# Exercise 4

#### Load data

```
# change to your own path!
data_path <- "C:/Users/mattl/OneDrive/Documents/Education/Masters/Courses/Spring Semester/Organizationa
applications <- read_parquet(paste0(data_path, "app_data_sample.parquet"))</pre>
edges <- read_csv(paste0(data_path,"edges_sample.csv"))</pre>
## Rows: 32906 Columns: 4
## -- Column specification -------
## Delimiter: ","
## chr (1): application_number
## dbl (2): ego_examiner_id, alter_examiner_id
## date (1): advice_date
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
applications
## # A tibble: 2,018,477 x 16
     application_number filing_date examiner_name_last examiner_name_first
##
##
      <chr>
                        <date>
                                    <chr>
                                                       <chr>
## 1 08284457
                        2000-01-26 HOWARD
                                                       JACQUELINE
## 2 08413193
                        2000-10-11 YILDIRIM
                                                      BEKIR
                        2000-05-17 HAMILTON
## 3 08531853
                                                      CYNTHIA
                        2001-07-20 MOSHER
## 4 08637752
                                                      MARY
## 5 08682726
                        2000-04-10 BARR
                                                      MICHAEL
## 6 08687412
                        2000-04-28 GRAY
                                                      I.TNDA
## 7 08716371
                        2004-01-26 MCMILLIAN
                                                      KARA
## 8 08765941
                        2000-06-23 FORD
                                                      VANESSA
## 9 08776818
                        2000-02-04 STRZELECKA
                                                      TERESA
## 10 08809677
                        2002-02-20 KIM
                                                      SUN
## # ... with 2,018,467 more rows, and 12 more variables:
      examiner_name_middle <chr>, examiner_id <dbl>, examiner_art_unit <dbl>,
## #
      uspc_class <chr>, uspc_subclass <chr>, patent_number <chr>,
## #
      patent_issue_date <date>, abandon_date <date>, disposal_type <chr>,
```

# Get gender for examiners

We'll get gender based on the first name of the examiner, which is recorded in the field examiner\_name\_first. We'll use library gender for that, relying on a modified version of their own example.

appl\_status\_code <dbl>, appl\_status\_date <chr>, tc <dbl>

Note that there are over 2 million records in the applications table – that's because there are many records for each examiner, as many as the number of applications that examiner worked on during this time frame. Our first step therefore is to get all *unique* names in a separate list examiner\_names. We will then guess gender for each one and will join this table back to the original dataset. So, let's get names without repetition:

```
#install_genderdata_package() # only run this line the first time you use the package, to get data for
# get a list of first names without repetitions
examiner_names <- applications %>%
  distinct(examiner_name_first)
#Now let's use function `gender()` as shown in the example for the package to attach a gender and proba
# get a table of names and gender
examiner_names_gender <- examiner_names %>%
  do(results = gender(.$examiner_name_first, method = "ssa")) %>%
  unnest(cols = c(results), keep_empty = TRUE) %>%
  select(
    examiner_name_first = name,
   gender,
   proportion_female
examiner_names_gender
## # A tibble: 1,822 x 3
##
      examiner_name_first gender proportion_female
##
                                             <dbl>
      <chr>
                          <chr>
##
   1 AARON
                          male
                                            0.0082
## 2 ABDEL
                                            0
                          male
## 3 ABDOU
                                            0
                          male
                                            0
## 4 ABDUL
                          male
## 5 ABDULHAKIM
                                            0
                          male
                                            0
## 6 ABDULLAH
                          male
##
   7 ABDULLAHI
                          male
## 8 ABIGAIL
                          female
                                            0.998
## 9 ABIMBOLA
                          female
                                            0.944
## 10 ABRAHAM
                                            0.0031
                          male
## # ... with 1,812 more rows
# Finally, let's join that table back to our original applications data and discard the temporary table
# remove extra columns from the gender table
examiner_names_gender <- examiner_names_gender %>%
  select(examiner_name_first, gender)
# joining gender back to the dataset
applications <- applications %>%
  left_join(examiner_names_gender, by = "examiner_name_first")
# cleaning up
rm(examiner_names)
rm(examiner_names_gender)
gc()
```

used (Mb) gc trigger (Mb) max used (Mb)

