50.039 Theory and Practice of Deep Learning W11-S3 More on Reinforcement Learning

Matthieu De Mari



Introduction

- 1. What are **actor-critic** learning methods? And which problems do these approaches address?
- 2. What are more advanced problems in RL?
 - Markov states
 - Partially observable environment
 - SARSA
 - Non-stationary problems
- 3. What is Reinforcement Learning with Human Feedback (RLHF)?

Time for something a bit more advanced! (cont'd)

Definitely out-of-scope, but interesting nonetheless!

A representation problem

- Problem: in many RL problems, the states and/or actions sets are not necessarily finite.
- In that case, it is impossible to represent the Q and V functions as tables.
- And, even worse, for these problems, coming up with a closed form expression of the V and Q functions might prove challenging.

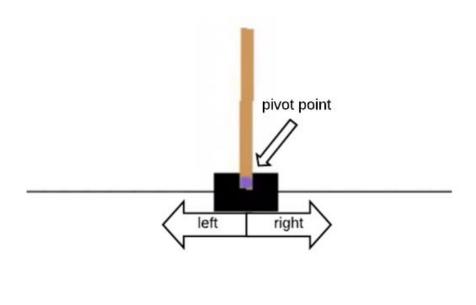
Q-Table				Actions		
		South (0)	North (1)	East (2)	West (3)	
	0	0	0	0	0	
States						
	327	0	0	0	0	
	499	0	0	0	0	



Q-Table		Actions			ons
		South (0)	North (1)	East (2)	West (3)
States	0	0	0	0	0
	328	-2.30108105	-1.97092096	-2.30357004	-2.20591839
	499	9.96984239	4.02706992	12.96022777	29

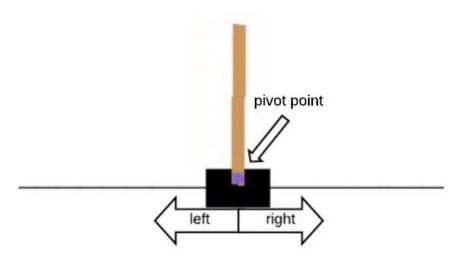
Example: the cart-pole problem.

- **State:** our current visualization of the cart (i.e. an image).
- Actions: 2 of them, go left or go right at a fixed speed.
- Reward: +1 for each unit of time where the cart does not leave the screen and the pole does not fall below a certain angle.
- Next state generation: cart and pole both follow simple programmed rules of physics.



- Problem: in many RL problems, the states and/or actions sets are not necessarily finite.
- In that case, it is impossible to represent the Q and V functions as tables.

- How do we address this issue?
- Give it to an Al! (as usual)



- **Solution:** replace the *Q*-table with a Deep Neural Network, whose job is to estimate the value of each action (left/right) in the current state.
- The objective is then to train, just like before with our *Q*-table.
- However, we are no longer changing the table values but the Neural Net parameters!

```
class DON(nn.Module):
       def init (self, h, w, outputs):
           super(DQN, self). init ()
           self.conv1 = nn.Conv2d(3, 16, kernel size=5, stride=2)
           self.bn1 = nn.BatchNorm2d(16)
           self.conv2 = nn.Conv2d(16, 32, kernel size=5, stride=2)
           self.bn2 = nn.BatchNorm2d(32)
           self.conv3 = nn.Conv2d(32, 32, kernel size=5, stride=2)
10
           self.bn3 = nn.BatchNorm2d(32)
11
            # Number of Linear input connections depends on output of conv2d layers
12
13
            # and therefore the input image size, so compute it.
14
           def conv2d size out(size, kernel size = 5, stride = 2):
               return (size - (kernel size - 1) - 1) // stride + 1
15
           convw = conv2d size out(conv2d size out(conv2d size out(w)))
16
           convh = conv2d size out(conv2d size out(conv2d size out(h)))
17
           linear input size = convw * convh * 32
18
           self.head = nn.Linear(linear input_size, outputs)
19
20
21
        # Called with either one element to determine next action, or a batch
22
        # during optimization. Returns tensor([[left0exp,right0exp]...]).
23
       def forward(self, x):
24
           x = F.relu(self.bn1(self.conv1(x)))
25
           x = F.relu(self.bn2(self.conv2(x)))
26
           x = F.relu(self.bn3(self.conv3(x)))
           return self.head(x.view(x.size(0), -1))
```

