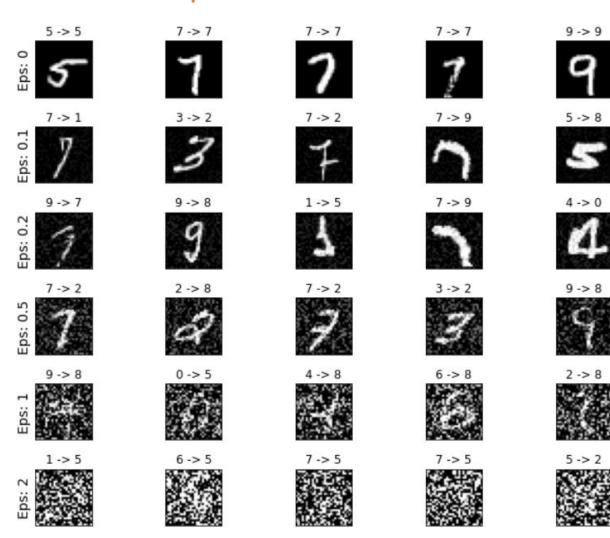
- Please refer to Notebook 1.
 Using Epsilon Noising Attack to Generate Attack Samples.
- All notebooks this week follow the same structure
 - Dataset and Dataloader
 - (Pre-trained) Model
 - Attack function
 - Testing effect of attack on model
 - Accuracy drop and attack samples visualization

Display some adversarial samples for each value of epsilon.

```
# Plot several examples of adversarial samples at each epsilon
   # Initialize figure
   plt.figure(figsize = (10, 10))
   # Browse through epsilon values and adversarial examples
   for i in range(len(epsilons)):
        for j in range(len(examples[i])):
10
            cnt += 1
11
            plt.subplot(len(epsilons), len(examples[0]), cnt)
12
            # Remove x-axis and y-axis ticks from plot
13
14
            plt.xticks([], [])
            plt.yticks([], [])
15
16
17
            # Labels for y axis
18
            if i == 0:
19
                plt.ylabel("Eps: {}".format(epsilons[i]), fontsize = 14)
20
21
            # Labels for each image subplot
2.2
            orig, adv, ex = examples[i][j]
23
            plt.title("{} -> {}".format(orig, adv))
24
25
            # Display image
26
            plt.imshow(ex, cmap = "gray")
2.7
   # Display full plot
   plt.tight layout()
30 plt.show()
```

- Please refer to Notebook 1.
 Using Epsilon Noising Attack to Generate Attack Samples.
- All notebooks this week follow the same structure
 - Dataset and Dataloader
 - (Pre-trained) Model
 - Attack function
 - Testing effect of attack on model
 - Accuracy drop and attack samples visualization

Display some adversarial samples for each value of epsilon.



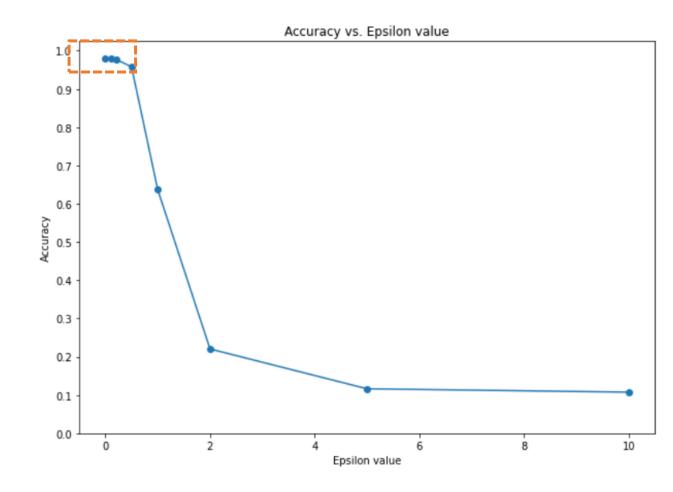
- Please refer to Notebook 1.
 Using Epsilon Noising Attack to Generate Attack Samples.
- All notebooks this week follow the same structure
 - Dataset and Dataloader
 - (Pre-trained) Model
 - Attack function
 - Testing effect of attack on model
 - Accuracy drop and attack samples visualization
 - Defense against such an attack



Effect of ENM on accuracy

Adding noise to an image tends to make the model malfunction.

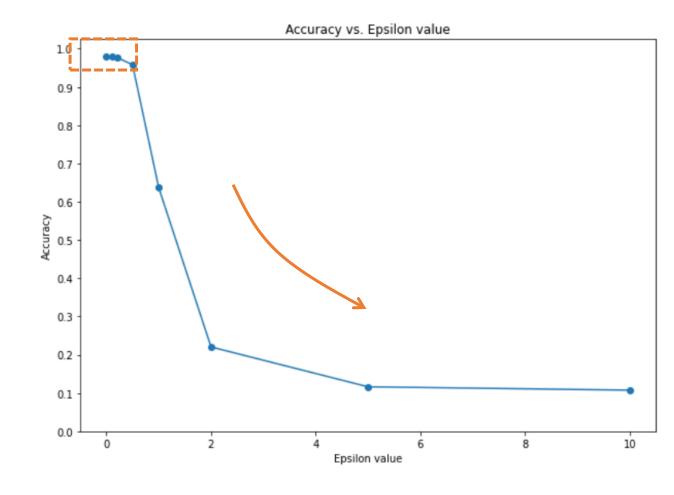
- When no noise (epsilon = 0), 98.1% accuracy.
 - This is our **baseline accuracy**.



