50.039 Theory and Practice of Deep Learning

W3-S3 Introduction to Deep Learning using the PyTorch framework

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Introduction (Week 3)

- 1. What is the **PyTorch library** and its **benefits**?
- 2. What is a **PyTorch tensor object** and its typical **attributes**?
- 3. How to implement some typical **tensor operations**?
- 4. What is **broadcasting** on tensors?
- 5. What are **tensor locations** in terms of computation?
- 6. How to transform our original NumPy shallow Neural Network class so it uses PyTorch now instead?
- 7. How to implement a **forward**, **loss** and **accuracy** metric in PyTorch?
- 8. What are some measurable **performance benefits** of using **PyTorch** over NumPy and **GPUs** over CPUs?

Introduction (Week 3)

- 9. What is the autograd/backprop module in PyTorch, and how does it use a computational graph to compute all derivatives?
- 10. How to use the **autograd** to implement **derivatives** and a **vanilla gradient descent**?
- 11. How to implement **backprop** in PyTorch for our **shallow Neural Network** class?
- 12. How to use **PyTorch** to implement **advanced optimizers**?
- 13. How to use **PyTorch** to implement **advanced initializers**?
- 14. How to use **PyTorch** to implement **regularization**?
- 15. How to finally revise our **trainer** function to obtain a minimal, yet complete Neural Network in PyTorch?

Introduction (Week 3)

- 16. What are the **Dataset** and **Dataloader** objects in **PyTorch**?
- 17. How to implement a custom **Dataloader** and **Dataset** object in PyTorch?
- 18. How to move from binary classification to multi-class classification?
- 19. How to adjust output probabilities using the **softmax** function?
- 20. How to change the **cross-entropy loss** so it works in **multi-class classification**?
- 21. How to implement **building blocks** in PyTorch?
- 22. How to implement and train our first **Deep Neural Network**?
- 23. What are additional good practices in PyTorch?

To summarize (last two sessions)

We now have a full Neural Network class, in PyTorch, with:

- 2 linear layers, sigmoid activation functions,
- Xavier uniform initialization on trainable parameters,
- Forward pass method,
- Autograd backpropagation and trainer method,
- Adam optimizer,
- Dataloader allowing for stochastic mini-batches,
- Cross entropy loss and accuracies,
- L1 regularization.

And it runs/trains at the speed of light (almost...) on GPU!

Restricted

```
class ShallowNeuralNet PT(torch.nn.Module):
   def __init__(self, n_x, n_h, n_y, device):
        super(). init ()
       self.n_x, self.n_h, self.n_y = n_x, n_h, n_y
        self.linear1 = nn.Linear(n_x, n_h, dtype = torch.double)
        self.linear2 = nn.Linear(n_h, n_y, dtype = torch.double)
        self.loss = torch.nn.BCELoss()
        self.accuracy = BinaryAccuracy()
   def forward(self, inputs):
        return torch.sigmoid(self.linear2(torch.sigmoid(self.linear1(inputs))))
   def train(self, inputs, outputs, N_max = 1000, alpha = 1, beta1 = 0.9, beta2 = 0.999, \
              batch size = 32, lambda val = 1e-3):
       dataset = torch.utils.data.TensorDataset(inputs, outputs)
       data_loader = torch.utils.data.DataLoader(dataset, batch_size = batch_size, shuffle = True)
       optimizer = torch.optim.Adam(self.parameters(), lr = alpha, betas = (beta1, beta2), eps = 1e-08)
       optimizer.zero_grad()
        self.loss history = []
       for iteration_number in range(1, N_max + 1):
           for batch in data loader:
                inputs batch, outputs batch = batch
                total loss = self.loss(self(inputs batch), outputs batch.to(torch.float64))\
                    + lambda val*sum(torch.abs(param).sum() for param in self.parameters()).item()
                self.loss history.append(total loss)
                total loss.backward()
                optimizer.step()
                optimizer.zero grad()
           if(iteration number % (N max//20) == 1):
                pred = self(inputs)
                acc val = self.accuracy(pred, outputs).item()
                print("Iteration {} - Loss = {} - Accuracy = {}".format(iteration_number, total_loss, acc_val))
```

Most of the time, when demonstrating concepts, we will rely on a "simple" **built-in dataset**, available in the PyTorch library.

In practice, and more specifically in your project, you will often play with a **custom dataset**, fitting your needs.

- Most datasets will be provided by your company, or can be found on dataset search engines, such as Kaggle, Google Dataset Search, etc.
- Today, we will play with a simplified version of the Ames Housing Dataset, which can be found online, here:

