

MTH/SL5 - 218

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Office hours: Zoom

Monday: 4:30pm - 5:30pm

Wednesday: 11:10AM - 12:10PM

Everything will stay the same!!

§11.4 Converting One unit to Another.

$$1 \text{ hour} = 60 \text{ min.}$$

$$1 \text{ min} = 60 \text{ sec.}$$

$$1 \text{ kg} = 2.2 \text{ lbs}$$

$$3 \text{ kg} \stackrel{?}{=} 3(2.2 \text{ lbs}) = 6.6 \text{ lbs.}$$

Example

$$1 \text{ gal} = 3.79 \text{ L}$$

$$25 \text{ L} = \underline{\hspace{1cm}} \text{ gal?}$$

$$\frac{25 \text{ L}}{3.79 \text{ L}} = \underline{6.6} \text{ gal}$$

$$1 \text{ meter} = \underline{\hspace{1cm}} \text{ feet?}$$

$$\text{Know: } \begin{cases} 1 \text{ in} = 2.54 \text{ cm} \\ 1 \text{ m} = 100 \text{ cm} \end{cases}$$

$$1 \cancel{\text{ m}} * \frac{100 \cancel{\text{ cm}}}{1 \cancel{\text{ m}}} * \frac{1 \cancel{\text{ in}}}{2.54 \cancel{\text{ cm}}} * \frac{1 \text{ ft}}{12 \cancel{\text{ in}}}$$

$$1 \cdot 100 \cdot \frac{1}{2.54} \cdot \frac{1}{12} = 3.280839 \dots \text{ ft.}$$

This Chain Process is known as

Dimensional Analysis

P518

1. A class needs a 175-inch long piece of rope for a project. How long is the rope in yards?

- Use multiplication or division or both to solve the rope problem. Explain your solution.
- Describe a number of different correct ways to write the answer to the rope problem. Explain briefly why these different ways of writing the answer mean the same thing.

$$1 \text{ Yard} = 3 \text{ ft.}, \quad 1 \text{ ft} = 12 \text{ in.}$$

We have 175 in.

Dimensional Analysis.

$$175 \cancel{\text{in}} * \frac{1 \cancel{\text{ft.}}}{12 \cancel{\text{in}}} * \frac{1 \text{ yd}}{3 \cancel{\text{ft}}}$$

$$\begin{array}{r} 4 \text{ R} 31 \\ 36 \overline{) 175} \\ \underline{-144} \\ 31 \end{array}$$

$$175 \text{ yd} = 4.86 \text{ yds}$$

36

4 yds 31 in
4 yds 2 ft 7 in

1.

2. The children in Mrs. Watson's class made chains of small paper dolls, as pictured in Figure 11.18. A chain of 5 dolls is 1 foot long. How long would the following chains of dolls be? In each case, give your answer in either feet or miles, depending on which answer is easiest to understand.

- a. 100 dolls
- b. 1000 dolls
- c. 10,000 dolls
- d. 100,000 dolls
- e. 1 million dolls
- f. 1 billion dolls



Figure 11.18 A chain of paper dolls.

$$1 \text{ mile} = 5280 \text{ ft}$$

(a) 100 dolls.

$$* \frac{100 \text{ dolls}}{5 \text{ dolls}} = 20 \text{ ft.}$$

$$* 100 \text{ dolls} * \frac{1 \text{ ft}}{5 \text{ dolls}} = \frac{100 \text{ ft}}{5} = 20 \text{ ft}$$

$$\underline{100 \text{ dolls} = 20 \text{ ft}}$$

(b) 1000 dolls.

$$* 1000 \text{ dolls} * \frac{20 \text{ ft}}{100 \text{ dolls}} = \frac{1000}{100} \cdot 20 \text{ ft}$$

$$= 200 \text{ ft}$$

$$1000 \text{ dolls} = 200 \text{ ft}$$

(c) 10,000 dolls = 2000 ft.

$$* (d) 100,000 \text{ dolls} = 20,000 \text{ ft.} \rightarrow \frac{20,000}{5280} = 3.8 \text{ miles}$$

3. Solve the following conversion problems, using the basic fact 1 inch = 2.54 cm in each case:

- A track is 100 meters long. How long is it in feet?
- If the speed limit is 70 miles per hour, what is it in kilometers per hour?
- Some farmland covers 2.4 square kilometers. How many square miles is it?
- Convert the volume of a compost pile, 1 cubic yard, to cubic meters.
- A man is 1.88 meters tall. How tall is he in feet?
- How many miles is a 10-kilometer race?

$$\textcircled{a} \quad 100 \cancel{m} \cdot \frac{100 \cancel{cm}}{1 \cancel{m}} \cdot \frac{1 \cancel{in}}{2.54 \cancel{cm}} \cdot \frac{1 \text{ ft}}{12 \cancel{in}}$$

$$\frac{100 \cdot 100}{2.54 \cdot 12} = \frac{10000}{2.54 \cdot 12} = \underline{\underline{328.08 \text{ ft}}}$$

$$\textcircled{b} \quad 70 \frac{\cancel{mi}}{h} \cdot \frac{5280 \cancel{ft}}{1 \cancel{mi}} \cdot \frac{12 \cancel{in}}{1 \cancel{ft}} \cdot \frac{2.54 \cancel{cm}}{1 \cancel{in}} \cdot \frac{1 \cancel{m}}{100 \cancel{cm}} \cdot \frac{1 \text{ km}}{1000 \cancel{m}}$$

$$\frac{70 \times 5280 \times 12 \times 2.54}{100 \times 1000} \quad \frac{\text{km}}{h}$$

$$= 112.65408 \frac{\text{km}}{h}$$

$$= 113 \frac{\text{km}}{hr}$$

$$\textcircled{c} \quad 2.4 \text{ km}^2 \xrightarrow{\times 100} \text{ mi}^2 \xrightarrow{\div 2.54} \text{ mi}^2$$

$$1 \text{ km} = 1000 \text{ m} = 100,000 \text{ cm} = 3937 \text{ in}$$

$$= 3280 \text{ ft} = 0.621 \text{ miles}$$

$$\frac{1}{2} \text{ km} = 0.621 \text{ miles}$$

$$2.4 \text{ km}^2 \times \left(\frac{0.621 \text{ mi}}{1 \text{ km}} \right)^2$$

$$2.4 \cancel{\text{km}^2} \times \frac{0.39 \cancel{\text{mi}^2}}{1 \cancel{\text{km}^2}} = 2.4 \times 0.39 = \boxed{0.9 \text{ mi}^2}$$

e. A man is 1.88 meters tall. How tall is he in feet?

$$1.88 \cancel{\text{m}} \times \frac{100 \cancel{\text{cm}}}{1 \cancel{\text{m}}} \times \frac{1 \cancel{\text{m}}}{2.54 \cancel{\text{cm}}} \times \frac{1 \text{ ft}}{12 \cancel{\text{in}}}$$

$$\frac{1.88 \times 100}{(2.54 \times 12)} = 6 \text{ ft}$$

↳ approx. 6.17 ft