Effect of ENM on accuracy

Adding noise to an image tends to make the model malfunction.

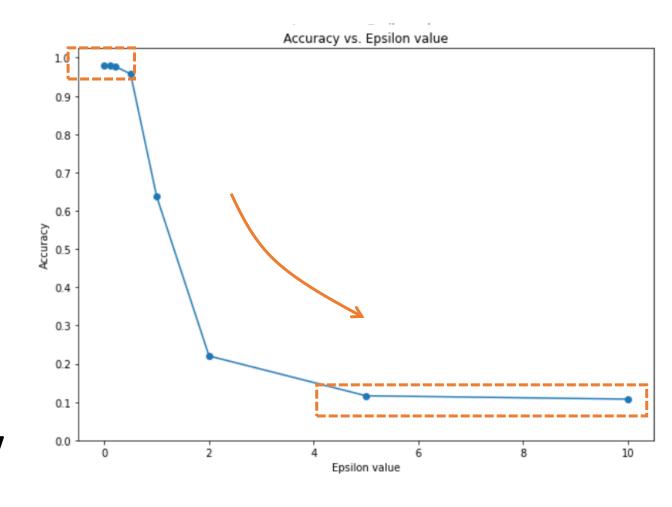
- When no noise (epsilon = 0), 98.1% accuracy.
 - This is our **baseline accuracy**.
- Accuracy decreases, the further we increment the noise amplitude epsilon.



Effect of ENM on accuracy

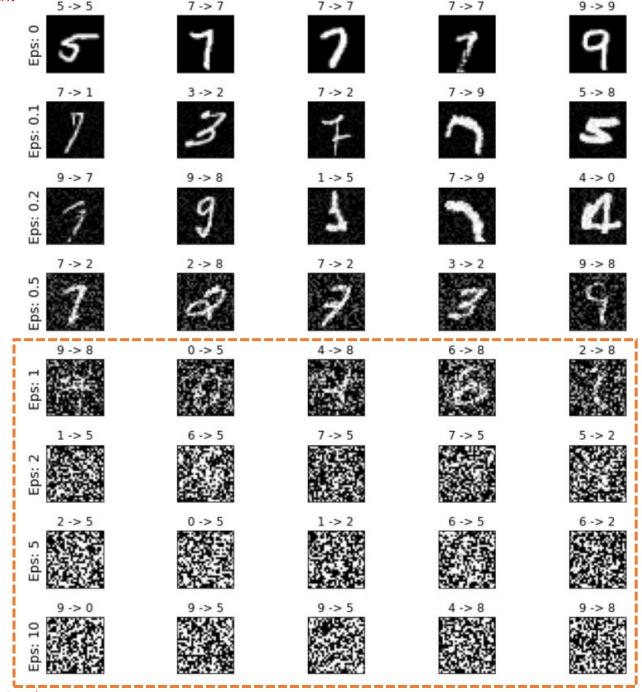
Adding noise to an image tends to make the model malfunction.

- When no noise (epsilon = 0), 98.1% accuracy.
 - This is our baseline accuracy.
- Accuracy decreases, the further we increment the noise amplitude epsilon.
- Eventually, with full noise (large epsilon), the image will be **randomly classified** (Accuracy $\sim 10\%$).



What makes a good attack sample?

- However, for large values of epsilon, the attack samples simply become random noise.
- This is mostly why the classifier ends up struggling.
- These are NOT considered good attack samples!
- (<u>Think:</u> humans would struggle to classify those as well!)



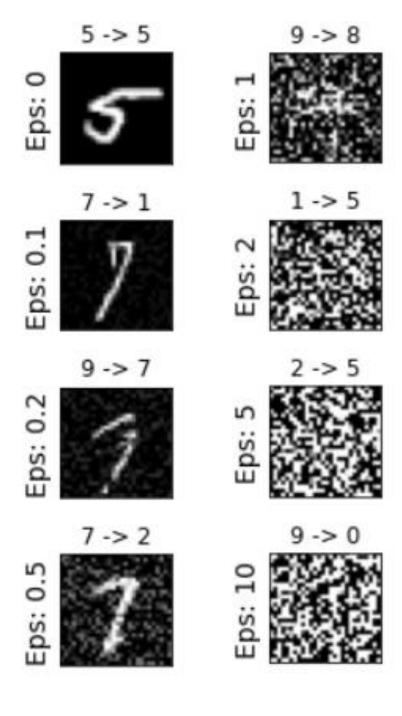
Restric

What makes a good attack sample?