- On each round of the game, use the Q network to compute the Q-value of both actions (left/right) in the current state.
- Use the one with the maximal value (**exploitation**) or a randomly chosen action (**exploration**).
- Use ϵ -greedy policy to decide how to explore/exploit.

```
def select action(state):
        global steps done
        sample = random.random()
        eps_threshold = EPS_END + (EPS_START - EPS_END) * \
    math.exp(-1. * steps_done / EPS_DECAY)
        steps done += 1
        if sample > eps threshold:
            with torch.no grad():
                 # Here, t.max(1) will return largest column value of each row.
10
                 # Second column on max result is index of where max element was
                 # found, so we pick action with the larger expected reward.
11
                 return policy net(state).max(1)[1].view(1, 1)
12
13
        else:
14
            return torch.tensor([[random.randrange(n actions)]], device=device, dtype=torch.long)
```

Toy example #3

To train this DNN, we need a dataset of some sort.

- Do so by playing the game multiple times and keeping a history of the (state, action, rewards, next_state, done) tuples.
- Here, done indicates that the game has ended (out of screen or low angle on pole).
- Structure is roughly similar to our dataloaders?

```
# Define namedtuples for transitions and history
Transition = namedtuple('Transition', ('state', 'action', 'next_state', 'reward'))
```

```
class ReplayMemory(object):
       def init (self, capacity):
           self.capacity = capacity
            self.memory = []
            self.position = 0
       def push(self, *args):
           Saves a transition to memory.
11
12
           if len(self.memory) < self.capacity:</pre>
13
                self.memory.append(None)
14
            self.memory[self.position] = Transition(*args)
15
            self.position = (self.position + 1) % self.capacity
16
       def sample(self, batch size):
18
19
           Get sample from history.
20
21
           return random.sample(self.memory, batch size)
22
23
       def __len__(self):
24
25
           Get length of history (number of samples).
26
           return len(self.memory)
```

- Core idea for memory replay: we are trying to approximate a complex, nonlinear function Q, with a Neural Network.
- To do this, we must calculate targets using the **Bellman equation** and then consider that we have a **supervised learning** problem at hand.
- **Important:** However, one of the fundamental requirements for SGD optimization is that the training data is independent and identically distributed and when the Agent interacts with the game, the sequence of experience tuples can be highly correlated.
- The naive Q-learning algorithm that learns from each of these experiences tuples in sequential order runs the risk of getting swayed by the effects of this correlation.

Definition (experience buffer in RL):

- We can prevent action values from oscillating or diverging catastrophically using a large buffer of our past experience and sample training data from it, instead of using our latest experience.
- This is called an experience buffer.
- The experience buffer contains a collection of experience tuples (state, action, rewards, next_state).
- The tuples are gradually added to the buffer as the agents keep on interacting with the game.

Definition (experience replay):

- The simplest implementation is a buffer of fixed size, with new data added to the end of the experience buffer, so that it pushes the oldest experience out of it.
- The act of sampling a small batch of tuples from the experience buffer in order to learn is known as experience replay.
- In addition to breaking harmful correlations, experience replay allows us to learn more from individual tuples multiple times, recall rare occurrences, and in general make better use of our experience.

