

STAGE 2

$$B(2) = [A(0) - A(2)] W_8^0 = [1 - 0](1) = 1$$

$$B(3) = [A(1) - A(3)] W_8^2 = [1 - 0](-j) = -j$$

$$B(0) = [A(0) + A(2)] = 1$$

$$B(1) = A(1) + A(3) = 1$$

$$B(4) = A(4) + A(6) = 1 + 0$$

$$B(5) = A(5) + A(7) = \frac{\sqrt{2}}{2} - j\frac{\sqrt{2}}{2} + 0$$

$$B(6) = [A(4) - A(6)] W_8^0 = (1)(1)$$

$$B(7) = [A(5) - A(7)] W_8^2 = \left(\frac{\sqrt{2}}{2} - j\frac{\sqrt{2}}{2}\right)(-j) = -\frac{\sqrt{2}}{2} - j\frac{\sqrt{2}}{2}$$

STAGE 3

$$X(0) = B(0) + B(1) = 1 + 1 = 2$$

$$X(4) = [B(0) - B(1)] W_8^0 = [1 - 1](1) = 0$$

$$X(2) = [B(2) + B(3)] = 1 - j$$

$$X(6) = [B(2) - B(3)] W_8^0 = (1 + j)(1) = 1 + j$$

$$X(1) = B(4) + B(5) = \left(1 + \frac{\sqrt{2}}{2}\right) - j\frac{\sqrt{2}}{2}$$

$$X(5) = [B(4) - B(5)] W_8^0 = \left[1 - \frac{\sqrt{2}}{2} + j\frac{\sqrt{2}}{2}\right](1) = \left(1 - \frac{\sqrt{2}}{2}\right) + j\frac{\sqrt{2}}{2}$$

$$X(3) = B(6) + B(7) = \left(1 - \frac{\sqrt{2}}{2}\right) - j\frac{\sqrt{2}}{2}$$

$$X(7) = [B(6) - B(7)] W_8^0 = \left(1 + \frac{\sqrt{2}}{2}\right) + j\frac{\sqrt{2}}{2}$$

(B) The main advantage of FFT vs. DFT is the amount of time to compute.
complexity for FFT is $\frac{N}{2} \log_2 N$ vs. N^2 for DFT.