Definition (what makes a "good" attack sample):

A "good" attack sample satisfies two properties:

- **1. Model failure:** it makes the model malfunction.
- 2. Plausibility: It looks "plausible" or "normal" to a human. It looks like it could have been a sample from the dataset.

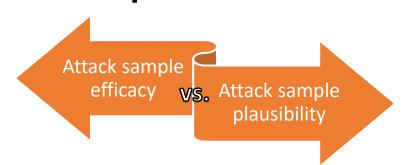


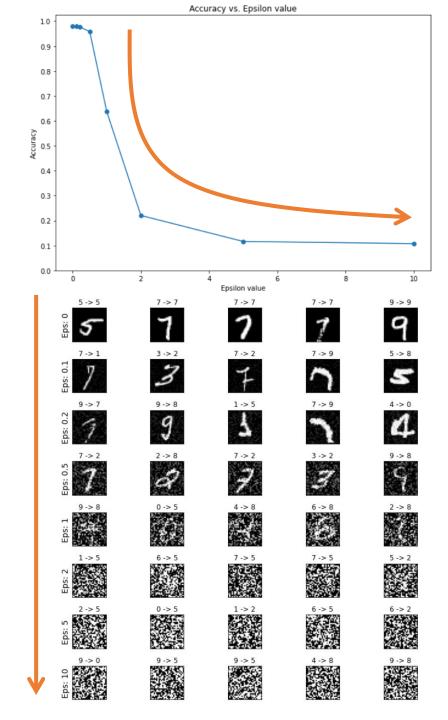
Attack samples tradeoff

Definition (attack samples tradeoff in adversarial ML):

Attack samples are subject to a **tradeoff**. In general,

- the higher the odds of the attack sample to make the model malfunction,
- the less plausible it will look.





Plausibility

• In general, we would like to have the generated attack sample \tilde{x} , to be "close enough" to the original sample x.

$$\forall i, j \in Pixel_Indexes_{x}$$

$$\tilde{x}_{i,j} = x_{i,j} + \omega_{i,j}$$

$$\left\{ \omega_{i,j} \to U([-\epsilon, \epsilon]) \quad (Unif.Dist.) \right\}$$

$$\left\{ \omega_{i,j} \to N([-\epsilon, \epsilon]) \quad (Normal Dist.) \right\}$$

Plausibility

- In general, we would like to have the generated attack sample \tilde{x} , to be "close enough" to the original sample x.
- This is a simple way to ensure plausibility for the attack sample.

$$\forall i, j \in Pixel_Indexes_{\chi}$$

$$\tilde{\chi}_{i,j} = \chi_{i,j} + \omega_{i,j}$$

$$\left\{ \omega_{i,j} \to U([-\epsilon, \epsilon]) \quad (Unif.Dist.) \right\}$$

$$\left\{ \omega_{i,j} \to N([-\epsilon, \epsilon]) \quad (Normal Dist.) \right\}$$

Plausibility

- In general, we would like to have the generated attack sample \tilde{x} , to be "close enough" to the original sample x.
- This is a simple way to ensure plausibility for the attack sample.
- In practice, we often enforce a constraint on a distance metric (or norm) between both the original image x and attack sample \tilde{x} .

$$\forall i, j \in Pixel_Indexes_{x}$$

$$\tilde{x}_{i,j} = x_{i,j} + \omega_{i,j}$$

$$\left\{ \begin{array}{l} \omega_{i,j} \to U([-\epsilon, \epsilon]) & (Unif.Dist.) \\ \omega_{i,j} \to N([-\epsilon, \epsilon]) & (Normal Dist.) \end{array} \right.$$

 $\|\widetilde{x} - x\| \le \alpha$, with α chosen arbitrarily

• L^0 norm: bounds the total number of pixels in \tilde{x} that can be modified with respect to x (though they can be modified by any amount).

$$\|\tilde{x} - x\|_0 = card(\{(i,j) \text{ s. t. } x_{i,j} \neq \tilde{x}_{i,j}\})$$

- L^0 norm: bounds the total number of pixels in \tilde{x} that can be modified with respect to x (though they can be modified by any amount).
- L^1 norm: bounds the average absolute distance between the values of pixels in \tilde{x} and the corresponding pixels in x.

$$\|\tilde{x} - x\|_1 = \frac{1}{N} \sum_{i,j} |\tilde{x}_{i,j} - x_{i,j}|, \quad \text{with N the number of pixels}$$

- L^0 norm: bounds the total number of pixels in \tilde{x} that can be modified with respect to x (though they can be modified by any amount).
- L^1 norm: bounds the average absolute distance between the values of pixels in \tilde{x} and the corresponding pixels in x.
- L^2 norm: bounds the total squared distance between the values of pixels in \tilde{x} and the corresponding pixels in x. Most commonly referred to as Euclidean distance.

$$\|\tilde{x} - x\|_2 = \frac{1}{N} \sqrt{\sum_{i,j} (\tilde{x}_{i,j} - x_{i,j})^2}$$
, with N the number of pixels

