```
In [1]: import pandas as pd
   import numpy as np
   import statsmodels.api as sm
   import scipy.stats as stats
   import matplotlib.pyplot as plt
   import seaborn as sns
   from sklearn.preprocessing import OrdinalEncoder
   from sklearn.model_selection import cross_val_score
   from sklearn.linear_model import LinearRegression
In [2]: df = pd.read_csv('./data/cleaned_kc_house_data.csv')
```

Analyzing Variables of High Value Houses ¶

In this notebook, we analyze and visualize relationships between variables of high-value houses, to understand how those variables affect variation in price, in order to answer our business problem. We defined high value houses as any house with a sale price above \\$800,000. We chose this number because it represents houses that a large enough quantity of data points not to be skewed too severely by the biggest outliers, while also being distant enough from the whole dataset to behave similarly. For reference, the high value sample comprises about 3,000 houses whose mean sale price is nearly double the average sale price of the full dataset of houses sold in 2014-15.

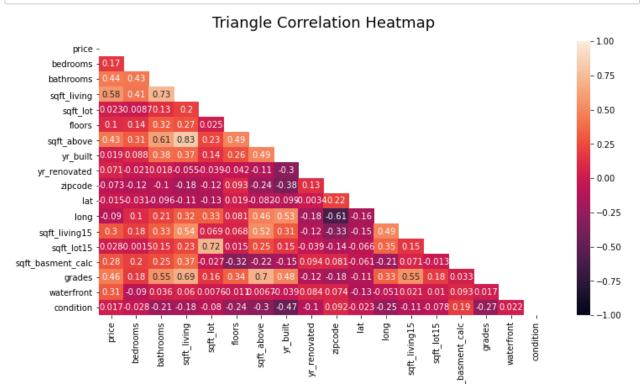
```
In [3]: #create new df for houses above $800,000
target_df = df.loc[df['price'] >= 800000]
```

In [4]: target df.describe()

Out[4]:

	price	bedrooms	bathrooms	sqft_living	sqft_lot	floors	sqft_abov
count	3.000000e+03	3000.000000	3000.00000	3000.000000	3.000000e+03	3000.000000	3000.00000
mean	1.203345e+06	3.966667	2.89775	3372.903000	2.289503e+04	1.763000	2822.59633
std	5.484658e+05	0.886840	0.83332	1092.722341	6.061375e+04	0.484158	1040.45570
min	8.000000e+05	1.000000	1.00000	1050.000000	6.090000e+02	1.000000	710.00000
25%	8.750000e+05	3.000000	2.50000	2650.000000	6.000000e+03	1.500000	2010.00000
50%	9.986500e+05	4.000000	2.75000	3240.000000	9.690500e+03	2.000000	2700.00000
75%	1.320000e+06	4.000000	3.50000	3920.000000	1.667500e+04	2.000000	3480.00000
max	7.700000e+06	10.000000	8.00000	13540.000000	1.024068e+06	3.500000	9410.00000

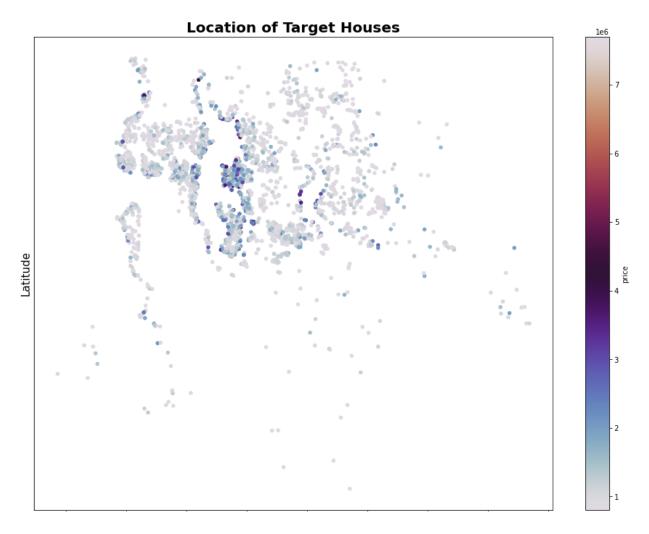
```
In [5]: plt.figure(figsize=(12,6))
    mask = np.triu(np.ones_like(target_df.corr(), dtype=bool))
    heatmap = sns.heatmap(target_df.corr(), mask=mask, vmin=-1, vmax=1, annot = heatmap.set_title('Triangle Correlation Heatmap', fontdict={'fontsize':18},
```



