Machine Learning Engineer Nanodegree

Report

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Definition

Project Overview

The continued integration of automation into everyday life will require further refined computer vision. Computer vision is the process in which computers are trained to interpret and understand the visual world [1]. Some of the industries that use computer vision are: Manufacturing, Health Care, Insurance and Retail [1, 2]. One of the applications of computer vision within retail is the recognition of food, which is used in cashier-less stores like Amazon GO [2]. By being able to accurate identify fruit from images taken from video cameras, a store can know two main things: 1. When a customer has "purchased" it and 2. When the shelf is running low on a fruit.

Problem Statement

The main objective of this project is to use machine learning to be able to identify fruits within images, thus this is a computer vision problem. The input is an RGB picture of a piece of fruit and the output is the prediction vector of what type of fruit it is. The problem is to train an algorithm that when given an image of a fruit, can accurately identify what type of fruit it is. The solution to this problem will be a Convolutional Neural Network (CNN) model built in python using Keras on the Tensorflow backend. This model will accept a 100 pixel by 100 pixel RGB image as input and output the name of the predicted fruit.

Evaluation Metrics

The first evaluation metric for this project will be the Accuracy Score of the testing set, after training and validation have been done. This accuracy score is produced by Keras itself with metric specified as *accuracy* during the compile step of the model creation. When specifying *accuracy* as the metric, Kera itself will decide between *binary accuracy*, *sparse categorical accuracy*, or *categorical accuracy* [3]. For this model, Keras would decide to use categorical accuracy because the size of the final layer is not 1 (for binary accuracy), and then the loss function would not be used as to determine if the data is sparse enough. An analysis of the sparseness of the data will be completed in the Data Exploration section.

The second evaluation metric will be the Accuracy Score of internet sourced images. This will be done because the images used for testing and training have a white background and I want to see how well the model does with images with backgrounds.

Analysis

Data Exploration

The chosen data set is the Fruit-360 dataset from Kaggle.com (https://www.kaggle.com/moltean/fruits) [4]. This data set has approximately 70000 100 pixel by 100 pixel RGB images of fruit that are already split into a training and testing set. I will split the training set into a training set and a validation set to allow the model to take advantage of validation during training.

Both the training and testing have subfolders with the name of each fruit as the name of the subfolder. Within the dataset different pieces of fruit are given different numbers (Apple Golden 1 vs Apple Golden 2); for this project I will strip out the numbers so all Apple Golden will be trained, validated and tested the same.







Figure 2: Example of Apple Golden 2



Figure 3: Example of Apple Granny
Smith

Originally, without the above trimming, there are 103 targets; after the trimming there are 87 targets. The highest count of any one target in either the training set or target set is 5% of the total images. I do not believe this upsets the distribution of the images.

As mentioned above, the sparseness of the dataset must be determined so the proper loss function can be used. To do this, the average intensity of all the pixels in each image were determined (1 is full intensity - white, 0 is no intensity - black). Ideally the average intensity would be in the 0.4-0.6 with a low standard deviation as that would mean that on average the pixels were some variation between white and black. The results of the training, validation, and testing set can be seen below in Table 1.

Table 1: Pixel Intensity by Dataset

| Data Set Average | | Standard Deviation |
|------------------|--------|--------------------|
| Training | 0.5845 | 0.0717 |
| Validation | 0.5834 | 0.0724 |
| Testing | 0.5947 | 0.0715 |

Also, the max intensity for a class was found to be for Strawberry Wedges with an average intensity of 0.6164 and a standard deviation of 0.0533. The minimum intensity for a class was found to be for Mangostan with an average intensity of 0.4992 and a standard deviation of 0.0402.

Visual Exploration

In the Figure 4 below, the distribution of the number of images in each fruit category has been plotted for the full training set (before split into training and validation set). A large majority (~85%) of the classifications of fruit have been 300 and 550 images in the training dataset, whereas there is only one classification (Tomato) that has more than 2000 images. I do not believe this will cause an overfit of the model, because this does not even represent 5% of the total number of images within the training set.

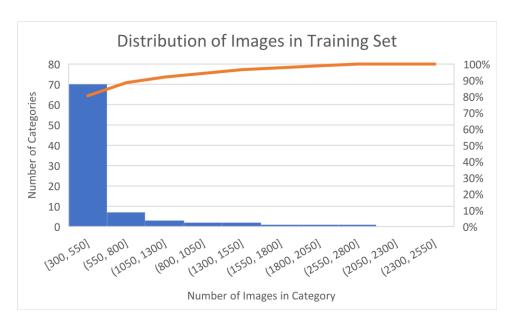


Figure 4: Plot of Distribution of Number of Images in the Training Set

The same also holds true for the testing set. A large majority of the images have a similar range of images with only a few being outside that range. This can be seen in Figure 5.

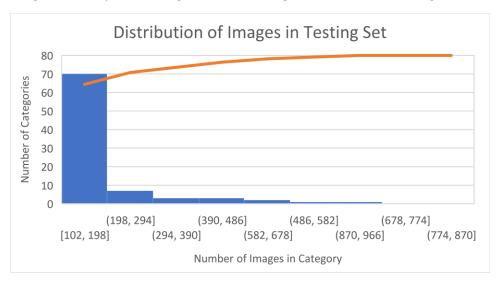


Figure 5: Plot of Distribution of Number of Images in the Testing Set

Doing a cursory glance over the dataset there does not appear to be any images that are mislabeled, blurry or otherwise corrupted that would cause issues with training.

Algorithms and Techniques

The main algorithm that will be used is the Convolutional Neural Network (CNN). This type of neural network is ideally suited for image classification because it combines the neural network architecture with the feature finding power of convolution [5]. Convolution across the images with various filters also different features to be determined by each filter. A CNN typically consists of pairs of convolutional layers and pooling layers followed by at least one densely connected layer [5]. The input into the first

convolutional layer would be the dimensions of the image and the output from the last densely connected layer would be a one-dimensional array with the same length as the number of classifiers [5]. This output would contain one entry per node with the probability that the node corresponds to the image that was classified.

Convolutional Layer

A convolutional layer works by using a filter (for images a 2D array of initially randomized values) to try to detect features of an image. As the filter convolves around the image, each element of the filter is multiplied against its corresponding element in the image. This brings up the issue of padding; as when trying to convolve around an edge or at a vertex, the filter is going to be technically out of bound of the image. This can be resolved in many ways, but for the purposes of this project I have chosen to deal with it by filling those out-of-bound elements with zeroes.

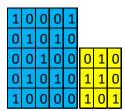


Figure 6: Example Image (left) and Filter

For example, given the image (in array form) and the filter in Figure 6, doing the first convolution calculation (top left corner), with zero padding, and a stride of one, would look like below (filter application in green):

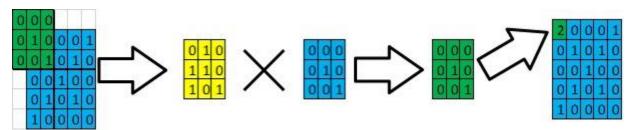


Figure 7: Example of Convolutional Step

Applying the entire filter over the image would result in the below figure:

| 2 | 1 | 2 | 0 | 2 |
|---|---|---|---|---|
| 1 | 2 | 1 | 2 | 2 |
| 1 | 1 | 3 | 2 | 1 |
| 0 | 2 | 2 | 1 | 1 |
| 1 | 2 | 0 | 1 | 0 |

Figure 8: Example of fully convoluted array

Pooling

Pooling is the process in which an aggregation function is used to reduce the dimensionality of the data. This helps in feature identification because as the aggregation occur, the important parts of the arrays will become more prominent. In this project max pooling has being chosen as the pooling layer of

choice. In this type of pooling, the output of the previous is divided into sections (as determined by the size and stride of the pooling layer). Then the max value of that section is found and used to produce a new smaller array. Using Figure 8 as a starting point, using valid padding (no padding), with a size of 2 and a stride of 2, a max pooling layer would divide the array as follows:

| 2 | 1 | 2 | 0 | 2 |
|---|---|---|---|---|
| 1 | 2 | 1 | 2 | 2 |
| 1 | 1 | 3 | 2 | 1 |
| 0 | 2 | 2 | 1 | 1 |
| 1 | 2 | 0 | 1 | 0 |

Figure 9: Sectioned Array for Max-Pooling

The yellow elements in Figure 9 are not included in the pooling calculations because no padding is being used in this case. Thus, the output of this max pooling layer would be:

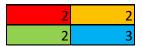


Figure 10: Output of example max pooling layer

As we can see, the dimensionality of the array has been reduced by at least the size of the pooling layer filter.

Dropout

The use of dropout is a relatively new concept in terms of densely connected layers. A densely connected layer is a layer in which every node of that layer is connected to every node of the previous layer. While this is a very good thing for CNNs because it combines features together that would not be combined otherwise, it can lead to overfitting of the model [6]. An example of a densely connected layer can be seen in Figure 11.

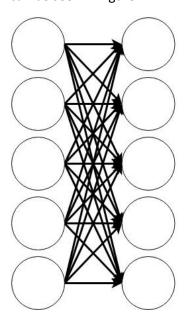


Figure 11: Example of two fully connected dense layers

The process of dropout means that only a certain percentage of nodes will be connected to the node from the previous layer. So, for example, a dropout of 0.4 (40% of nodes are not connected) could look like the below figure:

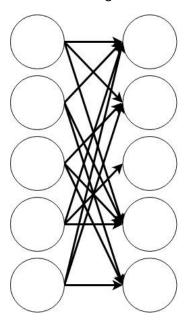


Figure 12: Two dense layers with 40% dropout

When using dropout, the nodes that connected to each other change with every propagation. Also, as dropout is applied randomly, some nodes might still be fully connected still, while others are completely disconnected from all other nodes.

