STAA 577: HW7

Your Name

## Problem 1

```
data(OJ)
set.seed(577)
n <- nrow(OJ)
tr_index <- sample(seq_len(n), size = 800, replace = F)
OJtrain <- OJ[tr_index, ]
OJtest <- OJ[-tr_index, ]</pre>
```

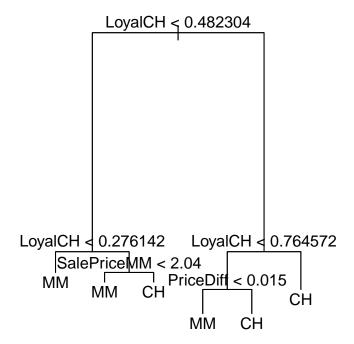
no output needed

## Problem 1b

```
##
## Classification tree:
## tree(formula = Purchase ~ ., data = OJtrain)
## Variables actually used in tree construction:
## [1] "LoyalCH" "SalePriceMM" "PriceDiff"
## Number of terminal nodes: 6
## Residual mean deviance: 0.7588 = 602.5 / 794
## Misclassification error rate: 0.1638 = 131 / 800
```

insert answer

## Problem 1c



insert answer

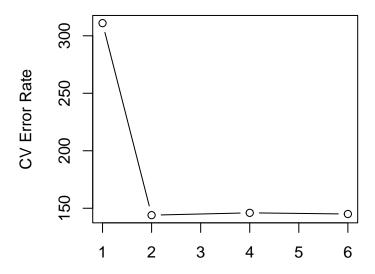
# Problem 1d

```
## oj_pred
## CH MM
## CH 134 30
## MM 24 82
## [1] 0.2
```

Test error is .2

## Problem 1e

## **CV Error Rate vs. Tree Size**



Tree Size (Number of Terminal Nodes)

#### ## [1] 2

tree size 2 has the lowest error rate

## Problem 1f

no output is needed

## Problem 1g

- $\mbox{\tt \#\#}$  Training Error Rate (Unpruned Tree): 0.1638
- ## Training Error Rate (Pruned Tree): 0.1762
  - Training error for full tree: .1638
  - Training error for pruned tree: .1762

#### Problem 1h

## [1] 0.2333

## [1] 0.2

• Test error for full tree: .2

• Test error for pruned tree: .2333

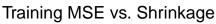
## Problem 2a

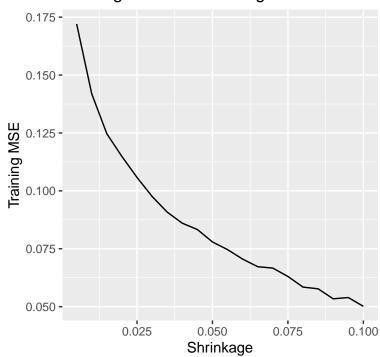
Nothing to report

## Problem 2b

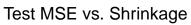
no output to report

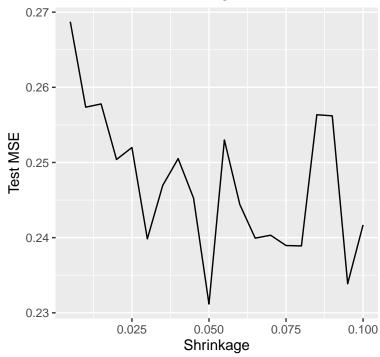
## Problem 2c





# Problem 2d

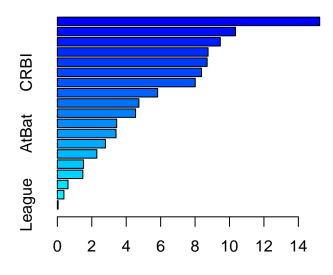




##

## Optimal lambda: 0.05

# Problem 2e



Relative influence

##		var	rel.inf
##	CAtBat	$\mathtt{CAtBat}$	15.24022191
##	CHits	CHits	10.34858112
##	CWalks	CWalks	9.46601826
##	CRuns	CRuns	8.75659634
##	PutOuts	PutOuts	8.70145002
##	CRBI	CRBI	8.37371811
##	Years	Years	8.01096804
##	Walks	Walks	5.82616246
##	Hits	Hits	4.73823746
##	CHmRun	$\tt CHmRun$	4.54399401
##	RBI	RBI	3.44740626
##	AtBat	AtBat	3.40962732
##	HmRun	HmRun	2.79316846
##	Assists	Assists	2.29404133
##	Runs	Runs	1.52040819
##	Errors	Errors	1.48151576
##	NewLeague	NewLeague	0.61977849
##	Division	Division	0.38174580
##	League	League	0.04636065

C At Bat, hits and Walks seem to be the top 3. Generally anything related to getting on base is important to salary which makes sense.