https://www.kaggle.com/datasets/prevek18/ames-housing-dataset?resource=download

A look at our dataset Excel file

	А	В	С		D	E	F F	G	н	ı J	К	
1 L	ot Area	Overall Qual	▼ Overall Co	nd 🔽 Year B	uilt 🔽 Year	Remod/Add 🔻 Tota	al Bsmt SF 🔽 1st Flr S	F 🔻 2nd Flr	r SF 🔻 Gr Liv A	Area 🔻 Full Bath	▼ Half Bath	▼ Bedro
2	3177	0	6	5	1960	1960	1080	1656	0	1656	1	0
3	1162	2	5	6	1961	1961	882	896	0	896	1	0
4	1426	7	6	6	1958	1958	1329	1329	0	1329	1	1
5	1116	0	7	5	1968	1968	2110	2110	0	2110	2	1
6	1383	0	5	5	1997	1998	928	928	701	1629	2	1
7	997	8	6	6	1998	1998	926	926	678	1604	2	1
8	492	0	8	5	2001	2001	1338	1338	0	1338	2	0
9	500	5	8	5	1992	1992	1280	1280	0	1280	2	0
10	538	9	8	5	1995	1996	1595	1616	0	1616	2	0
11	750	0	7	5	1999	1999	994	1028	776	1804	2	1
12	1000	0	6	5	1993	1994	763	763	892	1655	2	1
13	798	0	6	7	1992	2007	1168	1187	0	1187	2	0
14	840	2	6	5	1998	1998	789	789	676	1465	2	1
15	1017	6	7	5	1990	1990	1300	1341	0	1341	1	1
16	682	0	8	5	1985	1985	1488	1502	0	1502	1	1
17	5350	4	8	5	2003	2003	1650	1690	1589	3279	3	1
18	1213	4	8	7	1988	2005	559	1080	672	1752	2	0
19	1139	4	9	2	2010	2010	1856	1856	0	1856	1	1
20	1913	8	4	5	1951	1951	864	864	0	864	1	0
21	1317	5	6	6	1978	1988	1542	2073	0	2073	2	0
22	1175	1	6	6	1977	1977	1844	1844	0	1844	2	0
22	1063	5	7	6	107/	107/	1050	1170	0	1170	2	0

The Ames dataset includes a variety of features for approximately 2,800 houses in Ames, Iowa.

- Features include the size of the house (in square feet), the number of bedrooms and bathrooms, and many more. It also includes the sale price for each house.
- The Ames Housing Dataset is a popular choice for machine learning projects, and it has been used to build AI models for predicting house prices, based on various house features.
- It consists of an Excel file (AmesHousing.xlsx) stored in the ./ames/ folder. The original dataset can be found in the AmesHousing.csv file, but we have simplified it by removing some of its features.

The features we are interested in are:

- Lot Area: The area of the lot in square feet.
- Overall Qual: A rating of the overall material and finish of the house (1-10).
- Overall Cond: A rating of the overall condition of the house (1-10).
- Year Built: The year the house was built.
- Year Remod/Add: The year the house was remodeled or had an addition added.
- And many more features! (not describing all of them)
- The last column is the selling price, which is our output.

Let us start by loading the **Excel** file into a pandas **DataFrame** first.

(Note: Not familiar with the **pandas** library? Find 10 minutes to learn it, it will definitely serve you in the long run!

https://pandas.pydata.org/docs/
user guide/10min.html)

Restricted

```
# Load dataset using pandas, and showing the first five entries
    ames dataset = pd.read excel("./ames/AmesHousing.xlsx")
    print(ames dataset.head(5))
   Lot Area Overall Qual Overall Cond Year Built Year Remod/Add
      31770
                                                1960
                                                                 1960
      11622
                                                1961
                                                                 1961
      14267
                                                1958
                                                                 1958
      11160
                                                1968
                                                                 1968
      13830
                                                1997
                                                                 1998
                                                                   Half Bath
                              2nd Flr SF
   Total Bsmt SF
                  1st Flr SF
                                                        Full Bath
            1080
                        1656
                                                  1656
0
             882
                         896
                                                   896
            1329
                                                  1329
                        1329
                                                  2110
            2110
                         2110
                                                  1629
             928
                         928
                                      701
                  Kitchen AbvGr
                                 TotRms AbvGrd
                                                 Garage Area
                                                               Yr Sold \
   Bedroom AbvGr
                                                          528
                                                                  2010
                                                          730
                                                                  2010
                                                          312
                                                                  2010
                                                          522
                                                                  2010
                                                         482
                                                                  2010
  SalePrice
      215000
      105000
2
      172000
3
      244000
4
      189900
```

To write a custom **dataset class** in PyTorch, we need to:

- Create a class that subclasses torch.utils.data.Dataset.
- Define a an __init__ that loads the excel file and stores data accordingly.
- Define a __getitem__ that takes index as input, and returns the data and label at that index as an array. This will allow to use the square bracket notation on our dataset object.
- Define a method __len__ that returns the number of samples in the dataset.

```
class AmesHousingDataset(torch.utils.data.Dataset):
   #The init method will simply initialize attributes, which consist
   # of the details related to the dataset.
   def init (self, file path = "./ames/AmesHousing.xlsx"):
       # Whole data as a pandas array
       self.data = pd.read excel(file path)
       self.dataset length = len(self.data) #2928
       # Extract inputs
       self.input fetaures number = 16
       self.input features = self.data.iloc[:, :16]
       # Extract outputs
       self.output_fetaures_number = 1
       self.output feature = self.data.iloc[:, 16]
    # The getitem method returns the sample with given index
   # x will consist of the 16 input features for the given sample,
   # whereas y will consist of the 1 output feature for the given sample.
   def __getitem__(self, index):
       # Fetch inputs
       x = self.input_features.iloc[index].values
       # Fetch outputs
       y = self.output feature.iloc[index]
   # Finally, the len special method should return the number of samples,
   # in the dataset. We could use self.dataset length, but it is more
   # modular to use len(self.data).
   def __len__(self):
       return len(self.data)
```

The __getitem__() and __len__() special methods will allow for indexing and using for loops on the dataset object.

