ILP 2020 – W5S1 Numpy library (part 1) and imports

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Outline (Week5, Session1 – W5S1)

- Memory management and lists: aliasing, shallow and deep copies
- The Numpy library (part 1): arrays, math functions, etc.
- About the import procedure
- Project organizing
- Mini-project

Memory of a computer

• The memory of a computer consists of several "boxes", which can contain values for variables. Each "box" is identified by an **integer**, which corresponds to the **address/ID** of the "box".



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- When a variable is created:
 - A "box" is assigned for the variable and its value is stored in the "box".
 - The variable name simply refers to the address/ID of the "box".



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- When a variable is created:
 - A "box" is assigned for the variable and its value is stored in the "box".
 - The variable name simply refers to the address/ID of the "box".



```
1 x1 = 10
2 print(x1)
3 print(id(x1))
```

 The id() function returns an integer, which corresponds to the address/ID, where the variable is stored in memory.

```
1 x1 = 10
2 print(x1)
3 print(id(x1))
```

10 140725454247872

```
1 x2 = 17
2 print(x2)
3 print(id(x2))
```

- The id() function returns an integer, which corresponds to the address/ID, where the variable is stored in memory.
- Two variables names with identical values will have the same id().

```
1 x1 = 10
2 print(x1)
3 print(id(x1))
```

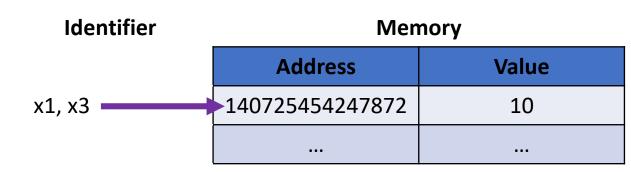
10 140725454247872

```
1 x2 = 17
2 print(x2)
3 print(id(x2))
```

17 140725454248096

```
1 x3 = x1
2 print(x3)
3 print(id(x3))
4 print(id(x1))
```

- The id() function returns an integer, which corresponds to the address/ID, where the variable is stored in memory.
- Two variables names with identical values will have the same id().
- Aliasing: Python saves memory space by having two variables names point to the same memory ID.



```
1 x3 = x1
2 print(x3)
3 print(id(x3))
4 print(id(x1))
```

- The id() function returns an integer, which corresponds to the address/ID, where the variable is stored in memory.
- Two variables names with identical values will have the same id().
- Aliasing: Python saves memory space by having two variables names point to the same memory ID.

Identifier Memory Address Value

	Address	Value
x3	140725454247872	10
x1	140725454247936	12

```
1 x1 = 12
2 print(x1)
3 print(x3)
4 print(id(x1))
5 print(id(x3))
```

Memory management in lists

• A **list** is a collection of variables.

```
1 list1 = [x1, x2, x3]
2 print(list1)
3 print(id(list1))
```

```
[12, 17, 10]
1769354632448
```

```
print(id(list1))
print("-")
print(id(list1[0]))
print(id(x1))
print("-")
print(id(list1[1]))
print(id(x2))
print("-")
print(id(list1[2]))
print(id(x3))
```

```
1769354632448

-

140725454247936

140725454247936

-

140725454248096

140725454248096

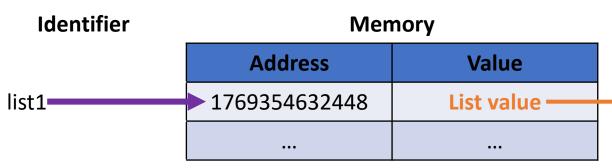
-

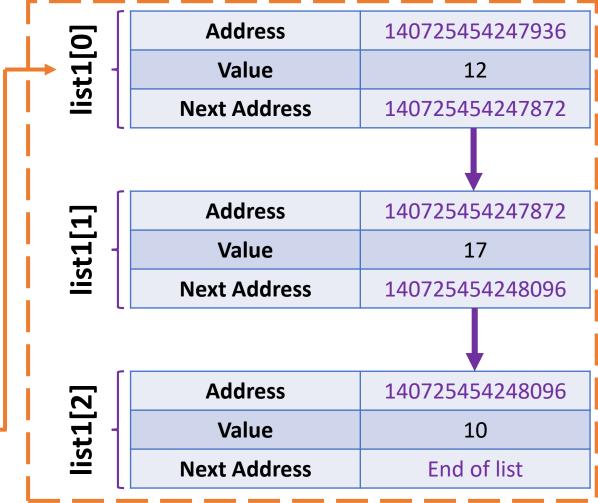
140725454247872

140725454247872
```

Memory management in lists

A list is a collection of variables.
 The variables in a list are chained together.