Location Analysis

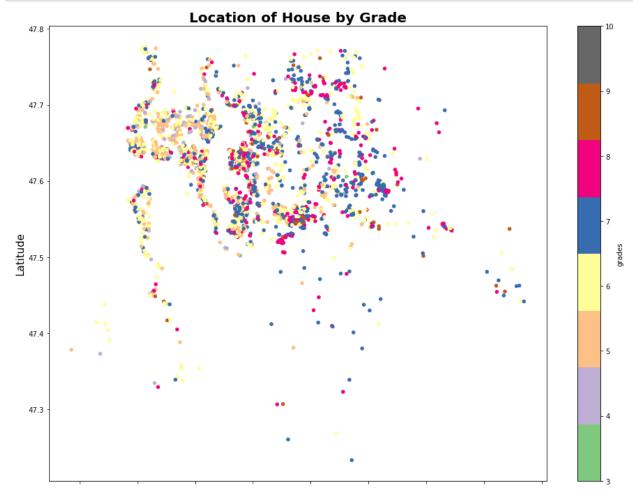
Because location is difficult to explain with our data, the first thing we are interested in visualizing is the geographical distribution of all houses compared to that of high value houses.

Out[6]: ''





We see a distinct concentration of high value houses near the center of the map and investigate a map of King County. This area appears to generally surround Seattle, so we choose to look more closely at how that group of locations behave relative to one another.



Based on this visualization grades 5 and 6 seem to be clustered closer to Seattle while higher grades are located more in the eastern part of the county. Because we know the relationship between sqft_living and grade, we suspect that houses in Seattle are smaller than houses outside of Seattle, and we create groups to check this assumption.

We create a dataframe that comprises houses inside Seattle's general coordinates, as well as

houses outside. For houses outside, we omit coastal houses, which behave similarly to houses in the Seattle group in terms of grade and sale price.

```
In [9]: seattle = target_df.loc[(target_df['long'] <= -122.2) & (target_df['lat'] >
In [10]: outside = target_df.loc[target_df['long'] >= -122.2]
```

We look at the distribution of price and square feet for the houses in these groups. The Seattle group is smaller and more expensive on average. Because sqft_living is our single best explanatory variable of price, and the smaller houses in the Seattle group cost more than the bigger houses in the Outside group, we can see why our r-squared value would be lower for this subset of high value houses than the entire set of houses sold in '14-15.

```
In [11]: |seattle['price'].describe()
Out[11]: count
                   1.247000e+03
                   1.318553e+06
         mean
         std
                   6.658068e+05
                   8.000000e+05
         min
         25%
                   8.999750e+05
         50%
                   1.100000e+06
          75%
                   1.480000e+06
         max
                   7.700000e+06
         Name: price, dtype: float64
In [12]: outside['price'].describe()
Out[12]: count
                   1.288000e+03
         mean
                   1.077051e+06
                   3.675764e+05
         std
         min
                   8.000000e+05
         25%
                   8.550000e+05
         50%
                   9.459000e+05
         75%
                   1.150000e+06
         max
                   4.210000e+06
         Name: price, dtype: float64
In [13]: |seattle['sqft living'].describe()
Out[13]: count
                    1247.000000
                    3070.947073
         mean
         std
                    1108.631708
         min
                    1050.000000
         25%
                    2360.000000
         50%
                    2900.000000
         75%
                    3590.000000
                   12050.000000
         max
         Name: sqft living, dtype: float64
```

```
outside['sqft_living'].describe()
Out[14]: count
                    1288.000000
                    3682.016304
         mean
         std
                    1007.982645
                    1180.000000
         min
         25%
                    3050.000000
         50%
                    3560.000000
         75%
                    4150.000000
                   13540.000000
         max
         Name: sqft_living, dtype: float64
```

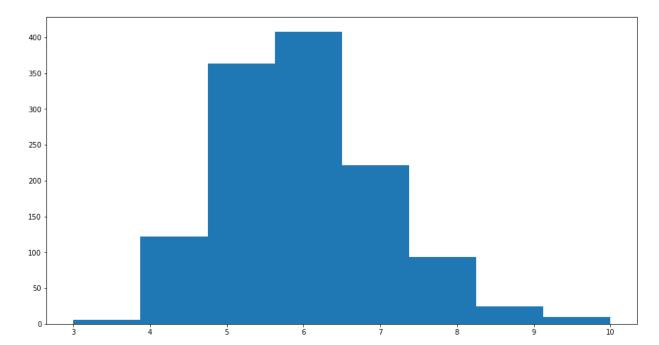
We calculate the price per square foot of both groups and compare them.

```
In [15]: seattle_price_space = seattle['sqft_living'].sum()/seattle['price'].sum()
In [16]: outside_price_space = outside['sqft_living'].sum()/outside['price'].sum()
In [17]: outside_price_space / seattle_price_space
Out[17]: 1.4678261911471926
```

Based on this metric, houses in the Outside group have 146% the square footage as the Seattle group for the same price