 Later on, we could ask for the sample #286 using the square bracket notation, as shown on side.

Similarly, the two special methods are all we need to make a **for loop** that uses the dataset object as the **generator** to be looped over!

```
# Instantiate the dataset
    ames dataset = AmesHousingDataset('./ames/AmesHousing.xlsx')
    # Fetch sample with index 286
    sample input, sample output = ames dataset[286]
    # Input is a (16,) numpy array, with the following values
    print(type(sample input), sample input.shape)
    print(sample input)
    # Output is a single value, of type numpy int64
    print(type(sample_output), sample_output.shape)
    print(sample output)
<class 'numpy.ndarray'> (16,)
[6858
             4 1915 1950 806 841 806 1647
 216 2010]
<class 'numpy.int64'> ()
128000
```



Writing a custom Dataloader

Before we can feed this dataset object to Neural Networks, we need to supplement it with a Dataloader. It serves as a "conveyor belt" processing and feeding data from the Dataset to the Neural Network.

- The Dataloader will **shuffle the samples randomly** and produce **mini-batches** of a given size.
- This Dataloader typically allows for stochastic mini-batches.
- The Dataloader will also transform any arrays data into tensors.

```
# Instantiate the dataset
ames_dataset = AmesHousingDataset('./ames/AmesHousing.xlsx')

# Create a DataLoader for the dataset
ames_dataloader = torch.utils.data.DataLoader(ames_dataset, \
batch_size = 32, \
shuffle = True)
```

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Writing a custom Dataloader

We can then use this custom
Dataloader object as the
generator in a **for loop**, to
generate mini-batches of samples.

- Notice how this Dataloader generates 92 (i.e. 2928/32, rounded up) batches of 32 samples.
- With the exception of the last batch (with index 91), that only contains 16 samples (that is 2928 % 32).

```
for batch_number, batch in enumerate(ames_dataloader):
    inputs, outputs = batch
    print("---")
    print("Batch number: ", batch_number)
    print(inputs.shape)
    print(outputs.shape)
```

```
Batch number: 0
torch.Size([32, 16])
torch.Size([32])
Batch number: 1
torch.Size([32, 16])
torch.Size([32])
Batch number: 2
torch.Size([32, 16])
torch.Size([32])
Batch number: 3
torch.Size([32, 16])
torch.Size([32])
Batch number: 4
              Batch number: 91
              torch.Size([16, 16])
              torch.Size([16])
```

Restricted

Writing a custom Dataloader

We can then use this custom
Dataloader object as the
generator in a **for loop**, to
generate mini-batches of samples.

- Good practice: the custom
 Dataset and custom Dataloader
 definition should be repeated to
 generate training, testing and
 validation sets dataloaders.
- These Dataloaders will then be given to our **trainer** function.

```
for batch_number, batch in enumerate(ames_dataloader):
    inputs, outputs = batch
    print("---")
    print("Batch number: ", batch_number)
    print(inputs.shape)
    print(outputs.shape)
```

```
Batch number: 0
torch.Size([32, 16])
torch.Size([32])
Batch number: 1
torch.Size([32, 16])
torch.Size([32])
Batch number: 2
torch.Size([32, 16])
torch.Size([32])
Batch number: 3
torch.Size([32, 16])
torch.Size([32])
Batch number: 4
              Batch number:
              torch.Size([16, 16])
              torch.Size([16])
```

Built-in datasets

Pytorch has a few **built-in datasets**, ready to be downloaded and used on models: typically, the most common ones that have been used in research to demonstrate concepts, such as **MNIST** or **CIFAR-10**.

For more details on the available **built-in datasets** in Pytorch, have a look at the following page:

https://pytorch.org/vision/stable/datasets.html.

Built-in datasets

Let us demonstrate using the **FashionMNIST** dataset first.

- This dataset inputs consists of 28 by 28 greyscale images.
- Each input is therefore a 28 by 28 matrix, where each element value represents the grey shade of the pixel at the given location.
- Logic: 0 = black, 1 = white, and anything between 0 and 1 describes a shade of grey.

Built-in datasets

Let us demonstrate using the **FashionMNIST** dataset first.

- This dataset is used to design image classification models (i.e. models that receive images as inputs) and attempt to predict what is in the image in question.
- The 10 output classes (bag, shirt, etc.) are indexed with 0-9 values, corresponding to the 10 types of fashion objects found in the dataset.

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Built-in datasets

Let us demonstrate using the **FashionMNIST** dataset first.

- This dataset is used to design image classification models (i.e. models that receive images as inputs) and attempt to predict what is in the image in question.
- The 10 output classes (bag, shirt, etc.) are indexed with 0-9 values, corresponding to the 10 types of fashion objects found in the dataset.

```
# Dataset contains 60000 samples, that are greyscale
# images with size 28 by 28 pixels.
print(training_data.data.shape)
```

torch.Size([60000, 28, 28])

```
# We can then fetch a sample using the [] notations
sample_index = 894
img, label = training_data[sample_index]
print("Image: ", img.shape)
print("Label: ", label)
```

Image: torch.Size([1, 28, 28])
Label: 8

Image 894 - Label = 8 (Bag)



Introducing the MNIST dataset

MNIST is another widely-used dataset for the benchmarking of machine learning and computer vision algorithms.