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16
17
       def sample(self, batch size):
18
19
           Get sample from history.
20
21
           return random.sample(self.memory, batch size)
22
23
       def len (self):
24
25
           Get length of history (number of samples).
26
           return len(self.memory)
```

To train this DNN, we need a loss function and weight update procedure of some sort, as well.

Our previous Q-learning was using this iterative update formula.

$$Q^{new}(s_t, a_t) \leftarrow \underbrace{Q(s_t, a_t)}_{ ext{old value}} + \underbrace{lpha}_{ ext{learning rate}} \cdot \underbrace{\left(\underbrace{r_t}_{ ext{reward}} + \underbrace{\gamma}_{ ext{discount factor}} \cdot \underbrace{\max_{a} Q(s_{t+1}, a)}_{ ext{estimate of optimal future value}} - \underbrace{Q(s_t, a_t)}_{ ext{old value}} \right)}_{ ext{new value (temporal difference target)}}$$

temporal difference

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• **Problem:** update $Q(s_t, a)$ via $Q(s_{t+1}, a)$. However, both states have only one step between them. This makes them very similar, and it is very hard for a Neural Network to distinguish between them.

Solution: use **two Neural Networks**, one for **training** $Q(s_t, a)$ and one for producing **targets** $Q(s_{t+1}, a)$, or **evaluating** the other.

- That is, the predicted Q values of this second Q-network called the target network, are used to backpropagate through and train the main Q-network.
- **Note:** the target network's parameters are <u>not trained</u>, but they are periodically synchronized with the parameters of the main Q-network.
- The idea is that using the target network's Q values to train the main Q-network will improve the stability of the training.

```
1 def optimize model():
       if len(memory) < BATCH SIZE:</pre>
           return
       transitions = memory.sample(BATCH SIZE)
       # Transpose the batch (see https://stackoverflow.com/a/19343/3343043 for
       # detailed explanation). This converts batch-array of Transitions
       # to Transition of batch-arrays.
       batch = Transition(*zip(*transitions))
 9
10
        # Compute a mask of non-final states and concatenate the batch elements
11
        # (a final state would've been the one after which simulation ended)
12
       non final mask = torch.tensor(tuple(map(lambda s: s is not None,
13
                                             batch.next state)), device=device, dtype=torch.bool)
14
       non final next states = torch.cat([s for s in batch.next state
15
                                                   if s is not Nonel)
16
       state batch = torch.cat(batch.state)
17
       action batch = torch.cat(batch.action)
18
       reward batch = torch.cat(batch.reward)
19
20
       # Compute Q(s t, a) - the model computes Q(s t), then we select the
21
       # columns of actions taken. These are the actions which would've been taken
22
       # for each batch state according to policy net
23
       state action values = policy net(state batch).gather(1, action batch)
24
       # Compute V(s \{t+1\}) for all next states.
25
26
       # Expected values of actions for non final next states are computed based
       # on the "older" target net; selecting their best reward with max(1)[0].
27
       # This is merged based on the mask, such that we'll have either the expected
28
29
       # state value or 0 in case the state was final.
30
       next state values = torch.zeros(BATCH SIZE, device=device)
       next state values[non final mask] = target net(non final next states).max(1)[0].detach()
31
32
       # Compute the expected Q values
33
       expected state action values = (next state values * GAMMA) + reward batch
34
35
        # Compute Huber loss
36
       loss = F.smooth 11 loss(state action values, expected state action values.unsqueeze(1))
37
       # Optimize the model
38
39
       optimizer.zero grad()
       loss.backward()
40
41
       for param in policy net.parameters():
           param.grad.data.clamp (-1, 1)
42
43
       optimizer.step()
```

To train this DNN, we need a loss function and weight update procedure of some sort.

To create a loss function, let us first recall that

$$Q_t^{\pi}(s_t, a_t) = R_t(s_t, a_t) + \gamma Q_{t+1}^{\pi}(s_{t+1}, \pi(s_{t+1}))$$

Let us denote the error δ as

$$\delta = Q_t^{\pi}(s_t, a_t) - \left(R_t(s_t, a_t) + \gamma \max_{a} Q_{t+1}^{\pi}(s_{t+1}, a)\right)$$

To train this DNN, we need a loss function and weight update procedure of some sort.

To train our DNN, we want to minimize this error δ .

We will use the L1 norm on delta to do so.

$$L(\delta) = |\delta|$$

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Note: we can also use a slightly different loss function known as the **Huber loss**, which is slightly more robust to outliers.

$$L_d(\delta) = \begin{cases} \frac{1}{2}\delta^2 & if \ |\delta| \le d \\ d\left(|\delta| - \frac{1}{2}d\right) & else \end{cases}$$

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```

Restricted

Trainer function

- Our trainer function will play the game 500 times.
- Keep track of different histories over the 500 games.
- Sample from history to train our main *Q*-Network.
- Backpropagate with mixed main and target *Q*-networks values.
- Occasionally update the target network.