Memory management in lists

- A list is a collection of variables.
 The variables in a list are chained together.
- If x1 is changed, Python will adjust so that the list remains unaffected.
- It simply reallocates x1 to another location in memory.

```
1 print(x1)
2 print(id(x1))
3 x1 = "Hello"
4 print(id(x1))
5 print(list1)
```

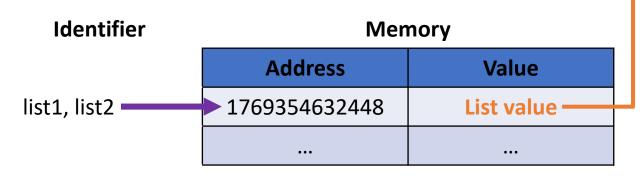
```
12
140726382041088
2120755150000
[12, 17, 10]
```

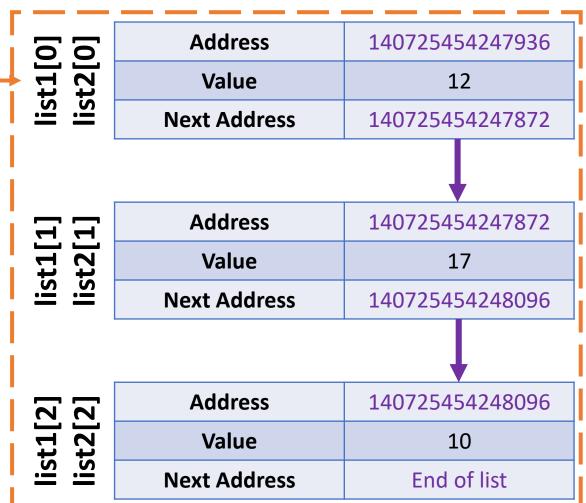
- A list is a collection of variables.
 The variables in a list are chained together.
- Aliasing: We can assign a list to another variable name.

```
1 list2 = list1
2 print(list2)
3 print(id(list1))
4 print(id(list2))
```

```
[12, 17, 10]
1983742564288
1983742564288
```

- A list is a collection of variables.
 The variables in a list are chained together.
- Aliasing: We can assign a list to another variable name.





- A list is a collection of variables.
 The variables in a list are chained together.
- Aliasing: We can assign a list to another variable name.
- **Problem:** changing list1[0] changes list1 values, but also changes list2.

```
1 print(id(list1[0]))
2 list1[0] = "SUTD"
3 print(list1)
4 print(id(list1[0]))

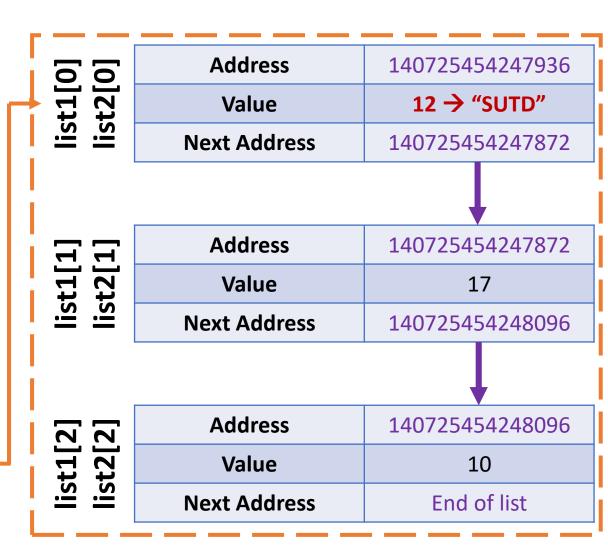
140726382041088
['SUTD', 17, 10]
2120755353584
```

```
1 print(list2)
2 print(id(list2[0]))
```

```
['SUTD', 17, 10]
2120755353584
```

- A list is a collection of variables.
 The variables in a list are chained together.
- Aliasing: We can assign a list to another variable name.
- **Problem:** changing list1[0] changes list1 values, but also changes list2.

ldentifier	Memory	
	Address	Value
list1, list2	1769354632448	List value



Shallow copy of a list

- **Problem:** changing list1[0] changes list1 values, but also changes list2.
- Shallow copy: list1[:] makes list2 a shallow copy of list1. By doing so, list2 will be saved to its own location of memory.

```
1 list1 = [12, 17, 10]
2 list2 = list1[:]
3 print(list1)
4 print(list2)
5 print(id(list1))
6 print(id(list2))
```

```
[12, 17, 10]
[12, 17, 10]
2120755431296
2120755345920
```

