ILP 2022 – W4S3 Numpy library (part 1) and imports

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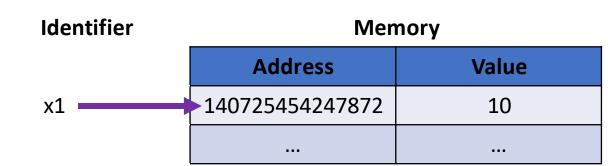


Outline (Week4, Session3 – W4S3)

- Memory management and lists: aliasing, shallow and deep copies
- The Numpy library (part 1): arrays, math functions, etc.
- About the import procedure
- Project organizing
- Mini-project

Memory of a computer

• The memory of a computer consists of several "boxes", which can contain values for variables. Each "box" is identified by an **integer**, which corresponds to the **address/ID** of the "box".



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- When a variable is created:
 - A "box" is assigned for the variable and its value is stored in the "box".
 - The variable name simply refers to the address/ID of the "box".



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 - A "box" is assigned for the variable and its value is stored in the "box".
 - The variable name simply refers to the address/ID of the "box".



```
1 x1 = 10
2 print(x1)
3 print(id(x1))
```

 The id() function returns an integer, which corresponds to the address/ID, where the variable is stored in memory.

```
1 x1 = 10
2 print(x1)
3 print(id(x1))
```

10 140725454247872

```
1 x2 = 17
2 print(x2)
3 print(id(x2))
```

- The id() function returns an integer, which corresponds to the address/ID, where the variable is stored in memory.
- Two variables names with identical values will have the same id().

```
1 x1 = 10
2 print(x1)
3 print(id(x1))
```

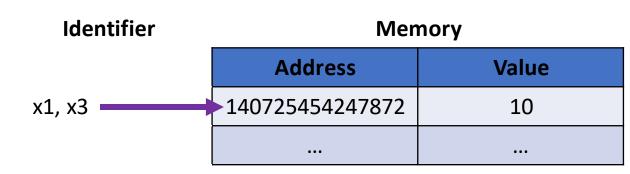
10 140725454247872

```
1 x2 = 17
2 print(x2)
3 print(id(x2))
```

17 140725454248096

```
1 x3 = x1
2 print(x3)
3 print(id(x3))
4 print(id(x1))
```

- The id() function returns an integer, which corresponds to the address/ID, where the variable is stored in memory.
- Two variables names with identical values will have the same id().
- Aliasing: Python saves memory space by having two variables names point to the same memory ID.



```
1 x3 = x1
2 print(x3)
3 print(id(x3))
4 print(id(x1))
```

- The id() function returns an integer, which corresponds to the address/ID, where the variable is stored in memory.
- Two variables names with identical values will have the same id().
- Aliasing: Python saves memory space by having two variables names point to the same memory ID.

Identifier Memory

	Address	Value
x3	140725454247872	10
x1	140725454247936	12

```
1 x1 = 12
2 print(x1)
3 print(x3)
4 print(id(x1))
5 print(id(x3))
```

Memory management in lists

• A **list** is a collection of variables.

```
1 list1 = [x1, x2, x3]
2 print(list1)
3 print(id(list1))
```

```
[12, 17, 10]
1769354632448
```

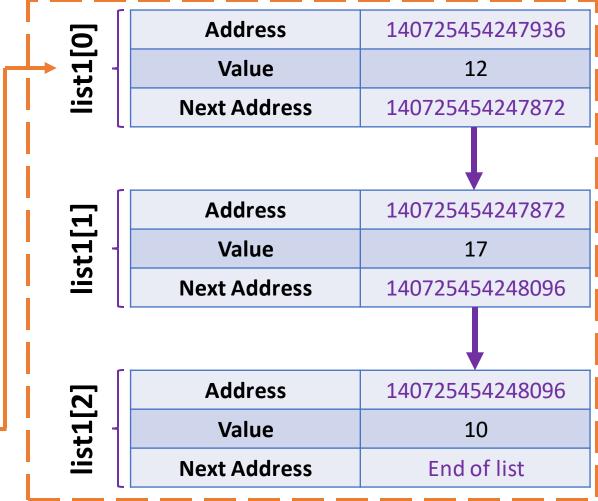
```
print(id(list1))
print("-")
print(id(list1[0]))
print(id(x1))
print("-")
print(id(list1[1]))
print(id(x2))
print("-")
print(id(list1[2]))
print(id(x3))
```

```
1769354632448
140725454247936
140725454247936
140725454248096
140725454248096
140725454247872
140725454247872
```

Memory management in lists

A list is a collection of variables.
 The variables in a list are chained together.