##

```
## Ncells 4815461 257.2
                           8039874 429.4 5177008 276.5
## Vcells 50061480 382.0
                          93358455 712.3 80377241 613.3
```

#### Guess the examiner's race

## 10 KIM

## # ... with 3,796 more rows

We'll now use package wru to estimate likely race of an examiner. Just like with gender, we'll get a list of unique names first, only now we are using surnames.

```
examiner_surnames <- applications %>%
  select(surname = examiner_name_last) %>%
  distinct()
examiner_surnames
## # A tibble: 3,806 x 1
##
      surname
##
      <chr>
##
   1 HOWARD
##
   2 YILDIRIM
##
   3 HAMILTON
##
   4 MOSHER
## 5 BARR
##
  6 GRAY
##
  7 MCMILLIAN
## 8 FORD
## 9 STRZELECKA
## 10 KIM
## # ... with 3,796 more rows
examiner_race <- predict_race(voter.file = examiner_surnames, surname.only = T) %>%
 as_tibble()
## [1] "Proceeding with surname-only predictions..."
## Warning in merge_surnames(voter.file): Probabilities were imputed for 698
## surnames that could not be matched to Census list.
examiner_race
## # A tibble: 3,806 x 6
##
                 pred.whi pred.bla pred.his pred.asi pred.oth
      surname
                                                <dbl>
##
      <chr>
                    <dbl>
                             <dbl>
                                       <dbl>
                                                         <dbl>
##
   1 HOWARD
                   0.643
                           0.295
                                    0.0237
                                              0.005
                                                        0.0333
##
  2 YILDIRIM
                   0.861
                           0.0271
                                    0.0609
                                              0.0135
                                                        0.0372
  3 HAMILTON
                   0.702
                           0.237
                                    0.0245
                                             0.0054
                                                        0.0309
##
##
  4 MOSHER
                   0.947
                           0.00410
                                    0.0241
                                              0.00640
                                                        0.0185
##
  5 BARR
                   0.827
                           0.117
                                    0.0226
                                             0.00590
                                                        0.0271
##
  6 GRAY
                   0.687
                           0.251
                                    0.0241
                                              0.0054
                                                        0.0324
  7 MCMILLIAN
                   0.359
##
                           0.574
                                    0.0189
                                              0.00260
                                                        0.0463
##
   8 FORD
                   0.620
                           0.32
                                    0.0237
                                              0.0045
                                                        0.0313
## 9 STRZELECKA
                   0.666
                           0.0853
                                    0.137
                                                        0.0318
```

