

Our Environment

Project Euler

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- ▶ Create a new directory for this project.
- ▶ Using an editor, create a file `euler.hs`. Add the following two lines to it:

```
1 inc :: Integer -> Integer
2 inc x = x + 1
```

- ▶ Now type `stack repl euler.hs`.

Expected Output

```
% stack repl euler.hs
```

```
[1 of 1] Compiling Main                ( /home/mattox/euler/euler.hs, interpreted )
Ok, one module loaded.
Loaded GHCi configuration from /run/user/1000/ghci4772/ghci-script
*Main> :t inc
inc :: Integer -> Integer
*Main> inc 10
11
*Main> :r
Ok, one module loaded.
*Main>
Leaving GHCi.
```

Problem 1 – Multiples of 3 or 5

If we list all the natural numbers below 10 that are multiples of 3 or 5, we get 3, 5, 6, and 9. The sum of these multiples is 23. Find the sum of all the multiples of 3 or 5 below 1000.

Some Arithmetic

```

1 *Main> mod 10 3
2 1
3 *Main> 10 `mod` 3
4 1
5 *Main> 10 `mod` 3 == 0
6 False
7 *Main> 10 `mod` 3 == 0 || 10 `mod` 5 == 0
8 True
9 *Main> mod3or5 x = x `mod` 3 == 0 || x `mod` 5 == 0
10 *Main>

```

Add the following line to your `euler.hs`.

```
1 mod3or5 x = x `mod` 3 == 0 || x `mod` 5 == 0
```

A Type Constraint

- ▶ HASKELL will *infer* the types of things if you don't specify them!
- ▶ Let's see what it thinks of our new function ...

```

1 *Main> :t mod3or5
2 mod3or5 :: Integral a => a -> Bool

```

- ▶ "The input can be any type that is an Integral, and the output is a Bool."

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```

1 *Main> :t mod3or5
2 mod3or5 :: Integral a => a -> Bool

```

List Operations

```

1 *Main> [3,5,7,9]
2 [3,5,7,9]
3 *Main> map inc [3,5,7,9]
4 [4,6,8,10]
5 *Main> map mod3or5 [3,5,7,9]
6 [True,True,False,True]
7 *Main> filter mod3or5 [3,5,7,9]
8 [3,5,9]
9 *Main> sum (filter mod3or5 [3,5,7,9])
10 17

```

Put the following definition into your `euler.hs`:

```
1 sumMods xx = sum (filter mod3or5 xx)
```

So how do we get a list from 1 to 999?

Big Lists

```
1 *Main> [1..20]
2 [1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20]
3 *Main> [1,3..20]
4 [1,3,5,7,9,11,13,15,17,19]
5 *Main> [1,5..20]
6 [1,5,9,13,17]
7 *Main> [1..999] -- Go ahead and try it!
```

So now add this line to your `euler.hs`:

```
1 euler1 = sumMods [1..999]
```

Final Result

```
1 inc :: Integer -> Integer
2 inc x = x + 1
3
4 -- Euler Problem 1
5
6 mod3or5 x = x `mod` 3 == 0 || x `mod` 5 == 0
7 sumMods xx = sum (filter mod3or5 xx)
8 euler1 = sumMods [1..999]
```

We can clean this up a little ...

Sample Run

```
1 *Main> :r
2 [1 of 1] Compiling Main ( /home/mattox/euler/euler.hs, interp
3 Ok, one module loaded.
4 *Main> euler1
5 233168
```

Cleaner Version

```
1 inc :: Integer -> Integer
2 inc x = x + 1
3
4 -- Euler Problem 1
5
6 euler1 = sumMods [1..999]
7   where mod3or5 x = x `mod` 3 == 0 || x `mod` 5 == 0
8         sumMods xx = sum (filter mod3or5 xx)
```

- ▶ The `where` keyword introduces local definitions.
- ▶ Indentation determines the scope of definitions.
- ▶ Be sure your editor never uses tabs!!

Euler Problem 3 – Prime Factors

The prime factors of 13195 are 5, 7, 13, and 29. What is the largest prime factor of the number 600851475143?

Sectioning

```

1 *Main> plus a b = a + b
2 *Main> :t plus
3 plus :: Num a => a -> a -> a
4 *Main> plus 10 20
5 30
6 *Main> :t (plus 1)
7 (plus 1) :: Num a => a -> a
8 *Main> addTwo = plus 2
9 *Main> addTwo 10
10 12

```

- ▶ You can also say things like (+1) to get a partially applied operator.

The Sieve

- ▶ We will make something like the Sieve of Eratosthenes.

```

1 *Main> notDivides a n = n `mod` a /= 0
2 *Main> notDivides 2 10
3 False
4 *Main> notDivides 3 10
5 True
6 *Main> filter (notDivides 3) [1..10]
7 [1,2,4,5,7,8,10]

```

Go ahead and add the definition of notDivides to your file.

Building Up Lists

- ▶ The operator : creates a list from an element and another list.
- ▶ Haskell “a:b” is like JAVA/C++ “new Node(a,b).”
- ▶ The built-in function head will get you the first element of a list.

```

1 *Main> 2 : filter (notDivides 2) [2..20]
2 [2,3,5,7,9,11,13,15,17,19]
3 *Main> 2 : filter (notDivides 2)
4         (3 : filter (notDivides 3) [2..20])
5 [2,3,5,7,11,13,17,19]
6 *Main> 2 : filter (notDivides 2)
7         (3 : filter (notDivides 3)
8         (5 : filter (notDivides 5) [2..20]))
9 [2,3,5,7,11,13,17,19]

```

- ▶ We need a recursive solution for this!

Making the Sieve

```
1 sieve (x:xs) = x : (sieve (filter (notDivides xs) xs))
2
3 primes = sieve [2..]
```

Sample Run

```
1 *Main> sieve [2..20]
2 [2,3,5,7,11,13,17,19,*** Exception: Prelude.head: empty list
3 *Main> take 20 (primes)
4 [2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71]
5 *Main> take 20 $ primes
6 [2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71]
```

Factors

► Now to get the factors ...

```
1 factors n = aux n primes
2   where aux 1 _ = []
3         aux n (p:ps) = case divMod n p of
4                           (n', 0) -> p : aux n' ps
5                           (_ , _) -> aux n ps
6
7 maxFactor n = foldr1 max $ factors n
8
9 euler3 = maxFactor 600851475143
10
11 *Main> foldr1 (+) [2,3,4,5]
12 14
13 *Main> euler3
14 6857
```

Problem 20 – Factorial Digit Sum

$n!$ means $n \times (n-1) \times \dots \times 3 \times 2 \times 1$.

For example, $10! = 10 \times 9 \times \dots \times 3 \times 2 \times 1 = 3628800$, and the sum of the digits in the number $10!$ is $3 + 6 + 2 + 8 + 8 + 0 + 0 = 27$.

Find the sum of the digits in the number $100!$