Memory management in lists

- A list is a collection of variables.
 The variables in a list are chained together.
- If x1 is changed, Python will adjust so that the list remains unaffected.
- It simply reallocates x1 to another location in memory.

```
1 print(x1)
2 print(id(x1))
3 x1 = "Hello"
4 print(id(x1))
5 print(list1)
```

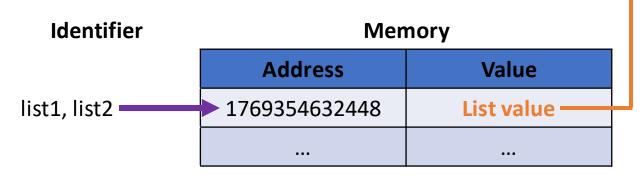
```
12
140726382041088
2120755150000
[12, 17, 10]
```

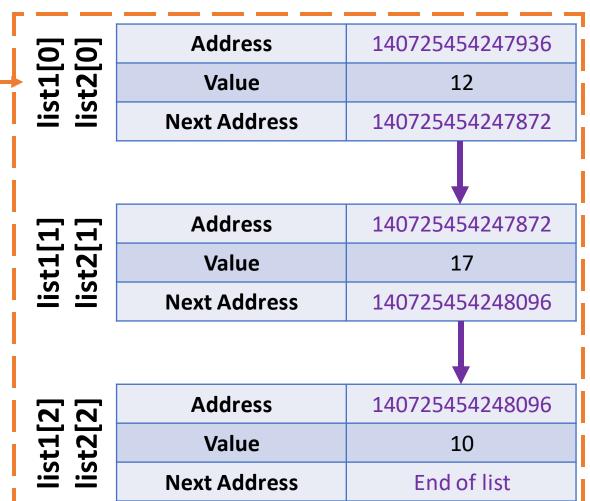
- A list is a collection of variables.
 The variables in a list are chained together.
- Aliasing: We can assign a list to another variable name.

```
1 list2 = list1
2 print(list2)
3 print(id(list1))
4 print(id(list2))
```

```
[12, 17, 10]
1983742564288
1983742564288
```

- A list is a collection of variables.
 The variables in a list are chained together.
- Aliasing: We can assign a list to another variable name.



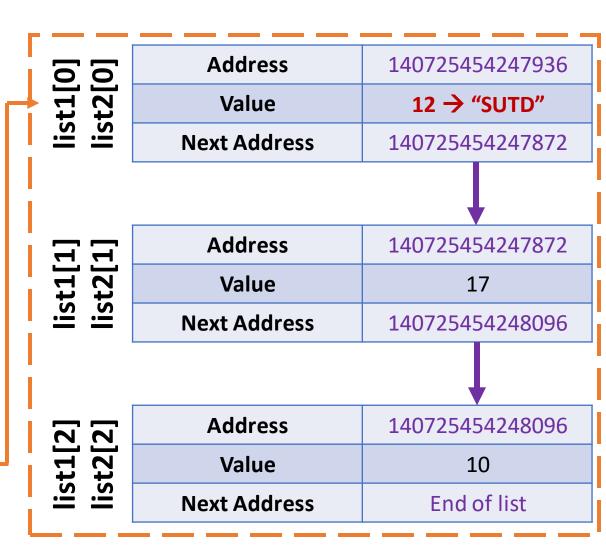


- A list is a collection of variables.
 The variables in a list are chained together.
- Aliasing: We can assign a list to another variable name.
- **Problem:** changing list1[0] changes list1 values, but also changes list2.

```
print(id(list1[0]))
   list1[0] = "SUTD"
   print (list1)
   print(id(list1[0]))
140726382041088
['SUTD', 17, 10]
2120755353584
   print(list2)
   print(id(list2[0]))
['SUTD', 17, 10]
2120755353584
```

- A list is a collection of variables.
 The variables in a list are chained together.
- Aliasing: We can assign a list to another variable name.
- **Problem:** changing list1[0] changes list1 values, but also changes list2.