Benchmark

The benchmark model for this project will be the best performing configuration that was used by Mureşan and Oltean in their creation of the dataset that I am using. Their best performing network had a training accuracy of 99.62% and a test accuracy of 95.88% with the following configuration¹:

Table 2: Simplified Configuration of Best Performing CNN for Mureşan and Oltean [4, p. 21]

| Layer | Filter Size | Number of Nodes/Filters |
|-----------------------|-------------|-------------------------|
| Convolutional/Pooling | 5x5 | 16 |
| Convolutional/Pooling | 5x5 | 32 |
| Convolutional/Pooling | 5x5 | 64 |
| Convolutional/Pooling | 5x5 | 128 |
| Fully Connected | | 1024 |
| Fully Connected | | 256 |

They used the *adam* optimizer and *categorical crossentropy* for the loss. Thus, this model is the model that I will base my initial model on and iterate on. Since I will not be able to replicate their model 100%

¹ For the full network configuration please see [3, pp. 35-39]

accurately, I will use the internet sourced fruit accuracy as a benchmark solely on my iteration to determine if the model is getting better or not.

Methodology

Data Preprocessing

In order to use an image in a machine learning application, the image must be converted into a form that a machine can understand, into a zero or one, or in this case and array of arrays of zeroes and ones. For this problem, each of the images are 100px by 100px RGB images. Thus, they are first loaded in as a 100 by 100 by 3 matrix, with each layer representing one colour and each cell of the layer representing the saturation of it's layer's color in that cell. For example, Figure 13 below is a 5 pixel by 5 pixel RGB image and must be converted into a 5 by 5 by 3 matrix.



Figure 13: Example 5 pixel by 5 pixel RGB image

Each layer of the 5 by 5 by 3 matrix can be seen below in Figures Figure 14 through Figure 16.

| 120 | 186 | 241 | 205 | 226 |
|-----|-----|-----|-----|-----|
| 167 | 197 | 234 | 243 | 249 |
| 204 | 247 | 232 | 123 | 118 |
| 153 | 253 | 204 | 143 | 67 |
| 151 | 221 | 58 | 214 | 235 |

| Figure | 14: R | ed layer | of F | Figure | 13 |
|---------------|-------|----------|------|--------|----|
|---------------|-------|----------|------|--------|----|

| 226 | 238 | 251 | 179 | 202 |
|-----|-----|-----|-----|-----|
| 212 | 235 | 247 | 233 | 246 |
| 217 | 253 | 249 | 74 | 164 |
| 80 | 243 | 210 | 228 | 149 |
| 87 | 177 | 227 | 255 | 244 |

Figure 15: Green layer of Figure 13

| 252 | 225 | 243 | 204 | 224 |
|-----|-----|-----|-----|-----|
| 192 | 194 | 193 | 231 | 253 |
| 208 | 227 | 213 | 95 | 153 |
| 172 | 244 | 196 | 205 | 207 |
| 201 | 90 | 24 | 154 | 249 |

Figure 16: Blue layer of Figure 13

Therefore, we can see that each pixel in the example image can be represented by a red, green, and blue saturation number. So, for example, the top left pixel in the example image has a RGB value of (120, 226, 225), which logically follows considering that the actual color of the pixel is a teal colour which itself is primarily a mix of green and blue.

After every image has been decomposed into its three-color layers, it is best to normalize the values in each layer to make the fitting of the model quicker and more efficient. In the RGB image format, the maximum saturation of any layer (color) is 255 and the minimum is 0, so it would make sense to divide every cell by 255 to normalize the value between 0 and 1 instead of 0 and 255.

The final step in the preprocessing is to expand the dimensions of the array from three dimensions to four dimensions, where the fourth dimension is the sample size. This is a requirement of the Keras 2D convolutional layers that are used in the model [7].

Implementation

After preprocessing the data, the implementation of the actual CNN involves:

1. Define the model architecture and parameters

- 2. Define the loss function and the testing metric
- 3. Fit the model and keep track of the loss and if it has improved save that model as the best model
- 4. Iterate through step 3 for a set number of epochs or until an appropriate loss value has been produced.

Refinement

Model Refinement

The first step of the refinement was to determine if any layers should be added or removed from the model. The layers that I looked at were the 2D Convolutional, 2D MaxPooling, dense, and dropout layers. The convolutional and maxPooling layers are the hallmarks layers of CNNs, so I knew that changing the number of pairs of those would be crucial to improving the performance. Adding in dense layers and dropout layers after the convolutional layers might assist in the classification. Thus, I decided to test both the number of convolutional/maxPooling pairs, the number of dense/dropout pairs after the flatten operation and the sizes of each layer. For this process I first created all the model and then tested them one by one.

It should be noted that there are some restrictions on the size and number of the maxpooling layers. As each maxpooling layer used will decrease the size of the length and width of the tenors, only a certain size and number of them can be used before a 1 by 1 tensor is produced. For example, use the four-layer benchmark model with a maxpooling pool size of four for each layer, the size of the layers would go from 100 by 100 to 25 by 25 (1st pooling) to 6 by 6 (2nd pooling) to 1 by 1 (3rd pooling) at which point the model size cannot be pooled anymore. For this reason, the maxpooling size wasn't increased past three for any number of maxpooling layers and was left at two for the five max pooling layer models.

I tested the following combinations for a grand total of 396 models²:

- Kernel size of Conv2D layers (3,5,7)
- Pool size of MaxPooling2D layers (2,3) [except where noted above]
- Number of Conv2D and MaxPooling2D layers (3,4,5)
- Size of 1st dense layer (1024, 2048)
- Size of 2nd dense layer (256, 512)

The models were created in modelRefinmentCreator.py and were tested in modelRefinmentTester.py

After testing the combinations above using five training epochs (total process took approximately 30 hours), there were three models that shared the highest internet image accuracy score of 19%. Out of those models, the one that has the highest test accuracy (98.69%) is the one I am going to use for the next stage of refinement. That model has the following architecture:

² I only tests kernel and layer sizes in ascending order away from the benchmark, so I never created a model that had a kernel size of 5 on the first layer and 3 on the second, or 7 on the third and 5 on the second. Otherwise there would have been close to 100,000 models to test

```
1. model = Sequential()
2. model.add(Conv2D(filters=16, kernel_size=3, padding='same', activation='relu',in-put_shape=(100, 100, 3)))
3. model.add(MaxPooling2D(pool_size=3))
4. model.add(Conv2D(filters=32, kernel_size=3, padding='same', activation='relu'))
5. model.add(MaxPooling2D(pool_size=2))
6. model.add(Conv2D(filters=64, kernel_size=3, padding='same', activation='relu'))
7. model.add(MaxPooling2D(pool_size=2))
8. model.add(Flatten())
9. model.add(Dense(2048, activation='relu'))
10. model.add(Dense(812, activation='relu'))
11. model.add(Dense(812, activation='relu'))
12. model.add(Dense(87, activation='softmax'))
```

Figure 17: Best Model after Model Refinement

The full result set can be found in Appendix 1: Model Refinement Results.

Variable Refinement

After determining a better model, the next step in refinement is determining the best parameters to be used in the model. In order to do this, I will implement a grid search-like operation on various parameters to determine the best option for those parameters. The following parameters can be modified:

- Conv2D (per layer)
 - Number of filters
 - Strides
 - Kernel Size
 - Padding
 - Activation
 - Use bias
 - Kernel initializer
 - Bias initializer
 - Kernel regularizer
 - Bias regularizer
 - Activity regularizer
 - Kernel Constraint
 - Bias Constraint
- MaxPooling2D (per layer)
 - Pool_size
 - Strides
 - Padding
- Dropout (per layer)
 - Rate
 - Noise shape
 - Seed (for random seed)
- Dense (per layer)

- Units
- Activation
- Use bias
- Kernel initializer
- Bias initializer
- Kernel regularizer
- Bias regularizer
- Activity regularizer
- Kernel Constraint
- Bias Constraint

Compile

- Optimizer (along with the hyperparameters for each unique optimizer)
- Loss
- Metrics
- Loss weights
- Sample weight mode
- Weighted Metrics

Just as with the model refinement, due to the sheer number of parameters that can be tuned a much smaller set must be used. The parameters I chose are the dropout rates for the two dropout layers along with the optimizer. I chose the dropouts due to research that showed that changing the dropout rate can have a significant impact on the performance [6]. I chose to include the optimizer because it is one of the only single parameters that can be changed that will affect the entire way the model fits. Also, because the model takes about three and a half minutes to fit and test (on my computer), I didn't want to choose too many parameters or values for those parameters to keep the total testing time to within a reasonable length of time. The values that I chose to test on can be seen below in Table 3.

Table 3: Parameters and Values to Grid Search

| Parameter | Values to Test |
|----------------|-----------------------------|
| First Dropout | 0.2, 0.3, 0.4, 0.5 |
| Second Dropout | 0.2, 0.3, 0.4, 0.5 |
| Optimizer | SGD, RMSprop, Adam, Adagard |

I chose the values of 0.2 to 0.5 for the dropouts based on the findings by Srivastava Et al. [6]³. I chose to use the four optimizers listed because I have experience in using them in other projects. The metrics I am using to determine the best parameters are the same as I used to test the benchmark model:

- 1. the accuracy of the prediction of the testing set
- 2. the accuracy of predicting internet sourced images

³ Srivastava Et al. indicate a dropout rate of 1 as meaning no dropout [7], whereas dropout is implemented in Keras where a rate of 0 means no dropout [6]

The code that I created to do this grid search is in *parameterTuning.py* where I go through the same initial stages of creating a CNN of loading in the tenors. I then created a pandas data frame with all combination of the above parameters (64 in total). I then iterate through each row of the data frame creating, compile, fitting, and testing a model with those parameters. I then record the test accuracy, the time taken to fit the model and the accuracy against the internet images. The full result set can be seen in Appendix 2: Variable Refinement Results.

Results

The top ten results from the grid search in decreasing accuracy against the internet sourced images can be seen in Table 4.

