Closures

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- ► Add conditional expressions (if then else) to your language.
- ► Add functions and function application to your interpreter.
- Explain the parts of a closure and why they are necessary.

Review

- ▶ Last time: made an interpreter with arithmetic, booleans, variables, and let.
- ► This time:
 - ► Add if expressions.
 - ► Add functions and function calls.
- ► Code can be found in the i5 directory.

Variables and Let Expressions

```
1 eval (VarExp var) env =
2   case lookup var env of
3     Just val -> val
4     Nothing -> IntVal 0
5
6 eval (LetExp var e1 e2) env =
7   let v1 = eval e1 env
8   in eval e2 (insert var v1 env)
```

▶ **N.B.** The variable let creates disappears after the let body is evaluated!!

For Example

Objectives

0000

```
In HASKELL ...
Prelude let z = 10 in z + 1
2 11
3 Prelude> z
4 <interactive>:2:1: error: Variable not in scope: z
ln i5...
i5 > let z = 10 in z + 1 end
IntVal 11
i5 > z
IntVal 0
```

Adding If Expressions

```
idata Exp = IfExp Exp Exp
i5>if 5>2 then 10 else 20 fi
IntVal 10
i5 if 5 > 22 then 10 else 20 fi
IntVal 20
```

The Eval

```
1 eval (IfExp e1 e2 e3) env =
2 let v1 = eval e1 env
3 in case v1 of
4 BoolVal True -> eval e2 env
5 _ -> eval e3 env
```

Adding Functions to Our Language

► Consider this function application in HASKELL.

$$_{1}(\x -> x + 10)$$
 20

- ► We have:
 - A parameter
 - ► A function body
 - An argument

Adding Functions: Take 1

```
_{1}(\x -> x + 10) 20
_2 => AppExp
     (FunExp "x" (IntOpExp "+" (VarExp "x") (IntExp 10)))
     (IntExp 20)
 ► The following attempt almost works.
data Exp = FunExp String Exp
          AppExp Exp Exp | ...
3 data Val = FunVal String Exp | ...
5 eval (FunExp v body) env = FunVal v body
6 eval (AppExp e1 e2) env =
     let (FunVal v body) = eval e1 env
         arg = eval e2 env
      in eval body (insert v arg env)
```

What Could Possibly Go Wrong?

Objectives

► Consider this function definition and function call.

Now we use a second let to define the increment.

```
1 Main> let f =
2          let delta = 10
3          in \ x -> x + delta
4          in f 20
5 30
```

▶ When we run f 20, is delta still in scope?



The Need for Closures

- ▶ Now consider this one. We have *two* variables called delta!
- ► How does the function know which one to use?

```
1 Main> let f =
2         let delta = 10 in \ x -> x + delta
3         in
4         let delta = 20 in f 20
5 30 --- Why not 40??
```

Closures

- ▶ The "function value" needs to remember the values of free variables in its function body.
- ▶ The resulting data structure is called a *closure*.

An Example Evaluation

Objectives

► Let's evaluate this expression:

```
let d = 10 in \xspace x -> x + d
```

► Initial call to eval:

▶ Step 1: eval will be called on the IntExp 10 to get the value of d.

```
eval (IntExp 10) [] => IntVal 10
```

Example, Continued

Now d is part of the environment when we evaluate the body of the let.

Now Let's Call the Function!

```
let f =
    let d = 10 in \xspace x -> x + d
in let y = 20 in f y
eval (LetExp "f"
        (LetExp "d" (IntExp 10)
           (FunExp "x"
               (IntOpExp "+"
                  (VarExp "x") (VarExp "d"))))
        (LetExp "y" (IntExp 20)
           (AppExp (VarExp "f") (VarExp "y"))))
```

Now Let's Call the Function! Pt 2

► After the function has been evaluated into a closure ...

Now Let's Call the Function! Pt 3

- ► After the function has been evaluated into a closure ...
- ► And y has been defined ...

Reminder of the Code

Objectives

Remember what eval says to do with function calls.

```
1 eval (AppExp e1 e2) env =
2  let (Closure v body clenv) = eval e1 env
3  arg = eval e2 env
4  in eval body (insert v arg clenv)
```



Functions

Now Let's Call the Function! Pt 4

We unfold the f and y values ...

```
eval (IntOpExp "+" (VarExp "x") (VarExp "d"))
     [("x", eval (VarExp "y") [("y",IntVal 20)), ...]
    ,("d", IntVal 10)]
```

Conclusions

- Some history
 - ► The first language to use closures (and call them that) was Peter Landin's SECD machine.
 - ► The first widespread use of closures was in SCHEME, a dialect of LISP.
 - ► Today they are very common!
- ► Things to try
 - What if you wanted C-style ifs?
 - Try some other examples of function calls.
 - Try making multi-parameter functions.