0.00650 0.945

0.0252 0.00390

0.0797

0.0198

```
#As you can see, we get probabilities across five broad US Census categories: white, black, Hispanic, A
#Our final step here is to pick the race category that has the highest probability for each last name a
examiner_race <- examiner_race %>%
  mutate(max_race_p = pmax(pred.asi, pred.bla, pred.his, pred.oth, pred.whi)) %>%
  mutate(race = case_when(
   max_race_p == pred.asi ~ "Asian",
   max_race_p == pred.bla ~ "black",
   max_race_p == pred.his ~ "Hispanic",
   max_race_p == pred.oth ~ "other",
   max_race_p == pred.whi ~ "white",
    TRUE ~ NA_character_
  ))
examiner_race
## # A tibble: 3,806 x 8
##
      surname
                 pred.whi pred.bla pred.his pred.asi pred.oth max_race_p race
##
      <chr>
                    <dbl>
                             <dbl>
                                      <dbl>
                                                <dbl>
                                                         <dbl>
                                                                    <dbl> <chr>
  1 HOWARD
                                    0.0237
                                                        0.0333
                                                                    0.643 white
##
                   0.643
                           0.295
                                              0.005
##
  2 YILDIRIM
                   0.861
                           0.0271
                                    0.0609
                                              0.0135
                                                        0.0372
                                                                    0.861 white
## 3 HAMILTON
                   0.702
                           0.237
                                    0.0245
                                              0.0054
                                                        0.0309
                                                                    0.702 white
## 4 MOSHER
                   0.947
                           0.00410
                                    0.0241
                                              0.00640
                                                        0.0185
                                                                    0.947 white
## 5 BARR
                   0.827
                           0.117
                                    0.0226
                                              0.00590
                                                        0.0271
                                                                    0.827 white
## 6 GRAY
                   0.687
                           0.251
                                    0.0241
                                              0.0054
                                                        0.0324
                                                                    0.687 white
## 7 MCMILLIAN
                   0.359
                           0.574
                                    0.0189
                                              0.00260
                                                        0.0463
                                                                    0.574 black
## 8 FORD
                                    0.0237
                   0.620
                           0.32
                                              0.0045
                                                        0.0313
                                                                    0.620 white
## 9 STRZELECKA
                   0.666
                           0.0853
                                    0.137
                                              0.0797
                                                        0.0318
                                                                    0.666 white
                                    0.00650 0.945
## 10 KIM
                   0.0252 0.00390
                                                        0.0198
                                                                    0.945 Asian
## # ... with 3,796 more rows
# Let's join the data back to the applications table.
# removing extra columns
examiner_race <- examiner_race %>%
  select(surname, race)
applications <- applications %>%
  left_join(examiner_race, by = c("examiner_name_last" = "surname"))
rm(examiner_race)
rm(examiner_surnames)
gc()
              used (Mb) gc trigger (Mb) max used (Mb)
## Ncells 5155084 275.4
                            8039874 429.4 6183262 330.3
```

### Examiner's tenure

## Vcells 53747594 410.1

To figure out the timespan for which we observe each examiner in the applications data, let's find the first and the last observed date for each examiner. We'll first get examiner IDs and application dates in a separate table, for ease of manipulation. We'll keep examiner ID (the field examiner\_id), and earliest and

93358455 712.3 92712276 707.4

latest dates for each application (filing\_date and appl\_status\_date respectively). We'll use functions in package lubridate to work with date and time values.

```
examiner_dates <- applications %>%
  select(examiner_id, filing_date, appl_status_date)
examiner_dates
## # A tibble: 2,018,477 x 3
##
      examiner_id filing_date appl_status_date
##
            <dbl> <date>
                              <chr>
##
   1
           96082 2000-01-26 30jan2003 00:00:00
## 2
           87678 2000-10-11 27sep2010 00:00:00
           63213 2000-05-17 30mar2009 00:00:00
##
  3
           73788 2001-07-20 07sep2009 00:00:00
## 4
## 5
           77294 2000-04-10 19apr2001 00:00:00
           68606 2000-04-28 16jul2001 00:00:00
## 6
## 7
           89557 2004-01-26
                             15may2017 00:00:00
## 8
           97543 2000-06-23
                             03apr2002 00:00:00
## 9
           98714 2000-02-04
                             27nov2002 00:00:00
## 10
            65530 2002-02-20 23mar2009 00:00:00
## # ... with 2,018,467 more rows
# The dates look inconsistent in terms of formatting. Let's make them consistent. We'll create new vari
examiner_dates <- examiner_dates %>%
  mutate(start_date = ymd(filing_date), end_date = as_date(dmy_hms(appl_status_date)))
# Let's now identify the earliest and the latest date for each examiner and calculate the difference in
examiner_dates <- examiner_dates %>%
  group_by(examiner_id) %>%
  summarise(
    earliest_date = min(start_date, na.rm = TRUE),
    latest_date = max(end_date, na.rm = TRUE),
    tenure_days = interval(earliest_date, latest_date) %/% days(1)
    ) %>%
  filter(year(latest_date)<2018)
examiner_dates
## # A tibble: 5,625 x 4
##
      examiner_id earliest_date latest_date tenure_days
                                                  <dbl>
##
            <dbl> <date>
                               <date>
##
  1
            59012 2004-07-28
                               2015-07-24
                                                   4013
## 2
           59025 2009-10-26
                               2017-05-18
                                                   2761
## 3
           59030 2005-12-12
                               2017-05-22
                                                   4179
## 4
           59040 2007-09-11
                               2017-05-23
                                                   3542
## 5
           59052 2001-08-21
                               2007-02-28
                                                   2017
## 6
           59054 2000-11-10
                               2016-12-23
                                                   5887
  7
           59055 2004-11-02
                               2007-12-26
                                                   1149
           59056 2000-03-24
                               2017-05-22
                                                   6268
##
   8
```

```
## 9
           59074 2000-01-31
                               2017-03-17
                                                  6255
## 10
           59081 2011-04-21
                               2017-05-19
                                                  2220
## # ... with 5,615 more rows
# Joining back to the applications data.
applications <- applications %>%
  left_join(examiner_dates, by = "examiner_id")
rm(examiner_dates)
gc()
             used (Mb) gc trigger
                                     (Mb) max used
                                                       (Mb)
## Ncells 5169252 276.1
                          14332328 765.5 14332328 765.5
## Vcells 66126675 504.6 134612175 1027.1 134358658 1025.1
```