Identifier	Memory		
	Address	Value	
list1, list2	1 769354632448	List value —	



Shallow copy of a list

- **Problem:** changing list1[0] changes list1 values, but also changes list2.
- **Shallow copy:** list1[:] makes list2 a shallow copy of list1. By doing so, list2 will be saved to its own location of memory.

```
1 list1 = [12, 17, 10]
2 list2 = list1[:]
3 print(list1)
4 print(list2)
5 print(id(list1))
6 print(id(list2))
```

```
[12, 17, 10]
[12, 17, 10]
2120755431296
2120755345920
```

Shallow copy of a list

- **Problem:** changing list1[0] changes list1 values, but also changes list2.
- Shallow copy: list1[:] makes list2 a shallow copy of list1. By doing so, list2 will be saved to its own location of memory.
- Changing a value in list1, with list1[index] = ..., no longer affects list2.
- **Note:** you can also use the copy() method.

```
1 list1 = [12, 17, 10]
2 list2 = list1[:]
3 print(list1)
4 print(list2)
5 print(id(list1))
6 print(id(list2))
[12, 17, 10]
```

```
[12, 17, 10]
[12, 17, 10]
2120755431296
2120755345920
```

```
1 list1[0] = "SUTD"
2 print(list1)
3 print(list2)
```

```
['SUTD', 17, 10]
[12, 17, 10]
```

Shallow copy: problem

- **Note:** if an element of a list is a list (case of lists of lists), then the shallow copy will not copy the sublists to different locations of memory.
- **Problem:** changing a sublist element then affects both lists, even though these lists are shallow copies of each other.

```
1 | list1 = [[8, 9, 11], 7, 4]
 2 | list2 = list1[:]
    print(list1)
 4 | print(list2)
 5 print(id(list1))
 6 print(id(list2))
   print(id(list1[0][1]))
   print(id(list2[0][1]))
[[8, 9, 11], 7, 4]
[[8, 9, 11], 7, 4]
2120755333248
2120755332928
140726382040992
140726382040992
   list1[0][1] = "Damn it!"
 2 print(list1)
    print(list2)
[[8, 'Damn it!', 11], 7, 4]
```

[[8, 'Damn it!', 11], 7, 4]

Deep copy

• Solution: make a deep copy, using the Python built-in copy library.

 A deep copy forces Python to make sure all elements and subelements are assigned to different locations in memory.

```
1 from copy import deepcopy
 1 | list1 = [[8, 9, 11], 7, 4]
 2 list2 = deepcopy(list1)
 3 print(list1)
 4 print (list2)
 5 print(id(list1[0]))
 6 print(id(list2[0]))
[[8, 9, 11], 7, 4]
[[8, 9, 11], 7, 4]
2120754851072
2120754850304
 1 | list1[0][1] = "Deep copy works?"
 2 print(list1)
 3 print(list2)
 4 print(id(list1[0][1]))
   print(id(list2[0][1]))
[[8, 'Deep copy works?', 11], 7, 4]
[[8, 9, 11], 7, 4]
2120755409424
140726382040992
```

Matt's Great advice #?

Matt's Great Advice #?: Keep the aliasing, shallow and deep copies concepts in mind for now.

If you find that modifying a list object ends up unexpectedly changing another, then you might have an aliasing or shallow copy problem.

When in doubt, make a deep copy.