Shallow copy of a list

- **Problem:** changing list1[0] changes list1 values, but also changes list2.
- **Shallow copy:** list1[:] makes list2 a shallow copy of list1. By doing so, list2 will be saved to its own location of memory.
- Changing a value in list1, with list1[index] = ..., no longer affects list2.

```
1 list1 = [12, 17, 10]
2 list2 = list1[:]
3 print(list1)
4 print(list2)
5 print(id(list1))
6 print(id(list2))
[12, 17, 10]
```

```
[12, 17, 10]
[12, 17, 10]
2120755431296
2120755345920
```

```
1 list1[0] = "SUTD"
2 print(list1)
3 print(list2)
```

```
['SUTD', 17, 10]
[12, 17, 10]
```

Shallow copy: problem

- **Note:** if an element of a list is a list (case of lists of lists), then the shallow copy will not copy the sublists to different locations of memory.
- **Problem:** changing a sublist element then affects both lists, even though these lists are shallow copies of each other.

```
1 | list1 = [[8, 9, 11], 7, 4]
 2 | list2 = list1[:]
   print(list1)
  print(list2)
 5 print(id(list1))
 6 print(id(list2))
   print(id(list1[0][1]))
   print(id(list2[0][1]))
[[8, 9, 11], 7, 4]
[[8, 9, 11], 7, 4]
2120755333248
2120755332928
140726382040992
140726382040992
   list1[0][1] = "Damn it!"
 2 print(list1)
   print(list2)
[[8, 'Damn it!', 11], 7, 4]
```

[[8, 'Damn it!', 11], 7, 4]

Deep copy

• Solution: make a deep copy, using the Python built-in copy library.

 A deep copy forces Python to make sure all elements and subelements are assigned to different locations in memory.

```
1 from copy import deepcopy
 1 \mid list1 = [[8, 9, 11], 7, 4]
 2 list2 = deepcopy(list1)
 3 print(list1)
 4 print (list2)
 5 | print(id(list1[0]))
 6 print(id(list2[0]))
[[8, 9, 11], 7, 4]
[[8, 9, 11], 7, 4]
2120754851072
2120754850304
 1 | list1[0][1] = "Deep copy works?"
 2 print(list1)
 3 print(list2)
 4 print(id(list1[0][1]))
   print(id(list2[0][1]))
[[8, 'Deep copy works?', 11], 7, 4]
[[8, 9, 11], 7, 4]
2120755409424
140726382040992
```

Matt's Great advice #?

Matt's Great Advice #?: Keep the aliasing, shallow and deep copies concepts in mind for now.

If you find that modifying a list object ends up unexpectedly changing another, then you might have an aliasing or shallow copy problem.

When in doubt, make a deep copy.

Do not worry about understanding all these memory concepts, these will be covered in another specific course on computer hardware!

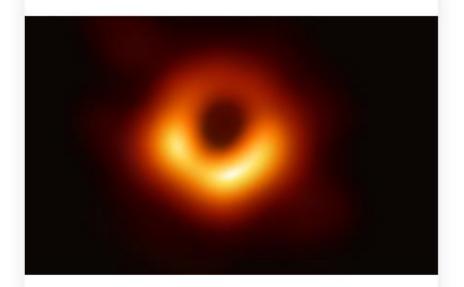


About the numpy library

- Numpy is one of the most common (if not the most popular) libraries in Python.
- Used for many applications: computing, modelling, data science, astrophysics, etc.



FIRST IMAGE OF A BLACK HOLE



How NumPy, together with libraries like SciPy and Matplotlib that depend on NumPy, enabled the Event Horizon Telescope to produce the first ever image of a black hole

A new type of objects: Numpy Arrays

- Numpy arrays are objects from the Numpy library.
 - Typically used to describe matrices and vectors,
 - Or **tables** of data.
- The look very similar to (nested) lists of lists, which we have used earlier for many applications.
- The Numpy library, however, comes with many additional functions and methods.

```
import numpy as np
 1 array1 = np.array([0, 2, 1, 4])
 2 print (array1)
[0 2 1 4]
 1 print (array1)
 2 print(type(array1))
   array1 as list = list(array1)
   print(arrayl as list)
 5 print(type(array1 as list))
[0 2 1 4]
<class 'numpy.ndarray'>
[0, 2, 1, 4]
<class 'list'>
```