Below, we look at distribution of house grades between the groups, to verify our earlier assumption that houses in Seattle have lower grades on average

```
In [18]: fig, ax = plt.subplots(figsize = (15, 8))
    ax.hist(seattle['grades'], bins=8)
```



```
In [19]: fig, ax = plt.subplots(figsize = (15, 8))
         ax.hist(outside['grades'], bins=8)
Out[19]: (array([ 3.,
                        23., 128., 392., 448., 236., 55.,
          array([ 3.
                           3.875, 4.75, 5.625, 6.5, 7.375, 8.25, 9.125,
                  10.
                        ]),
          <BarContainer object of 8 artists>)
          400
          300
          100
In [20]: seattle['grades'].describe()
Out[20]: count
                  1247.000000
         mean
                      5.914996
         std
                      1.223430
         min
                      3.000000
         25%
                      5.000000
         50%
                      6.000000
         75%
                      7.000000
         max
                     10.000000
         Name: grades, dtype: float64
In [21]: outside['grades'].describe()
Out[21]: count
                  1288.000000
                      6.709627
         mean
         std
                      1.091537
         min
                      3.000000
         25%
                      6.000000
         50%
                      7.000000
         75%
                      7.000000
         max
                     10.00000
```

Based on the analysis above, we conclude that the Seattle location is more lucrative than the Outside location, and that is why houses are more expensive on average despite having less square footage and lower grades.

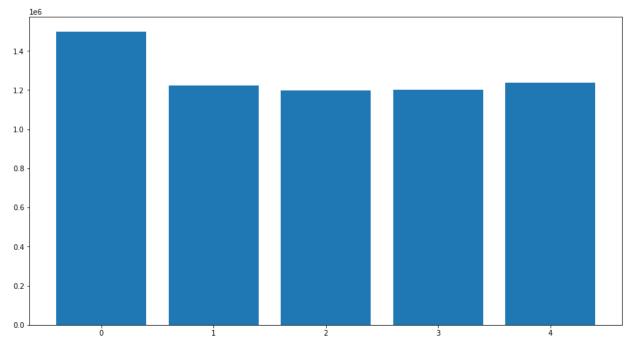
Name: grades, dtype: float64

Year Built, Condition, and Renovation effects on Price

Next, we take a look at variables that were less highly correlated with price of houses in the whole sample, to see if there is any relationship between them in the high value sample.

```
In [22]: target_df['yr_built'].describe()
Out[22]: count
                   3000.000000
                   1973.708333
         mean
         std
                     32.524594
         min
                   1900.000000
         25%
                   1951.000000
         50%
                   1983.000000
         75%
                   2001.250000
         max
                   2015.000000
         Name: yr_built, dtype: float64
In [23]: target df['yr_built'].value_counts()
Out[23]: 2014
                  159
         2006
                   90
         2007
                   78
         2001
                   73
         2008
                   68
         1935
                    4
         1903
                    3
         1934
                    2
         1901
                    2
         1944
         Name: yr built, Length: 116, dtype: int64
In [24]: |target_df['condition'].value_counts()
Out[24]: 2.0
                 1951
          3.0
                  705
         4.0
                  337
          1.0
                    6
                    1
         0.0
         Name: condition, dtype: int64
In [25]: condition prices = target df.groupby("condition")["price"].mean()
```

```
In [26]: #average price per 'condition' value
fig, ax = plt.subplots(figsize = (15, 8))
ax.bar(x = condition_prices.index, height = condition_prices);
```

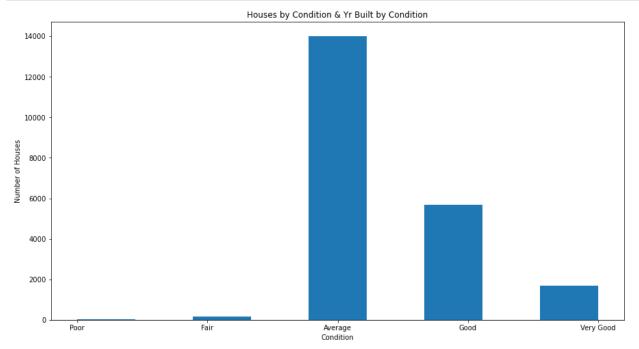


Here, we find that houses of all Conditions sell for similar prices among the high value houses.