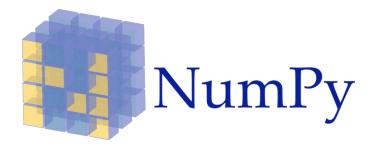
For now, do not worry about understanding all these memory concepts, these will be covered in another advanced course!



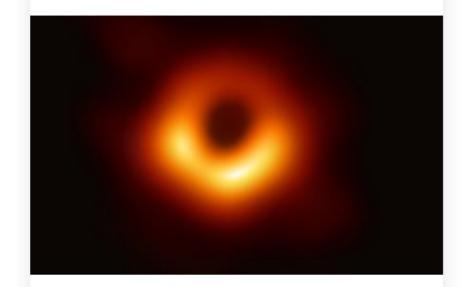
About the numpy library

 Numpy is one of the most common (if not the most popular) libraries in Python.

- Used for many applications: computing, modelling, data science, astrophysics, etc.
- Linear algebra (one of the main concepts of math with many applications in computing)



FIRST IMAGE OF A BLACK HOLE



How NumPy, together with libraries like SciPy and Matplotlib that depend on NumPy, enabled the Event Horizon Telescope to produce the first ever image of a black hole

A new type of objects: Numpy Arrays

- Numpy arrays are objects from the Numpy library.
 - Typically used to describe matrices and vectors,
 - Or **tables** of data.
- The look very similar to (nested lists of) lists, which we have used earlier for many applications.
- The Numpy library, however, comes with many additional functions and methods.

```
import numpy as np
 1 array1 = np.array([0, 2, 1, 4])
 2 print (array1)
[0 2 1 4]
 1 print (array1)
 2 print(type(array1))
 3 array1 as list = list(array1)
   print(array1 as list)
 5 print(type(array1 as list))
[0 2 1 4]
<class 'numpy.ndarray'>
[0, 2, 1, 4]
<class 'list'>
```

Length, size, shape

- Just like lists, the Numpy arrays have a length, which can be checked with len().
- The also have a **shape** and a **size attribute**, which give additional information, in the case of arrays with more than 1D.
- Attribute: "sub-variable" of an object; applies to an object using the . operator. (Object-oriented concept, not covered yet)

```
array1 = np.array([0, 2, 1, 4])
   print(len(array1))
   print(array1.shape)
   print(array1.size)
(4,)
   two d array = np.array([[1,2],[3,4]])
   print(two d array)
   print(len(two d array))
   print(two d array.shape)
   print(two d array.size)
[[1 2]
 [3 4]]
(2, 2)
```

Indexing an array

- Just like lists, the Numpy arrays are indexed and their element can be accessed with [].
- You can equivalently use the [i,j] and [i][j] notations on arrays.
- Replacing an index with a colon symbol:, means "take all".
- For instance, [:, j] means all elements in column j, whereas [i, :] means all elements in row i.

```
1 array1 = np.array([0, 2, 1, 4])
 2 print (array1)
   print(array1[0])
 4 print (array1[1])
[0 2 1 4]
   two d array = np.array([[1,2],[3,4]])
  print (two d array)
   print(two d array[0])
   print(two d array[0][1])
[[1 2]
 [3 4]]
[1 2]
   print(two d array[0,1])
   print(two d array[:,1])
 3 print(two d array[0,:])
```

Traversing an array with for

 As with lists, we can traverse a Numpy array, in an element-wise manner, using a for loop.

```
1 array1 = np.array([0, 2, 1, 4])
2 print(array1)
3 for element in array1:
4 print(element)
```

```
[0 2 1 4]
0
2
1
```

```
my list = [1, 4, 9, 14, 15]
2 print (my list)
[1, 4, 9, 14, 15]
   # Element-wise
 2 for element in my list:
       print("--")
       print(element)
```

The + operator on arrays

• The + operator on lists: On lists, the + operator will concatenate both lists into a new one.

```
1 a_list = [0, 1, 2]
2 another_list = [1, 4, 7]
3 list_sum = a_list + another_list
4 print(list_sum)
```

```
[0, 1, 2, 1, 4, 7]
```