It consists of

- a **training set** of 60,000 examples,
- and a **testing set** of 10,000 examples.

All samples consist of 28x28 pixel grayscale images of handwritten digits (0 to 9).

MNIST is often used as a "Hello, World!" dataset example, due to its simplicity, which allows for efficient implementations of ML/DL algorithms.



Introducing the MNIST dataset

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It consists of

- a **training set** of 60,000 examples,
- and a **testing set** of 10,000 examples.

All samples consist of 28x28 pixel grayscale images of handwritten digits (0 to 9).

Careful however: the MNIST dataset is often accused of having been overused (which is true) and of being too simple.

For now, however, this will do.



Introducing the MNIST dataset

Nevertheless, it is a good dataset to use for testing and comparing the performance of different models, as well as for getting familiar with the basics of machine learning and deep learning algorithms.

• The images serve as inputs, and the task is therefore to predict which of the ten digits appears in the image. This is therefore a classification task, like before, except that it consists of 10 different classes (corresponding to the 0-9 digits) instead of just two like in binary classification.



Writing the MNIST Dataset and Dataloader

```
# Try the dataloader
for batch_number, batch in enumerate(train_loader):
    inputs, outputs = batch
    print("---")
    print("Batch number: ", batch_number)
    print(inputs.shape)
    print(outputs.shape)
    break
```

```
Batch number: 0
torch.Size([64, 1, 28, 28])
torch.Size([64])
```

Quick parenthesis: normalizing input data

Good practice: Always a good idea to normalize your inputs!

In general, do the following:

- Scale the data (pixel values) to the [0,1] range.
- Normalize to have zero mean and unit standard deviation.

In MNIST, we will then subtract a mean of 0.1307 and divide by a standard deviation of 0.3081.

These values are the original mean and standard deviation of the dataset before normalization!

Writing the MNIST Dataset and Dataloader

```
# Try the dataloader
for batch_number, batch in enumerate(train_loader):
    inputs, outputs = batch
    print("---")
    print("Batch number: ", batch_number)
    print(inputs.shape)
    print(outputs.shape)
    break
```

```
Batch number: 0
torch.Size([64, 1, 28, 28])
torch.Size([64])
```

Recall (Binary classification probabilities as output):

In **binary classification**, we would produce **a single value** p as **output**, with p between 0 and 1.

- This value p would correspond to the probability of being of class 1.
- The probability of being of class 0 would then simply be 1 p.
- We would then use a **threshold 0.5** to decide if the sample is predicted of class 0 or 1.

Problem: How could we produce multi-class classification probabilities for all possible N>2 classes as outputs?

Unfortunately, when we have more than 2 classes, we can no longer rely on a single output value p.

- Instead, it is often preferable to have the model output **10 values**: $(p_0, p_1, p_2, ..., p_9)$
- Where each p_i corresponds to the **probability of being of class** i.
- This could typically be done by asking for the final layer to produce $n_y=10$ values instead of just a single $n_y=1$ value.

Unfortunately, this is not good enough.

• The p_i produced by the network are supposed to represent **probabilities** and **their sum should therefore be equal to 1**, i.e.

$$\sum_{i=0}^{9} p_i = 1$$

A fully connected (or linear) layer (which implements the WX + b operation) cannot do that on its own, as

- it might produce negative values as probabilities p_i ,
- and those values may not sum up to 1.

To normalize the outputs produced by the final fully connected layer, we will use the **softmax** operation, which is a special activation function.

It has two effects:

- It will force the values of the p_i to fall in the range of [0, 1].
- It will force their sum to be equal to 1, that is

$$\sum_{i=0}^{9} p_i = 1$$

Softmax function

Definition (the softmax function):

The softmax operation

$$p_i = s(y_i, y_{-i})$$

is defined, $\forall i$, as:

$$p_i = s(y_i, y_{-i}) = \frac{\exp(y_i)}{\sum_{k=0}^{K} \exp(y_k)}$$

Note: the y_{-i} notation comes from game theory, and consists of every element in vector Y except y_i , i.e.:

$$y_{-i} = (y_1, \dots, y_{i-1}, y_{i+1}, \dots, y_K)$$

Softmax function

Definition (the softmax function):

The **softmax function** transforms a vector of values

$$Y = (y_0, y_1, y_2, ... y_K),$$

into another vector of values

$$P = (p_0, p_1, p_2, ... p_K).$$

The new vector P is guaranteed to contain <u>positive</u> values, and those values will be summing up to 1_{f} i.e.

$$\sum_{i=0}^{K} p_i = 1$$

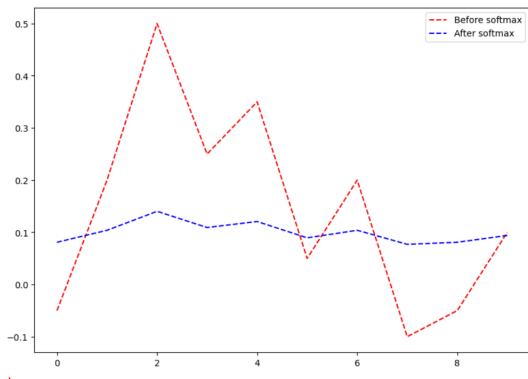
Softmax function

Softmax can be manually implemented as:

def softmax(x):

```
# Subtract the maximum value from each element of the input vector x
        # to avoid numerical instability (this is optional, but equivalent)
        x = x - np.max(x)
        # Compute the exponent of each element
        exp x = np.exp(x)
        # Normalize the exponentiated values by their sum
        return exp x/np.sum(exp x)
 1 # Ten values that do not sum up to 1
 2 \mid Y = \text{np.array}([-1, 4, 10, 5, 7, 1, 4, -2, -1, 2])/20
    print(sum(Y))
    P = softmax(Y)
    print(P)
 6 print(np.sum(P))
1.45
[0.08089815 0.10387528 0.14021696 0.10920108 0.12068586 0.08940628
0.10387528 0.0769527 0.08089815 0.09399024]
0.99999999999999
```