Table 4: Top Ten Results from Grid Search (descending internet accuracy)

| | | | | Train | Test | Learning | Internet |
|-------|----------|----------|-----------|----------|----------|----------|----------|
| index | dropout1 | dropout2 | optimizer | Accuracy | Accuracy | Time | Accuracy |
| 4 | 0.2 | 0.2 | Adam | 0.99146 | 98.58224 | 03:12.3 | 19.04762 |
| 27 | 0.3 | 0.4 | RMSprop | 0.991527 | 97.99384 | 04:11.9 | 19.04762 |
| 3 | 0.2 | 0.2 | RMSprop | 0.993518 | 97.51751 | 04:13.1 | 19.04762 |
| 23 | 0.3 | 0.3 | RMSprop | 0.991571 | 98.16195 | 04:12.4 | 14.28571 |
| 5 | 0.2 | 0.3 | Adagrad | 0.97531 | 96.42477 | 03:52.8 | 14.28571 |
| 40 | 0.4 | 0.3 | Adam | 0.989027 | 98.54861 | 03:12.1 | 11.90476 |
| 39 | 0.4 | 0.3 | RMSprop | 0.991305 | 98.39731 | 04:12.5 | 11.90476 |
| 51 | 0.5 | 0.2 | RMSprop | 0.990619 | 98.14514 | 04:11.5 | 11.90476 |
| 48 | 0.4 | 0.5 | Adam | 0.989823 | 97.90417 | 03:13.1 | 11.90476 |
| 19 | 0.3 | 0.2 | RMSprop | 0.992168 | 97.52872 | 04:11.2 | 11.90476 |

The best model after variable refinement is still the best model from the model refinement. It seems that overall *adam* and *RMSprop* and low levels of dropout are the best for the internet accuracy score.

Results

Model Evaluation and Validation

The final model is a three-layer 2Dconvolutional with maxpooling layers followed by two layers of dropout and densely connected layers. The model was compiled with the adam optimizer and loss function of categorial crossentropy. The training accuracy of the final model was 99.146%, with a test accuracy of 98.58%, training time of 3 minutes and 12 seconds, and an accuracy against the internet sourced images of 19%. The final architecture of the model can be seen below in Figure 18.

```
1. model = Sequential()
2. model.add(Conv2D(filters=16, kernel_size=3, padding='same', activation='relu',in-put_shape=(100, 100, 3)))
3. model.add(MaxPooling2D(pool_size=3))
4. model.add(Conv2D(filters=32, kernel_size=3, padding='same', activation='relu'))
5. model.add(MaxPooling2D(pool_size=2))
6. model.add(Conv2D(filters=64, kernel_size=3, padding='same', activation='relu'))
7. model.add(MaxPooling2D(pool_size=2))
8. model.add(Flatten())
9. model.add(Dense(2048, activation='relu'))
10. model.add(Dense(812, activation='relu'))
11. model.add(Dense(812, activation='relu'))
12. model.add(Dropout(0.2))
13. model.add(Dense(87, activation='softmax'))
14. model.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])
```

Figure 18: Final Model Architecture

I used the internet sourced images of fruit to measure the robustness of the model. However, what I found was that due to the limitations of the initial data set, the model did tend to overfit to the type of image that it was trained on; 100px by 100px with a white background. In Table 5, I have selected a few rows from the full table of the prediction of all the internet sourced images to highlight some interesting cases.

Table 5: Excerpt from Final Model Internet Sourced Image Prediction

| | | | | Target |
|--|------------|--------------|------------|------------|
| | | | Prediction | Prediction |
| path | target | prediction | Percent | Percent |
| | | Apple Pink | | |
| fruits/internet_resized\Apple_Red_1.jpg | Apple Red | Lady | 0.654492 | 8.57E-12 |
| fruits/internet_resized\Apple_Red_3.jpg | Apple Red | Cherry | 0.603045 | 0.328073 |
| fruits/internet_resized\Avocado_1.jpg | Avocado | Avocado ripe | 0.760063 | 7.67E-08 |
| fruits/internet_resized\Banana_3.jpg | Banana | Banana | 0.503727 | 0.503727 |
| fruits/internet_resized\Cantaloupe_1.jpeg | Cantaloupe | Cantaloupe | 0.997193 | 0.997193 |
| fruits/internet_resized\Cantaloupe_2.jpg | Cantaloupe | Cantaloupe | 0.977307 | 0.977307 |
| fruits/internet_resized\Cantaloupe_3.jpg | Cantaloupe | Cantaloupe | 0.949618 | 0.949618 |
| fruits/internet_resized\Cherry_3.jpg | Cherry | Pear Red | 0.99999 | 7.71E-17 |
| fruits/internet_resized\Pear_Red_1.jpg | Pear Red | Pear Red | 0.949801 | 0.949801 |
| | Pepper | Pepper | | |
| fruits/internet_resized\Pepper_Green_1.jpg | Green | Green | 1 | 1 |
| | Pepper | Banana Lady | | |
| fruits/internet_resized\Pepper_Green_2.jpg | Green | Finger | 0.998981 | 0.000441 |
| fruits/internet_resized\Tomato_1.jpg | Tomato | Tomato | 0.923479 | 0.923479 |
| fruits/internet_resized\Tomato_2.jpg | Tomato | Pear Red | 1 | 9.99E-25 |

For example, all the Cantaloupe images were classified correctly, but none of the Apple images were. It is also interesting to note that in the data set there was a distinction between Avocado ripe and Avocado, but as I did not know the ripeness of the avocados in the images, I found I classified them generically. Overall, I think that fruits with distinct shapes, colours or surfaces were more easily and accurate classifiable (Cantaloupe and Banana for example), then fruits that have a common size, colour or shape (Apple, Red Pear, Cherry and Tomato). The full version of the Table 5 can be found in Appendix 3: Internet Sourced Images Predictions.

Justification

The model itself I believe is good, but I think after going through the training/validation/testing process, the images are all too alike to provide any meaningful real-world data for a model. Another shortcoming in the data is that all information about size is lost when all the images were made to be 100px by 100px. I believe this is why such things as real-world Apples, Cherries, and Pears were misclassified as each other because when all scaled down to 100px by 100px almost all information about the size of the fruit is lost.

However, when compared to the benchmark model, the model that I refined did perform better similarly against the training set (99.15 vs 99.62%) and better for the testing set (98.58% vs 95.88%). I believe these accuracy differences stem from the fact that my model used one less layer so it didn't overfitting as much versus the images as it might with three layers.

Conclusion

Free-Form Visualization



Figure 19: Apple Red (left); identified as Apple Pink Lady



Figure 20: Cantaloupe (left) identified as Cantaloupe

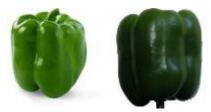


Figure 21: Pepper Green (left) identified as Pepper Green



Figure 22: Pepper Green (left) Identified as Banana Lady Finger



Figure 23: Tomato (left) identified as Pear Red



Figure 24: Cherry (left) identified as Pear Red

In the above images it can be seen that in some cases the features were very similar to each other and understandably why the model may have gotten the classification wrong (Figure 19). However, there were other cases in which the difference does not make logical sense as in Figure 22 where the model classifies a Green Pepper as a type of banana when it have also identified a Green Pepper Correctly.

Reflection

The process using for this project can be broken down in the following way:

- A problem was identified and a dataset that was applicable to that project was found and downloaded
- 2. The data was preprocessed into a format that Keras can utilize
- 3. A benchmark model was referenced and recreated from other literature
- 4. The exact layout of the model and the parameters were iterated to determine the best combinations
- 5. Internet sourced images of fruit were used to determine how effect the final model was

The most difficult step in the process was step number 4 for a few reasons. First, determining what parameters and changes to the model should be tested proved to be difficult because it is impossible to fully understand the impact of a change to this type of model. Second, the actual testing of these parameters, while not technically difficult (once GPU memory issues were resolved), were time consuming, with each test of the model taking approximately 5 minutes. The third reason why step four was so difficult was because of the random nature of GPU training. Even though a seed number can be set for keras, there are still things that a GPU may do to add randomness to a model.

Improvement

The biggest improvement that I could see for this model would be additional data items that include real world images of fruits in real world resolutions. I believe that the biggest downside of the dataset that I used was that each image of the same type of fruit was normally just the fruit rotated a few degrees and that all fruit almost completely filled the image, so that the size difference between a cherry and a red pear could not be appreciated by the model. This might also mean that features that are present on most pieces of a typical piece of fruit may have been missing from the fruit in this dataset.

Further, this provokes a question of what makes a good, well-rounded representative data set, and if a specific issue is trying to be solved, how specific does the dataset need to be. For example, in this problem of fruit identification in stores, would the model require images of fruit only in how they are laid out in a store, or would generic images like the one in the dataset I use still provide some use.

Final Thoughts

Overall, I did have a lot of fun with the problem as it really made me think critically about how a dataset can or should be used to solve a particular problem. I also enjoyed the challenge of trying to determine the best parameters and model features to try and tune to improve the performance of the model. I do believe that I have reached the limits of the dataset I used to solve this problem, and that in order to get an accuracy against real world fruits greater than 20%, a bespoke data set would have to be created.

