

§13.3 Volumes of Solid Shapes.

Volume - the amount of space inside a solid shape.

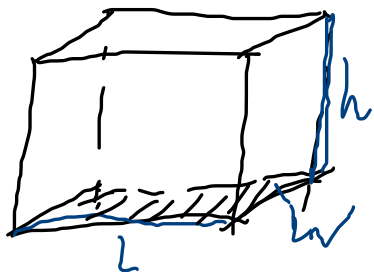
Area: Amt of space in 2-D.



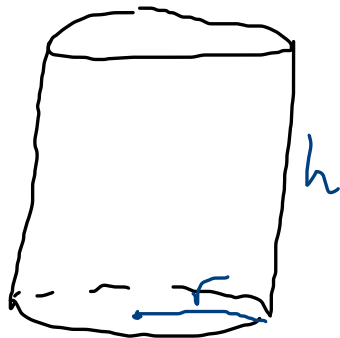
Volume: Amt of space in 3-D

What is the general formula for volume of a Prism and Cylinder?

→ Prism.



→ Cylinder.

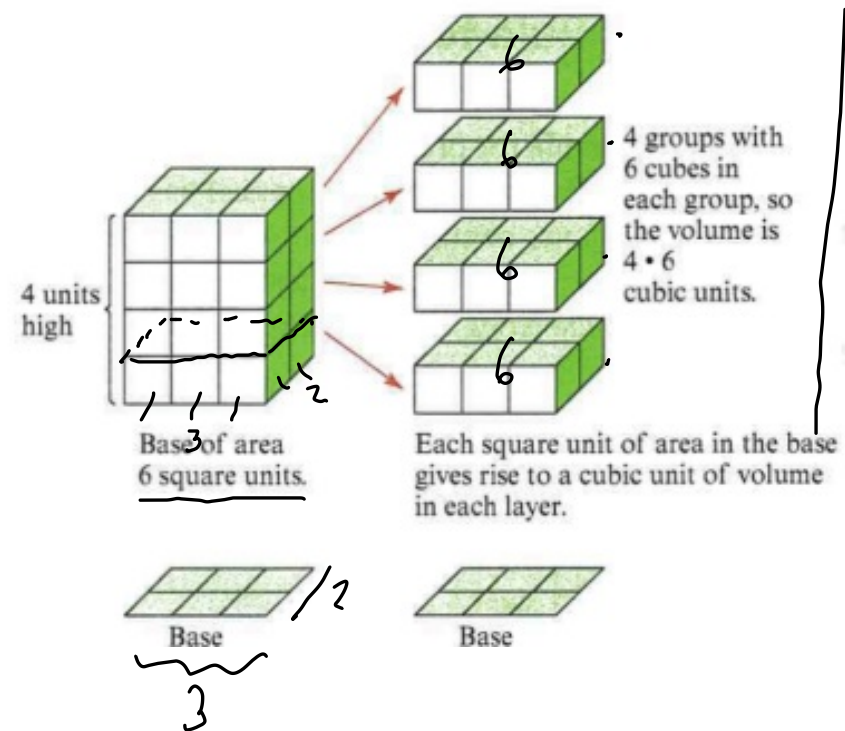


for a Prism $V = L \times W \times h$.

$$V = (\text{Area of base}) \cdot h.$$

$$\text{Cylinder: } V = (\text{Area of base}) \times h = \pi r^2 h.$$

Pg 600, Figure 13.32.



4 layers.
of
the base.

Area of base = 6 units.

Volume: $6 * 4 = \boxed{24 \text{ units}^3}$

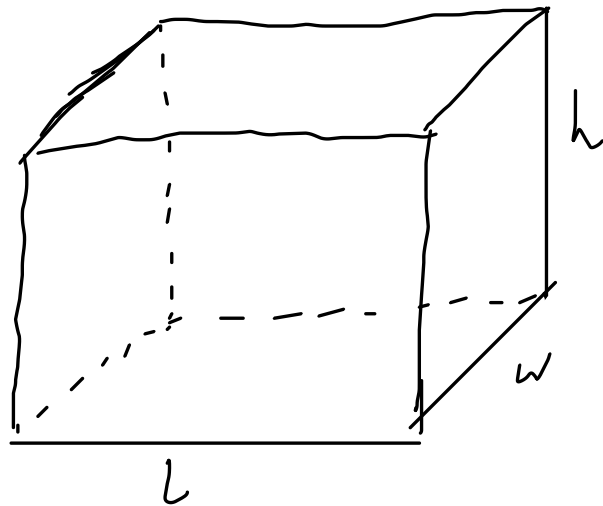
How does Cavalieri's Principle apply to Volume?