# **Application Processing Time**

```
# Since an application can only be issued or abandoned, one or the other will always be NA, therefore I applications$appl_end_date <- paste(applications$patent_issue_date, applications$abandon_date, sep=',')

# Then I will clean up the column by removing instances of commas and NA's applications$appl_end_date <- gsub('NA', "", as.character(applications$appl_end_date))

applications$appl_end_date <- gsub(',', "", as.character(applications$appl_end_date))

# Ensure date format is consistent for both columns applications$appl_end_date <- as.Date(applications$appl_end_date, format="%Y-%m-%d")

applications$filing_date <- as.Date(applications$filing_date, format="%Y-%m-%d")

# Finding the difference in days between the application end date and the filing date applications$appl_proc_days <- as.numeric(difftime(applications$appl_end_date, applications$filing_date

# Remove instances where the filing date happens after the issue or abandon dates (these must be mistak applications <- applications %>% filter(appl_proc_days >=0 | appl_proc_days != NA)
```

### Additional Data Cleaning Prior to Modelling

```
# Find the count of missing values in each column
sapply(applications, function(x) sum(is.na(x)))
```

```
##
     application_number
                                 filing_date
                                                examiner_name_last
##
##
   examiner_name_first examiner_name_middle
                                                       examiner_id
##
                                       390396
                                                              3746
##
      examiner_art_unit
                                  uspc_class
                                                     uspc_subclass
##
                                                               1555
                      0
##
          patent_number
                           patent_issue_date
                                                      abandon_date
##
                 601857
                                                           1087295
                                       601383
##
          disposal_type
                                                  appl_status_date
                           appl_status_code
```

```
355
                                                               356
##
                      0
##
                                                             race
                     tc
                                      gender
##
                      0
                                      253871
                                                                0
                                 latest_date
##
                                                      tenure_days
          earliest_date
##
                  18240
                                       18240
                                                            18240
##
          appl_end_date
                              appl_proc_days
##
# Remove unnecessary columns for modelling
applications_mod <- subset(applications, select = -c(filing_date, abandon_date, earliest_date, appl_end
sapply(applications_mod, function(x) sum(is.na(x)))
##
    application number
                        examiner_name_last examiner_name_first
                                                                        examiner id
##
                                                                               3746
##
                                                                      disposal_type
     examiner_art_unit
                                uspc_class
                                                 uspc_subclass
##
                                         4
                                                          1555
##
      appl_status_code
                                        tc
                                                        gender
                                                                               race
##
                                         0
                                                        253871
                                                                                  0
                   355
##
           tenure_days
                            appl_proc_days
##
                 18240
applications_mod <- applications_mod %>% drop_na(examiner_id)
Use mice to impute missing values
applications_mod$gender <- as.factor(applications_mod$gender)</pre>
applications_mod_imp <- complete(mice(applications_mod, m=3, maxit=3))
##
##
   iter imp variable
##
     1
         1 appl_status_code gender tenure_days
##
     1
         2 appl_status_code gender tenure_days
##
         3 appl_status_code gender tenure_days
     1
##
     2
       1 appl_status_code gender tenure_days
        2 appl_status_code gender tenure_days
##
     2
##
    2
        3 appl_status_code gender tenure_days
##
     3
        1 appl_status_code gender tenure_days
##
    3
         2 appl_status_code gender tenure_days
##
         3 appl_status_code gender tenure_days
## Warning: Number of logged events: 7
rm(applications_mod)
```