Softmax effect: It will rescale values so that the trend is preserved, but the new vector consists of positive values that sum up to 1.



Softmax function and prediction

In the case of multi-label classification, we will use the **softmax** operation as the final activation after the last fully connected layer.

This will produce a vector of 10 positive values,

$$P = (p_0, p_1, p_2, \dots p_9),$$

Which can be used as the probabilities for sample of being of class i.

The **predicted class according to the model** is then defined as the variable pred, corresponding to the index i of the highest probability value p_i , i.e.:

$$pred = \arg \max_{i} [p_i]$$
.

Implementation

For instance, this simple neural network consists of **two fully-connected/linear layers**.

A **single ReLU activation** is used between both layers.

No final softmax activation yet.

It also consists of a **flattening** operation, which will transform our input images (2D tensors, size 28 by 28), into a "flattened" 1D tensor with size $784 (= 28 \times 28)$.

```
class ShallowNeuralNet(torch.nn.Module):
        def __init__(self, n_x, n_h, n_y):
            super(). init_()
            # Define two layers using the nn.Linear()
            self.fc1 = torch.nn.Linear(n_x, n_h)
            self.fc2 = torch.nn.Linear(n h, n y)
       def forward(self, x):
            # Flatten images (transform them from 28x28 2D
 9
10
            # matrices to 784 1D vectors)
           x = x.view(x.size(0), -1)
11
12
            # First Wx + b operation
13
            out1 = self.fc1(x)
            # Using ReLU operation as activation after first layer
14
15
            act1 = torch.relu(out1)
            # Second Wx + b operation anbd return
16
17
            out2 = self.fc2(act1)
18
            return out2
```

Implementation

Consider a neural network model, with **784 input size**, **128 hidden size**, and **10 output size**, and transferring all the model parameters to a device (e.g. CUDA).

- Next, we get a single sample from the train_loader iterator and extract sample info in the variables data and target.
- This can be simply done with the next and iter functions.

```
# Initialize model
   model = ShallowNeuralNet(n x = 784, \
                            n h = 128, \
                            n y = 10).to(device)
   # Get a single sample
   sample = next(iter(train loader))
   data, target = sample
   print(data.shape)
   print(target.shape)
   data1 = data[0].to(device)
   target1 = target[0].to(device)
   print(data1.shape)
14 print(target1)
15
16 # Forward pass
17 out2 = model(data1)
18 act2 = torch.nn.functional.softmax(out2, dim = 1)
19 print(out2)
20 print(act2)
21 print(act2.sum())
```

Implementation

- Next, perform a forward pass through the model, storing the output in the variable out2.
- Apply the softmax operation on out2. PyTorch offers a functional implmentation of the softmax:

torch.nn.functional.softmax()

 We can then verify that softmax will adjust the output of the neural network correctly.

```
# Initialize model.
   model = ShallowNeuralNet(n x = 784, \
                            n h = 128, \
                            n y = 10).to(device)
   # Get a single sample
   sample = next(iter(train loader))
   data, target = sample
   print(data.shape)
   print(target.shape)
   data1 = data[0].to(device)
   target1 = target[0].to(device)
   print(data1.shape)
14 print(target1)
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16 # Forward pass
17 out2 = model(data1)
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19 print(out2)
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```

Forward Implementation

Our model is however implementing the same forward method as before.

In fact, we will not use the softmax operation as the final activation function in the forward method.

This is normal as the softmax operation will be applied in the loss function instead, that is the cross_entropy() function, which will be summoned in the trainer() later.