```
Full trainer on 500 iteration (for meaningful improvements)
        num episodes = 500
        for i episode in range (num episodes):
             print("Episode:", i episode)
             # Initialize the environment and state
             env.reset()
             last screen = get screen()
             current screen = get screen()
     11
             state = current screen - last screen
    12
             for t in count():
     13
                 # Select and perform an action
    14
                 action = select action(state)
                 , reward, done, _ = env.step(action.item())
     15
     16
                 reward = torch.tensor([reward], device=device)
    17
     18
                 # Observe new state
     19
                 last screen = current screen
     20
                 current screen = get screen()
     21
                 if not done:
     22
                     next_state = current_screen - last_screen
     23
                 else:
     24
                     next state = None
     25
     26
                 # Store the transition in memory
     27
                 memory.push(state, action, next state, reward)
     28
     29
                 # Move to the next state
                 state = next state
     31
     32
                 # Perform one step of the optimization (on the policy network)
     33
                 optimize model()
     34
                 if done:
     35
                     episode durations.append(t + 1)
     36
                     plot durations()
     37
     38
             # Update the target network, copying all weights and biases in DQN
             if i episode % TARGET UPDATE == 0:
     39
                 target net.load state dict(policy net.state dict())
Restricted
```

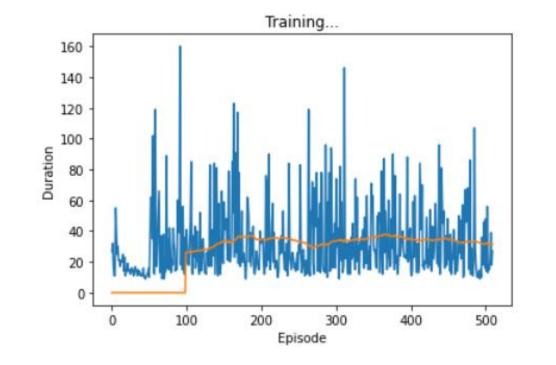
Restricted

Training results

- Our RL agent will learn to balance the pole on the cart, by playing the game.
- Can display the length of each game/episode to see the progression!

 This RL approach of training some DNNs to replace the Q functions is commonly referred to as Deep Q-learning.