The + operator on arrays

- The + operator on lists: On lists, the + operator will concatenate both lists into a new one.
- The + operator on Numpy arrays – (vector sum): On Numpy arrays, however, the + operator will <u>sum</u> the elements of both Numpy arrays.

```
1 | a list = [0, 1, 2]
    another list = [1, 4, 7]
    list sum = a list + another list
    print(list sum)
[0, 1, 2, 1, 4, 7]
 1 | array1 = np.array([0, 2, 1, 4]) |
   array2 = np.array([1, 2, 3, 5])
   print(array1)
   print(array2)
   sum array = array1 + array2
 6 print(sum array)
[0 2 1 4]
[1 2 3 5]
```

[1 4 4 9]

The + operator on arrays

- The + operator on lists: On lists, the + operator will concatenate both lists into a new one.
- The + operator on Numpy arrays – (vector sum): On Numpy arrays, however, the + operator will <u>sum</u> the elements of both Numpy arrays.
- **Broadcasting:** If summed with a number instead, the elements in the Numpy array will each be incremented by the given value.

```
1 | a list = [0, 1, 2]
    another list = [1, 4, 7]
    list sum = a list + another list
    print(list sum)
[0, 1, 2, 1, 4, 7]
 1 array1 = np.array([0, 2, 1, 4])
   array2 = np.array([1, 2, 3, 5])
   print (array1)
   print (array2)
   sum array = array1 + array2
 6 print(sum_array)
[0 2 1 4]
[1 2 3 5]
[1 \ 4 \ 4 \ 9]
 1 array1 = np.array([0, 2, 1, 4])
 2 | number = 7
   print (array1)
   sum array = array1 + number
 5 print(sum array)
    9 8 11]
```

Concatenation on arrays

• Since the + operator cannot be used for **concatenation**, Numpy comes with a **concatenate()** function.

```
1 print(array1)
2 print(array2)
3 conc_array = np.concatenate([array1, array2])
4 print(conc_array)

[0 2 1 4]
[1 2 3 5]
[0 2 1 4 1 2 3 5]
```

The * operator on arrays

- The * operator behaves as the + operator on Numpy arrays.
- It consists of an **element-wise multiplication** of the elements in arrays.
- **Broadcasting:** if a Numpy array is multiplied by a number, the number will multiply each element in the array.

```
1 array1 = np.array([0, 2, 1, 4])
2 array2 = np.array([1, 2, 3, 5])
3 print(array1)
4 print(array2)
5 mult_arrays = array1*array2
6 print(mult_arrays)
```

```
[0 2 1 4]
[1 2 3 5]
[ 0 4 3 20]
```

```
1  n = 4
2  mult_array_int = array1*n
3  print(mult_array_int)
```

```
[ 0 8 4 16]
```

Additional functions

Additional Numpy functions

- Min, max: returns the minimal, resp. maximal, values in array.
- Argmin, argmax: returns the index where the minimal, resp. maximal, values are.
- Mean, median: returns the mean, resp. median, value for a given array.
- **Sum:** sums all the elements in the array together

```
array1 = np.array([0, 2, 1, 4, 7])
   print (array1)
   min val = np.min(array1)
   print(min val)
   argmin val = np.argmin(array1)
  print(argmin val)
   max val = np.max(array1)
   print (max val)
   argmax val = np.argmax(array1)
   print(argmax val)
   mean val = np.mean(array1)
   print(mean val)
   median val = np.median(array1)
   print (median val)
   summed val = np.sum(array1)
  print(summed val)
[0 2 1 4 7]
```

```
2.8
2.0
14
```

Mathematical functions and constants

Numpy also contains

- Many mathematical functions (cosine, sine, logarithm, exponential, etc.)
- And many mathematical constants (pi, etc.)

```
1 print(np.cos(0))
2 print(np.sin(0))
3 print(np.pi)
4 print(np.log(1))
5 print(np.exp(0))
```

```
1.0
0.0
3.141592653589793
0.0
1.0
```

Aliasing, Shallow and Deep copies in arrays

 As with lists, Numpy arrays are subject to the same issues about aliasing, shallow and deep copies.