# **Generating Network Information**

```
# first get work group for each examiner and limit to our two wgs of interest
examiner_aus = distinct(subset(applications_mod_imp, select=c(examiner_art_unit, examiner_id)))
# we eventually want to make a network with nodes colored by work group, so lets add that indicator
examiner_aus$wg = substr(examiner_aus$examiner_art_unit, 1,3)
# restrict down to our selected art units to reduce merging complexity later on
examiner aus = examiner aus[examiner aus$wg==162 | examiner aus$wg==219,]
# now we will merge in the aus df on applications
adv_network = merge(x=edges, y=examiner_aus, by.x="ego_examiner_id", by.y="examiner_id", all.x=TRUE)
adv_network = adv_network %>% rename(ego_art_unit=examiner_art_unit, ego_wg=wg)
adv_network = drop_na(adv_network)
# now repeat for the alter examiners
adv_network = merge(x=adv_network, y=examiner_aus, by.x="alter_examiner_id", by.y="examiner_id", all.x=
adv_network = adv_network %>% rename(alter_art_unit=examiner_art_unit, alter_wg=wg)
adv_network = drop_na(adv_network)
# we are left with 870 edges corresponding to instances of examiners in wg173 or wg175 asking for advic
egoNodes = subset(adv_network, select=c(ego_examiner_id,ego_art_unit, ego_wg)) %>% rename(examiner_id=e,
alterNodes = subset(adv_network, select=c(alter_examiner_id,alter_art_unit, alter_wg))%>% rename(examiner_id,alter_art_unit, alter_wg))%>%
nodes = rbind(egoNodes, alterNodes)
nodes = distinct(nodes)
# problem: when we reduce to the list of distinct nodes, we actually have more than we should, since so
nodes = nodes %>% group by(examiner id) %% summarise(examiner id=first(examiner id), art unit=first(ar
network <- graph_from_data_frame(d=adv_network, vertices=nodes, directed=TRUE)</pre>
network
## IGRAPH 761341c DN-- 98 916 --
## + attr: name (v/c), art_unit (v/n), wg (v/c), application_number (e/c),
## | advice_date (e/n), ego_art_unit (e/n), ego_wg (e/c), alter_art_unit
## | (e/n), alter_wg (e/c)
## + edges from 761341c (vertex names):
## [1] 59491->76935 59491->76935 59491->76935 59491->76935
## [6] 59491->76935 59491->76935 59491->76935 59491->76935 61889->88905
## [11] 61889->88905 62114->72495 62114->66534 62114->72495 62114->66534
## [16] 62253->67690 62253->67690 62253->67690 62253->67690 63657->73150
## [21] 63657->73150 63657->73150 63657->73150 63657->73150
## [26] 63822->61417 64904->96780 65111->65111 65111->65111 65111->65111
## + ... omitted several edges
# Calculate the node metrics
Degree <- degree(network)</pre>
Closeness <- closeness(network)</pre>
Betweenness <- betweenness(network)</pre>
Eig <- evcent(network)$vector</pre>
```