For 2-D Shapes.

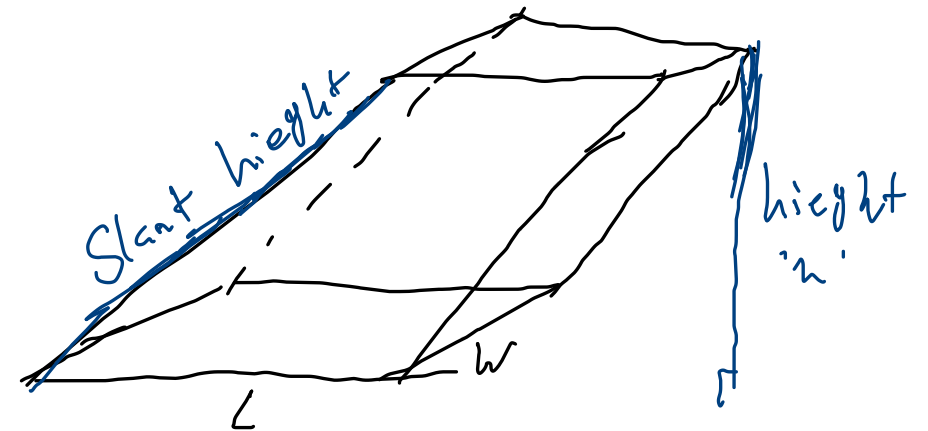
Does NOT Change AREA (and height) but Perimeter does Change.

For 3-D Shapes.

Does NOT Change VOLUME but the Surface Area does Change.



Shear it
Push it right →



Pyramids and Cones.