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Appendix 1: Model Refinement Results

| Test Train Test | | Test | Learning | Internet |
|-----------------|-------------|-------------|----------|-------------|
| Number | Accuracy | Accuracy | Time | Accuracy |
| 1 | 0.98714602 | 96.74978986 | 04:58.2 | 11.9047619 |
| 2 | 0.986393809 | 94.41300084 | 05:13.7 | 4.761904762 |
| 3 | 0.987123907 | 94.43541608 | 05:26.8 | 11.9047619 |
| 4 | 0.983517706 | 95.80274587 | 05:31.2 | 4.761904762 |
| 5 | 0.985951304 | 95.63463155 | 05:35.2 | 2.380952381 |
| 6 | 0.988805294 | 97.06920706 | 09:21.0 | 2.380952381 |
| 7 | 0.991238952 | 97.0916223 | 04:08.4 | 19.04761905 |
| 8 | 0.991415918 | 96.31269263 | 03:55.4 | 7.142857143 |
| 9 | 0.992765486 | 96.04931353 | 03:54.1 | 4.761904762 |
| 10 | 0.988761067 | 96.67133651 | 03:13.0 | 11.9047619 |
| 11 | 0.987035394 | 95.33202578 | 03:26.3 | 2.380952381 |
| 12 | 0.98993361 | 95.02942001 | 03:51.7 | 9.523809524 |
| 13 | 0.986836255 | 95.78033062 | 04:06.4 | 4.761904762 |
| 14 | 0.982101798 | 95.58980106 | 04:02.6 | 7.142857143 |
| 15 | 0.988561928 | 98.16195013 | 02:59.4 | 9.523809524 |
| 16 | 0.990929186 | 97.84253292 | 02:46.4 | 2.380952381 |
| 17 | 0.990995586 | 97.59596526 | 02:40.4 | 9.523809524 |
| 18 | 0.990597367 | 97.56234239 | 02:38.1 | 16.66666667 |
| 19 | 0.987831831 | 96.27906977 | 02:42.3 | 4.761904762 |
| 20 | 0.985840678 | 95.80834968 | 02:59.2 | 7.142857143 |
| 21 | 0.984955728 | 95.13589241 | 03:21.3 | 2.380952381 |
| 22 | 0.983716786 | 95.2927991 | 03:33.6 | 4.761904762 |
| 23 | 0.983871698 | 97.27654805 | 03:32.5 | 7.142857143 |
| 24 | 0.988296449 | 97.84813673 | 02:33.5 | 7.142857143 |
| 25 | 0.990420341 | 98.45895209 | 02:21.3 | 9.523809524 |
| 26 | 0.990376115 | 97.89296722 | 02:16.8 | 9.523809524 |
| 27 | 0.989977896 | 98.54300925 | 02:16.2 | 4.761904762 |
| 28 | 0.985088468 | 97.70243766 | 02:34.8 | 7.142857143 |
| 29 | 0.982035398 | 95.8755954 | 02:51.7 | 4.761904762 |
| 30 | 0.981438041 | 96.00448305 | 03:14.6 | 9.523809524 |
| 31 | 0.979955733 | 96.25105071 | 03:25.5 | 7.142857143 |
| 32 | 0.98252213 | 98.20678061 | 03:25.2 | 9.523809524 |
| 33 | 0.986482322 | 97.05799944 | 02:24.3 | 9.523809524 |
| 34 | 0.990398228 | 97.78649482 | 02:12.8 | 4.761904762 |
| 35 | 0.987721264 | 97.06360325 | 02:07.8 | 11.9047619 |
| 36 | 0.987411499 | 99.07537125 | 02:09.3 | 11.9047619 |
| 37 | 0.985088468 | 97.0355842 | 02:33.8 | 9.523809524 |
| 38 | 0.982964575 | 97.60156907 | 02:51.8 | 7.142857143 |

| 39 | 0.981415927 | 94.83889045 | 03:13.9 | 7.142857143 |
|----|-------------|-------------|---------|-------------|
| 40 | 0.985641599 | 96.44158027 | 03:25.4 | 11.9047619 |
| 41 | 0.980265498 | 96.18380499 | 03:24.8 | 4.761904762 |
| 42 | 0.98904866 | 96.8786775 | 02:23.2 | 4.761904762 |
| 43 | 0.98707962 | 98.4141216 | 02:12.1 | 7.142857143 |
| 44 | 0.988230109 | 97.21490614 | 02:08.2 | 11.9047619 |
| 45 | 0.985752225 | 99.46203418 | 02:09.5 | 9.523809524 |
| 46 | 0.989977896 | 96.85065845 | 04:35.9 | 7.142857143 |
| 47 | 0.988340735 | 94.9733819 | 04:52.4 | 7.142857143 |
| 48 | 0.988318563 | 95.35444102 | 05:08.8 | 9.523809524 |
| 49 | 0.987699091 | 95.10226954 | 05:12.2 | 2.380952381 |
| 50 | 0.98612833 | 93.83020454 | 05:11.6 | 11.9047619 |
| 51 | 0.987854004 | 97.27094424 | 04:28.8 | 11.9047619 |
| 52 | 0.991128325 | 97.31017092 | 04:02.1 | 4.761904762 |
| 53 | 0.988606215 | 97.13084898 | 03:48.7 | 11.9047619 |
| 54 | 0.993230104 | 96.74978986 | 03:49.0 | 2.380952381 |
| 55 | 0.988252223 | 96.57046792 | 03:10.7 | 7.142857143 |
| 56 | 0.984646022 | 94.73241804 | 03:30.3 | 9.523809524 |
| 57 | 0.985951304 | 96.38554217 | 03:51.1 | 2.380952381 |
| 58 | 0.98422569 | 95.97086018 | 04:05.2 | 7.142857143 |
| 59 | 0.985752225 | 95.77472681 | 04:04.7 | 4.761904762 |
| 60 | 0.989469051 | 98.69991594 | 02:59.9 | 7.142857143 |
| 61 | 0.990973473 | 95.61221631 | 02:51.1 | 4.761904762 |
| 62 | 0.989535391 | 97.59036145 | 02:41.9 | 2.380952381 |
| 63 | 0.991592944 | 98.66068927 | 02:40.9 | 7.142857143 |
| 64 | 0.988318563 | 97.11964136 | 02:45.2 | 9.523809524 |
| 65 | 0.985154867 | 96.32390025 | 03:01.2 | 2.380952381 |
| 66 | 0.983561933 | 95.75231157 | 03:25.0 | 7.142857143 |
| 67 | 0.982013285 | 96.63210983 | 03:37.5 | 9.523809524 |
| 68 | 0.983185828 | 95.69066966 | 03:36.4 | 11.9047619 |
| 69 | 0.989380538 | 96.09414402 | 02:36.7 | 2.380952381 |
| 70 | 0.989181399 | 98.1507425 | 02:22.3 | 4.761904762 |
| 71 | 0.990575194 | 97.92098627 | 02:18.1 | 4.761904762 |
| 72 | 0.990973473 | 98.8344074 | 02:18.1 | 7.142857143 |
| 73 | 0.987256646 | 96.23984309 | 02:37.0 | 7.142857143 |
| 74 | 0.982367277 | 96.83384702 | 02:55.8 | 4.761904762 |
| 75 | 0.980000019 | 95.06304287 | 03:15.7 | 4.761904762 |
| 76 | 0.983008862 | 97.18128327 | 03:28.1 | 4.761904762 |
| 77 | 0.97986728 | 96.07733259 | 03:26.9 | 11.9047619 |
| 78 | 0.986371696 | 97.5679462 | 02:25.6 | 9.523809524 |
| 79 | 0.986946881 | 97.9377977 | 02:14.7 | 2.380952381 |
| | | - | - | |

| 80 | 0.990132749 | 97.988232 | 02:10.9 | 9.523809524 |
|-----|-------------|-------------|---------|-------------|
| 81 | 0.98707962 | 98.04987391 | 02:11.4 | 2.380952381 |
| 82 | 0.98530972 | 98.38049874 | 02:37.3 | 14.28571429 |
| 83 | 0.982212365 | 97.17567946 | 02:55.4 | 7.142857143 |
| 84 | 0.98081857 | 93.26982348 | 03:15.2 | 2.380952381 |
| 85 | 0.980398238 | 94.09358364 | 03:28.7 | 4.761904762 |
| 86 | 0.980995595 | 94.3401513 | 03:26.5 | 7.142857143 |
| 87 | 0.988340735 | 97.18688708 | 02:25.6 | 9.523809524 |
| 88 | 0.990508854 | 98.91846456 | 02:14.5 | 4.761904762 |
| 89 | 0.985398233 | 99.08097506 | 02:10.1 | 2.380952381 |
| 90 | 0.989358425 | 97.8313253 | 02:12.0 | 7.142857143 |
| 91 | 0.99075222 | 96.95152704 | 05:57.6 | 4.761904762 |
| 92 | 0.988119483 | 94.56430373 | 06:09.9 | 2.380952381 |
| 93 | 0.989601791 | 96.04931353 | 06:20.0 | 4.761904762 |
| 94 | 0.988119483 | 96.0325021 | 06:24.5 | 4.761904762 |
| 95 | 0.986681402 | 96.7722051 | 06:24.0 | 9.523809524 |
| 96 | 0.988827407 | 96.68254413 | 05:59.9 | 11.9047619 |
| 97 | 0.990464628 | 98.65508546 | 05:20.3 | 2.380952381 |
| 98 | 0.990663707 | 97.04118801 | 05:03.8 | 7.142857143 |
| 99 | 0.99163717 | 97.01877277 | 05:01.6 | 7.142857143 |
| 100 | 0.984668136 | 97.34379378 | 03:47.7 | 2.380952381 |
| 101 | 0.989181399 | 97.82011768 | 04:03.8 | 0 |
| 102 | 0.983738959 | 97.76407957 | 04:23.6 | 7.142857143 |
| 103 | 0.983783185 | 94.56990754 | 04:35.8 | 7.142857143 |
| 104 | 0.98721236 | 93.98150743 | 04:36.6 | 7.142857143 |
| 105 | 0.991128325 | 97.95460913 | 03:37.4 | 4.761904762 |
| 106 | 0.989535391 | 96.68814794 | 03:39.5 | 4.761904762 |
| 107 | 0.991482317 | 98.22359204 | 03:20.0 | 4.761904762 |
| 108 | 0.992101789 | 97.4614738 | 03:17.6 | 9.523809524 |
| 109 | 0.990796447 | 94.05435696 | 03:01.7 | 2.380952381 |
| 110 | 0.987455726 | 97.47268142 | 03:17.1 | 7.142857143 |
| 111 | 0.983871698 | 94.62594564 | 03:41.0 | 4.761904762 |
| 112 | 0.986017704 | 96.20061642 | 03:49.9 | 4.761904762 |
| 113 | 0.983783185 | 94.68758756 | 03:51.2 | 4.761904762 |
| 114 | 0.98816371 | 98.97450266 | 02:50.8 | 16.66666667 |
| 115 | 0.990464628 | 97.48388904 | 02:41.8 | 11.9047619 |
| 116 | 0.991792023 | 96.97954609 | 02:35.5 | 4.761904762 |
| 117 | 0.990309715 | 97.62958812 | 02:37.5 | 7.142857143 |
| 118 | 0.986747801 | 95.78033062 | 02:45.3 | 2.380952381 |
| 119 | 0.984048665 | 97.31577473 | 03:03.1 | 4.761904762 |
| 120 | 0.98238939 | 95.51134772 | 03:23.5 | 9.523809524 |
| | | | | |