Interestingly, houses in the best Condition are older than houses in Average Condition

```
In [28]: fig, ax = plt.subplots(figsize = (15, 8))

ax.hist(df['condition'], bins = 9)
ax.set_xticks([0, 1, 2, 3, 4])
plt.xlabel('Condition')
plt.xticks([0, 1, 2, 3, 4], ['Poor', 'Fair', 'Average', 'Good', 'Very Good'
plt.ylabel('Number of Houses')
plt.title('Houses by Condition & Yr Built by Condition');
```

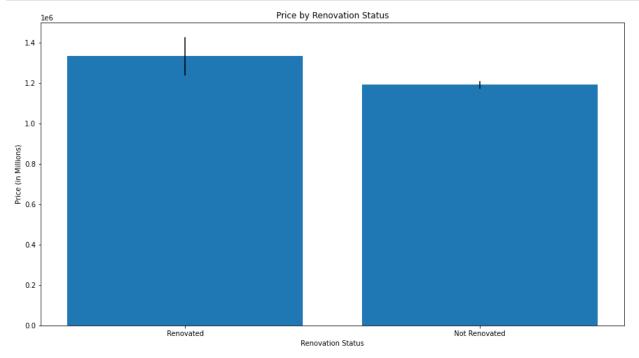


```
In [29]: #separate by houses that are and are not renovated
renovated = target_df.loc[target_df['yr_renovated'] > 0]
not_renovated = target_df.loc[target_df['yr_renovated'] == 0]
```

```
In [30]: #average price per 'condition' value
fig, ax = plt.subplots(figsize = (15, 8))

x_vals = ['Renovated', 'Not Renovated']
y_vals = [renovated['price'].mean(), not_renovated['price'].mean()]
y_stds = [renovated['price'].std()/np.sqrt(renovated['price'].shape[0])*1.9

plt.bar(x_vals, y_vals, yerr=y_stds)
plt.xlabel('Renovation Status')
plt.ylabel('Price (in Millions)')
plt.title('Price by Renovation Status');
```



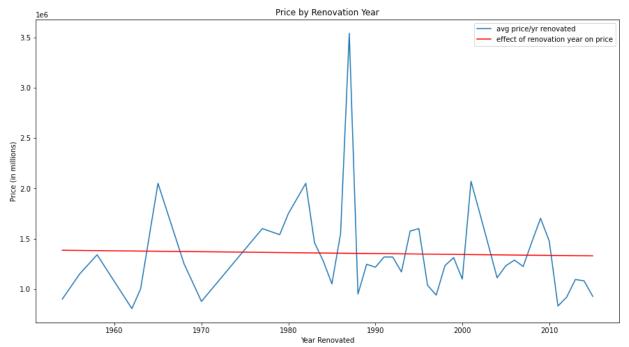
Here we see that Renovated houses sell for more than houses without renovations in this price range. A 2 sample t-test below verifies this to be significant of the whole groups.

```
In [31]: import numpy as np
         from scipy.stats import ttest ind
         from scipy.stats import t
         import pandas as pd
         def welch_ttest(x1, x2):
             n1 = x1.size
             n2 = x2.size
             m1 = np.mean(x1)
             m2 = np.mean(x2)
             v1 = np.var(x1, ddof=1)
             v2 = np.var(x2, ddof=1)
             pooled_se = np.sqrt(v1 / n1 + v2 / n2)
             delta = m1-m2
             tstat = delta / pooled_se
             df = (v1 / n1 + v2 / n2)**2 / (v1**2 / (n1**2 * (n1 - 1)) + v2**2 / (n2)
             # two side t-test
             p = 2 * t.cdf(-abs(tstat), df)
             # upper and lower bounds
             lb = delta - t.ppf(0.975,df)*pooled_se
             ub = delta + t.ppf(0.975,df)*pooled se
             return pd.DataFrame(np.array([tstat,df,p,delta,lb,ub]).reshape(1,-1),
                                   columns=['T statistic','df','pvalue 2 sided','Diff
```

```
In [33]: target_df['yr_renovated'].value_counts()
Out[33]: 0.0
                     2745
          2014.0
                       20
          2007.0
                       16
          2005.0
                       14
          2003.0
                       14
          2000.0
                       14
          2013.0
                       11
          2002.0
                       10
          2004.0
                        9
          1999.0
                        9
                        9
          2006.0
          1990.0
                        8
          2010.0
                        8
          2009.0
                        8
          2008.0
                        8
          2015.0
                        7
          1991.0
                        7
          2001.0
                        7
          1993.0
                        6
          1998.0
                        6
                        5
          1994.0
                        5
          1989.0
                        5
          1995.0
          1985.0
                        4
          1992.0
                        4
          1988.0
                        4
                        4
          1996.0
          1987.0
                        4
                        3
          1997.0
          1984.0
                        3
          2012.0
                        3
                        2
          1956.0
                        2
          1983.0
          1982.0
                        2
          1980.0
                        2
          1979.0
                        2
          1954.0
                        1
          1968.0
                        1
          1986.0
                        1
          1962.0
                        1
          1965.0
                        1
          1963.0
                        1
          1970.0
                        1
          1977.0
                        1
          1958.0
                        1
          2011.0
                        1
          Name: yr_renovated, dtype: int64
In [34]: renovations_df = target_df.loc[target_df['yr_renovated'] >= 1954]
In [35]: renovated_prices = renovations_df.groupby("yr_renovated")["price"].mean()
```

```
In [36]: fig, ax = plt.subplots(figsize = (15, 8))

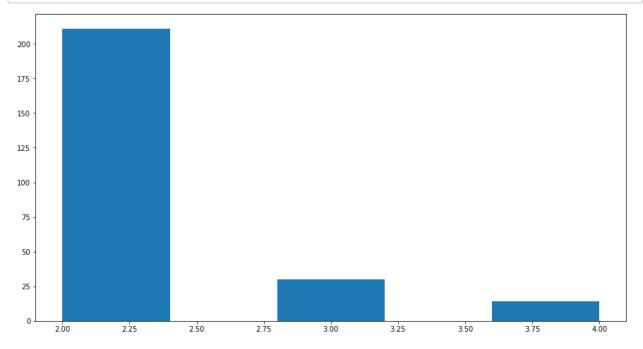
ax.plot(renovated_prices, label='avg price/yr renovated')
theta = np.polyfit(renovated_prices.index, renovated_prices, 1)
y_line = theta[1] + theta[0] * renovated_prices.index
plt.plot(renovated_prices.index, y_line, 'r', label ='effect of renovation
plt.xlabel('Year Renovated')
plt.ylabel('Price (in millions)')
plt.title('Price by Renovation Year')
plt.legend()
plt.show()
;
```



