Complete Search

Sometimes you need to check all the things....

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Objectives

- Describe four patterns of brute force;
- ▶ Describe the times when a brute force solution is necessary.
- ▶ Describe some techniques to optimize brute force algorithms.

What is it?

- You must traverse the entire problem space to get the answer.
- Sometimes you can prune the problem space.

```
max=a[0]; // why not just put 0 here?
for(int i=1; i<7; i++)
if (a[i]>max) max=a[i];
```

When to Use It

- ▶ Tradeoffs
 - ► Bad: It's slow!
 - ► Good: It's simple! More likely to give correct solution.
- ▶ Three situations:
 - When you have no choice.
 - ► When the problem set is small.
 - To verify your real solution!Introduction

Categories

- ▶ Code Pattern
 - Iterative
 - Recursive
- ▶ Traversal Pattern
 - Filtering
 - GeneratingIntroduction

Speed

- Use bits instead of boolean arrays
- Use primitive types when appropriate:
 - int32 instead of int64
 - arrays instead of vector
 - character arrays instead of string
- Prefer iteration to recursion
- The STL algorithm include has next_permutation, which is very fast
- Declare large data structures in the global scope

The *n*-queens problem

	Х		х	
Х	х	Х		
Х	Q	Х	Х	Х
Х	х	Х		
	Х		Х	

- ▶ If you don't know chess, you might want to learn the basic rules.
- ▶ Classic problem: place n queens on a $n \times n$ chessboard.
 - ► How many ways can you do it?

Two examples

Q				
			Q	
	Q			
				Q
		Q		

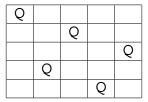
Q				
		Q		
				Q
	Q			
			Q	

How to write this?

```
Attempt 1 : Massive nested for loops
   vvi board(8, vi(8)); // get
  count = 0;
   for(i=0; i<7; ++i) {
     board[0][i] = 1; // place queen
     for(j=0; j<7; ++j)
5
       if (! collides(board,1,j)) {
         board[1][j] = 1;
         for(k=0; ...); // rest of program
8
         board[1][i] = 0;
10
     board[0][i] = 0; // remove queen
11
```

- ► Final position; if no collisions increment count.
- \blacktriangleright What do you think of this code? 8^8 attempts....

Improvements



- ► We don't need 8⁸ checks.
- Instead of modeling the chess board, model where the queens are placed.
 - ► This example is {0,3,1,4,2}.

Backtracking

► Example code from Competive Programming 4

```
void backtrack(int c) {
     if ((c == 8) & (row[b] == a))  { // a candidate solution
       printf("%2d %d", ++lineCounter, row[0]+1);
3
       for (int j = 1; j < 8; ++j)
4
         printf(" %d", row[j]+1);
5
       printf("\n");
6
       return; // optional statement
7
     for (int r = 0; r < 8; ++r) { // try all possible row
       if ((c == b) && (r != a)) continue; // early pruning
10
       if (canPlace(r, c)) // can place a Queen here?
11
         row[c] = r, backtrack(c+1); // put here and recurse
12
13
14
```

Checking Placement

Don't walk the diagonals; use math!

bool canPlace(int r, int c) {

for (int prev = 0; prev < c; ++prev) // check previous

if ((row[prev] == r) ||

(abs(row[prev]-r) == abs(prev-c)))

return false; // infeasible

return true;

}</pre>

Using bitmasks

- Keep three bit-vectors.
- Shifting the bits handles the diagonals.

```
// Place a queen in row $r$
rows |= (1 << r);
up |= (1 << r);
down |= (1 << r);

// Moving to the next column...
up <<= 1;
down >>= 1;
```