```
class ShallowNeuralNet(torch.nn.Module):
        def __init__(self, n_x, n_h, n_y):
            super(). init_()
           # Define two layers using the nn.Linear()
            self.fc1 = torch.nn.Linear(n_x, n_h)
            self.fc2 = torch.nn.Linear(n h, n y)
       def forward(self, x):
 9
           # Flatten images (transform them from 28x28 2D
10
           # matrices to 784 1D vectors)
           x = x.view(x.size(0), -1)
11
12
           # First Wx + b operation
13
           out1 = self.fc1(x)
           # Using ReLU operation as activation after first layer
14
15
            act1 = torch.relu(out1)
           # Second Wx + b operation and return
16
17
           out2 = self.fc2(act1)
18
            return out2
```

From binary cross entropy...

 Speaking of, in the case of the binary classification, we used the following loss function, namely the log-likelihood binary cross entropy function.

$$L(x,y) = -\frac{1}{N} \sum_{k=0}^{N} y_k \ln(p(x_k)) + (1 - y_k) \ln(1 - p(x_k))$$

• But in the case of MNIST, we have more than two classes...

How does the loss function change now that we have N > 2 classes?

...To multi-class cross entropy!

The adjustment is actually quite simple, and the log-likelihood multiclass cross-entropy loss function simply rewrites as shown below:

$$L(x,y) = -\frac{1}{N} \sum_{k=0}^{N} \sum_{i=0}^{9} y_k^i \ln(p_i(x_k)).$$

In the formula above, $p_i(x_k)$ denotes the **probability for sample** x_k of being of being predicted as class i, according to our model.

In other words, it is the i-th value of the output vector produced by the model for sample x_k , after softmax has been applied to the output o_i of the forward method of the model.

...To multi-class cross entropy!

Recall the function in the previous slide:

$$L(x,y) = -\frac{1}{N} \sum_{k=0}^{N} \sum_{i=0}^{9} y_k^i \ln(p_i(x_k)).$$

Similarly, we will define the value y_k^i as the ground truth value for the probability of being of class i for sample x_k .

For instance, if the sample x_k is of class $y_k = 2$, we define:

$$Y_k = (y_k^0, y_k^1, y_k^2, y_k^3, \dots y_k^9) = (0, 0, 1, 0, \dots, 0).$$

We say that Y_k is the one-hot vector for the sample k with class 2.

Setting a model in train/eval mode

New good practice: some operations (layers, activations, etc.) in the forward method will have **two different behaviors** depending whether

- the model is currently training,
- or if we are using its trained version for evaluation.

(Note: at the moment, we have not seen such operations.)

But let us keep this in mind and accept that is good practice to set the model to either train() or eval() mode.

```
# Initialize the model and optimizer
model = ShallowNeuralNet(n_x = 784, n_h = 64, n_y = 10).to(device)
optimizer = torch.optim.Adam(model.parameters(), lr = 1e-3)
# Set model in train mode!
model.train()
```

Training our model with Adam GD, as before

```
1 # Training model
 2 num epochs = 5
 3 for epoch in range(num epochs):
        # Go trough all samples in train dataset
        for i, (images, labels) in enumerate(train_loader):
            # Get from dataloader and send to device
            images = images.to(device)
            labels = labels.to(device)
            # Forward pass
            outputs = model(images)
10
            # Compute loss
11
            loss = torch.nn.functional.cross entropy(outputs, labels)
12
            # Backward and optimize
13
            optimizer.zero grad()
14
            loss.backward()
15
            optimizer.step()
16
17
            # Display
18
            if (i+1) % 300 == 0:
                print (f'Epoch [{epoch+1}/{num epochs}], Step [{i+1}/{len(train loader)}], Loss: {loss.item():.4f}')
19
Epoch [1/5], Step [300/938], Loss: 0.2895
Epoch [1/5], Step [600/938], Loss: 0.1588
Epoch [1/5], Step [900/938], Loss: 0.1753
Epoch [2/5], Step [300/938], Loss: 0.0461
Epoch [2/5], Step [600/938], Loss: 0.1251
Epoch [2/5], Step [900/938], Loss: 0.1592
Epoch [3/5], Step [300/938], Loss: 0.1241
Epoch [3/5], Step [600/938], Loss: 0.0511
Epoch [3/5], Step [900/938], Loss: 0.0553
Epoch [4/5], Step [300/938], Loss: 0.0514
Fnoch [1/5] Sten [600/938] Loss: 0 0339
```

Eval mode and accuracy after training

After training, we will evaluate our trained model to check its accuracy on the test set.

- Set the model in eval() mode (good practice for later).
- Predict on test dataloader.
- Calculate accuracy manually (we could have probably also used a torch function to do that).
- 97% accuracy = a rather nicely trained model!

```
# Evaluate model accuracy on test after training
   # Set model in eval mode!
   model.eval()
   # Evaluate
   with torch.no grad():
       correct = 0
       total = 0
       for images, labels in test loader:
           # Get images and labels from test loader
           images = images.to(device)
           labels = labels.to(device)
11
           # Forward pass and predict class using max
           outputs = model(images)
           _, predicted = torch.max(outputs.data, 1)
14
           # Check if predicted class matches label
           # and count numbler of correct predictions
           total += labels.size(0)
           correct += (predicted == labels).sum().item()
   # Compute final accuracy and display
   accuracy = correct/total
   print(f'Evaluation after training, Accuracy: {accuracy:.4f}')
```

Evaluation after training, Accuracy: 0.9712

It is now time...

It is now time for us to define and train a Deep Neural Network.

Definition (Deep Neural Networks):

By definition, a deep neural network is a neural network, which consists of more than two hidden layers.

To demonstrate, we will create a deep neural network with <u>four</u> layers:

- three linear layers with ReLU activation,
- followed by one linear layer, finished with a softmax activation.

It is now time...

Reminder: it is good practice to have the size of layers decrease progressively by a factor of at least 2.

- the first layer has inputs size 784 and outputs size 80,
- the second layer has inputs size 80 and outputs size 40,
- the third layer has inputs size 40 and outputs size 20,
- and the fourth layer has inputs size 20 and outputs size 10, matching the number of classes in the dataset.

Note: a layer-by-layer model summary can be seen by printing the model object!