- L^0 norm: bounds the total number of pixels in \tilde{x} that can be modified with respect to x (though they can be modified by any amount).
- L^1 norm: bounds the average absolute distance between the values of pixels in \tilde{x} and the corresponding pixels in x.
- L^2 norm: bounds the total squared distance between the values of pixels in \tilde{x} and the corresponding pixels in x. Often referred to as the Euclidean distance.
- L^{∞} norm: bounds the maximum difference between any pixel in \tilde{x} and the corresponding pixel in x. Often referred to as max norm.

$$\|\tilde{x} - x\|_{\infty} = \max_{i,j} (|\tilde{x}_{i,j} - x_{i,j}|)$$

- L^0 norm: bounds the total number of pixels in \tilde{x} that can be modified with respect to x (though they can be modified by any amount).
- L^1 norm: bounds the average absolute distance between the values of pixels in \tilde{x} and the corresponding pixels in x.
- L^2 norm: bounds the total squared distance between the values of pixels in \tilde{x} and the corresponding pixels in x. Often referred to as the Euclidean distance.
- L^{∞} norm: bounds the maximum difference between any pixel in \tilde{x} and the corresponding pixel in x. Often referred to as max norm.

$$\|\tilde{x} - x\|_{\infty} = \max_{i,j} (|\tilde{x}_{i,j} - x_{i,j}|)$$

preferred one!

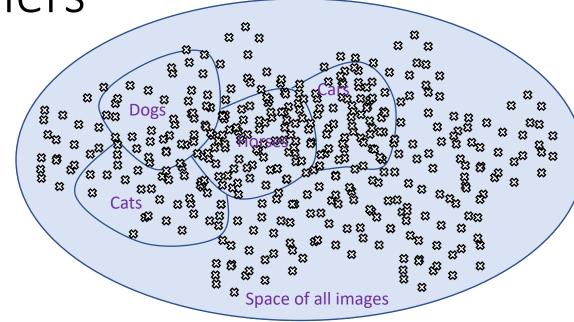
• Expectation for Neural Networks: Just like with human perception, small changes on inputs should not yield a different label!

- Unfortunately, deep learning predictions are different: Deep learning algorithms process data differently from humans, with strong discontinuities in the change of prediction as a function the inputs.
- And that is the reason for their vulnerability to attacks.

Following: A tentative of explaining why that is the case (not the absolute truth, but my intuition as to why this happens!)

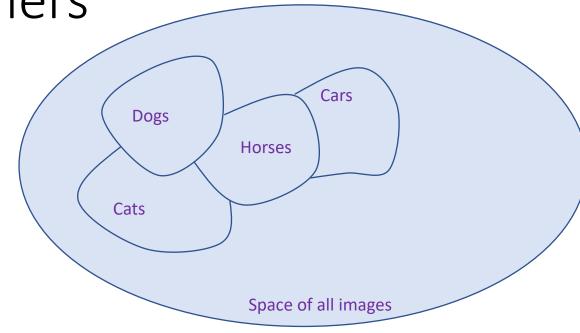
Consider the arbitrary representation, with regions and boundaries between them.

 Misconception #1: the whole space of possible inputs was densely filled with training examples during training.



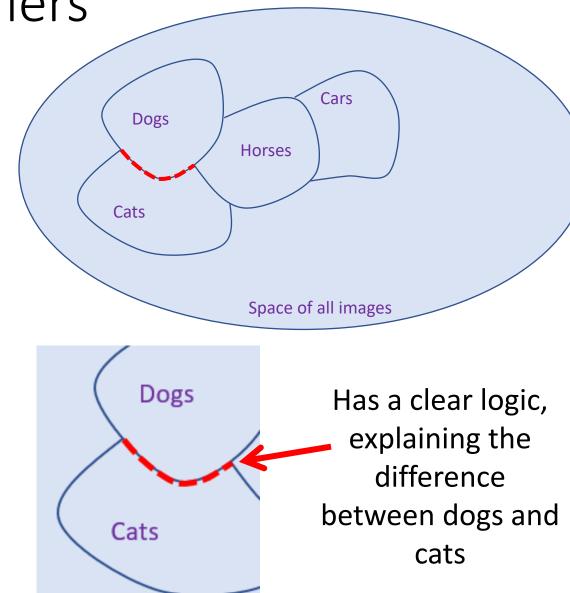
Consider the arbitrary representation, with regions and boundaries between them.

- Misconception #1: the whole space of possible inputs was densely filled with training examples during training.
- Misconception #2: regions are contiguous and filled with samples.

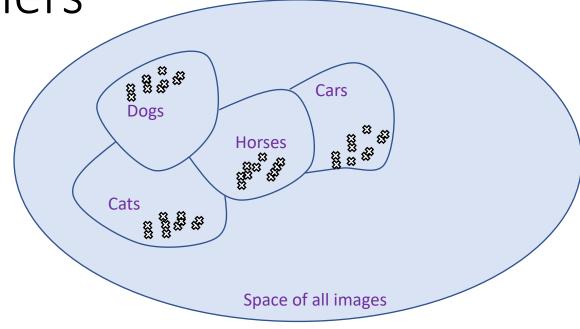


Consider the arbitrary representation, with regions and boundaries between them.