## Problem 2f

```
## Test MSE for Bagging: 0.1879
```

• test MSE is .1879

## Problem 2g

```
## Test MSE for Random Forest: 0.1953
```

• test MSE is .1953

## Problem 3

```
##
## Test MSE for Linear Regression: 25.2694
## Test MSE for Boosting: 15.1895
## Test MSE for Bagging: 9.6815
## Test MSE for Random Forest: 11.4519
```

Bagging is the most effective in this case with a MSE of 9.6815

## Problem 4

• Include both sketches. You can draw it with R (not easy) or just draw the sketch by hand.

#### Problem 5

```
## Majority vote classification = Red
## Average probability classification = Green
```

#### **Appendix**

```
library(knitr)
# install the tidyverse library (do this once) install.packages('tidyverse')
library(tidyverse)
# set chunk and figure default options
knitr::opts_chunk$set(echo = FALSE, message = FALSE, warning = FALSE, fig.width = 4,
    fig.height = 4, tidy = TRUE)
library(tidyverse) # data manip
library(ISLR) # data
library(GGally) # pairs plots
library(gam) # qam models
library(leaps) # regression subsets
library(tree) # trees
library(randomForest) # random forest
library(gbm) # boosting
library(glmnet) # lasso
library(ISLR)
data(OJ)
set.seed(577)
n \leftarrow nrow(OJ)
tr_index <- sample(seq_len(n), size = 800, replace = F)</pre>
OJtrain <- OJ[tr index, ]
OJtest <- OJ[-tr_index, ]</pre>
# prob 1b
library(tree)
oj_tree <- tree(Purchase ~ ., data = OJtrain)</pre>
summary(oj_tree)
# problem 1c
plot(oj_tree)
text(oj_tree, pretty = 0)
# problem 1d
oj_pred <- predict(oj_tree, newdata = OJtest, type = "class")</pre>
conf_mat <- table(OJtest$Purchase, oj_pred)</pre>
test_error_rate_unpruned <- (conf_mat[1, 2] + conf_mat[2, 1])/sum(conf_mat)</pre>
conf mat
test_error_rate_unpruned
set.seed(577)
cv_oj <- cv.tree(oj_tree, FUN = prune.misclass)</pre>
plot(cv_oj$size, cv_oj$dev, type = "b", xlab = "Tree Size (Number of Terminal Nodes)",
    ylab = "CV Error Rate", main = "CV Error Rate vs. Tree Size")
optimal_size <- cv_oj$size[which.min(cv_oj$dev)]</pre>
```

```
optimal_size
# problem f
pruned_oj <- prune.misclass(oj_tree, best = optimal_size)</pre>
# prob1g
train_pred_unpruned <- predict(oj_tree, newdata = OJtrain, type = "class")</pre>
conf_mat_train_unpruned <- table(OJtrain$Purchase, train_pred_unpruned)</pre>
train_error_unpruned <- (conf_mat_train_unpruned[1, 2] + conf_mat_train_unpruned[2,</pre>
    1])/sum(conf_mat_train_unpruned)
cat("Training Error Rate (Unpruned Tree):", round(train_error_unpruned, 4), "\n")
train_pred_pruned <- predict(pruned_oj, newdata = OJtrain, type = "class")</pre>
conf_mat_train_pruned <- table(OJtrain$Purchase, train_pred_pruned)</pre>
train_error_pruned <- (conf_mat_train_pruned[1, 2] + conf_mat_train_pruned[2, 1])/sum(conf_mat_train_pr
cat("Training Error Rate (Pruned Tree):", round(train_error_pruned, 4), "\n")
# prob1h
test_pred_pruned <- predict(pruned_oj, newdata = OJtest, type = "class")</pre>
conf_mat_test_pruned <- table(OJtest$Purchase, test_pred_pruned)</pre>
test_error_pruned <- (conf_mat_test_pruned[1, 2] + conf_mat_test_pruned[2, 1])/sum(conf_mat_test_pruned
round(test_error_pruned, 4)
test_error_rate_unpruned
# prob 2a
Hitters <- Hitters[complete.cases(Hitters), ]</pre>
Hitters$lsalary <- log(Hitters$Salary)</pre>
Hitters <- Hitters[, !(names(Hitters) %in% "Salary")]</pre>
set.seed(577)
n <- nrow(Hitters)</pre>
tr_index <- sample(seq_len(n), size = 200, replace = F)</pre>
Htrain <- Hitters[tr_index, ]</pre>
Htest <- Hitters[-tr_index, ]</pre>
# prob 2c
lambda_seq \leftarrow seq(0.005, 0.1, length.out = 20)
train mse <- numeric(length(lambda seq))</pre>
test_mse <- numeric(length(lambda_seq))</pre>