• If needed, use deep copies of the arrays.

```
two d array1 = np.array([[1,2],[3,4]])
 2 two d array2 = two d array1
 3 print (two d array1)
 4 print (two d array2)
   print(id(two d array1))
 6 print(id(two d array2))
[[1 2]
 [3 4]]
 [3 4]]
1750029422960
1750029422960
   two d array1[0][0] = 17
 2 print(two d array1)
 3 print (two d array2)
      4]]
```

And so much more! RTFM!

- Numpy has many more functions and tools to offer!
- Random functions (to be covered in an upcoming session, if time allows?)

Learn more about Numpy (RTFM!) here:

https://numpy.org/doc/stable/

```
# Numpy.random.choice() mimics a dice roll
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print (dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print (dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
```

```
6 1 4 3
```

Activity 1 - Exam adjustments

 Let us assume, that I have grades from my students listed in some np.array variables, as shown below.

```
[[60 80 70]
[50 80 65]
[40 70 55]
[60 70 65]
[60 90 75]]
```

Activity 1 - Exam adjustments

- Let us assume, that I have grades from my students listed in a np.array.
- The first line contains the column labels (student name, some scores) and the other lines will consist of entries regarding some of the students.
- Let us assume that, as a professor, I have decided to be lenient towards my students.
- I realized that the midterm was a bit too difficult compared to last year.
- To compensate for that, I would like to increase the scores of all students on the midterm by 50%.

Activity 1 - Exam adjustments

Write a function grade_adjustment(),

- which receives a grades table, grades_table,
- increases the scores of all students on the midterm by 50%,
- re-calculates the average score, with the new adjusted midterm score,
- and then returns the updated grades table as its sole output.

Activity 1 - Exam adjustments

Write a function grade_adjustment(),

- which receives a grades table, grades_table,
- increases the scores of all students on the midterm by 50%,
- re-calculates the average score, with the new adjusted midterm score,
- and then returns the updated grades table as its sole output.

• Important note: The maximal score for the midterm exam is capped to 100. This means that a student which scores 80 points on the midterm, will not obtain 120 points after the adjustment, but only 100.

The import procedure

• The import procedure is used to import functions defined in external .py files.

my_code.py file

```
jupyter my_code.py ✓ Last Tuesday at 1:22 PM
 File
       Edit
              View
                     Language
    def my function(x):
        return 2*x + 1
    def my function2(x):
        return 3*x + 4
    def my function3(x):
        return 4*x + 7
```

The import procedure

- The import procedure is used to import functions defined in external .py files.
- To demonstrate, we have defined a my_code.py file with three functions.

my_code.py file

```
    Jupyter my_code.py
    Last Tuesday at 1:22 PM

 File
        Edit
               View
                      Language
    def my function(x):
        return 2*x + 1
    def my function2(x):
 5
        return 3*x + 4
    def my function3(x):
        return 4*x + 7
```

The import procedure

- The import procedure is used to import functions defined in external .py files.
- To demonstrate, we have defined a my_code.py file with three functions.
- We can then import one of these functions in our Notebook, by using the from ... import ... command.

my_code.py file

```
    Jupyter my_code.py
    Last Tuesday at 1:22 PM

 File
        Edit
               View
                      Language
    def my function(x):
        return 2*x + 1
    def my function2(x):
        return 3*x + 4
    def my function3(x):
         return 4*x + 7
```

```
1 from my_code import my_function
1 print(my_function(2))
5
```

Importing as

 If needed, we can import and rename a function by using the as keyword.

The whole command then reads
 from ... import ... as ...

 Note: if you rename the function, its calling name changes to the alias you specified.

my_code.py file

```
  Jupyter my_code.py
  Last Tuesday at 1:22 PM

 File
       Edit
              View
                      Language
    def my function(x):
        return 2*x + 1
    def my function2(x):
        return 3*x + 4
    def my function3(x):
        return 4*x + 7
```

```
1 print(my_function2(2))

NameError Traceback (most recent call last)

ipython-input-4-20b74e0a7273> in <module>
----> 1 print(my_function2(2))

NameError: name 'my_function2' is not defined

1 print(custom_name(2))

10
```

Importing several functions

 If needed, you can import multiple functions in a single import call.