Out[36]: ''

Though Renovation status has an effect on sale price, here we find that the year of renovations has little effect on the sale price of a house. Surprisingly, the line of best fit suggests that the more recently a home has been renovated, the less it will sell for.

```
In [37]: fig, ax = plt.subplots(figsize = (15, 8))
ax.hist(renovated['condition'], bins = 5);
```



These graphs show us that whether a house has been renovated has little effect on its Condition

2.0

2.5

3.0

3.5

4.0

1.5

0.5

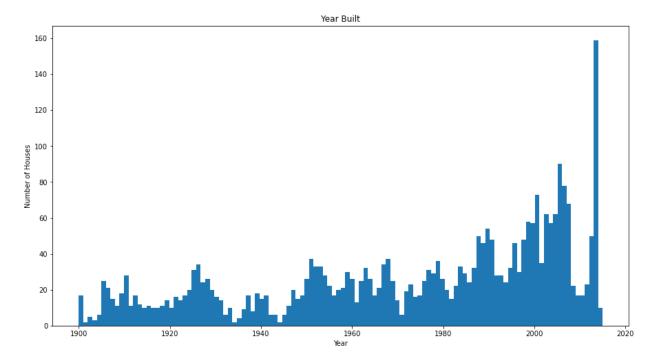
0.0

1.0

```
In [39]: #distribution of high value houses by Year Built
fig, ax = plt.subplots(figsize = (15, 8))

ax.hist(target_df['yr_built'], bins = 116);
plt.xlabel('Year')
plt.ylabel('Number of Houses')
plt.title('Year Built')
```

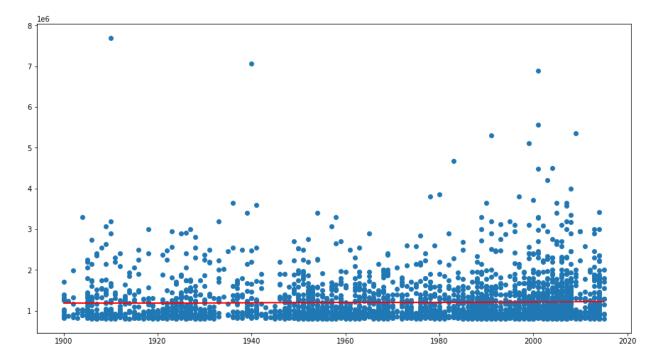
Out[39]: Text(0.5, 1.0, 'Year Built')



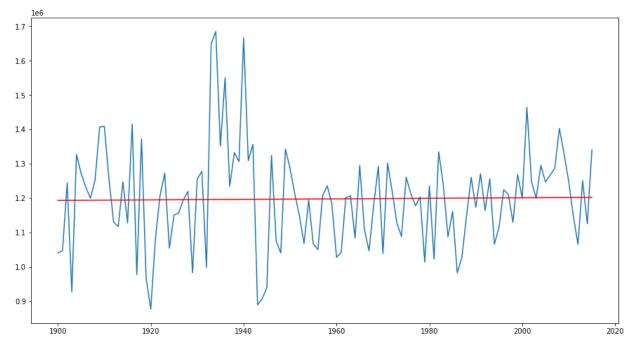
```
In [40]: #scatter plot w line of best fit
fig, ax = plt.subplots(figsize = (15, 8))

ax.scatter(x = target_df['yr_built'], y = target_df['price']);
theta = np.polyfit(target_df['yr_built'], target_df['price'], 1)
y_line = theta[1] + theta[0] * target_df['yr_built']
plt.plot(target_df['yr_built'], y_line, 'r')
```