```
def plot durations():
        Show episode durations for each episode.
        plt.figure(2)
       plt.clf()
        durations t = torch.tensor(episode durations, dtype=torch.float)
        plt.title('Training...')
        plt.xlabel('Episode')
        plt.ylabel('Duration')
11
        plt.plot(durations t.numpy())
12
        # Take 100 episode averages and plot them too
13
        if len(durations t) >= 100:
            means = durations t.unfold(0, 100, 1).mean(1).view(-1)
14
15
            means = torch.cat((torch.zeros(99), means))
16
            plt.plot(means.numpy())
```



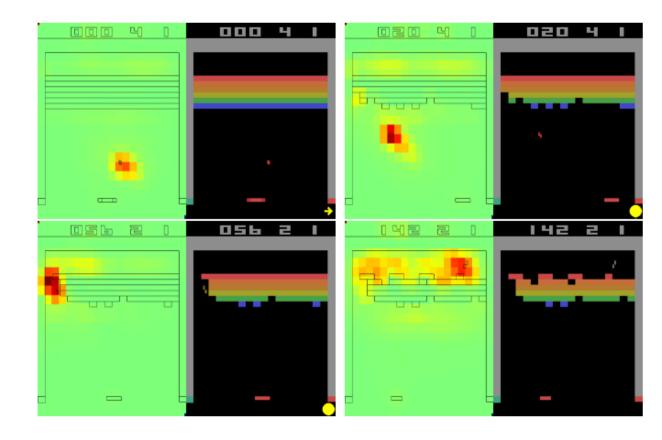
Following this cart-pole balance idea...

- Train an AI to keep a robot on its feet, despite some "minor environment perturbations" (a polite way of saying you kick the hell out of the robot for fun).
- Video: <u>https://www.youtube.com/watc</u> h?v=NR32ULxbjYc
- BostonDynamics blog: <u>https://blog.bostondynamics.co</u> <u>m/</u>



Following this idea of using computer vision to identify state and act...

- Train an AI to play video games with Deep Reinforcement Learning (Mnih, 2013)!
- Paper:
 https://www.cs.toronto.edu/~v
 mnih/docs/dqn.pdf
- Video: <u>https://www.youtube.com/watc</u> <u>h?v=TmPfTpjtdgg</u>



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> Replace more elements of the RL system with Deep Neural Networks.

Definition (actor-critic):

Actor-critic algorithms consist of two components.

• **Actor:** a DNN, whose purpose is to produce actions in response to given states, i.e. a policy. Can be trained as in Deep Q-learning.

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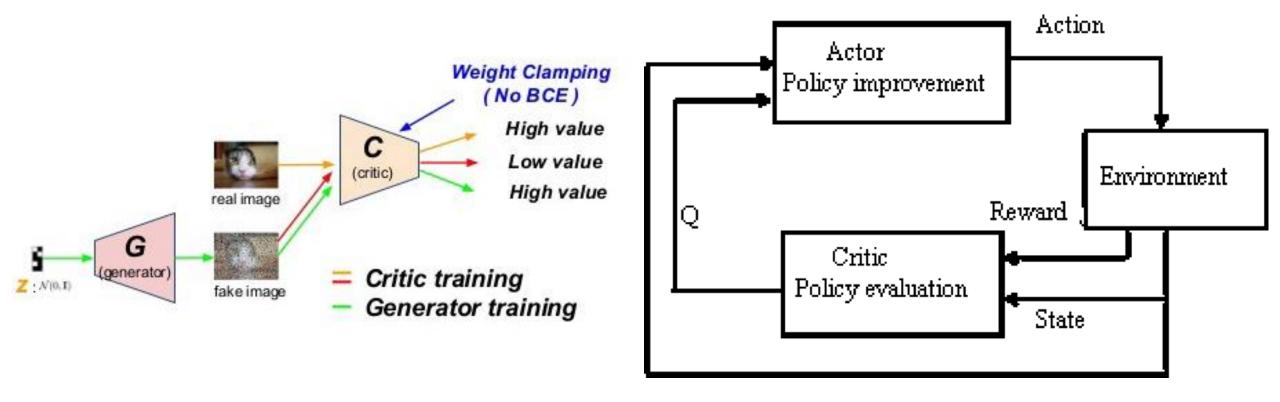
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- **Critic:** a DNN, whose purpose is to evaluate the quality of the selected actions and suggesting directions for improvement, by defining a reward function or a *Q* function.

In a sense, similar to the Generator-Critic pair of the Wasserstein GANs!

- Generator: produce fake images.
- Critic: evaluate said images.

From Deep Q learning to actor-critic



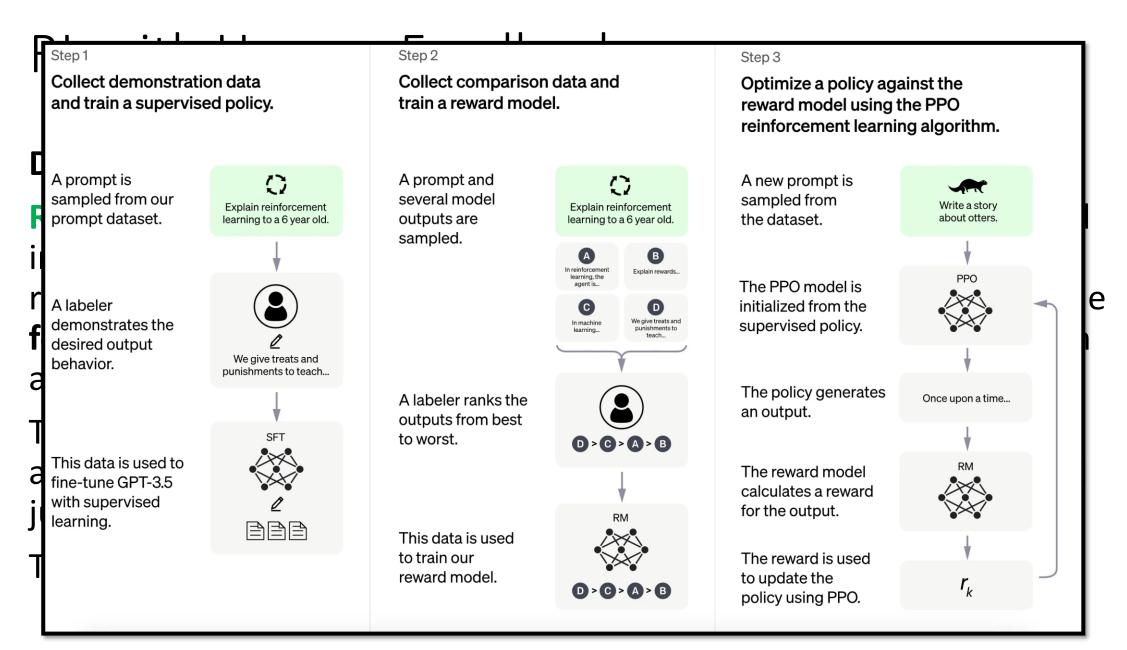
RL with Human Feedback