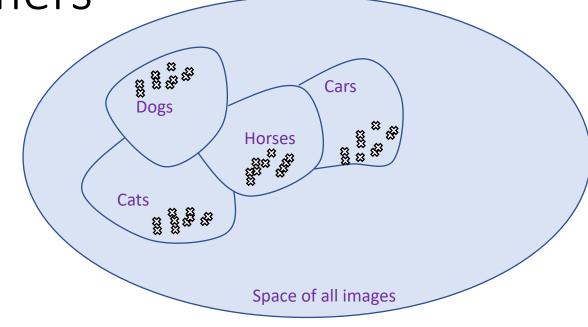
- Misconception #1: the whole space of possible inputs was densely filled with training examples during training.
- Misconception #2: regions are contiguous and filled with samples.
- Misconception #3: the decision boundaries between classes are smooth and make perfect sense.



- Misconception #1: the whole space of possible inputs was densely filled with training examples during training.
- Correction #1: the space is mostly noise images and sparsely filled with relevant training examples.
- Also, the training samples do not cover for all possible relevant images.

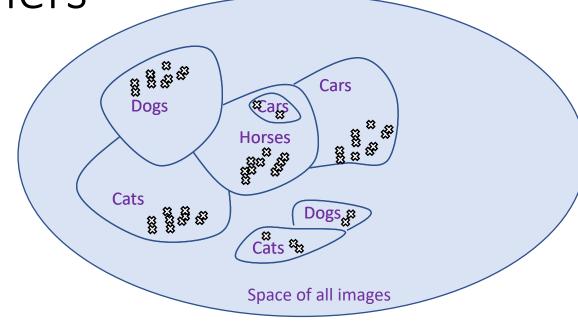


- Misconception #1: the whole space of possible inputs was densely filled with training examples during training.
- Correction #1: the space is mostly noise images and sparsely filled with relevant training examples.
- Also, the training samples do not cover for all possible relevant images.



E.g. MNIST contains 28 by 28 pixels images, with pixel values in [0, 255]. The whole space is roughly $(256)^{28\times28}\approx 10^{1888}$ images, and most of them are noise. The MNIST dataset contains 60000 images only.

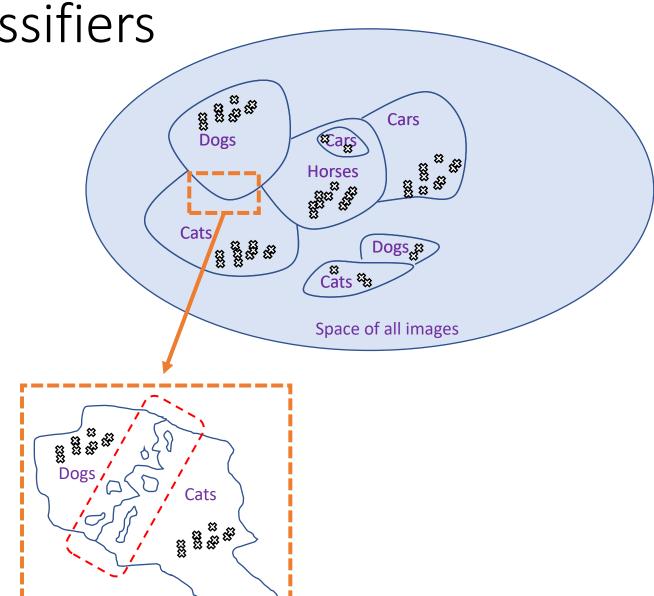
- Misconception #2: regions are contiguous and filled with samples.
- Correction #2: regions will not necessarily be contiguous.



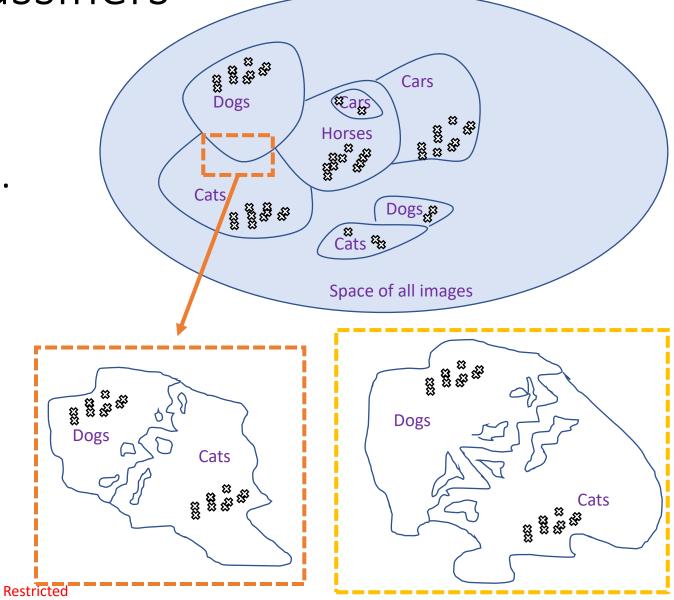
Restricted

Impact of noise on classifiers

- Misconception #2: regions are contiguous and filled with samples.
- Correction #2: regions will not necessarily be contiguous.
 Boundaries between classes might even be very erratic!