Length, size, shape

- Just like lists, the Numpy arrays have a length, which can be checked with len().
- The also have a **shape** and a **size attribute**, which give additional information, in the case of arrays with more than 1D.
- Attribute: "sub-variable" of an object; applies to an object using the operator. (Object-oriented concept, not covered)

```
array1 = np.array([0, 2, 1, 4])
   print(len(array1))
   print(array1.shape)
   print(array1.size)
(4,)
   two d array = np.array([[1,2],[3,4]])
   print(two d array)
   print(len(two d array))
   print(two d array.shape)
   print(two d array.size)
[[1 2]
 [3 4]]
(2, 2)
```

Indexing an array

- Just like lists, the Numpy arrays are indexed and their element can be accessed with [].
- You can equivalently use the [i,j] and [i][j] notations on arrays.
- Replacing an index with a colon symbol:, means "take all".
- For instance, [:, j] means all elements in column j, whereas [i, :] means all elements in row i.

```
1 array1 = np.array([0, 2, 1, 4])
   print (array1)
   print(array1[0])
   print(array1[1])
[0 2 1 4]
   two d array = np.array([[1,2],[3,4]])
   print(two d array)
   print(two d array[0])
   print(two d array[0][1])
[[1 2]
 [3 4]]
[1 2]
   print(two d array[0,1])
   print(two d array[:,1])
   print(two d array[0,:])
```

Traversing an array with for

 As with lists, we can traverse a Numpy array, in an element-wise manner, using a for loop.

```
1 array1 = np.array([0, 2, 1, 4])
2 print(array1)
3 for element in array1:
4 print(element)
```

```
[0 2 1 4]
0
2
1
4
```

```
1 my list = [1, 4, 9, 14, 15]
2 print (my list)
[1, 4, 9, 14, 15]
   # Element-wise
 2 | for element in my list:
       print("--")
        print(element)
```

The + operator on arrays

• The + operator on lists: On lists, the + operator will concatenate both lists into a new one.

```
1 a_list = [0, 1, 2]
2 another_list = [1, 4, 7]
3 list_sum = a_list + another_list
4 print(list_sum)
```

```
[0, 1, 2, 1, 4, 7]
```

The + operator on arrays

- The + operator on lists: On lists, the + operator will **concatenate** both lists into a new one.
- The + operator on Numpy arrays - (vector sum): On Numpy arrays, however, the + operator will **sum** the elements of both Numpy arrays.

```
1 | a list = [0, 1, 2]
    another list = [1, 4, 7]
    list sum = a list + another list
    print(list sum)
[0, 1, 2, 1, 4, 7]
 1 | array1 = np.array([0, 2, 1, 4]) |
   array2 = np.array([1, 2, 3, 5])
   print (array1)
   print (array2)
   sum array = array1 + array2
 6 print(sum array)
[0 2 1 4]
[1 2 3 5]
```

```
[1 4 4 9]
```

The + operator on arrays

- The + operator on lists: On lists, the + operator will concatenate both lists into a new one.
- The + operator on Numpy arrays – (vector sum): On Numpy arrays, however, the + operator will <u>sum</u> the elements of both Numpy arrays.
- Broadcasting: If summed with a number instead, the elements in the Numpy array will each be incremented by the given value.

```
1 | a list = [0, 1, 2]
    another list = [1, 4, 7]
    list sum = a list + another list
    print(list sum)
[0, 1, 2, 1, 4, 7]
 1 | array1 = np.array([0, 2, 1, 4]) |
   array2 = np.array([1, 2, 3, 5])
   print (array1)
   print (array2)
   sum array = array1 + array2
 6 print(sum_array)
[0 2 1 4]
[1 2 3 5]
[1 \ 4 \ 4 \ 9]
 1 array1 = np.array([0, 2, 1, 4])
 2 | number = 7
   print (array1)
   sum array = array1 + number
 5 print(sum array)
       8 11]
```

Concatenation on arrays

• Since the + operator cannot be used for **concatenation**, Numpy comes with a **concatenate()** function.

```
1 print(array1)
2 print(array2)
3 conc_array = np.concatenate([array1, array2])
4 print(conc_array)

[0 2 1 4]
[1 2 3 5]
[0 2 1 4 1 2 3 5]
```

The * operator on arrays

- The * operator behaves as the + operator on Numpy arrays.
- It consists of an **element-wise multiplication** of the elements in arrays.
- **Broadcasting:** if a Numpy array is multiplied by a number, the number will multiply each element in the array.

```
1 array1 = np.array([0, 2, 1, 4])
2 array2 = np.array([1, 2, 3, 5])
3 print(array1)
4 print(array2)
5 mult_arrays = array1*array2
6 print(mult_arrays)
[0 2 1 4]
[1 2 3 5]
```

```
1 n = 4
2 mult_array_int = array1*n
3 print(mult_array_int)
```

```
[ 0 8 4 16]
```