Out[40]: [<matplotlib.lines.Line2D at 0x7eff6afaf0d0>]



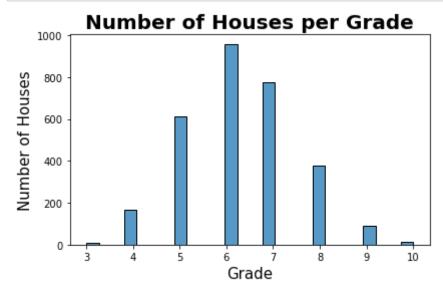
```
In [41]: year_built_prices = target_df.groupby("yr_built")["price"].mean()
```



This line graph of average sale price by year built and a line of best fit show there is no relationship between year built and price of houses in this sample.

Investigate relationship between price and grades

```
In [43]: sns.histplot(target_df['grades'])
   plt.title('Number of Houses per Grade', fontsize =20, weight = 'bold')
   plt.ylabel('Number of Houses', fontsize =15)
   plt.xlabel('Grade', fontsize =15)
   plt.tight_layout();
```



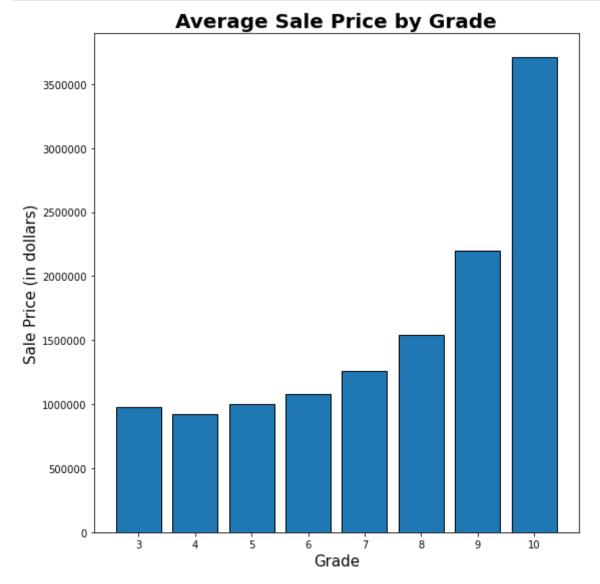
```
In [44]: # grades for target housing market appears mostly normally distributed.
# the majority of the houses have grades between 6 and 7
```

```
In [45]: target_grades_mean = target_df.groupby('grades')['price'].mean()
target_grades_mean
```

```
Out[45]: grades
                  9.739091e+05
         3.0
         4.0
                  9.245640e+05
         5.0
                  1.002244e+06
         6.0
                  1.079464e+06
         7.0
                  1.256389e+06
         8.0
                  1.540967e+06
         9.0
                  2.202528e+06
         10.0
                  3.710769e+06
         Name: price, dtype: float64
```

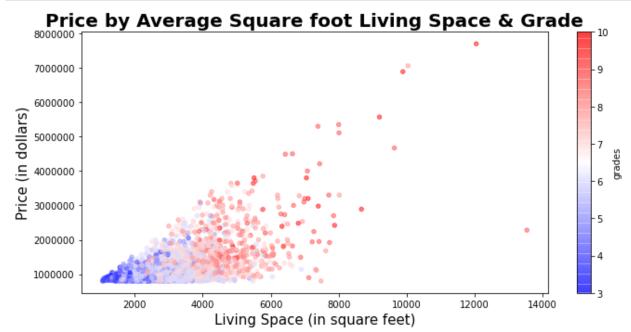
```
In [46]: fig, ax = plt.subplots(figsize = (8, 8))

ax.bar(x = target_grades_mean.index, height = target_grades_mean, edgecolor
plt.ticklabel_format(style='plain', axis = 'y')
plt.title('Average Sale Price by Grade', fontsize =20, weight = 'bold')
plt.ylabel('Sale Price (in dollars)', fontsize =15)
plt.xlabel('Grade', fontsize =15)
plt.tight_layout();
```



```
In [47]: # as shown in the LR model, the sale price increases as grade increases.
```

```
In [48]: fig, ax = plt.subplots(figsize=(10,5))
    target_df.plot.scatter(x="sqft_living", y="price", c='grades', cmap="bwr",
    plt.title('Price by Average Square foot Living Space & Grade', fontsize =20
    plt.ylabel(('Price (in dollars)'), fontsize =15)
    plt.xlabel(('Living Space (in square feet)'), fontsize =15)
    plt.ticklabel_format(style='plain', axis = 'y')
    plt.tight_layout();
```



Sales price, square feet of living space and grade appear to highly related. Based on the graph as squarefoot increases both the price and grade.