• Simply use **commas (,) symbols** to separate the different functions names.

 Or, you can also import all functions at once, by simply entering *.

my_code.py file

```
Jupyter my_code.py ✓ Last Tuesday at 1:22 PM
 File
       Edit
              View
                     Language
   def my function(x):
        return 2*x + 1
   def my function2(x):
        return 3*x + 4
   def my function3(x):
        return 4*x + 7
```

```
1 from my_code import my_function, my_function2

1 from my_code import *

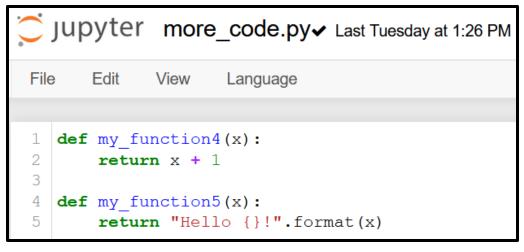
1 print(my_function3(2))

15
```

Importing an entire module

- You can also import a whole file, as a module.
- To do so, simply start with import instead of from.
- By doing so, you import all the functions, but they have to be called using the module name and the dot operator (.).
- This can make the code more readable, but is also a bit more inconvenient.

more_code.py file



Importing an entire module

- You can also use an alias for the module using the as keyword, as before.
- Typically, we often do it with Numpy!

import numpy as np

more_code.py file



```
1 import more_code as mc

1 print(mc.my_function4(2))
3

1 import numpy as np

1 print(np.cos(0))
1.0
```

- **Observation:** Python imported functions from my_code.py, which was located in the same folder as my Notebook.
- But there was no <u>numpy.py file</u> in this location.
- What happened?

- **Observation:** Python imported functions from my_code.py, which was located in the same folder as my Notebook.
- But there was no <u>numpy.py file</u> in this location.
- What happened?

- Python looks for files in your current folder first,
- and then looks in your Python installation directory.