B: Area of base

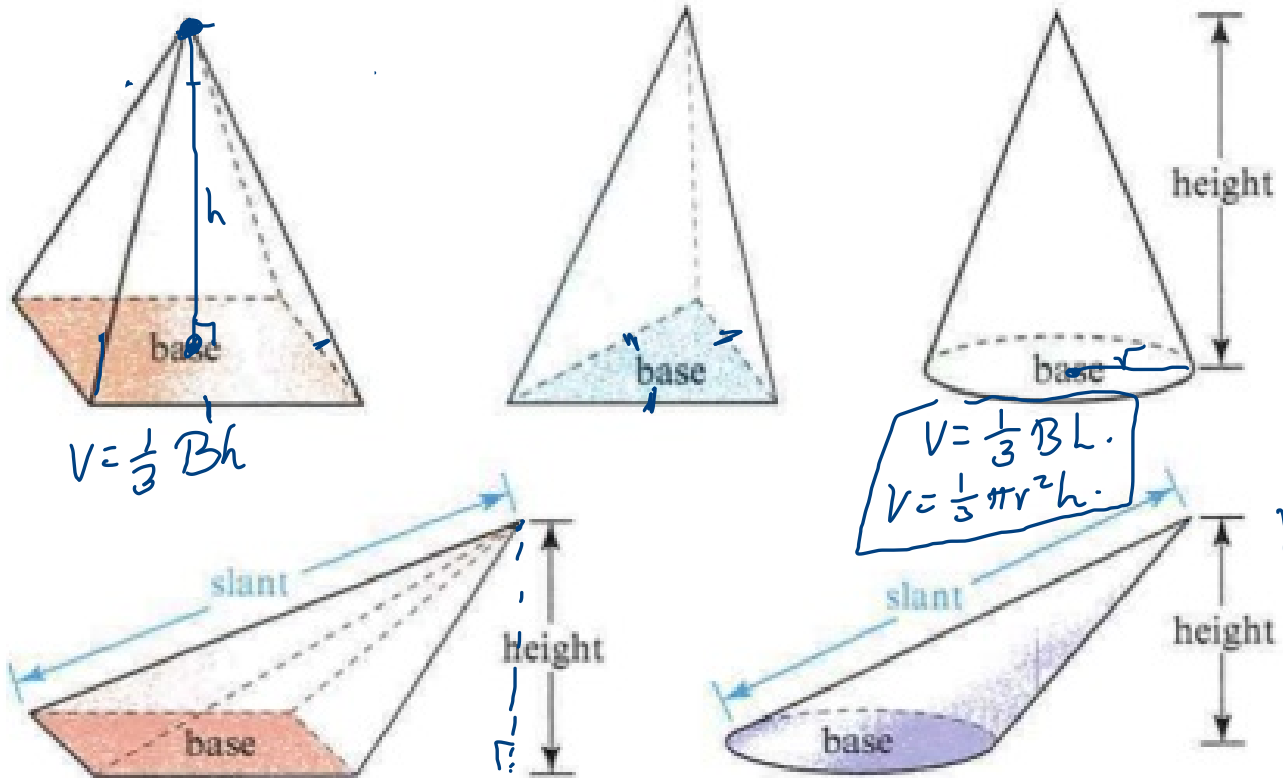


Figure 13.33 The base and height of a pyramid or cone.

Volume of

Pyramid	Cone
$V = \frac{1}{3} B \cdot h$	$V = \frac{1}{3} B \cdot h$ $= \frac{1}{3} \pi r^2 h$

Basically, it takes
up $\frac{1}{3}$ of space
in a Prism.

From video 3:1 ratio for
Volume, Pyramid to Prism.

$$\frac{3}{3} V = \frac{(\text{Area of base}) \cdot h}{3}$$

$$V = \frac{1}{3} (\text{Area of base}) h$$

Same case for cone.

Quick Example : Determine the volume of a cone with radius of 3 cm and height 5 cm.

$$V = \frac{1}{3} \pi r^2 h.$$


$$= \frac{1}{3} \cdot \pi \cdot (3 \text{ cm})^2 (5 \text{ cm})$$

$$= \frac{1}{3} \pi (9 \text{ cm}^2) (5 \text{ cm})$$

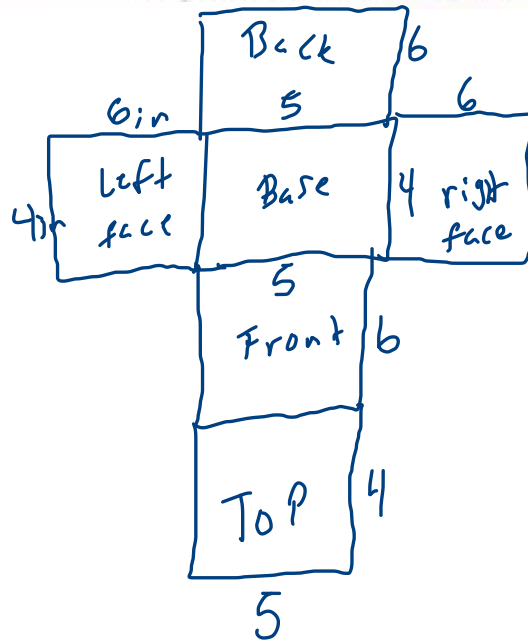
$$= \frac{1}{3} \pi 45 \text{ cm}^3$$

$$= \underline{15\pi \text{ cm}^3} * \checkmark \checkmark$$

$$\approx \underline{47.12 \text{ cm}^3}$$

2.  a. Students are sometimes confused about the difference between the surface area and the volume of a box. Explain the two concepts in a way that could help students learn to distinguish between them.

- b. Determine the surface area and the volume of a closed box that is 5 in. wide, 4 in. deep, and 6 in. tall. Explain in detail why you calculate as you do. 148 in^2 ; 120 in^3 .