comp <- data.frame(nodes, Degree, Eig, Closeness, Betweenness)
comp</pre>

##		${\tt examiner\_id}$	art_unit	wg	Degree	Eig	Closeness	Betweenness
##	59491	59491	2196	219	48	2.644753e-02	1.00000000	0.90
##	59664	59664	2193	219	3	1.875528e-03	NaN	0.00
##	60302	60302	1626	162	6	0.000000e+00	NaN	0.00
##	60465	60465	2193	219	5	1.897166e-03	NaN	0.00
##	60768	60768	2191	219	2	8.131513e-05	NaN	0.00
##	61064	61064	2192	219	5	1.221863e-04	NaN	0.00
##	61417	61417	1626	162	2	0.000000e+00	NaN	0.00
##	61529	61529	1628	162		0.000000e+00	NaN	0.00
##	61889	61889	2193	219	24	9.429415e-03	1.00000000	4.00
##	61980	61980	2195		1	1.856425e-05	NaN	0.00
##	62114	62114	2195		4	3.187399e-05	0.50000000	0.00
##	62253	62253	1623		5	0.000000e+00	1.00000000	0.00
##	62661	62661	1627		13	0.000000e+00	NaN	0.00
	63657	63657	2196			2.804044e-03		0.00
	63822	63822	1624			0.000000e+00	1.00000000	0.00
	63971	63971	2192			5.780753e-05	NaN	0.00
	64904	64904	2192			1.592129e-05		0.00
	65111	65111	1623			0.000000e+00	1.00000000	0.00
	65353	65353	2193			2.027090e-04	NaN	0.00
	65536	65536	1625			0.000000e+00		0.00
	65537	65537	1624			0.000000e+00		0.00
	65554	65554	2194			3.320903e-02	NaN	0.00
	65713	65713	1623			0.00000e+00		0.00
	65737	65737	1621			0.00000e+00		0.00
	66030	66030	2193			3.703110e-04		0.00
	66359	66359	2194			1.844651e-05	NaN	0.00
	66534	66534	2194			1.919068e-03	NaN	0.00
	67078	67078	2196			5.682276e-03	NaN	0.00
	67208	67208	1624			9.962709e-01		0.00
	67226	67226	2197			1.000000e+00		3.10
	67256	67256	1627			0.000000e+00		0.00
	67581	67581	1621			0.000000e+00		0.00
	67690	67690	1623			0.000000e+00	NaN	0.00
	67731	67731	1621			0.000000e+00		0.00
	67753	67753	1623			0.000000e+00	NaN	0.00
	68166	68166	1625			0.000000e+00		0.00
	68339	68339	1626			0.000000e+00		0.00
	68695	68695	1627			0.000000e+00		1.00
	68752 69896	68752	2192 1628			3.924478e-03 0.000000e+00	NaN NaN	0.00 0.00
	70026	69896	2192			3.481434e-03		0.00
	70206	70026 70206	1627			0.000000e+00	NaN	0.00
	70767	70767	1624			0.000000e+00	NaN	0.00
	71175	71175	2193			1.896603e-03		2.25
	71175	71175	2193			8.131513e-05	NaN	0.00
	71996	71996	2191			1.618863e-03	NaN NaN	0.00
	72089	71996	2192			2.236048e-03		0.00
	72495	72009	2193			5.292522e-07	NaN	0.00
	72941	72941	1626			0.000000e+00	NaN	0.00
ii m	. 2011	120-11	1020	102		3.0000000.00	IVAIV	0.00

