```
# import libraries
import numpy as np
def driver():
# use routines
    f = lambda x: (x-5) ** 9
    a = 4.82
    b = 5.2
   f = lambda x: np.sin(x)
    a = 0.1
#
#
   b = np.pi+0.1
    tol = 1e-4
    print('')
    [astar,ier,count] = bisection(f,a,b,tol)
    print('the approximate root is',astar)
    print('the error message reads:',ier)
    print('f(astar) =', f(astar))
    print('Iterations:', count)
# define routines
def bisection(f,a,b,tol):
#
     Inputs:
#
      f,a,b
                  - function and endpoints of initial interval
       tol - bisection stops when interval length < tol
#
     Returns:
       astar - approximation of root
#
#
       ier – error message
             - ier = 1 => Failed
#
             - ier = 0 == success
      first verify there is a root we can find in the interval
    fa = f(a)
    fb = f(b);
    if (fa*fb>0):
       ier = 1
       astar = a
       return [astar, ier, count]
    verify end points are not a root
    if (fa == 0):
      astar = a
      ier =0
      return [astar, ier, count]
    if (fb == 0):
      astar = b
      ier = 0
      return [astar, ier, count]
```

```
count = 0
    d = 0.5*(a+b)
   while (abs(d-a)> tol):
     fd = f(d)
     if (fd ==0):
       astar = d
        ier = 0
       return [astar, ier, count]
     if (fa*fd<0):
        b = d
     else:
       a = d
       fa = fd
     d = 0.5*(a+b)
     count = count +1
     print('abs(d-a) = ', abs(d-a))
    astar = d
    ier = 0
    return [astar, ier, count]
driver()
Terminal print
the approximate root is 5.000073242187501
the error message reads: 0
f(astar) = 6.065292655789404e-38
Iterations: 11
```