Definition (Reinforcement Learning with Human Feedback):

Reinforcement Learning with Human Feedback (or RLHF) is a method in which an AI model (pre-trained or not), is typically represented as a reinforcement learning agent, and is fine-tuned/trained based on some feedback/reward provided by humans to improve its performance on a specific task.

This approach combines the strengths of reinforcement learning algorithms, which learn through trial and error, with the expertise and judgment of human evaluators.

The way ChatGPT was trained in fact!



Markov Decision Processes (more advanced stuff, out of scope)

Sometimes, the transition from state s_t to next state s_{t+1} , following from action a_t , will not always be **deterministic**.

• In that case, we have to define some system dynamics, as below.

$$p(s',r|s,a) = P(s_{t+1} = s',r_t = r \mid s_t = s,a_t = a)$$

- Similar to our previous problem, with a stochastic twist.
- It is called a Markov Decision Process (MDP) problem.

Markov Decision Processes (more advanced stuff, out of scope)

• In MDPs, all the previous formulas have to be reworked to account for the stochastic aspect of the problem.

$$V_t^{\pi}(s) = E[G_t \mid s_t = s]$$

$$Q_t^{\pi}(s, a) = E[G_t \mid s_t = s, a_t = a]$$

• In MDPs, the Q and V functions can still be learned from experience, but their Bellman equations change slightly, to account for the stochasticity.

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$$V_t^{\pi}(s) = E[G_t \mid s_t = s]$$

$$V_t^{\pi}(s) = E[R_t + \gamma G_{t+1} \mid s_t = s]$$

$$V_t^{\pi}(s) = \sum_{a} \pi(a \mid s) \sum_{s'} \sum_{r} p(s', r \mid s, a) \left[r + \gamma E[G_{t+1} \mid s_{t+1=s'}] \right]$$

$$V_t^{\pi}(s) = \sum_{a} \pi(a \mid s) \sum_{s'} \sum_{r} p(s', r \mid s, a) \left[r + \gamma V_{t+1}^{\pi}(s') \right]$$

Partially observable MDP (more advanced stuff, out of scope)

Definition (partially observable Markov Decision Process):

In our original RL framework, we assumed that the agent was seeing the exact state of the game at each time t.

This is also an assumption, which can be challenged.

State s_t is ground truth, agent received observation o_t and uses to decide on action.