##	73150	73150	2192	219	44	1.	.151042e-03	NaN	0.00
##	73364	73364	1629	162	1	0	.000000e+00	NaN	0.00
##	73777	73777	1623	162	7	0	.000000e+00	1.00000000	0.00
##	75034	75034	1626	162	3	0.	.000000e+00	1.00000000	1.00
##	75431	75431	2195	219	6	3.	.751055e-03	NaN	0.00
##	75940	75940	2191	219	52	8.	.568931e-03	NaN	0.00
##	76141	76141	2191	219	30	7.	.733290e-03	0.50000000	4.00
##	76935	76935	2199	219	24	5.	.200072e-02	NaN	0.00
##	77348	77348	1626	162	1	0	.000000e+00	1.00000000	0.00
##	81211	81211	1628	162	3	0.	.000000e+00	NaN	0.00
##	81865	81865	1621	162	6	0.	.000000e+00	1.00000000	0.00
##	81959	81959	1629	162	3	0.	.000000e+00	NaN	0.00
##	82386	82386	2191	219	8	0.	.000000e+00	NaN	0.00
##	83552	83552	2194	219	8	1.	.338727e-03	0.25000000	0.00
##	84460	84460	2193	219	15	8.	.461901e-04	0.16666667	12.00
##	85216	85216	1627	162	5	0.	.000000e+00	NaN	0.00
##	87028	87028	2191	219	186	4.	.897170e-03	0.09090909	16.00
##	87486	87486	1621	162	5	0.	.000000e+00	0.14285714	0.00
##	87994	87994	2191	219	5	1.	.020354e-05	1.00000000	0.00
##	88077	88077	2191		80	2	.649855e-03	NaN	0.00
	88508	88508	1621				.000000e+00	NaN	0.00
	88905	88905	2199				.565709e-04	NaN	0.00
	89882	89882	1623				.000000e+00		0.00
	91747	91747	1627				.000000e+00	1.00000000	0.00
	91956	91956	1627				.000000e+00	NaN	0.00
	92902	92902	1621				.000000e+00	NaN	0.00
	93403	93403	1626				.000000e+00		0.00
	93677	93677	1623				.000000e+00	NaN	0.00
	94070	94070	1623				.000000e+00		0.00
	94513	94513	2193				.927300e-03	NaN	0.00
	94925	94925	1626				.000000e+00	NaN	0.00
	95339	95339	2193				.814301e-02	NaN	0.00
	95446	95446	1625				.000000e+00	NaN	0.00
	95769	95769	2193				.882553e-03		0.75
	95997	95997	2192				.000000e+00	NaN NaN	0.00
##	96206	96206	2194				.067542e-05	NaN NaN	0.00
	96780	96780	2192				.917706e-03	NaN N-N	0.00
	96898	96898	1628				.000000e+00	NaN	0.00
	97328	97328	2199				.530191e-02		0.00
	97520	97520	1624				.000000e+00 .956133e-05		0.00
	97590	97590	2193					NaN NaN	0.00
	97673	97673	2193				.751055e-03 .502279e-02	NaN NaN	0.00
	98228	98228	2195					NaN	0.00
	98700	98700	1625				.000000e+00		0.00
	98717	98717 99047	2192				.914968e-04 .000000e+00		0.00
	99047		1627				.000000e+00 .453124e-04	NaN	0.00
	99346	99346 99424	2192				.453124e-04 .000000e+00		0.00
	99424		1625					NaN NaN	0.00
##	99514	99514	2192	219	8	9	.570456e-05	NaN	0.00

Now, we will merge the centrality measurements back into our imputed dataset

```
applications_final <- merge(x=applications_mod_imp, y=comp, by='examiner_id', all.x=TRUE)

# Filter to only include selected work groups
applications_final = applications_final %>% filter(wg==162 | wg==219)

# Remove NaN values for instances where examiner didnt ask for any advice
applications_final <- drop_na(applications_final)</pre>
```

# Modelling

First we will do a simple model with no interaction variables.

```
lm1 <- lm(appl_proc_days~Eig + Degree + Closeness + Betweenness + gender + tenure_days, data=application
summary(lm1)</pre>
```

```
##
## Call:
## lm(formula = appl_proc_days ~ Eig + Degree + Closeness + Betweenness +
      gender + tenure days, data = applications final)
##
## Residuals:
##
      Min
               1Q Median
                               ЗQ
                                      Max
## -1964.6 -409.7
                    -82.6
                            304.0 4233.2
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.603e+03 6.311e+01 25.401 < 2e-16 ***
              -2.302e+02 3.026e+01 -7.606 2.90e-14 ***
## Eig
## Degree
               2.941e+00 1.334e-01 22.042 < 2e-16 ***
              -1.359e+02 1.144e+01 -11.878 < 2e-16 ***
## Closeness
## Betweenness 2.651e+01 1.767e+00 15.007
                                            < 2e-16 ***
## gendermale
              4.114e+00 7.472e+00
                                     0.551
                                               0.582
## tenure_days -6.778e-02 9.973e-03 -6.796 1.09e-11 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 572.5 on 28881 degrees of freedom
## Multiple R-squared: 0.05473,
                                   Adjusted R-squared: 0.05454
## F-statistic: 278.7 on 6 and 28881 DF, p-value: < 2.2e-16
```

Some notes/insights/hypothesis based on these results: - Stat significant model and most variables are significant, except for any influence by gender