Volume

$$V = (5 \times 4) \cdot 6$$

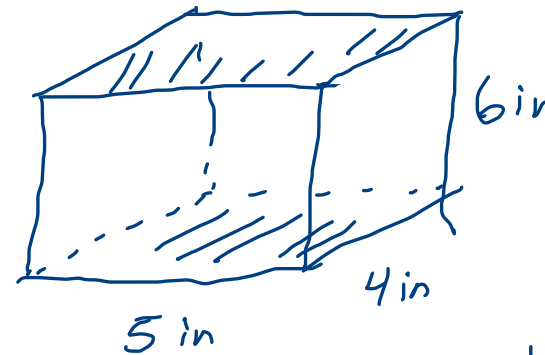
$$V = (20) 6$$

$$V = 120 \text{ in}^3$$

2a) • Surface area measures the area of faces outside the box

• Volume measure amt of space inside the box.

⑥



SA:

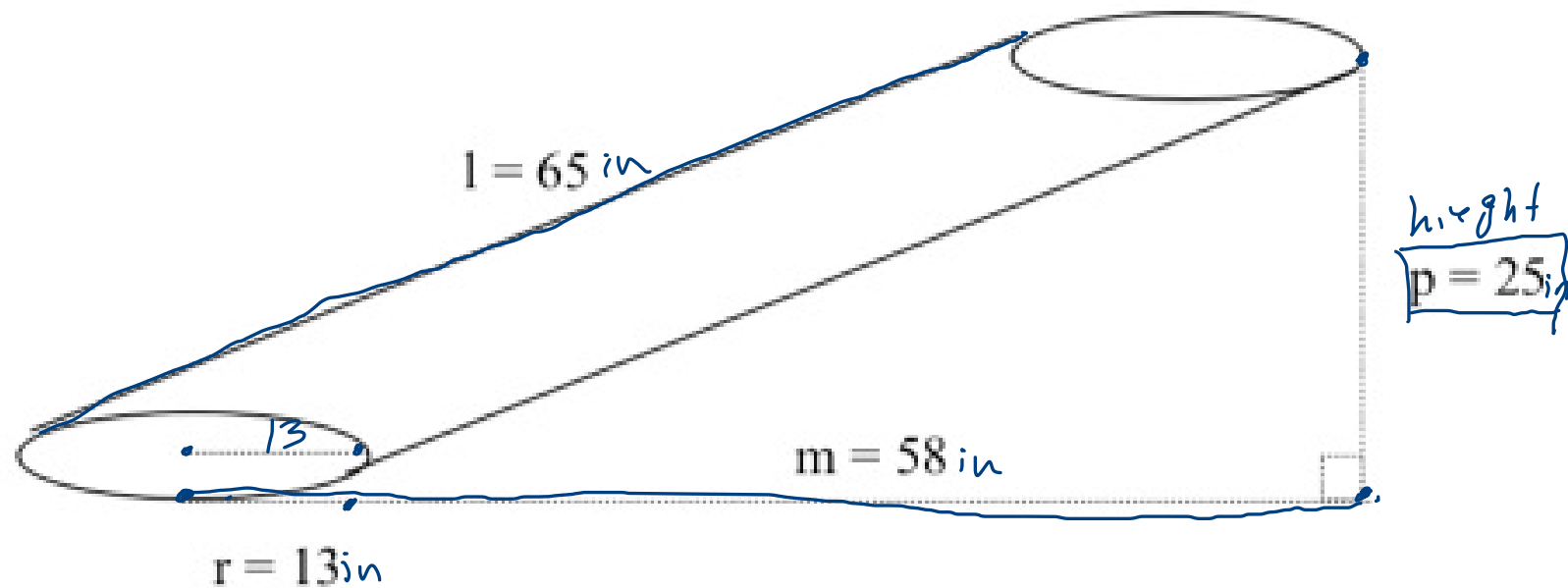
Area TOP + Area Bottom -
+ Area of left + Area of right +
+ Area of Front and back.