| 121 | 0.984734535 | 97.06360325 | 03:34.5 | 4.761904762 |
|-----|-------------|-------------|---------|-------------|
| 122 | 0.982411504 | 95.06864668 | 03:34.5 | 7.142857143 |
| 123 | 0.989889383 | 97.89296722 | 02:33.7 | 11.9047619 |
| 124 | 0.988296449 | 98.44214066 | 02:20.8 | 4.761904762 |
| 125 | 0.988340735 | 98.22359204 | 02:17.1 | 9.523809524 |
| 126 | 0.98980087 | 97.94900532 | 02:17.7 | 7.142857143 |
| 127 | 0.986858428 | 96.22303166 | 02:44.7 | 0 |
| 128 | 0.983805299 | 97.90417484 | 03:01.3 | 2.380952381 |
| 129 | 0.983207941 | 97.12524517 | 03:24.2 | 4.761904762 |
| 130 | 0.98075223 | 94.62034183 | 03:35.7 | 4.761904762 |
| 131 | 0.98252213 | 97.32137854 | 03:34.4 | 9.523809524 |
| 132 | 0.989513278 | 96.25105071 | 02:31.5 | 4.761904762 |
| 133 | 0.987854004 | 98.03306248 | 02:21.2 | 9.523809524 |
| 134 | 0.989424765 | 97.5119081 | 02:17.8 | 2.380952381 |
| 135 | 0.987787604 | 98.65508546 | 02:17.7 | 7.142857143 |
| 136 | 0.990154862 | 93.9702998 | 05:57.1 | 4.761904762 |
| 137 | 0.985619485 | 96.0325021 | 06:19.8 | 4.761904762 |
| 138 | 0.987035394 | 95.18072289 | 06:28.3 | 7.142857143 |
| 139 | 0.982854009 | 95.48893247 | 06:27.0 | 14.28571429 |
| 140 | 0.986061931 | 95.6626506 | 06:29.1 | 0 |
| 141 | 0.991061926 | 95.83076492 | 05:50.2 | 16.66666667 |
| 142 | 0.992322981 | 95.44410199 | 05:22.7 | 14.28571429 |
| 143 | 0.98884958 | 96.19501261 | 05:11.0 | 4.761904762 |
| 144 | 0.989889383 | 97.9377977 | 05:09.1 | 11.9047619 |
| 145 | 0.985354006 | 96.07733259 | 03:51.7 | 4.761904762 |
| 146 | 0.983893812 | 96.32390025 | 04:08.4 | 11.9047619 |
| 147 | 0.984646022 | 96.33510787 | 04:28.8 | 9.523809524 |
| 148 | 0.987477899 | 96.38554217 | 04:41.8 | 11.9047619 |
| 149 | 0.985752225 | 93.23620062 | 04:41.5 | 4.761904762 |
| 150 | 0.991194665 | 97.08601849 | 03:39.5 | 16.66666667 |
| 151 | 0.990199089 | 97.90417484 | 03:28.7 | 7.142857143 |
| 152 | 0.990420341 | 97.36620902 | 03:21.7 | 9.523809524 |
| 153 | 0.991061926 | 98.69431213 | 03:18.7 | 19.04761905 |
| 154 | 0.988296449 | 97.0355842 | 03:02.5 | 2.380952381 |
| 155 | 0.982986748 | 96.64331746 | 03:20.7 | 2.380952381 |
| 156 | 0.985840678 | 94.34575511 | 03:46.3 | 4.761904762 |
| 157 | 0.980022132 | 95.79714206 | 03:55.6 | 2.380952381 |
| 158 | 0.986637175 | 95.05743906 | 03:54.3 | 9.523809524 |
| 159 | 0.987256646 | 97.5679462 | 02:53.2 | 0 |
| 160 | 0.989557505 | 97.45026618 | 02:43.8 | 11.9047619 |
| 161 | 0.990221262 | 97.91538246 | 02:39.0 | 9.523809524 |
| | | | | |

| 162 | 0.990154862 | 97.05799944 | 02:37.9 | 9.523809524 |
|-----|-------------|-------------|---------|-------------|
| 163 | 0.984314144 | 95.45530961 | 02:47.5 | 2.380952381 |
| 164 | 0.983982325 | 95.46091342 | 03:04.4 | 4.761904762 |
| 165 | 0.985110641 | 96.6657327 | 03:27.1 | 4.761904762 |
| 166 | 0.983384967 | 95.19193051 | 03:38.4 | 7.142857143 |
| 167 | 0.983738959 | 96.99635752 | 03:38.4 | 7.142857143 |
| 168 | 0.988185823 | 98.05547772 | 02:37.7 | 9.523809524 |
| 169 | 0.988407075 | 97.54553096 | 02:26.5 | 14.28571429 |
| 170 | 0.988053083 | 97.36620902 | 02:20.2 | 2.380952381 |
| 171 | 0.988805294 | 99.08657887 | 02:21.2 | 4.761904762 |
| 172 | 0.984668136 | 96.5592603 | 02:47.5 | 4.761904762 |
| 173 | 0.982035398 | 98.16195013 | 03:05.3 | 2.380952381 |
| 174 | 0.981150448 | 96.66012889 | 03:27.6 | 2.380952381 |
| 175 | 0.982234538 | 95.6626506 | 03:39.8 | 0 |
| 176 | 0.985663712 | 94.39618941 | 03:38.6 | 9.523809524 |
| 177 | 0.987278759 | 97.89296722 | 02:36.5 | 4.761904762 |
| 178 | 0.987411499 | 98.59344354 | 02:24.9 | 14.28571429 |
| 179 | 0.989889383 | 98.71672737 | 02:21.4 | 7.142857143 |
| 180 | 0.987831831 | 98.25721491 | 02:23.7 | 4.761904762 |
| 181 | 0.983584046 | 95.41047913 | 05:09.4 | 2.380952381 |
| 182 | 0.981924772 | 93.44354161 | 05:28.2 | 4.761904762 |
| 183 | 0.984048665 | 91.9585318 | 05:39.4 | 2.380952381 |
| 184 | 0.978473425 | 88.12552536 | 06:17.0 | 4.761904762 |
| 185 | 0.981371701 | 95.3992715 | 07:12.1 | 7.142857143 |
| 186 | 0.984469056 | 94.79966377 | 04:57.8 | 7.142857143 |
| 187 | 0.991902649 | 98.94648361 | 04:30.6 | 9.523809524 |
| 188 | 0.988053083 | 95.81395349 | 04:05.4 | 16.66666667 |
| 189 | 0.989469051 | 96.0829364 | 03:28.4 | 9.523809524 |
| 190 | 0.982035398 | 95.70748109 | 05:10.7 | 7.142857143 |
| 191 | 0.982854009 | 90.1036705 | 05:29.4 | 0 |
| 192 | 0.982322991 | 90.49593724 | 05:42.8 | 2.380952381 |
| 193 | 0.972765505 | 91.73998319 | 06:19.0 | 0 |
| 194 | 0.979579628 | 91.6391146 | 07:13.2 | 7.142857143 |
| 195 | 0.98258847 | 96.83384702 | 04:57.7 | 9.523809524 |
| 196 | 0.985398233 | 97.8313253 | 04:34.7 | 4.761904762 |
| 197 | 0.986725688 | 97.99943962 | 04:06.3 | 7.142857143 |
| 198 | 0.987898231 | 96.47520314 | 03:30.2 | 4.761904762 |
| 199 | 0.986017704 | 95.91482208 | 05:30.2 | 4.761904762 |
| 200 | 0.979601741 | 93.63967498 | 05:49.9 | 0 |
| 201 | 0.978517711 | 90.44550294 | 05:59.1 | 0 |
| 202 | 0.978694677 | 93.37629588 | 06:38.9 | 0 |
| | | | | |

| 203 | 0.981747806 | 90.0532362 | 07:33.3 | 2.380952381 |
|-----|-------------|-------------|---------|-------------|
| 204 | 0.985619485 | 96.78901653 | 05:21.4 | 11.9047619 |
| 205 | 0.985929191 | 96.88428131 | 04:52.8 | 7.142857143 |
| 206 | 0.988694668 | 94.96217428 | 04:22.7 | 4.761904762 |
| 207 | 0.989380538 | 96.01569067 | 03:49.5 | 7.142857143 |
| 208 | 0.984646022 | 97.43345475 | 05:35.3 | 7.142857143 |
| 209 | 0.980707943 | 91.57186887 | 05:54.1 | 2.380952381 |
| 210 | 0.980066359 | 91.71196414 | 06:03.2 | 2.380952381 |
| 211 | 0.981747806 | 93.11852059 | 06:44.9 | 11.9047619 |
| 212 | 0.980884969 | 92.15466517 | 07:38.9 | 0 |
| 213 | 0.985707939 | 96.15578593 | 05:25.0 | 4.761904762 |
| 214 | 0.983650446 | 96.9291118 | 04:55.8 | 4.761904762 |
| 215 | 0.98442477 | 95.88119922 | 04:27.6 | 2.380952381 |
| 216 | 0.985110641 | 97.50630429 | 03:50.5 | 9.523809524 |
| 217 | 0.985420346 | 94.24488652 | 04:28.9 | 0 |
| 218 | 0.984889388 | 93.7013169 | 04:47.4 | 0 |
| 219 | 0.98442477 | 95.30961054 | 04:58.2 | 7.142857143 |
| 220 | 0.986703515 | 95.14149622 | 05:42.1 | 4.761904762 |
| 221 | 0.985575199 | 92.00336229 | 05:41.7 | 2.380952381 |
| 222 | 0.987477899 | 94.6539647 | 04:18.9 | 9.523809524 |
| 223 | 0.988561928 | 97.70243766 | 03:56.9 | 11.9047619 |
| 224 | 0.988495588 | 95.68506584 | 03:27.3 | 14.28571429 |
| 225 | 0.98986727 | 97.53992715 | 03:25.5 | 7.142857143 |
| 226 | 0.985995591 | 96.54244887 | 03:15.9 | 9.523809524 |
| 227 | 0.986349583 | 95.12468479 | 03:35.2 | 7.142857143 |
| 228 | 0.984446883 | 94.37937798 | 03:55.9 | 7.142857143 |
| 229 | 0.985000014 | 93.10731297 | 04:20.9 | 11.9047619 |
| 230 | 0.982079625 | 94.99579714 | 04:19.9 | 11.9047619 |
| 231 | 0.987035394 | 96.89548893 | 03:06.5 | 7.142857143 |
| 232 | 0.988827407 | 97.43905856 | 02:55.0 | 7.142857143 |
| 233 | 0.988340735 | 98.12832726 | 02:34.1 | 9.523809524 |
| 234 | 0.988296449 | 97.76407957 | 02:33.1 | 7.142857143 |
| 235 | 0.983915925 | 95.39366769 | 02:50.6 | 2.380952381 |
| 236 | 0.982256651 | 96.66012889 | 03:08.2 | 7.142857143 |
| 237 | 0.97973454 | 95.48893247 | 03:32.0 | 0 |
| 238 | 0.983362854 | 94.83328663 | 03:56.8 | 9.523809524 |
| 239 | 0.983296454 | 96.42476884 | 03:55.2 | 2.380952381 |
| 240 | 0.988694668 | 96.19501261 | 02:41.5 | 4.761904762 |
| 241 | 0.986482322 | 96.23423928 | 02:29.1 | 7.142857143 |
| 242 | 0.986438036 | 97.99943962 | 02:19.0 | 4.761904762 |
| 243 | 0.986592948 | 97.96581676 | 02:17.8 | 14.28571429 |
| | | | | |