- Baseline processing time is 1604 days (Female, 0 days of tenure, never sought advice)
- Increasing an examiners eigenvector importance from 0 to 1 would be expected to decrease processing time by 236 days (i.e, the more important). This would make sense, if a particular examiner had a lot of influence over an advice network, with many other examiners seeking them for advice, they would likely be a subject matter expert and would need to take less time seeking out information online or from other individuals to get the answers they needed to process the application

- An examiner seeking advice one additional time from another examiner (an increase in degree by
  1) results in an increase in processing time of about 3 days. This could make sense, as seeking out
  additional advice, or having those come seek advice from you, is time consuming and could take time
  away from processing the applications
- An increase in closeness centrality from 0 to 1 would be expected to correspond to a 138 day decrease in processing time. This could also make sense, as a high closeness centrality would correspond to an examiner being well connected within the network. Even if they don't know someone who is an SME on a topic, they likely know someone who knows someone. This may make the process of finding the information they are looking for easier, and speed up the time taken to process the application
- A 1 unit increase in betweenness centrality corresponds to a 27 day increase in processing time. Similar to degree centrality, if an examiner is a main gate for information to pass in the network, this could be time consuming and take time away from them processing applications themselves.
- Finally, an increase in tenure by 1 day corresponds to a slight decrease in processing time. This seems intuitive that more experience would result in quicker processing times.

### Adding Interaction Variables

```
lm2 <- lm(appl_proc_days~Eig + Degree + Closeness + Betweenness + gender + tenure_days + Degree*gender
summary(lm2)</pre>
```

```
##
## Call:
## lm(formula = appl_proc_days ~ Eig + Degree + Closeness + Betweenness +
##
       gender + tenure_days + Degree * gender + Eig * gender + Closeness *
##
       gender + Betweenness * gender, data = applications final)
##
## Residuals:
##
       Min
                1Q
                   Median
                                3Q
                                       Max
  -1639.7 -405.3
                    -84.1
                             299.9
                                    4236.0
##
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          1398.46470
                                       66.48970
                                                 21.033 < 2e-16 ***
## Eig
                          -456.03124
                                       66.39166
                                                 -6.869 6.61e-12 ***
## Degree
                             4.47189
                                        0.53982
                                                   8.284
                                                          < 2e-16 ***
## Closeness
                                                   0.322
                             9.41931
                                       29.22512
                                                            0.747
## Betweenness
                           105.37691
                                        6.86764
                                                 15.344
                                                          < 2e-16 ***
## gendermale
                           174.52531
                                       30.97343
                                                   5.635 1.77e-08 ***
## tenure_days
                            -0.06056
                                        0.01002
                                                 -6.043 1.53e-09 ***
## Degree:gendermale
                            -3.53856
                                        0.58185
                                                 -6.082 1.20e-09 ***
## Eig:gendermale
                          6863.53189
                                      638.03872
                                                  10.757 < 2e-16 ***
## Closeness:gendermale
                          -144.21974
                                       31.85002
                                                 -4.528 5.98e-06 ***
## Betweenness:gendermale -78.60021
                                        7.12814 -11.027 < 2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 569.4 on 28877 degrees of freedom
## Multiple R-squared: 0.06525,
                                    Adjusted R-squared: 0.06493
## F-statistic: 201.6 on 10 and 28877 DF, p-value: < 2.2e-16
```

Some notes/insights/hypothesis based on these results: - Stat significant model and all variables are significant with at least 90% confidence

- Relationships for variables from previous model are similar, except closeness now has a more positive relationship with processing time (a unit increase in closeness centrality correlates with a 48 day increase in processing time)
- Tenure still has a reducing effect on processing time
- Unit increase in degree for male examiners reduces processing time by 4.5 days
- Unit increase in eig importance for male examiners increases processing time by 7270 days
- $\bullet\,$  Unit increase in closeness for males decreases processing time by 191 days
- Unit increase in betweenness for males decreases processing time by 78 days

It should be noted that it is difficult to infer how a change by one or many examiners would impact the processing times since each of the centrality scores are interrelated.