State **Environment** Observation is changes and a new made by agent state is produced Reward is given for Take action based taking action in on observation said state

Partially observable MDP (more advanced stuff, out of scope)

Definition (partially observable Markov Decision Process):

The agent then decides on an observation made of the actual (partially hidden) state.

This is called a partially observable Markov Decision Process.

Agent will have to learn to observe on top of acting properly (e.g. card game, with opponent hiding his/her hand).

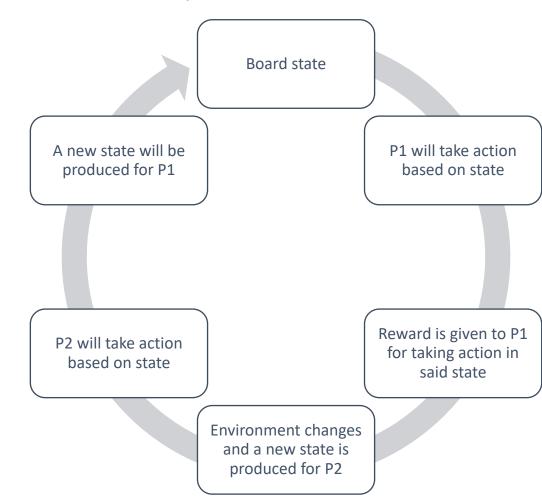
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Partially observable MDP De Ma Th ob (pa ation is agent Th ob Pro Ag ob (e. hic

- In many problems, e.g. Go, the new state seen by a given player is not the immediate result of the action of the said player.
- Instead, another player has to act first, before a new state is produced.

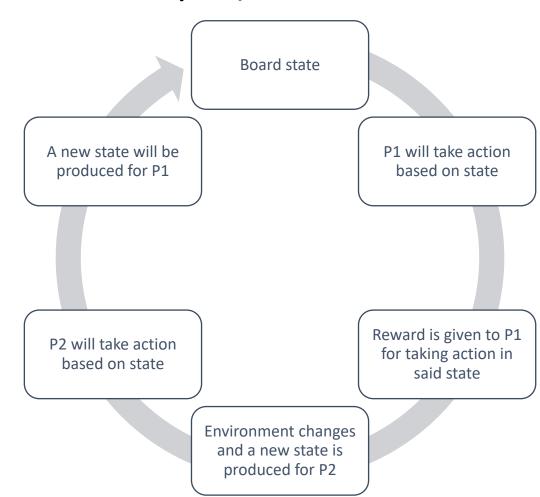


- In many problems, e.g. Go, the new state seen by a given player is not the immediate result of the action of the said player.
- Instead, another player has to act first, before a new state is produced.
- This adds steps to the cycle, which becomes (state, action, reward, state_P2, action_P2).

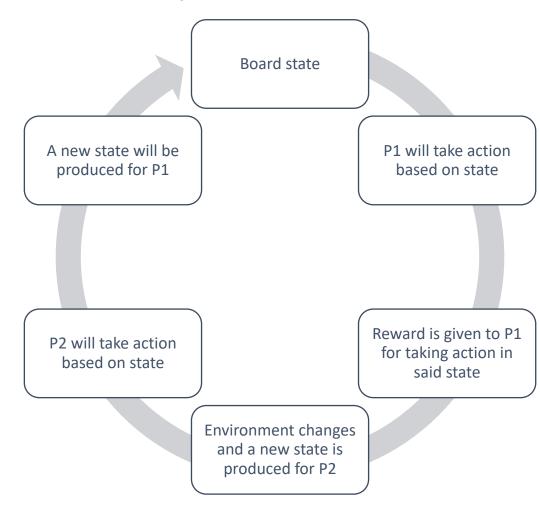


- This is called a State-Action-Reward-State-Action (SARSA) type of problem.
- In that case the agent has to learn how to play, but also has to learn how another player might respond to its actions.

RL meets game theory!



- This is called a State-Action-Reward-State-Action (SARSA) type of problem.
- In that case the agent has to learn how to play, but also has to learn how another player might respond to its actions.
- → Train two Als at the same time (one for black, one for whites)? Make them play against each other and train together like generator-critic in WGANs?



Conclusion

- 1. What are **actor-critic** learning methods? And which problems do these approaches address?
- 2. What are more advanced problems in RL?
 - Markov states
 - Partially observable environment
 - SARSA
 - Non-stationary problems
- 3. What is Reinforcement Learning with Human Feedback (RLHF)?