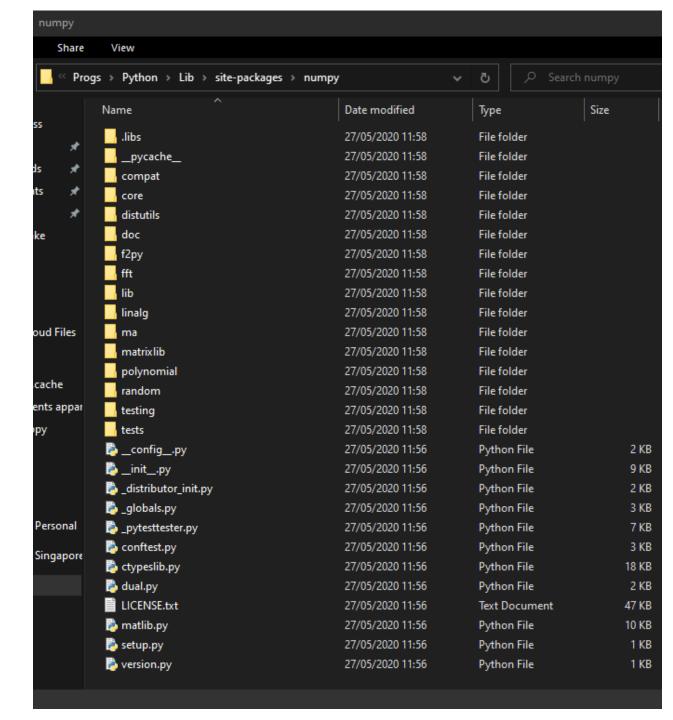
- **Observation:** Python imported functions from my_code.py, which was located in the same folder as my Notebook.
- But there was no <u>numpy.py file</u> in this location.
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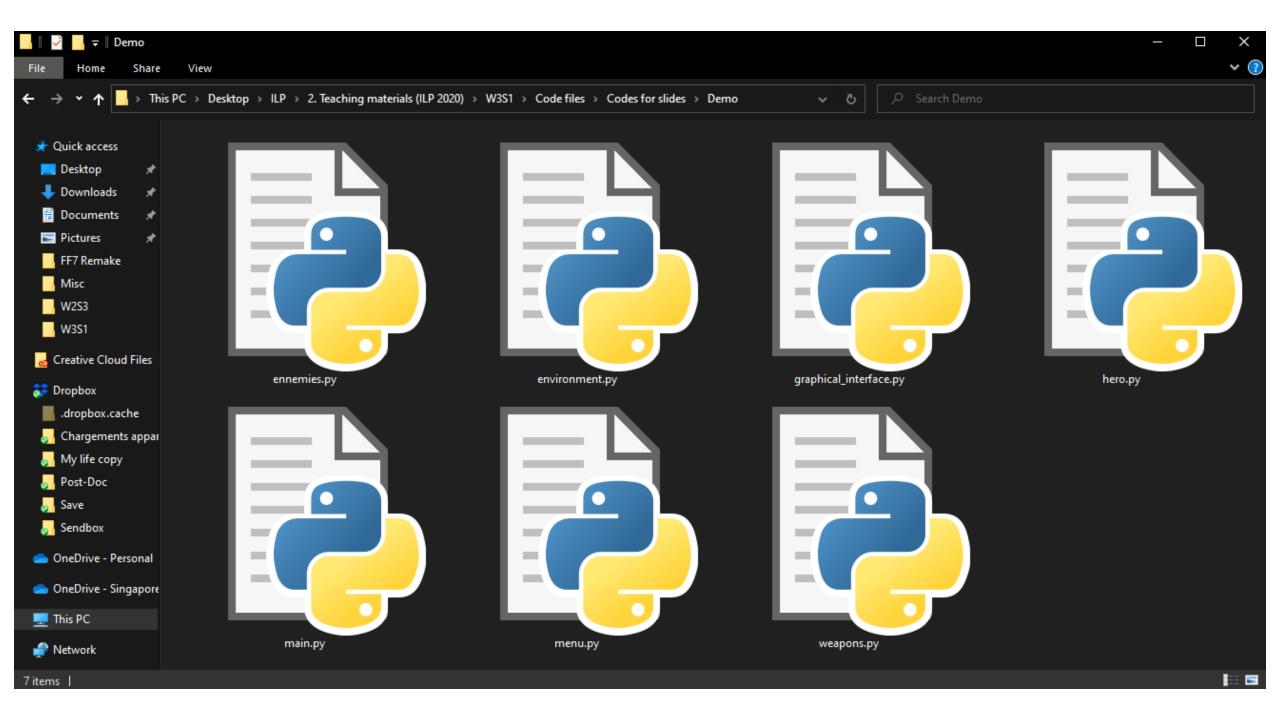


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E.g. in a video game:

- One developer can design the main character,
- Another one will develop enemies,
- Another one will develop items and weapons,
- Another one will design the map/environment in which heroes and enemies evolve,
- Etc.



- Each developer will then work on his/her own .py file, taking care of his/her specific subtask.
- Later on, other developers might import functions from files created by other people.
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 This is something very common in programming projects.

• Important: you need to build the habit of documenting your functions!

Matt's Great advice #?

Matt's Great Advice #10: Good import practices

Some good practices in projects

- 1. As with the variables and functions names, it is a good idea to **make** your file names explicit.
- 2. Have a file for each sub-concept, and a single main file that assembles them all at the end.
- 3. It is often better to **import only what is needed** (**from** ... **import** ...)
 rather than importing everything
 (**from** ... **import** *, **import** ...).



Conclusion

- Memory management and lists: aliasing, shallow and deep copies
- The Numpy library (part 1): arrays, math functions, etc.
- About the import procedure
- Project organizing
- Mini-project