for (i in 1:length(lambda_seq)) {
    boost_mod <- gbm(lsalary ~ ., data = Htrain, distribution = "gaussian", n.trees = 1000,
        shrinkage = lambda_seq[i], verbose = FALSE)
    train_pred <- predict(boost_mod, newdata = Htrain, n.trees = 1000)</pre>
    test_pred <- predict(boost_mod, newdata = Htest, n.trees = 1000)</pre>
    train_mse[i] <- mean((Htrain$lsalary - train_pred)^2)</pre>
    test_mse[i] <- mean((Htest$lsalary - test_pred)^2)</pre>
}
# Plot training MSE vs. lambda
df_train <- data.frame(lambda = lambda_seq, MSE = train_mse)</pre>
ggplot(df_train, aes(x = lambda, y = MSE)) + geom_line() + labs(title = "Training MSE vs. Shrinkage",
```

```
x = "Shrinkage", y = "Training MSE")
# prob 2d
df_test <- data.frame(lambda = lambda_seq, MSE = test_mse)</pre>
ggplot(df_test, aes(x = lambda, y = MSE)) + geom_line() + labs(title = "Test MSE vs. Shrinkage",
    x = "Shrinkage", y = "Test MSE")
# Identify and print the lambda value that minimizes the test MSE
optimal_lambda <- lambda_seq[which.min(test_mse)]</pre>
cat("\nOptimal lambda:", optimal_lambda, "\n")
# problem 2e
boost_mod_final <- gbm(lsalary ~ ., data = Htrain, distribution = "gaussian", n.trees = 1000,
    shrinkage = optimal_lambda, verbose = FALSE)
print(summary(boost_mod_final))
# prob 2f
set.seed(577)
bag_mod <- randomForest(lsalary ~ ., data = Htrain, mtry = ncol(Htrain) - 1, ntree = 500)
bag_pred <- predict(bag_mod, newdata = Htest)</pre>
bag_test_mse <- mean((Htest$lsalary - bag_pred)^2)</pre>
cat("Test MSE for Bagging:", round(bag_test_mse, 4), "\n")
# problem 2q
set.seed(577)
rf_mod <- randomForest(lsalary ~ ., data = Htrain, ntree = 500)</pre>
rf_pred <- predict(rf_mod, newdata = Htest)</pre>
rf_test_mse <- mean((Htest$lsalary - rf_pred)^2)</pre>
cat("Test MSE for Random Forest:", round(rf_test_mse, 4), "\n")
# problem 3
set.seed(577)
library(MASS)
n_boston <- nrow(Boston)</pre>
train_index <- sample(seq_len(n_boston), size = round(0.7 * n_boston), replace = FALSE)
BostonTrain <- Boston[train_index, ]</pre>
BostonTest <- Boston[-train_index, ]</pre>
# Linear
lm_mod <- lm(medv ~ ., data = BostonTrain)</pre>
lm_pred <- predict(lm_mod, newdata = BostonTest)</pre>
lm_test_mse <- mean((BostonTest$medv - lm_pred)^2)</pre>
cat("\nTest MSE for Linear Regression:", round(lm_test_mse, 4), "\n")
# Boosting
boost_boston <- gbm(medv ~ ., data = BostonTrain, distribution = "gaussian", n.trees = 1000,
    shrinkage = 0.01, verbose = FALSE)
boost_pred <- predict(boost_boston, newdata = BostonTest, n.trees = 1000)</pre>
boost_test_mse <- mean((BostonTest$medv - boost_pred)^2)</pre>
cat("Test MSE for Boosting:", round(boost_test_mse, 4), "\n")
# Baqqin
bag_boston <- randomForest(medv ~ ., data = BostonTrain, mtry = ncol(BostonTrain) -</pre>
    1, ntree = 500)
bag_pred_boston <- predict(bag_boston, newdata = BostonTest)</pre>
```

```
bag_test_mse_boston <- mean((BostonTest$medv - bag_pred_boston)^2)
cat("Test MSE for Bagging:", round(bag_test_mse_boston, 4), "\n")

# Random Forrest

rf_boston <- randomForest(medv ~ ., data = BostonTrain, ntree = 500)

rf_pred_boston <- predict(rf_boston, newdata = BostonTest)

rf_test_mse_boston <- mean((BostonTest$medv - rf_pred_boston)^2)
cat("Test MSE for Random Forest:", round(rf_test_mse_boston, 4), "\n")

# problem 5

p <- c(0.1, 0.15, 0.2, 0.2, 0.55, 0.6, 0.6, 0.65, 0.7, 0.75)

num_red <- sum(p > 0.5)
majority_vote <- ifelse(num_red > length(p)/2, "Red", "Green")

cat("Majority vote classification =", majority_vote, "\n")

p_avg <- mean(p)
avg_prob_class <- ifelse(p_avg > 0.5, "Red", "Green")

cat("Average probability classification =", avg_prob_class, "\n")
```