```
DeepNeuralNet(
  (layer1): DenseReLU(
     (fc): Linear(in_features=784, out_features=80, bias=True)
  )
  (layer2): DenseReLU(
     (fc): Linear(in_features=80, out_features=40, bias=True)
  )
  (layer3): DenseReLU(
     (fc): Linear(in_features=40, out_features=20, bias=True)
  )
  (layer4): DenseNoReLU(
     (fc): Linear(in_features=20, out_features=10, bias=True)
  )
```

Good practice: create building blocks for modularity.

- The DenseReLU class is a custom PyTorch module that consists of a linear layer followed by a ReLU activation function.
- The DenseNoRELU class is similar, but it applies no activation function.

Important note: not using softmax as final activation here, for the same reasons as before.

```
class DenseReLU(torch.nn.Module):
    def __init__(self, n_x, n_y):
        super().__init__()
        # Define Linear layer using the nn.Linear()
        self.fc = torch.nn.Linear(n_x, n_y)

def forward(self, x):
    # Wx + b operation
    # Using ReLU operation as activation after
    return torch.relu(self.fc(x))
```

```
class DenseNoReLU(torch.nn.Module):
    def __init__(self, n_x, n_y):
        super().__init__()
        # Define Linear layer using the nn.Linear()
        self.fc = torch.nn.Linear(n_x, n_y)

def forward(self, x):
    # Wx + b operation
    # No activation function
    return self.fc(x)
```

The DeepNeuralNet class will here represent the overall deep neural network.

It starts by initializing four layers:

- Three DenseReLU blocks,
- And one DenseNoReLU block.

It then combines all blocks into a single PyTorch sequential model using torch.nn.Sequential().

```
class DeepNeuralNet(torch.nn.Module):
   def __init__(self, n_x, n_h, n_y):
        super(). init__()
       # Define three Dense + ReLU layers,
       # followed by one Dense + Softmax layer
       self.layer1 = DenseReLU(n x, n h[0])
        self.layer2 = DenseReLU(n h[0], n h[1])
       self.layer3 = DenseReLU(n h[1], n h[2])
        self.layer4 = DenseNoReLU(n h[2], n y)
       # Combine all four layers
        self.combined layers = torch.nn.Sequential(self.layer1,
                                                   self.layer2,
                                                   self.layer3,
                                                   self.layer4)
   def forward(self, x):
       # Flatten images (transform them from 28x28
        # 2D matrices to 784 1D vectors)
       x = x.view(x.size(0), -1)
       # Pass through all four layers
       out = self.combined layers(x)
       return out
```

```
# Initialize the model and optimizer
model = DeepNeuralNet(n_x = 784, n_h = [80, 40, 20], n_y = 10).to(device)
optimizer = torch.optim.Adam(model.parameters(), lr = 1e-3)
```

The forward pass of the network is then simply defined, using the following steps:

- The input image is flattened, transforming a 2D tensor image into a 1D tensor,
- It is then passed through the combined layers/blocks we have assembled in the Sequential().

```
class DeepNeuralNet(torch.nn.Module):
   def __init__(self, n_x, n_h, n_y):
        super(). init ()
       # Define three Dense + ReLU layers,
       # followed by one Dense + Softmax layer
       self.layer1 = DenseReLU(n x, n h[0])
        self.layer2 = DenseReLU(n h[0], n h[1])
       self.layer3 = DenseReLU(n h[1], n h[2])
        self.layer4 = DenseNoReLU(n h[2], n y)
       # Combine all four layers
       self.combined layers = torch.nn.Sequential(self.layer1,
                                                   self.layer2,
                                                   self.layer3,
                                                   self.layer4)
   def forward(self, x):
       # Flatten images (transform them from 28x28
        # 2D matrices to 784 1D vectors)
       x = x.view(x.size(0), -1)
       # Pass through all four layers
       out = self.combined layers(x)
       return out
```

```
# Initialize the model and optimizer
model = DeepNeuralNet(n_x = 784, n_h = [80, 40, 20], n_y = 10).to(device)
optimizer = torch.optim.Adam(model.parameters(), lr = 1e-3)
```

Good practice: This modular block-based approach, which

- Defines blocks of layers,
- And eventually assembles them into a larger Deep Neural Network object,

Is very common and convenient, especially when the architectures are very heavy and include many layers. It helps to organize the mess!

```
class DeepNeuralNet(torch.nn.Module):
    def __init__(self, n_x, n_h, n_y):
        super(). init__()
        # Define three Dense + ReLU layers,
        # followed by one Dense + Softmax layer
        self.layer1 = DenseReLU(n x, n h[0])
        self.layer2 = DenseReLU(n h[0], n h[1])
        self.layer3 = DenseReLU(n h[1], n h[2])
        self.layer4 = DenseNoReLU(n_h[2], n_y)
        # Combine all four layers
        self.combined layers = torch.nn.Sequential(self.layer1,
                                                    self.layer2,
                                                    self.layer3,
                                                    self.layer4)
    def forward(self, x):
        # Flatten images (transform them from 28x28
        # 2D matrices to 784 1D vectors)
        x = x.view(x.size(0), -1)
        # Pass through all four layers
        out = self.combined layers(x)
        return out
```

```
# Initialize the model and optimizer
model = DeepNeuralNet(n_x = 784, n_h = [80, 40, 20], n_y = 10).to(device)
optimizer = torch.optim.Adam(model.parameters(), lr = 1e-3)
```

Training our model as before