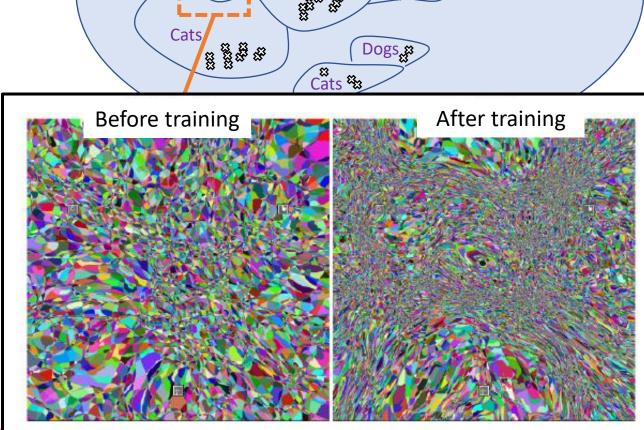
- Misconception #3: the decision boundaries between classes are smooth and make perfect sense.
- Correction #3: In fact, the boundaries between samples are often "randomly" decided.
- On different epochs, the boundaries might change randomly.



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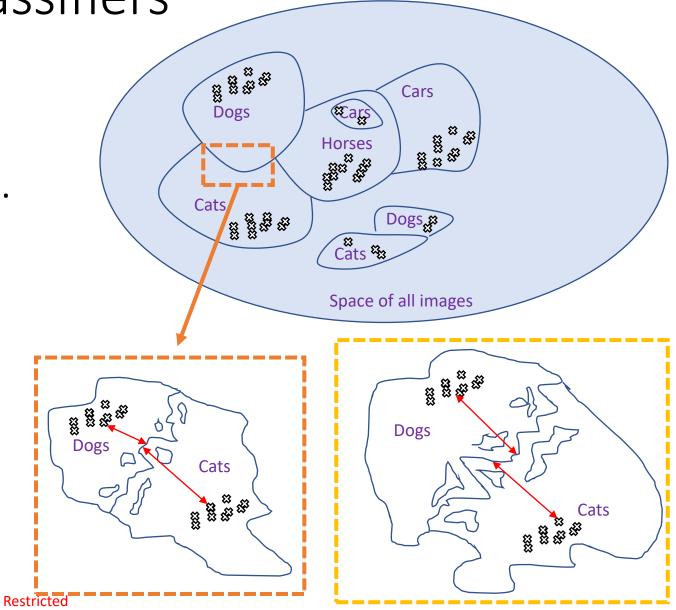
Horses

Cars

E E E E

Dogs

- Misconception #3: the decision boundaries between classes are smooth and make perfect sense.
- Correction #3-bis: Training samples are often condensed, far away from the boundaries.

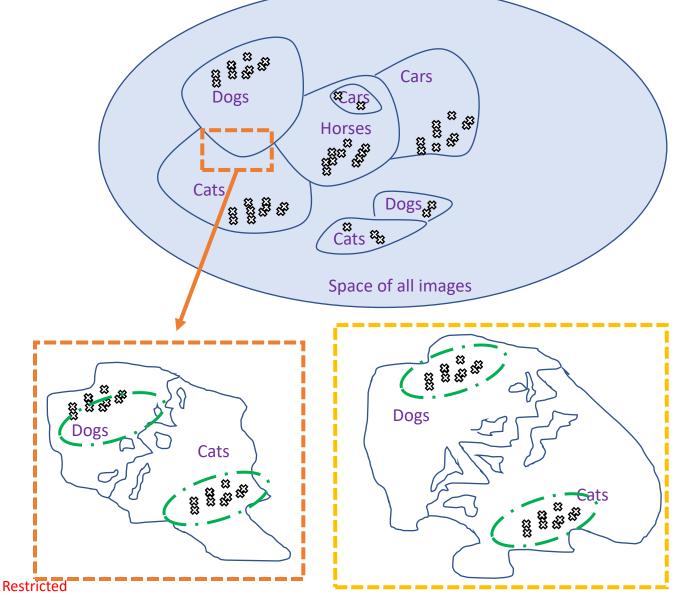


Correction #3-bis: Training samples are often condensed, far away from the boundaries.

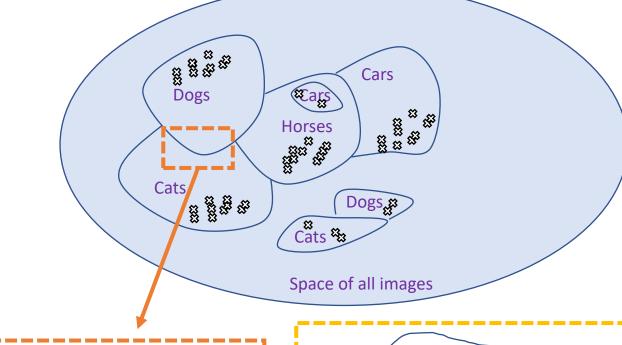
Definition (manifolds):

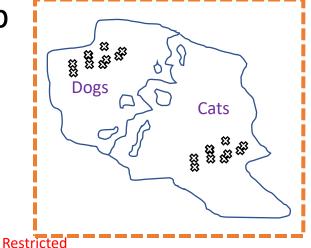
These small regions containing a large number of training examples are mathematically called manifolds.