[0 4 3 20]

Additional functions

Additional Numpy functions

- Min, max: returns the minimal, resp. maximal, values in array.
- **Argmin, argmax:** returns the index where the minimal, resp. maximal, values are.
- Mean, median: returns the mean, resp. median, value for a given array.
- **Sum:** sums all the elements in the array together

```
array1 = np.array([0, 2, 1, 4, 7])
    print (array1)
   min val = np.min(array1)
    print(min val)
   argmin val = np.argmin(array1)
   print(argmin val)
   max val = np.max(array1)
   print(max val)
    argmax val = np.argmax(array1)
   print(argmax val)
   mean val = np.mean(array1)
   print(mean val)
   median val = np.median(array1)
    print(median val)
    summed val = np.sum(array1)
   print(summed val)
[0 2 1 4 7]
2.8
2.0
14
```

Mathematical functions and constants

Numpy also contains

- Many mathematical functions (cosine, sine, logarithm, exponential, etc.)
- And many mathematical constants (pi, etc.)

```
1 print(np.cos(0))
2 print(np.sin(0))
3 print(np.pi)
4 print(np.log(1))
5 print(np.exp(0))
```

```
1.0
0.0
3.141592653589793
0.0
1.0
```

Aliasing, Shallow and Deep copies in arrays

 As with lists, Numpy arrays are subject to the same issues about aliasing, shallow and deep copies.

• If needed, use deep copies of the arrays.

```
two d array1 = np.array([[1,2],[3,4]])
 2 two d array2 = two d array1
 3 print (two d array1)
 4 print(two d array2)
   print(id(two d array1))
 6 print(id(two d array2))
[[1 2]
 [3 4]]
 [3 4]]
1750029422960
1750029422960
 1 | two d array1[0][0] = 17
 2 print(two d array1)
 3 print (two d array2)
      4]]
```

And so much more! RTFM!

- Numpy has many more functions and tools to offer!
- Random functions (to be covered in an upcoming session, if time allows?)

Learn more about Numpy (RTFM!) here:

https://numpy.org/doc/stable/

```
# Numpy.random.choice() mimics a dice roll
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print (dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
dice roll = np.random.choice([1, 2, 3, 4, 5, 6])
print(dice roll)
```

```
6 1 4 3
```

Activity 1 - Exam adjustments

 Let us assume, that I have grades from my students listed in a np.array. The first line contains the column labels (student name, some scores) and the other lines will consist of entries regarding some of the students.

- Let us assume, that I have grades from my students listed in a np.array.
- The first line contains the column labels (student name, some scores) and the other lines will consist of entries regarding some of the students.
- Let us assume that, as a professor, I have decided to be lenient towards my students.
- I realized that the midterm was a bit too difficult compared to last year.
- To compensate for that, I would like to increase the scores of all students on the midterm by 50%.

Write a function grade_adjustment(),

- which receives a grades table, grades_table,
- increases the scores of all students on the midterm by 50%,
- re-calculates the average score, with the new adjusted midterm score,
- and then returns the updated grades table as its sole output.

Write a function grade_adjustment(),

- which receives a grades table, grades_table,
- increases the scores of all students on the midterm by 50%,
- re-calculates the average score, with the new adjusted midterm score,
- and then returns the **updated grades table** as its sole output.

• Important note: The maximal score for the midterm exam is capped to 100. This means that a student which scores 80 points on the midterm, will not obtain 120 points after the adjustment, but only 100.

Write a function grade_adjustment(),

- which receives a grades table, grades_table,
- increases the scores of all students on the midterm by 50%,
- re-calculates the average score, with the new adjusted midterm score,
- and then returns the updated grades table as its sole output.

- Important note: The maximal score for the midterm exam is capped to 100. This means that a student which scores 80 points on the midterm, will not obtain 120 points after the adjustment, but only 100.
- Another important note: in this activity, the entries are strings, not numerical types! Do not forget to convert to int/float before doing any math on those!