Going to look into the relationship between price, sqft_living, bedrooms, and bathrooms.

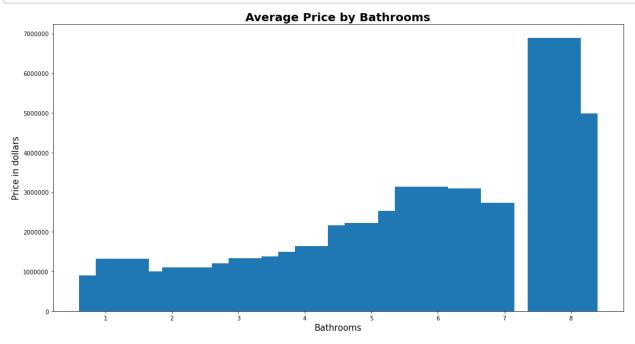
```
In [49]: highend_800 = target_df
In [50]: highend_800['bathrooms'].mean()
Out[50]: 2.89775
In [51]: highend_800['bedrooms'].mean()
Out[51]: 3.96666666666667
In [52]: highend_800['sqft_living'].mean()
Out[52]: 3372.903
```

```
In [ ]:
```

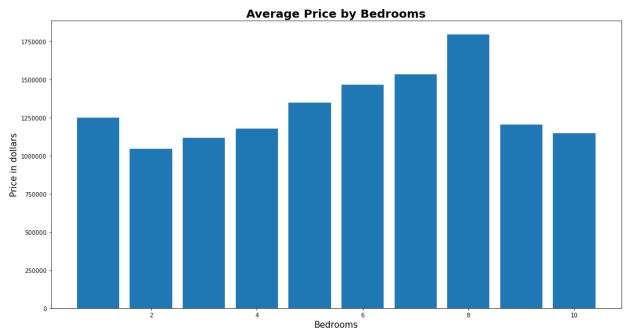
Creating 3 variables that will sort all three relationships buy the average price so we can graph them.

```
In [53]: price_bath = highend_800.groupby('bathrooms')['price'].mean()
    price_bed = highend_800.groupby('bedrooms')['price'].mean()
    price_sqft = highend_800.groupby('sqft_living')['price'].mean()
```

```
In [54]: fig, ax = plt.subplots(figsize = (15, 8))
    ax.bar(x = price_bath.index, height = price_bath);
    plt.title('Average Price by Bathrooms', fontsize =20, weight = 'bold')
    plt.ylabel(('Price in dollars'), fontsize =15)
    plt.xlabel(('Bathrooms'), fontsize =15)
    plt.ticklabel_format(style='plain', axis = 'y')
    plt.tight_layout();
```



```
In [55]: fig, ax = plt.subplots(figsize = (15, 8))
    ax.bar(x = price_bed.index, height = price_bed);
    plt.title('Average Price by Bedrooms', fontsize =20, weight = 'bold')
    plt.ylabel(('Price in dollars'), fontsize =15)
    plt.xlabel(('Bedrooms'), fontsize =15)
    plt.ticklabel_format(style='plain', axis = 'y')
    plt.tight_layout();
```



```
In [56]: y = highend_800['price']
X = highend_800.drop('price', axis=1)
from sklearn.model_selection import train_test_split
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=42)
```

Testing the linear regression modle on just the bedrooms, bathrooms, and sqft_living.

```
In [57]: relevant_columns = [
          'bedrooms',
          'bathrooms',
          'sqft_living'
         # 'sqft lot',
         # 'floors',
         # 'waterfront',
         # 'condition',
         # 'grades',
            'sqft above',
         # 'sqft basment calc',
         # 'yr_built',
         # 'yr renovated',
         # 'zipcode',
            'lat',
         # 'long',
         # 'sqft_living15',
           'sqft lot15'
         ]
In [58]: X train = X train.loc[:, relevant columns]
         lr = LinearRegression()
         lr.fit(X_train, y_train)
         cross_val_score(lr, X_train, y_train, cv=3)
Out[58]: array([0.31911078, 0.32169367, 0.39448431])
In [59]: X test = X test.loc[:, relevant columns]
In [60]: |lr.fit(X_train, y_train)
         lr.score(X_test, y_test)
Out[60]: 0.31230596757467466
```

```
In [61]: y = highend_800['price']
         X = highend_800.loc[:, relevant_columns]
         results_grade = sm.OLS(y, sm.add_constant(X)).fit()
         results_grade.summary()
```

Out[61]:

OLS Regression Results

0.340 Dep. Variable: price R-squared: Model: OLS Adj. R-squared: 0.339 Method: Least Squares 513.8 F-statistic: **Date:** Sun, 07 Aug 2022 Prob (F-statistic): 2.23e-269 20:14:05 -43278. Time: Log-Likelihood: 3000 AIC: 8.656e+04 No. Observations: **Df Residuals:** 2996 **BIC:** 8.659e+04 Df Model: 3

Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025	0.975]
const	3.452e+05	3.99e+04	8.655	0.000	2.67e+05	4.23e+05
bedrooms	-5.849e+04	1.03e+04	-5.669	0.000	-7.87e+04	-3.83e+04
bathrooms	4.788e+04	1.46e+04	3.275	0.001	1.92e+04	7.66e+04
sqft_living	282.0614	11.040	25.548	0.000	260.414	303.709

Omnibus: 1409.167 2.020 **Durbin-Watson:**

Jarque-Bera (JB): 13760.755 Prob(Omnibus): 0.000

> Skew: 1.988 Prob(JB): 0.00

12.710 Cond. No. 1.77e+04 **Kurtosis:**

Notes:

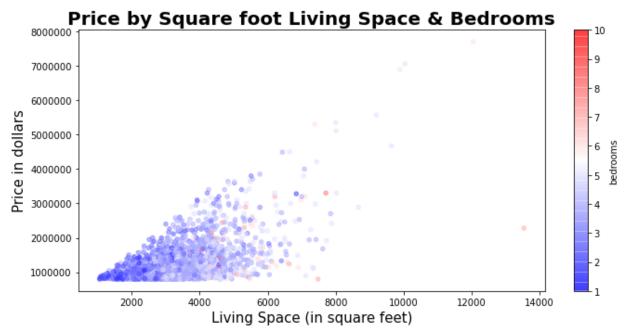
- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.77e+04. This might indicate that there are strong multicollinearity or other numerical problems.

This graph shows that the correlation between price and bedrooms isn't very signifiacnt.

```
In [82]: import pandas as pd
    import matplotlib.pyplot as plt
    import matplotlib.cm as cm
    %matplotlib nbagg
    %matplotlib inline

#highend_800["price"] = highend_800["price"] - highend_800["price"].mean()

fig, ax = plt.subplots(figsize=(10,5))
    plt.ticklabel_format(style='plain', axis = 'y')
    highend_800.plot.scatter(x="sqft_living", y="price", c='bedrooms', cmap="bw
    plt.title('Price by Square foot Living Space & Bedrooms', fontsize =20, wei
    plt.ylabel(('Price in dollars'), fontsize =15)
    plt.xlabel(('Living Space (in square feet)'), fontsize =15)
    plt.ticklabel_format(style='plain', axis = 'y')
    plt.tight_layout();
```

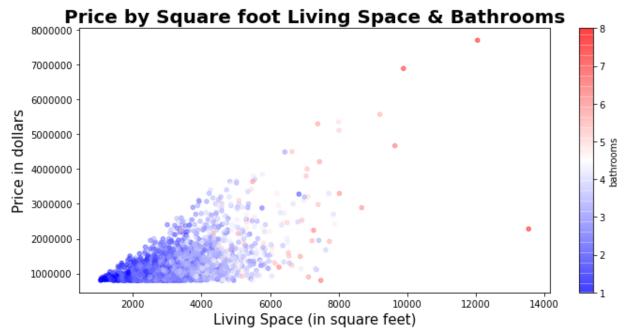


This graph shows that the correlation between price and bathrooms is signifiacnt.

```
In [83]: import pandas as pd
    import matplotlib.pyplot as plt
    import matplotlib.cm as cm
    %matplotlib inbagg
    %matplotlib inline

#highend_800["price"] = highend_800["price"] - highend_800["price"].mean()

fig, ax = plt.subplots(figsize=(10,5))
    plt.ticklabel_format(style='plain', axis = 'y')
    highend_800.plot.scatter(x="sqft_living", y="price", c='bathrooms', cmap="b
    plt.title('Price by Square foot Living Space & Bathrooms', fontsize =20, we
    plt.ylabel(('Price in dollars'), fontsize =15)
    plt.xlabel(('Living Space (in square feet)'), fontsize =15)
    plt.ticklabel_format(style='plain', axis = 'y')
    plt.tight_layout();
```



We decided to take a look at the Square Foot compared to the price inside and outside of Seattle.

```
In [78]: inside = highend_800.loc[(highend_800['lat'] >= 47.6) & (highend_800['long']
In [79]: outside = highend_800.loc[(highend_800['long'] >= -122.2)]
In [80]: long_test = highend_800.loc[highend_800['long'] <= -122.2]
In [81]: upper = inside['sqft_living'].sum()/ inside['price'].sum()
In [75]: lower = outside['sqft_living'].sum()/ outside['price'].sum()</pre>
```

We devided sum of all the sqft_living by the sum of all the price, for both inside and outside the city. then we took that result and divided the result of the inside by the result of the outside and found out that exactly how much more square foot you can get on average outside of the city.

```
In [77]: upper / lower
Out[77]: 0.6812795724938258
In [ ]:
```