| 244 | 0.984933615 | 97.13084898 | 02:45.5 | 4.761904762 |
|-----|-------------|-------------|---------|-------------|
| 245 | 0.980530977 | 95.32642197 | 03:03.9 | 2.380952381 |
| 246 | 0.978606224 | 95.4497058 | 03:26.0 | 0 |
| 247 | 0.979845107 | 96.77780891 | 03:47.7 | 9.523809524 |
| 248 | 0.982854009 | 95.53376296 | 03:47.7 | 2.380952381 |
| 249 | 0.983849585 | 97.78649482 | 02:35.9 | 9.523809524 |
| 250 | 0.984247804 | 96.16699356 | 02:23.5 | 14.28571429 |
| 251 | 0.984181404 | 97.27094424 | 02:14.5 | 7.142857143 |
| 252 | 0.985354006 | 97.64639955 | 02:30.3 | 9.523809524 |
| 253 | 0.980553091 | 95.92042589 | 03:12.0 | 4.761904762 |
| 254 | 0.979358435 | 95.10787335 | 03:24.4 | 4.761904762 |
| 255 | 0.981128335 | 92.19389185 | 03:44.9 | 0 |
| 256 | 0.980354011 | 96.39674979 | 03:59.2 | 11.9047619 |
| 257 | 0.982964575 | 96.47520314 | 03:57.9 | 4.761904762 |
| 258 | 0.986659288 | 97.69123004 | 02:54.7 | 4.761904762 |
| 259 | 0.986393809 | 96.34071168 | 02:41.7 | 14.28571429 |
| 260 | 0.983230114 | 96.88428131 | 02:31.1 | 7.142857143 |
| 261 | 0.984181404 | 98.21238442 | 02:34.5 | 9.523809524 |
| 262 | 0.984092891 | 96.45839171 | 05:00.2 | 9.523809524 |
| 263 | 0.986991167 | 93.89745027 | 05:35.2 | 2.380952381 |
| 264 | 0.984557509 | 95.37125245 | 05:21.0 | 0 |
| 265 | 0.98265487 | 94.26730177 | 06:00.1 | 4.761904762 |
| 266 | 0.982632756 | 94.25609414 | 05:59.8 | 11.9047619 |
| 267 | 0.987035394 | 96.70495937 | 04:34.8 | 4.761904762 |
| 268 | 0.989159286 | 96.42476884 | 04:08.7 | 4.761904762 |
| 269 | 0.990265489 | 98.67189689 | 03:40.3 | 9.523809524 |
| 270 | 0.990840733 | 97.7248529 | 03:41.2 | 9.523809524 |
| 271 | 0.985287607 | 93.93667694 | 03:22.5 | 14.28571429 |
| 272 | 0.984535396 | 93.10170916 | 03:45.1 | 2.380952381 |
| 273 | 0.982035398 | 94.25609414 | 04:10.6 | 4.761904762 |
| 274 | 0.985663712 | 93.89184646 | 04:32.6 | 11.9047619 |
| 275 | 0.98157078 | 93.4379378 | 04:26.8 | 0 |
| 276 | 0.985508859 | 97.74726814 | 03:08.9 | 7.142857143 |
| 277 | 0.988230109 | 98.58223592 | 02:56.9 | 4.761904762 |
| 278 | 0.987676978 | 98.520594 | 02:37.4 | 11.9047619 |
| 279 | 0.989092946 | 97.09722611 | 02:37.7 | 7.142857143 |
| 280 | 0.985752225 | 95.69627347 | 02:57.0 | 2.380952381 |
| 281 | 0.983584046 | 95.07425049 | 03:11.6 | 7.142857143 |
| 282 | 0.979601741 | 95.01821238 | 03:48.4 | 0 |
| 283 | 0.982765496 | 95.32081816 | 04:13.3 | 14.28571429 |
| 284 | 0.984004438 | 91.9585318 | 04:11.9 | 7.142857143 |
| | | | | |

| 285 | 0.985774338 | 97.66881479 | 02:56.2 | 9.523809524 |
|-----|-------------|-------------|---------|-------------|
| 286 | 0.990265489 | 99.27710843 | 02:42.1 | 2.380952381 |
| 287 | 0.988473475 | 97.71364528 | 02:32.3 | 4.761904762 |
| 288 | 0.985354006 | 96.21742785 | 02:24.3 | 7.142857143 |
| 289 | 0.981438041 | 96.41916503 | 02:51.9 | 7.142857143 |
| 290 | 0.979822993 | 96.13337069 | 03:12.7 | 4.761904762 |
| 291 | 0.979137182 | 96.78901653 | 03:40.2 | 9.523809524 |
| 292 | 0.977632761 | 96.40795741 | 04:06.6 | 0 |
| 293 | 0.976460159 | 93.99271505 | 04:05.1 | 0 |
| 294 | 0.984601796 | 95.15830765 | 02:50.6 | 9.523809524 |
| 295 | 0.98530972 | 97.84813673 | 02:52.1 | 4.761904762 |
| 296 | 0.983805299 | 98.53740544 | 02:34.6 | 4.761904762 |
| 297 | 0.985575199 | 97.6744186 | 02:42.6 | 7.142857143 |
| 298 | 0.982942462 | 94.90613617 | 02:56.7 | 2.380952381 |
| 299 | 0.981194675 | 94.98458952 | 03:14.4 | 2.380952381 |
| 300 | 0.97966814 | 96.37433455 | 03:47.3 | 9.523809524 |
| 301 | 0.978274345 | 94.27850939 | 04:02.7 | 7.142857143 |
| 302 | 0.97980088 | 95.56178201 | 03:55.1 | 2.380952381 |
| 303 | 0.986769915 | 97.37181283 | 02:38.5 | 2.380952381 |
| 304 | 0.984115064 | 96.5592603 | 02:24.9 | 11.9047619 |
| 305 | 0.986393809 | 98.33006444 | 02:15.1 | 7.142857143 |
| 306 | 0.986681402 | 97.49509667 | 02:16.2 | 0 |
| 307 | 0.985641599 | 95.82516111 | 05:09.5 | 7.142857143 |
| 308 | 0.984778762 | 94.19445223 | 05:25.2 | 0 |
| 309 | 0.985840678 | 96.79462034 | 05:39.6 | 4.761904762 |
| 310 | 0.981438041 | 93.37069207 | 06:18.5 | 4.761904762 |
| 311 | 0.984092891 | 95.04623144 | 06:17.1 | 9.523809524 |
| 312 | 0.986858428 | 96.51442981 | 04:58.2 | 14.28571429 |
| 313 | 0.988274336 | 97.248529 | 04:35.6 | 9.523809524 |
| 314 | 0.991194665 | 96.68254413 | 04:03.5 | 7.142857143 |
| 315 | 0.993871689 | 97.2989633 | 04:04.4 | 0 |
| 316 | 0.986570776 | 95.62342393 | 03:34.6 | 7.142857143 |
| 317 | 0.983185828 | 96.64331746 | 03:52.6 | 0 |
| 318 | 0.980088472 | 95.75231157 | 04:14.0 | 7.142857143 |
| 319 | 0.983606219 | 94.90053236 | 04:37.2 | 9.523809524 |
| 320 | 0.984822989 | 94.17203699 | 04:37.6 | 11.9047619 |
| 321 | 0.98701328 | 94.14962174 | 03:21.7 | 2.380952381 |
| 322 | 0.98891592 | 96.25665453 | 03:11.6 | 0 |
| 323 | 0.989026546 | 96.49201457 | 02:52.6 | 4.761904762 |
| 324 | 0.987809718 | 98.26281872 | 02:52.7 | 9.523809524 |
| 325 | 0.985929191 | 96.41356122 | 02:57.4 | 4.761904762 |
| - | | | | - |