The import procedure

• The import procedure is used to import functions defined in external .py files.

my_code.py file

```
    Jupyter my_code.py
    Last Tuesday at 1:22 PM

 File
        Edit
              View
                      Language
    def my function(x):
        return 2*x + 1
    def my function2(x):
        return 3*x + 4
    def my function3(x):
        return 4*x + 7
```

The import procedure

- The import procedure is used to import functions defined in external .py files.
- To demonstrate, we have defined a my_code.py file with three functions.

my_code.py file

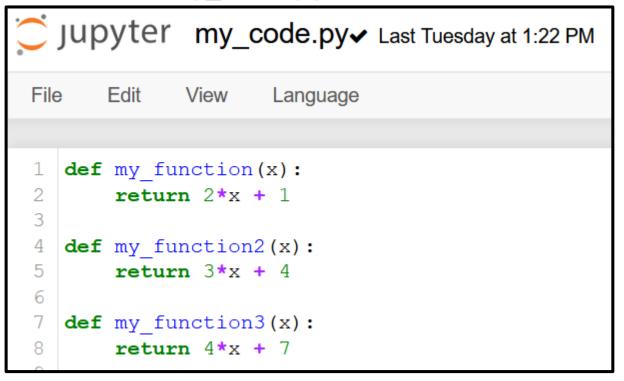
```
  Jupyter my_code.py
  Last Tuesday at 1:22 PM

 File
       Edit
              View
                      Language
    def my function(x):
        return 2*x + 1
    def my function2(x):
 5
        return 3*x + 4
 6
    def my function3(x):
        return 4*x + 7
```

The import procedure

- The import procedure is used to import functions defined in external .py files.
- To demonstrate, we have defined a my_code.py file with three functions.
- We can then import one of these functions in our Notebook, by using the from ... import ... command.

my_code.py file



```
1 from my_code import my_function

1 print(my_function(2))
5
```

Importing as

 If needed, we can import and rename a function by using the as keyword.

• The whole command then reads from ... import ... as ...

 Note: if you rename the function, its calling name changes to the alias you specified.

my_code.py file

```
my code.py ✓ Last Tuesday at 1:22 PM
File
      Edit
             View
                     Language
  def my function(x):
       return 2*x + 1
  def my function2(x):
       return 3*x + 4
  def my function3(x):
       return 4*x + 7
```

```
from my_code import my_function2 as custom_name

1 print(my_function2(2))

NameError Traceback (most recent call last)

<ipython-input-4-20b74e0a7273> in <module>
----> 1 print(my_function2(2))

NameError: name 'my_function2' is not defined

1 print(custom_name(2))

10
```

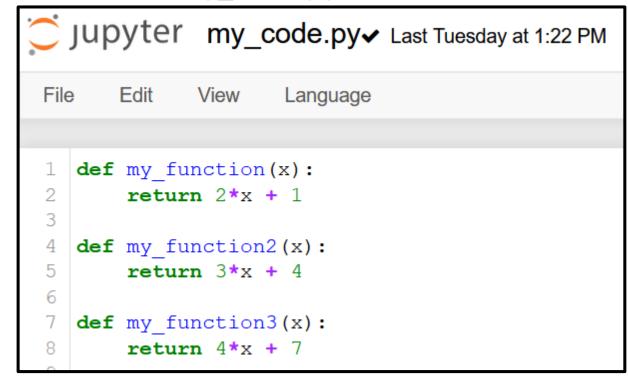
Importing several functions

 If needed, you can import multiple functions in a single import call.

• Simply use **commas (,) symbols** to separate the different functions names.

 Or, you can also import all functions at once, by simply entering *.

my_code.py file



```
1 from my_code import my_function, my_function2

1 from my_code import *

1 print(my_function3(2))

15
```

Importing an entire module

- You can also import a whole file, as a module.
- To do so, simply start with import instead of from.
- By doing so, you import all the functions, but they have to be called using the module name and the dot operator (.).
- This can make the code more readable, but is also a bit more inconvenient.

more_code.py file



Importing an entire module

- You can also use an alias for the module using the as keyword, as before.
- Typically, we often do it with Numpy!

import numpy as np

more_code.py file



```
1 import more_code as mc

1 print(mc.my_function4(2))
3

1 import numpy as np

1 print(np.cos(0))
1.0
```

- **Observation:** Python imported functions from my_code.py, which was located in the same folder as my Notebook.
- But there was <u>no numpy.py file</u> in this location.
- What happened?

- **Observation:** Python imported functions from my_code.py, which was located in the same folder as my Notebook.
- But there was <u>no numpy.py file</u> in this location.
- What happened?

- Python looks for files in your current folder first,
- and then looks in your Python installation directory.