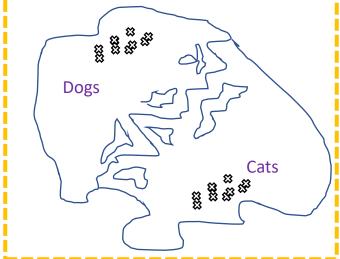
See [TDS1], if curious.



- Misconception #3: the decision boundaries between classes are smooth and make perfect sense.
- Correction #3-bis: Training samples are often condensed, far away from the boundaries.
- Boundaries decided by the Deep Learning models often exhibit the same behavior as the Support Vector Machines boundaries. But in a more random manner.



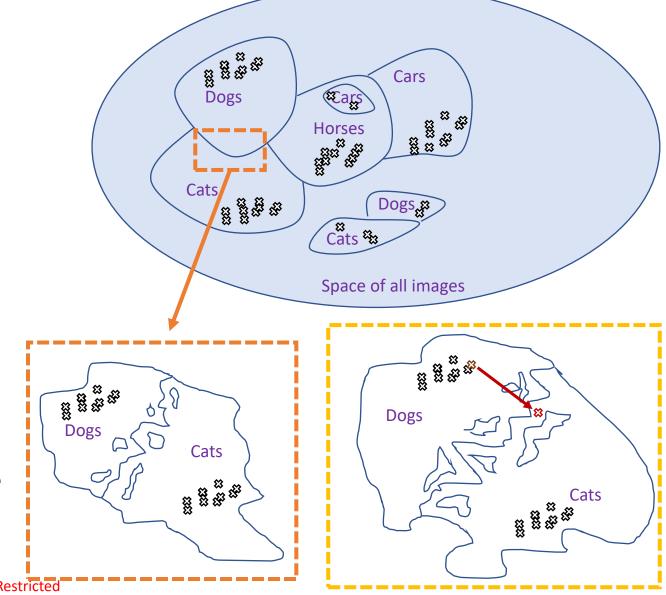




ENM prdocure, explained:
 When randomly noising an
 original sample to make an
 attack sample, we move
 randomly in the feature map.

 We may even move in the boundary region, where the sample might become misclassified.

• The attack sample will therefore look similar to a dog picture, but will be misclassified as a cat.



Here is my intuition about attacks. (Again, not claiming it is the universal truth, free from counter examples.)

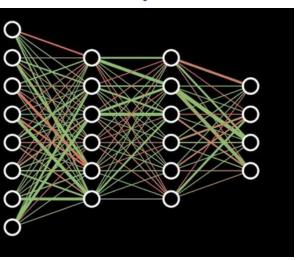
- In Deep Learning, to learn means to understand that some objects are similar on certain aspects/features and use that for classification.
- It means to discard irrelevant information which does not contribute to understand those similarities.





Cat or Dog Picture (high dimensional input)





Neural Network, processing input image



from dogs? No, discard info.

Is the **presence of fur** relevant for discerning cats



Is the **shape of eyes** relevant for discerning cats from dogs? **Yes, process info.**

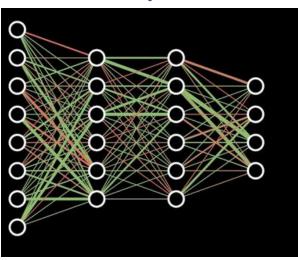
- Discarding information is achieved by progressively compressing input data into a space of lower dimensionality using several Neural Networks layers.
- A linear neuron would achieve this, by mapping inputs onto a lower-dimension hyperplane, and learns projections of the training data.





Cat or Dog Picture (high dimensional input)





Neural Network, processing input image



$$\boldsymbol{a} = [a_1 \quad a_2 \quad \dots \quad a_n]$$

Lower dimensional vector produced by final hidden layer of Neural Network.

Neural Network then aims to map similar objects close together in this low dimensionality space.

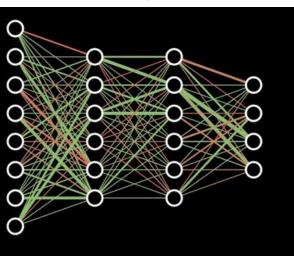
- For instance, all pictures of cats will produce vectors a, with roughly similar values. Same thing for dogs.
- Cats vectors and dogs vectors will, however, be very different!
- Final layer implements binary decision on vector *a*.





Cat or Dog Picture (high dimensional input)





Neural Network, processing input image



$$oldsymbol{a} = \left[egin{array}{cccc} a_1 & a_2 & \dots & a_n \end{array}
ight].$$

Lower dimensional vector produced by final hidden layer of Neural Network.