| 326 | 0.985929191 | 93.34267302 | 03:14.0 | 7.142857143 |
|-----|-------------|-------------|---------|-------------|
| 327 | 0.982699096 | 94.04875315 | 03:37.7 | 2.380952381 |
| 328 | 0.981747806 | 95.36004483 | 04:01.6 | 9.523809524 |
| 329 | 0.980420351 | 91.8520594 | 04:01.3 | 0 |
| 330 | 0.986238956 | 96.94031942 | 02:46.7 | 11.9047619 |
| 331 | 0.988761067 | 98.24600728 | 02:34.6 | 9.523809524 |
| 332 | 0.986814141 | 97.04118801 | 02:25.8 | 11.9047619 |
| 333 | 0.990243375 | 96.78341272 | 02:24.6 | 0 |
| 334 | 0.983738959 | 98.10591202 | 02:48.9 | 11.9047619 |
| 335 | 0.981659293 | 96.35191931 | 03:05.8 | 4.761904762 |
| 336 | 0.975508869 | 94.64275707 | 03:30.2 | 4.761904762 |
| 337 | 0.977544248 | 95.52255534 | 03:51.6 | 7.142857143 |
| 338 | 0.983075202 | 97.29335948 | 03:51.3 | 7.142857143 |
| 339 | 0.982035398 | 92.51330905 | 02:39.3 | 14.28571429 |
| 340 | 0.986393809 | 98.13393107 | 02:27.7 | 11.9047619 |
| 341 | 0.983274341 | 96.0829364 | 02:17.0 | 7.142857143 |
| 342 | 0.982610643 | 96.43037265 | 02:17.0 | 7.142857143 |
| 343 | 0.982101798 | 96.16699356 | 02:52.2 | 0 |
| 344 | 0.980000019 | 95.03502382 | 03:07.7 | 4.761904762 |
| 345 | 0.98170352 | 97.80891006 | 03:31.3 | 4.761904762 |
| 346 | 0.978362858 | 94.09918745 | 03:52.8 | 2.380952381 |
| 347 | 0.978008866 | 94.91734379 | 03:52.6 | 0 |
| 348 | 0.986504436 | 96.58727935 | 02:39.2 | 7.142857143 |
| 349 | 0.986504436 | 95.9260297 | 02:29.9 | 4.761904762 |
| 350 | 0.985685825 | 96.16138975 | 02:18.1 | 9.523809524 |
| 351 | 0.984092891 | 97.5679462 | 02:17.4 | 2.380952381 |
| 352 | 0.986305296 | 96.23984309 | 05:16.2 | 11.9047619 |
| 353 | 0.988495588 | 93.23059681 | 05:31.4 | 2.380952381 |
| 354 | 0.987190247 | 95.03502382 | 05:45.6 | 4.761904762 |
| 355 | 0.984491169 | 92.32277949 | 06:20.0 | 0 |
| 356 | 0.98707962 | 94.80526758 | 06:21.9 | 9.523809524 |
| 357 | 0.987544239 | 96.6657327 | 05:01.7 | 2.380952381 |
| 358 | 0.987455726 | 97.29335948 | 04:38.0 | 11.9047619 |
| 359 | 0.991924763 | 96.44718409 | 04:05.6 | 7.142857143 |
| 360 | 0.990221262 | 97.04679182 | 04:09.7 | 2.380952381 |
| 361 | 0.987168133 | 93.3875035 | 03:38.8 | 2.380952381 |
| 362 | 0.984004438 | 96.4527879 | 03:58.2 | 16.66666667 |
| 363 | 0.982765496 | 93.30905015 | 04:18.7 | 7.142857143 |
| 364 | 0.981659293 | 92.70383861 | 04:42.0 | 2.380952381 |
| 365 | 0.980464578 | 95.60100869 | 04:42.4 | 4.761904762 |
| 366 | 0.989446878 | 98.00504343 | 03:30.4 | 4.761904762 |
| | | | | |

| 367 | 0.984756649 | 95.83076492 | 03:15.1 | 7.142857143 |
|-----|-------------|-------------|---------|-------------|
| 368 | 0.988495588 | 96.13337069 | 02:57.8 | 2.380952381 |
| 369 | 0.987300873 | 98.22359204 | 02:56.3 | 2.380952381 |
| 370 | 0.980707943 | 97.21490614 | 03:02.8 | 9.523809524 |
| 371 | 0.981283188 | 95.72989633 | 03:19.0 | 9.523809524 |
| 372 | 0.979513288 | 95.00700476 | 03:42.3 | 9.523809524 |
| 373 | 0.97524339 | 91.17399832 | 04:07.0 | 2.380952381 |
| 374 | 0.986615062 | 95.1302886 | 04:05.6 | 9.523809524 |
| 375 | 0.985840678 | 99.0473522 | 02:52.8 | 0 |
| 376 | 0.990265489 | 95.7130849 | 02:41.8 | 7.142857143 |
| 377 | 0.986703515 | 98.22359204 | 02:30.7 | 4.761904762 |
| 378 | 0.98809737 | 98.34127207 | 02:33.8 | 4.761904762 |
| 379 | 0.980884969 | 98.04987391 | 02:53.2 | 11.9047619 |
| 380 | 0.971769929 | 94.26730177 | 03:10.8 | 0 |
| 381 | 0.978318572 | 93.14093584 | 03:32.8 | 2.380952381 |
| 382 | 0.97157079 | 92.42364808 | 03:55.4 | 2.380952381 |
| 383 | 0.980553091 | 91.94732418 | 03:54.0 | 0 |
| 384 | 0.984203517 | 96.7217708 | 02:44.0 | 2.380952381 |
| 385 | 0.98272121 | 95.69066966 | 02:51.2 | 14.28571429 |
| 386 | 0.987787604 | 96.9851499 | 02:36.3 | 7.142857143 |
| 387 | 0.984491169 | 96.73858224 | 02:36.5 | 7.142857143 |
| 388 | 0.98170352 | 97.51751191 | 02:59.8 | 19.04761905 |
| 389 | 0.97688055 | 94.86130569 | 03:28.8 | 11.9047619 |
| 390 | 0.97789824 | 96.06612496 | 03:36.5 | 9.523809524 |
| 391 | 0.982809722 | 93.34267302 | 03:56.5 | 7.142857143 |
| 392 | 0.977699101 | 94.39618941 | 03:57.7 | 4.761904762 |
| 393 | 0.985044241 | 96.35191931 | 02:42.3 | 0 |
| 394 | 0.986216843 | 96.34071168 | 02:29.7 | 4.761904762 |
| 395 | 0.985619485 | 97.54553096 | 02:21.0 | 4.761904762 |
| 396 | 0.985553086 | 96.71056318 | 02:23.4 | 2.380952381 |
| | | | | |

Appendix 2: Variable Refinement Results

| Test | | Table Ne | | | | | |
|-------|---------|----------|----------|----------|----------|----------|----------|
| Numbe | dropout | dropout | optimize | Train | Test | Learning | Internet |
| r | 1 | 2 | r | Accuracy | Accuracy | Time | Accuracy |
| 1 | 0.2 | 0.2 | Adagrad | 0.979159 | 97.65761 | 03:54.2 | 9.52381 |
| 2 | 0.2 | 0.2 | SGD | 0.994137 | 96.03811 | 02:29.1 | 0 |
| 3 | 0.2 | 0.2 | RMSprop | 0.993518 | 97.51751 | 04:13.1 | 19.04762 |
| 4 | 0.2 | 0.2 | Adam | 0.99146 | 98.58224 | 03:12.3 | 19.04762 |
| 5 | 0.2 | 0.3 | Adagrad | 0.97531 | 96.42477 | 03:52.8 | 14.28571 |
| 6 | 0.2 | 0.3 | SGD | 0.99458 | 97.14766 | 02:27.4 | 0 |
| 7 | 0.2 | 0.3 | RMSprop | 0.994071 | 98.52059 | 04:11.1 | 2.380952 |
| 8 | 0.2 | 0.3 | Adam | 0.993341 | 98.27963 | 03:13.9 | 4.761905 |
| 9 | 0.2 | 0.4 | Adagrad | 0.975531 | 97.19809 | 03:50.6 | 9.52381 |
| 10 | 0.2 | 0.4 | SGD | 0.99292 | 97.18689 | 02:28.0 | 2.380952 |
| 11 | 0.2 | 0.4 | RMSprop | 0.993186 | 98.03867 | 04:11.7 | 9.52381 |
| 12 | 0.2 | 0.4 | Adam | 0.992589 | 97.94901 | 03:11.0 | 2.380952 |
| 13 | 0.2 | 0.5 | Adagrad | 0.953296 | 96.07733 | 03:50.2 | 4.761905 |
| 14 | 0.2 | 0.5 | SGD | 0.98792 | 96.85626 | 02:27.5 | 0 |
| 15 | 0.2 | 0.5 | RMSprop | 0.99135 | 96.7666 | 04:12.1 | 4.761905 |
| 16 | 0.2 | 0.5 | Adam | 0.990022 | 98.10591 | 03:12.1 | 0 |
| 17 | 0.3 | 0.2 | Adagrad | 0.975708 | 96.06052 | 03:51.5 | 7.142857 |
| 18 | 0.3 | 0.2 | SGD | 0.995465 | 97.33819 | 02:27.0 | 0 |
| 19 | 0.3 | 0.2 | RMSprop | 0.992168 | 97.52872 | 04:11.2 | 11.90476 |
| 20 | 0.3 | 0.2 | Adam | 0.989358 | 97.00196 | 03:12.1 | 7.142857 |
| 21 | 0.3 | 0.3 | Adagrad | 0.961394 | 95.5954 | 03:50.5 | 4.761905 |
| 22 | 0.3 | 0.3 | SGD | 0.992655 | 96.15579 | 02:27.4 | 0 |
| 23 | 0.3 | 0.3 | RMSprop | 0.991571 | 98.16195 | 04:12.4 | 14.28571 |
| 24 | 0.3 | 0.3 | Adam | 0.991018 | 97.47829 | 03:12.2 | 4.761905 |
| 25 | 0.3 | 0.4 | Adagrad | 0.969912 | 96.761 | 03:50.9 | 4.761905 |
| 26 | 0.3 | 0.4 | SGD | 0.989137 | 96.27347 | 02:27.4 | 4.761905 |
| 27 | 0.3 | 0.4 | RMSprop | 0.991527 | 97.99384 | 04:11.9 | 19.04762 |
| 28 | 0.3 | 0.4 | Adam | 0.989381 | 97.28215 | 03:12.5 | 7.142857 |
| 29 | 0.3 | 0.5 | Adagrad | 0.950708 | 96.25105 | 03:51.2 | 7.142857 |
| 30 | 0.3 | 0.5 | SGD | 0.987235 | 95.8756 | 02:27.5 | 4.761905 |
| 31 | 0.3 | 0.5 | RMSprop | 0.989889 | 98.92407 | 04:10.9 | 9.52381 |
| 32 | 0.3 | 0.5 | Adam | 0.989226 | 97.98823 | 03:13.0 | 9.52381 |
| 33 | 0.4 | 0.2 | Adagrad | 0.966571 | 95.83076 | 03:50.9 | 2.380952 |
| 34 | 0.4 | 0.2 | SGD | 0.991748 | 94.87812 | 02:28.4 | 2.380952 |
| 35 | 0.4 | 0.2 | RMSprop | 0.992323 | 98.37489 | 04:10.5 | 9.52381 |
| 36 | 0.4 | 0.2 | Adam | 0.989049 | 97.21491 | 03:11.9 | 4.761905 |
| 37 | 0.4 | 0.3 | Adagrad | 0.957013 | 96.06052 | 03:51.2 | 4.761905 |