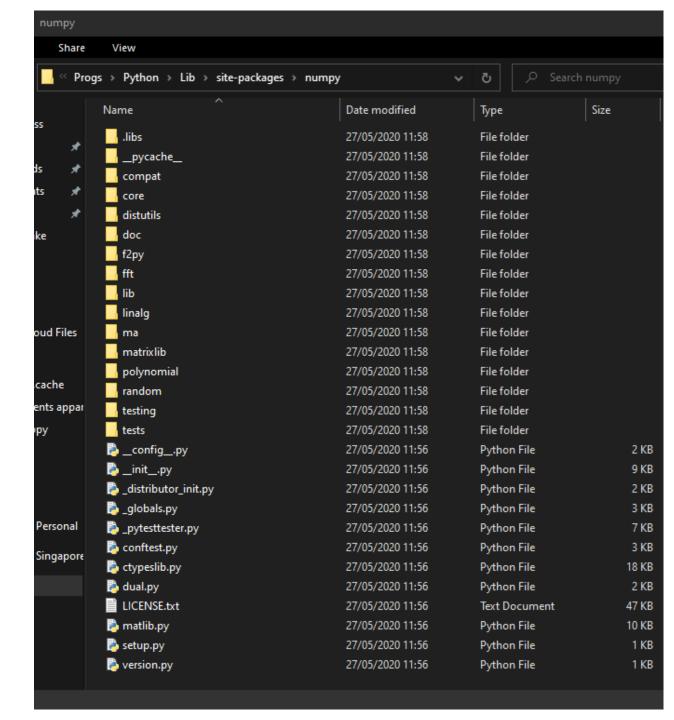
- **Observation:** Python imported functions from my_code.py, which was located in the same folder as my Notebook.
- But there was no numpy.py file in this location.
- What happened?

- Python looks for files in your current folder first,
- and then looks in your Python installation directory.

 When you installed the Numpy package with pip on Week 1, you downloaded some numpy files and stored them in your Python installation folder!

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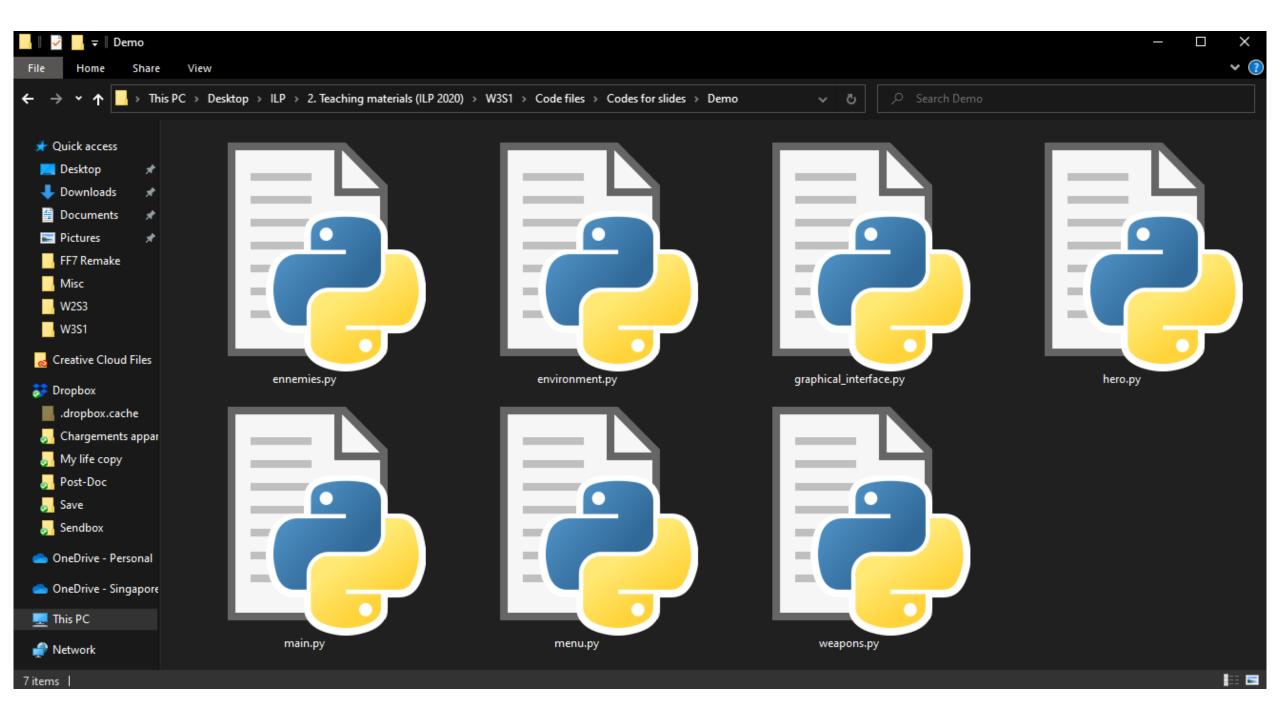


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E.g. in a video game:

- One developer can design the main character,
- Another one will develop enemies,
- Another one will develop items and weapons,
- Another one will design the map/environment in which heroes and enemies evolve,
- Etc.



