

Problem 1



$$\mathcal{L} = \frac{1}{2}m(\dot{x}_1^2 + \dot{x}_2^2 + \dot{y}_1^2 + \dot{y}_2^2)$$

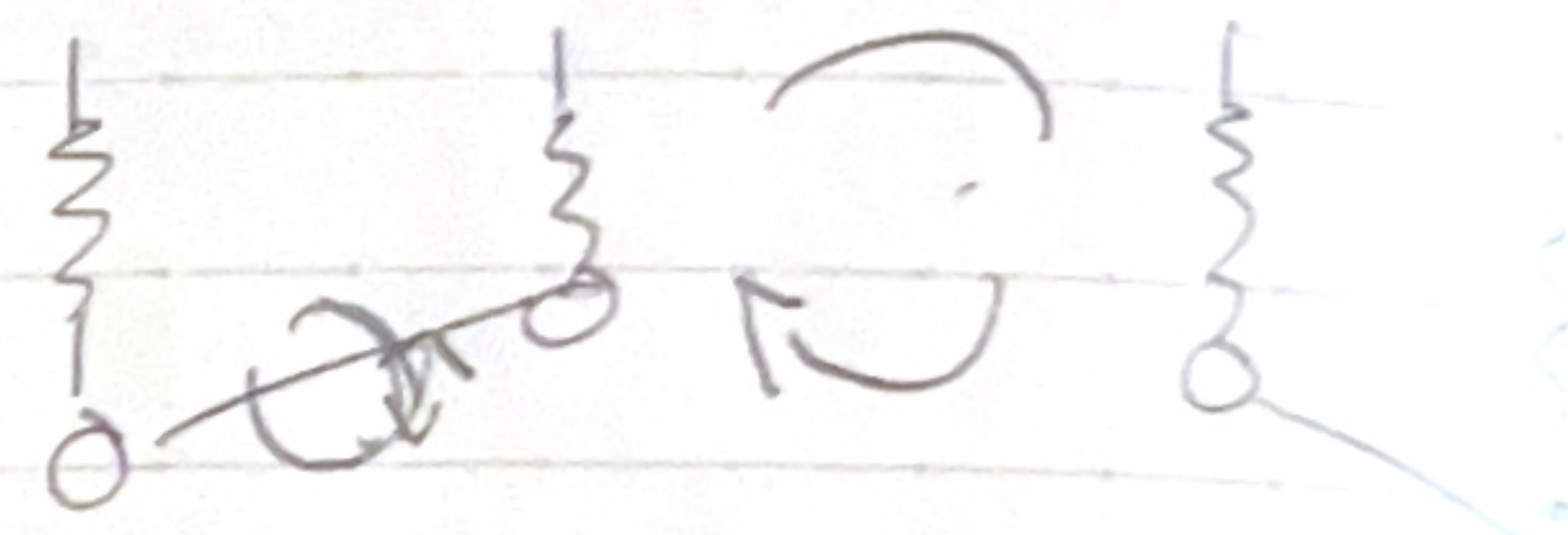
$$M = \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} \quad V = \begin{pmatrix} 0 & 0 \\ 0 & -\frac{L^2}{2} \end{pmatrix}$$

$$V - \lambda M = \begin{pmatrix} -2\lambda & 0 \\ 0 & -\frac{L^2}{2}(1 + \lambda) \end{pmatrix}$$

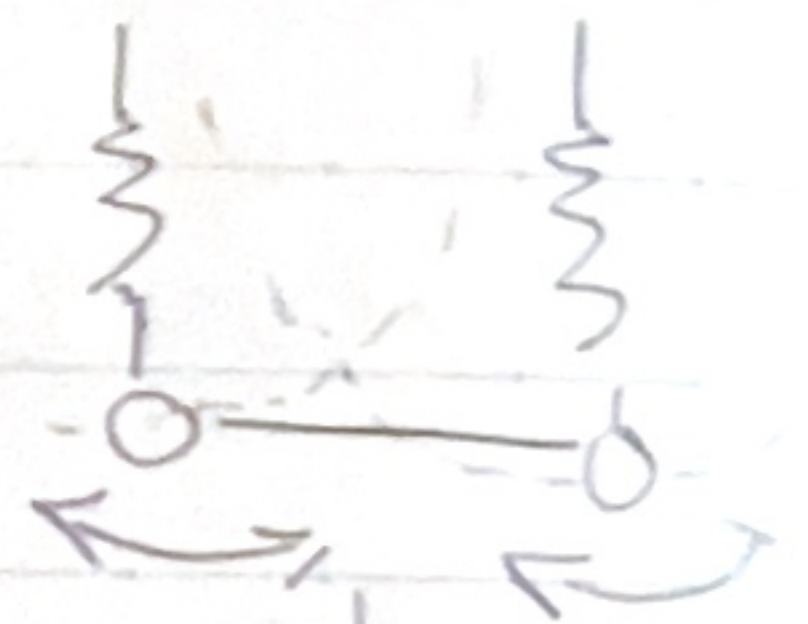
$$\det(V - \lambda M) = -2\lambda \cdot 2(1 + \lambda) \cdot -\frac{L^2}{2}(1 + \lambda) = 0$$

$$\lambda = -1, 0, +1$$

$$\lambda = -1 \rightarrow \begin{pmatrix} 0 & 0 \\ 0 & \frac{L^2}{2} \end{pmatrix}$$



$$\lambda = 0 \rightarrow \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$$



$$\lambda = 1 \rightarrow \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$$