```
# Training model
 2 num epochs = 10
 3 for epoch in range(num epochs):
        # Go trough all samples in train dataset
        for i, (images, labels) in enumerate(train_loader):
            # Get from dataloader and send to device
            images = images.to(device)
            labels = labels.to(device)
            # Forward pass
            outputs = model(images)
10
            # Compute loss
            loss = torch.nn.functional.cross entropy(outputs, labels)
13
            # Backward and optimize
14
            optimizer.zero grad()
            loss.backward()
15
            optimizer.step()
16
17
            # Display
            if (i+1) % 25 == 0:
18
                print (f'Epoch [{epoch+1}/{num epochs}], Step [{i+1}/{len(train loader)}], Loss: {loss.item():.4f}')
19
Epoch [1/10], Step [25/235], Loss: 2.2469
Epoch [1/10], Step [50/235], Loss: 2.1274
Epoch [1/10], Step [75/235], Loss: 1.9379
Epoch [1/10], Step [100/235], Loss: 1.8415
Epoch [1/10], Step [125/235], Loss: 1.6548
Epoch [1/10], Step [150/235], Loss: 1.4660
Epoch [1/10], Step [175/235], Loss: 1.2895
Epoch [1/10], Step [200/235], Loss: 1.1478
Epoch [1/10], Step [225/235], Loss: 0.9910
Fnoch [2/10] Sten [25/235] Loss: 0 8251
```

Careful: Deeper does not mean better!

Shallow Neural Net: 96.5% test acc. (not too bad in terms of acc.)

```
1 # Evaluate model accuracy on test after training
   # Set model in eval mode!
   model.eval()
   # Evaluate
   with torch.no_grad():
       correct = 0
       total = 0
       for images, labels in test loader:
9
           # Get images and labels from test loader
           images = images.to(device)
10
           labels = labels.to(device)
           # Forward pass and predict class using max
           outputs = model(images)
           _, predicted = torch.max(outputs.data, 1)
14
           # Check if predicted class matches label
16
           # and count numbler of correct predictions
           total += labels.size(0)
17
           correct += (predicted == labels).sum().item()
   # Compute final accuracy and display
   accuracy = correct/total
   print(f'Evaluation after training, Accuracy: {accuracy:.4f}')
```

Deep Neural Net: 93.7% test acc. (lower acc., even though we had a lower loss?!)

```
# Evaluate model accuracy on test after training
2 # Set model in eval mode!
   model.eval()
   # Evaluate
   with torch.no grad():
       correct = 0
       total = 0
       for images, labels in test loader:
           # Get images and labels from test loader
           images = images.to(device)
10
           labels = labels.to(device)
           # Forward pass and predict class using max
           outputs = model(images)
           _, predicted = torch.max(outputs.data, 1)
           # Check if predicted class matches label
           # and count numbler of correct predictions
17
           total += labels.size(0)
           correct += (predicted == labels).sum().item()
   # Compute final accuracy and display
   accuracy = correct/total
   print(f'Evaluation after training, test accuracy: {accuracy:.4f}')
```

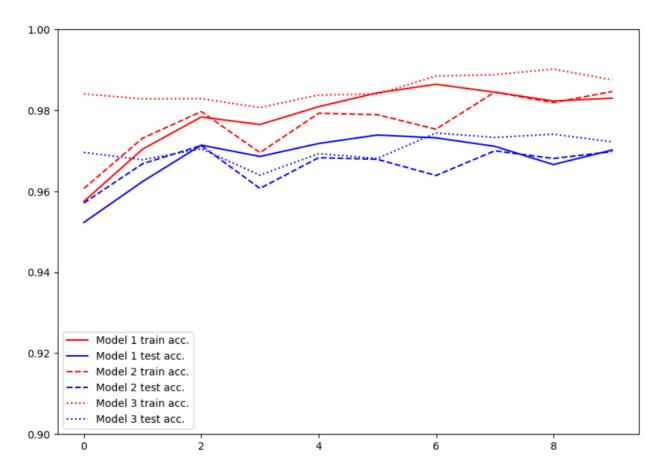
Evaluation after training, test accuracy: 0.9367

Experimenting on layers numbers and sizes

In fact, in Notebook 7, we trained three DNN models:

- Model 1: 6 layers (probably too many layers) $n_h = [320, 160, 80, 40, 20],$
- Model 2: 3 layers (layers probably too large) $n_h = [400, 200],$
- Model 3: 3 layers (just fine?) $n_h = [40, 20].$

While simpler, model 3 has highest test accuracy!



Important lesson: Larger and deeper network does not necessarily mean better performance! (Deeper and larger models could overfit!)

Restricted

Conclusion (Week 3)

- PyTorch library and its benefits
- Tensor objects, attributes and operations on tensors
- Converting our NumPy shallow neural network into PyTorch
- Parameter objects
- Forward method implementation
- Performance benefits of GPU acceleration
- Using autograd and compuitational graphs

- Advanced optimizers in PyTorch
- Initializers in PyTorch
- Regularization in PyTorch
- Dataset and Dataloader objects
- Multi-class classification
- Softmax function and multi-class cross entropy loss
- Building blocks in PyTorch
- Our first Deep Neural Network!
- Network size vs. overfitting tradeoff

Project and HW announcement!

Let us discuss it now.