- Each developer will then work on his/her own .py file, taking care of his/her specific subtask.
- Later on, other developers might import functions from files created by other people.
- Eventually assemble all pieces in a main.py file!

- Each developer will then work on his/her own .py file, taking care of his/her specific subtask.
- Later on, other developers might import functions from files created by other people.
- Eventually assemble all pieces in a main.py file!

 This is something very common in programming projects.

 Important: you need to build the habit of documenting your functions!

Matt's Great advice #?

Matt's Great Advice #?: Good import practices

Some good practices in projects

- 1. As with the variables and functions names, it is a good idea to **make** your file names explicit.
- 2. Have a file for each sub-concept, and a single main file that assembles them all at the end.
- 3. It is often better to **import only what is needed** (**from** ... **import** ...)
 rather than importing everything
 (**from** ... **import** *, **import** ...).



Conclusion

- Memory management and lists: aliasing, shallow and deep copies
- The Numpy library (part 1): arrays, math functions, etc.
- About the import procedure
- Project organizing
- Mini-project

Practice activities: our first programming project!

- Let us practice these Numpy, imports and project structuring concepts with the next three activities (2, 3, 4).
- In these activities, you will progressively design a tic tac toe game, reusing functions from previous activities, and using a function, which I designed, even though you do not know about the library I used (matplotlib, used to display figures in Python).
- Take these in order and follow the steps to work your way to a fully functional tic tac toe game!

Activity 2 - Tic Tac Toe display and check for valid actions

Two tasks are given in this first tic tac toe activity.

- First, import the display_board() function from an external file.
- This function is coded using a library you do not know about (yet), but that should not prevent you from using it!
- It will be used to display any tic tac toe board defined as a Numpy array.

Activity 2 - Tic Tac Toe display and check for valid actions

• Two tasks are given in this first tic tac toe activity.

- Second, you will have to design a check_valid_coordinates() function, which will receive a board, and two coordinates corresponding to an action.
- This function will return a Boolean, with value True, if the action is valid (i.e. the coordinates given correspond to an empty cell in our board); and False otherwise.

Activity 3 - Tic Tac Toe display and take actions

Two tasks are given in this second tic tac toe activity.

First, import the display_board() and check_valid_coordinates()
 functions from an external file.

Activity 3 - Tic Tac Toe display and take actions

• Two tasks are given in this second tic tac toe activity.

Second, you will have to design a function take_action(), which:

- receives a board, as a 3×3 number array; it consists of the current state of the game.
- receives two number coordinates x_coord and y_coord; it correspond to a position where the next player would like to play.
- receives a boolean is_circle set to True if it is circles' turn to play, and False if it is crosses' turn.

Activity 3 - Tic Tac Toe display and take actions

This function should

- display the current board in variable board, and right before that, print a message that reads "Displaying previous board.";
- check if the coordinates x_coord and y_coord are valid for this current board;
- if these are valid, it should alter the board, by adding an extra value somewhere, as to take into account the intent of the current player (circles or crosses) to play at coordinates x_coord and y_coord;

- once updated, it should then display the updated board, and right before that, print a message that reads "Displaying new board after action [..., ...].", with the blanks (...) filled accordingly;
- Finally, it should return the updated board, with the added action.
- Note that if the given action x_coord and y_coord is invalid, then the board should remain unchanged, and the function will simply return the original board, without any updates.

Two tasks are given in this final tic tac toe activity.

- First, you need to import four functions defined in the previous activity, from a file.
- Second, design our main function **tictactoe()**, which will reuse all other functions!

This function should

- 1. Initialize an empty board, as a 3×3 number array, filled with zeroes.
- 2. Display a message "Game just started!", and display the empty board.
- 3. While the game is not over (i.e. there is no winner and there are playable actions left), it should
 - ask the user for coordinates to play using two input() calls (one for the x coordinate, one of the y coordinate),
 - it should then check if the coordinates are valid (using the check_valid_coordinates() function), for the current board state,
 - if the coordinates are valid, it should add the action of the player at the given coordinates and update the board, using the take_action() function.

The output of the take_action() function gives the new board state after the current player's action was added to the board.

Once circles are done playing their turn, it should become crosses' turn to play, and vice versa.

- 4. When the end is reached (a player won, or no more actions left to play), the function should:
- display "It's a draw!" if no players have won,
- display "Player ... won!", where the blanks are filled accordingly (Player 1 has circles, player 2 has crosses.)
- Note: Player 1 (circles) should be the first to play.

Quite a lot of sub-tasks!

But take it slow and carefully assemble the game, by following the steps and reusing your previous functions!