| 38 39 40 41 42 | 0.4 0.4 0.4 0.4 0.4 0.4 | 0.3 0.3 0.3 0.4 | SGD RMSprop Adam Adagrad | 0.990907 0.991305 0.989027 0.950221 | 96.50883 98.39731 98.54861 | 02:28.1 04:12.5 03:12.1 | 0 11.90476 11.90476 |
|----------------------------|--|--------------------------|-----------------------------------|--|----------------------------------|-------------------------------|---------------------------|
| 40 41 42 | 0.4 0.4 0.4 | 0.3 0.4 | Adam | 0.989027 | | | |
| 41 42 | 0.4 | 0.4 | | | 98.54861 | 03:12.1 | 11 90/76 |
| 42 | 0.4 | | Adagrad | ი 950221 | | | 11.50470 |
| | | 0.4 | 1 | 0.550221 | 96.54245 | 03:50.6 | 7.142857 |
| | 0.4 | | SGD | 0.989027 | 97.24853 | 02:28.4 | 2.380952 |
| 43 | | 0.4 | RMSprop | 0.990022 | 98.58784 | 04:11.5 | 7.142857 |
| 44 | 0.4 | 0.4 | Adam | 0.989093 | 98.14514 | 03:13.0 | 4.761905 |
| 45 | 0.4 | 0.5 | Adagrad | 0.932633 | 96.25105 | 03:51.2 | 4.761905 |
| 46 | 0.4 | 0.5 | SGD | 0.987677 | 97.39423 | 02:27.7 | 4.761905 |
| 47 | 0.4 | 0.5 | RMSprop | 0.988805 | 98.32446 | 04:12.3 | 9.52381 |
| 48 | 0.4 | 0.5 | Adam | 0.989823 | 97.90417 | 03:13.1 | 11.90476 |
| 49 | 0.5 | 0.2 | Adagrad | 0.949823 | 94.5643 | 03:51.2 | 4.761905 |
| 50 | 0.5 | 0.2 | SGD | 0.990044 | 96.83385 | 02:27.5 | 7.142857 |
| 51 | 0.5 | 0.2 | RMSprop | 0.990619 | 98.14514 | 04:11.5 | 11.90476 |
| 52 | 0.5 | 0.2 | Adam | 0.989491 | 98.59344 | 03:11.5 | 9.52381 |
| 53 | 0.5 | 0.3 | Adagrad | 0.929513 | 95.06865 | 03:50.9 | 2.380952 |
| 54 | 0.5 | 0.3 | SGD | 0.989712 | 97.31577 | 02:27.4 | 2.380952 |
| 55 | 0.5 | 0.3 | RMSprop | 0.98885 | 97.60717 | 04:09.9 | 7.142857 |
| 56 | 0.5 | 0.3 | Adam | 0.988142 | 97.37742 | 03:12.7 | 11.90476 |
| 57 | 0.5 | 0.4 | Adagrad | 0.914403 | 92.63099 | 03:51.2 | 7.142857 |
| 58 | 0.5 | 0.4 | SGD | 0.98469 | 96.64892 | 02:27.1 | 0 |
| 59 | 0.5 | 0.4 | RMSprop | 0.988717 | 98.54861 | 04:10.4 | 7.142857 |
| 60 | 0.5 | 0.4 | Adam | 0.987876 | 97.94901 | 03:15.0 | 7.142857 |
| 61 | 0.5 | 0.5 | Adagrad | 0.907588 | 94.37938 | 03:51.5 | 7.142857 |
| 62 | 0.5 | 0.5 | SGD | 0.977633 | 96.464 | 02:27.3 | 0 |
| 63 | 0.5 | 0.5 | RMSprop | 0.988761 | 96.49762 | 04:11.5 | 7.142857 |
| 64 | 0.5 | 0.5 | Adam | 0.984889 | 97.96021 | 03:16.1 | 7.142857 |

Appendix 3: Internet Sourced Images Predictions

| math | towast | nuadiation | Prediction | Target Prediction Percent |
|---|--------------|-----------------------------|-------------|---------------------------|
| <pre>path fruits/internet_resized\Apple_Red_1.jpg</pre> | Apple Red | prediction Apple Pink Lady | 0.654491544 | 8.57E-12 |
| fruits/internet_resized\Apple_Red_2.jpg | Apple Red | Pear Red | 0.999998689 | 7.81E-17 |
| fruits/internet_resized\Apple_Red_3.jpg | Apple Red | Cherry | 0.603045106 | 0.328073 |
| fruits/internet_resized\Avocado_1.jpg | Avocado | Avocado ripe | 0.760063231 | 7.67E-08 |
| fruits/internet_resized\Avocado_1.jpg | Avocado | Avocado ripe | 0.601834297 | 6.93E-06 |
| fruits/internet_resized\Avocado_2.jpg | Avocado | Pepper Green | 0.996228456 | 8.34E-08 |
| | Banana | | 0.930228430 | 0.001867 |
| fruits/internet_resized\Banana_1.jpg | | Physalis with Husk | | |
| fruits/internet_resized\Banana_2.jpg | Banana | Pear Monster | 0.495245576 | 0.00409 |
| fruits/internet_resized\Banana_3.jpg | Banana | Banana | 0.503727078 | 0.503727 |
| fruits/internet_resized\Cantaloupe_1.jpeg | Cantaloupe | Cantaloupe | 0.997193277 | 0.997193 |
| fruits/internet_resized\Cantaloupe_2.jpg | Cantaloupe | Cantaloupe | 0.977306902 | 0.977307 |
| fruits/internet_resized\Cantaloupe_3.jpg | Cantaloupe | Cantaloupe | 0.94961828 | 0.949618 |
| fruits/internet_resized\Cherry_1.jpg | Cherry | Pear Red | 0.999910116 | 1.29E-09 |
| fruits/internet_resized\Cherry_2.jpg | Cherry | Pear Red | 0.999989748 | 9.63E-08 |
| fruits/internet_resized\Cherry_3.jpg | Cherry | Pear Red | 0.999990463 | 7.71E-17 |
| fruits/internet_resized\Grape_Pink_1.jpg | Grape Pink | Pepper Green | 0.999930739 | 1.70E-17 |
| fruits/internet_resized\Grape_Pink_2.jpg | Grape Pink | Strawberry Wedge | 0.999443471 | 4.23E-14 |
| fruits/internet_resized\Grape_Pink_3.jpg | Grape Pink | Cherry Rainier | 0.671511292 | 1.34E-10 |
| fruits/internet_resized\Grape_White_1.jpg | Grape White | Physalis with Husk | 0.999682069 | 6.91E-13 |
| fruits/internet_resized\Grape_White_2.jpg | Grape White | Physalis with Husk | 0.634479284 | 2.93E-10 |
| fruits/internet_resized\Grape_White_3.jpg | Grape White | Cantaloupe | 0.947030187 | 2.27E-08 |
| fruits/internet_resized\Lemon_1.jpg | Lemon | Carambula | 0.999988437 | 1.73E-14 |
| fruits/internet_resized\Lemon_2.jpg | Lemon | Quince | 0.705528498 | 2.36E-10 |
| fruits/internet_resized\Lemon_3.jpg | Lemon | Banana Lady Finger | 0.99985528 | 6.42E-10 |
| fruits/internet_resized\Orange_1.jpg | Orange | Carambula | 0.854445279 | 8.52E-15 |
| fruits/internet_resized\Orange_2.jpg | Orange | Lemon Meyer | 0.846696794 | 1.66E-14 |
| fruits/internet_resized\Orange_3.jpg | Orange | Pepper Green | 1 | 4.33E-25 |
| fruits/internet_resized\Pear_Red_1.jpg | Pear Red | Pear Red | 0.949800968 | 0.949801 |
| fruits/internet_resized\Pear_Red_2.jpg | Pear Red | Pepper Green | 1 | 6.76E-21 |
| fruits/internet_resized\Pear_Red_3.jpg | Pear Red | Granadilla | 0.999974847 | 2.31E-08 |
| fruits/internet_resized\Pepper_Green_1.jpg | Pepper Green | Pepper Green | 1 | 1 |
| fruits/internet_resized\Pepper_Green_2.jpg | Pepper Green | Banana Lady Finger | 0.998981297 | 0.000441 |
| fruits/internet_resized\Pepper_Green_3.jpg | Pepper Green | Pepper Green | 1 | 1 |
| fruits/internet_resized\Pineapple_1.jpg | Pineapple | Banana Lady Finger | 0.996977329 | 6.17E-09 |
| fruits/internet_resized\Pineapple_2.jpg | Pineapple | Banana Lady Finger | 0.539131999 | 2.69E-08 |
| fruits/internet_resized\Pineapple_3.jpg | Pineapple | Carambula | 0.902884543 | 9.56E-09 |
| fruits/internet_resized\Strawberry_1.jpg | Strawberry | Pear Red | 0.99985528 | 4.23E-08 |
| fruits/internet_resized\Strawberry_2.jpg | Strawberry | Pear Red | 0.999899387 | 7.19E-13 |

| fruits/internet_resized\Strawberry_3.jpg | Strawberry | Pear Red | 1 | 2.90E-11 |
|--|------------|----------|-------------|----------|
| fruits/internet_resized\Tomato_1.jpg | Tomato | Tomato | 0.923478901 | 0.923479 |
| fruits/internet_resized\Tomato_2.jpg | Tomato | Pear Red | 1 | 9.99E-25 |
| fruits/internet_resized\Tomato_3.jpg | Tomato | Pear Red | 0.999998689 | 6.71E-11 |