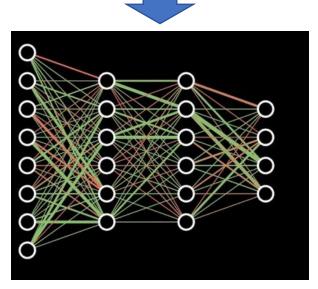
- Due to compression, there are many directions in a high dimension feature space along which a small step might lead to big changes in predictions.
- In zones with low training data densities, the decision boundaries can lie very close together, because they were never properly learned from training samples!





Cat or Dog Picture (high dimensional input)

Small change here...

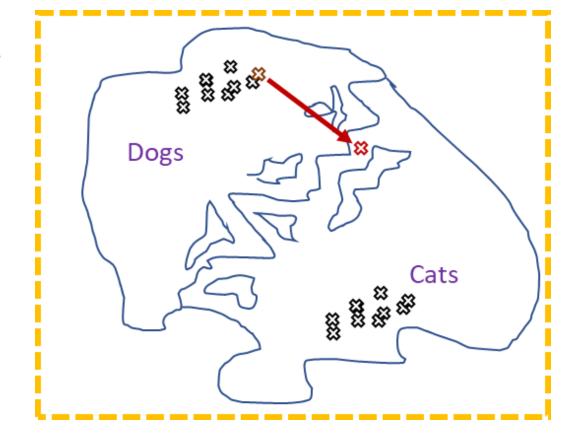


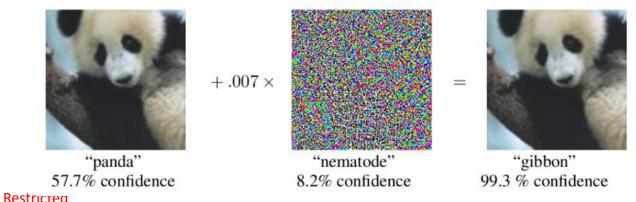
Neural Network, processing input image

... Huge change $oldsymbol{a} = [a_1 \quad a_2 \quad \dots \quad a_n]$.

Lower dimensional vector produced by final hidden layer of Neural Network.

- In zones with low training data densities, some small changes on an input can then lead to big changes in predictions produced by the trained Neural Network.
- And that is what we exploit to generate attack samples!





 → Unfortunately, this means that all deep learning models will always be susceptible to attacks.
 (And that is something we have to accept.)

 → Unfortunately, this means that all deep learning models will always be susceptible to attacks.
 (And that is something we have to accept.)

So what?

Is that it then?

Are Neural Networks flawed beyond repair? Are we giving up on Neural Networks then?

Reason #2: Defense

Definition (Defense on Neural Networks):

In adversarial machine learning, defense refers to machine learning techniques that attempt to protect models from being attacked by malicious attempts.

Important: defense mechanisms often rely on an understanding of how attacks work.



Conclusion (W5S1)

- Attacks on Neural Networks, a definition.
- Our first attack, simply by noising images.
- Attacks exploits intrinsic limitations that deep learning models will always have.
- We can defend against attacks.
- The random noise attacks are very random with unpredictable efficacy.

- These random noise attacks will not necessarily move the samples towards the boundary region.
- Advanced attacks techniques will improve on this matter.
 More on this later!
- Defense mechanics will attempt to prevent these attacks from working.

Out of class, supporting papers, for those of you who are curious.

• [Xie2017] Xie at al., "Adversarial Examples for Semantic Segmentation and Object Detection", 2017.

https://arxiv.org/abs/1703.08603

• [Szegedy2013] Szegedy et al., "Intriguing properties of neural networks", 2013.

https://arxiv.org/abs/1312.6199

• [Moosavi2017] Moosavi-Dezfooli et al., "Universal adversarial perturbations", 2017.

https://arxiv.org/abs/1610.08401

• [Hayes2017] Hayes et al., "Learning Universal Adversarial Perturbations with Generative Models", 2017. https://arxiv.org/abs/1708.05207

• [Goodfellow2018] **Goodfellow** et al., "Making machine learning robust against adversarial inputs", 2018.

https://dl.acm.org/doi/10.1145/3134599

Some extra (easy) reading and videos for those of you who are curious.

• [Verge1] Google's AI thinks this turtle looks like a gun, which is a problem:

https://www.theverge.com/2017/11/2/16597276/google-ai-image-attacks-adversarial-turtle-rifle-3d-printed

• [Spectrum1] Slight Street Sign Modifications Can Completely Fool Machine Learning Algorithms:

https://spectrum.ieee.org/cars-thatthink/transportation/sensors/slight-street-sign-modifications-canfool-machine-learning-algorithms

- [Verge2] These glasses trick facial recognition software into thinking you're someone else:
 - https://www.theverge.com/2016/11/3/13507542/facial-recognition-glasses-trick-impersonate-fool
- [YTB1] Defeating Facial Recognition: https://www.youtube.com/watch?v=tbdcL5Ux-9Y

• [TDS1] Manifolds in Data Science — A Brief Overview: https://towardsdatascience.com/manifolds-in-data-science-a-brief-overview-2e9dde9437e5