↳ $2 \text{ Area top} + 2 \text{ Area left} + 2 \text{ Area front.}$

$$2(5)(4) + 2(4)(6) + 2(5)(6)$$

$$= 148 \text{ in}^2$$

10. a) Find the Volume of the oblique circular cylinder shown below. State the Volume formula. |



$$V = \pi r^2 h.$$

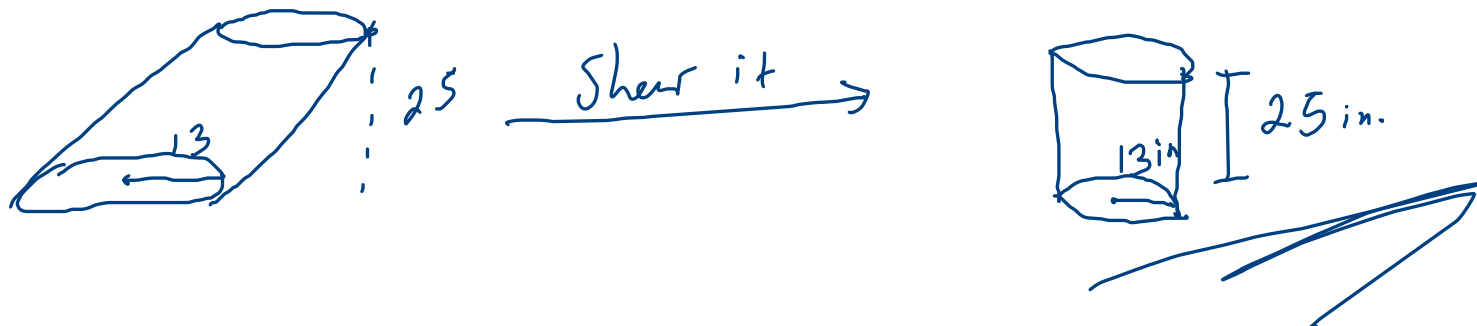
$$V = \pi (13)^2 (25)$$

$$V = \pi (169)(25)$$

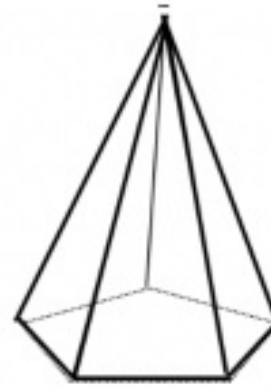
$$V = 4225\pi \text{ in}^3$$

$$V = 13,273.22 \text{ in}^3.$$

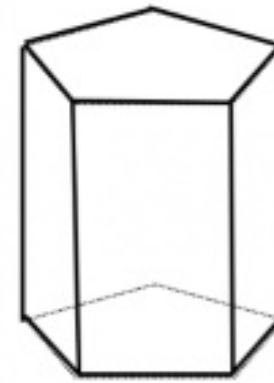
b) Using Cavalieri's Principle, shear the oblique circular cylinder shown above into a right circular cylinder. Draw the sheared cylinder in the space next to it, labeling its radius and height. [4p]



11. The pyramid and the prism as shown are "matching", that is, they share the same base and height. The volume of the pyramid is 270 cm^3 . Find the volume of the prism. Hint: Recall the basic volume relationship between the two shapes. (5p)



$$V = 270 \text{ cm}^3$$



$$V = 3 (270 \text{ cm}^3)$$

$$V = 810 \text{ cm}^3$$

* Pyramid and Prisms have
a 3:1 ratio for their
Volumes.

§13.4 Volume of Submerged objects and weight of floating.

Archimedes Principle

- ① A non Porous object that sinks displaces an amount of water that is equal to the volume of the submerged object.

Example.

A non-porous rock sinks to the bottom of a beaker of water, as a result it displaces 5cm^3 of water. What is the volume of the rock?

Ans: 5cm^3

2nd Principle: A non-porous object that floats displaces an amt of water. is equal to the weight of the floating object. Fact: 1cm^3 of water = 1 gram.

EX) When a turtle jumps into a tank, it floats and displaces 1045cm^3 of water. What is the weight of the turtle in Pounds? ($1\text{cm}^3 = 1\text{g}$, $454\text{g} = 1\text{lb}$)

$$1045\text{cm}^3 = 1045\text{g} \times \frac{1\text{lb}}{454\text{g}} = \frac{1045}{454}\text{lb} = \boxed{2.3\text{lb}}$$