

## 1 HIGHREGIME

### 1.1 Optimisation problem

$$\max_{\pi H_t, yH_t, iH_t} UH_t = -0.5 (\pi iH - \pi iCB + \pi iH_t)^2 + \beta E_t [UH_{t+1}] + \beta (-E_t [UH_{t+1}] + E_t [UL_{t+1}]) \left(1 - pH_{ss} - \tau (-\pi iCB + \pi iH_t)^2\right) - 0.5\kappa\theta^{-1}yH_t^2 \quad (1.1)$$

s.t. :

$$\pi iH_{t-1} = \log \det \pi i_{t-1} + \kappa yH_{t-1} + \beta \pi iH_t \left(pH_{ss} + \tau (-\pi iCB + \pi iH_t)^2\right) + \beta (-\pi iH_t + \pi iL_t) \left(1 - pH_{ss} - \tau (-\pi iCB + \pi iH_t)^2\right) \quad \left(\lambda_t^{\text{HIGHREGIME}^1}\right) \quad (1.2)$$

$$yH_{t-1} = yH_t - \sigma (iH_{t-1} - \pi iH_t) + (-yH_t + yL_t) \left(1 - pH_{ss} - \tau (-\pi iCB + \pi iH_t)^2\right) + \sigma (-\pi iH_t + \pi iL_t) \left(1 - pH_{ss} - \tau (-\pi iCB + \pi iH_t)^2\right) \quad \left(\lambda_t^{\text{HIGHREGIME}^2}\right) \quad (1.3)$$

### 1.2 First order conditions

$$\beta - \lambda_t^{\text{HIGHREGIME}^{\text{UH}}} - \beta \left(1 - pH_{ss} - \tau (-\pi iCB + \pi iH_{t-1})^2\right) = 0 \quad (UH_t) \quad (1.4)$$

$$- \pi iH + \pi iCB - \pi iH_t + \lambda_t^{\text{HIGHREGIME}^1} \left( \beta \left(pH_{ss} + \tau (-\pi iCB + \pi iH_t)^2\right) - \beta \left(1 - pH_{ss} - \tau (-\pi iCB + \pi iH_t)^2\right) + 2\beta\tau\pi iH_t (-\pi iCB + \pi iH_t) - 2\beta\tau (-\pi iCB + \pi iH_t) (-\pi iH_t + \pi iL_t) \right) + \lambda_t^{\text{HIGHREGIME}^2} \left( -\pi iH_t + \pi iL_t \right) = 0 \quad (yH_t) \quad (1.5)$$

$$\lambda_t^{\text{HIGHREGIME}^2} \left(pH_{ss} + \tau (-\pi iCB + \pi iH_t)^2\right) - \kappa\theta^{-1}yH_t + E_t \left[\lambda_{t+1}^{\text{HIGHREGIME}^{\text{UH}}} \left(-\lambda_{t+1}^{\text{HIGHREGIME}^2} + \kappa\lambda_{t+1}^{\text{HIGHREGIME}^1}\right)\right] = 0 \quad (yH_t) \quad (1.6)$$

$$-\sigma E_t \left[\lambda_{t+1}^{\text{HIGHREGIME}^{\text{UH}}} \lambda_{t+1}^{\text{HIGHREGIME}^2}\right] = 0 \quad (iH_t) \quad (1.7)$$

## 2 LOWREGIME

### 2.1 Optimisation problem

$$\max_{\pi iL_t, yL_t, iL_t} UL_t = -0.5 (-\pi iCB + \pi iL_t + \pi iL_t)^2 + \beta E_t [UL_{t+1}] + \beta (E_t [UH_{t+1}] - E_t [UL_{t+1}]) \left(1 - pL_{ss} - \tau (-\pi iCB + \pi iL_t)^2\right) - 0.5\kappa\theta^{-1}yL_t^2 \quad (2.1)$$

s.t. :

$$\pi iL_{t-1} = \log \det \pi i_{t-1} + \kappa yL_{t-1} + \beta \pi iL_t \left(pL_{ss} + \tau (-\pi iCB + \pi iL_t)^2\right) + \beta (\pi iH_t - \pi iL_t) \left(1 - pL_{ss} - \tau (-\pi iCB + \pi iL_t)^2\right) \quad \left(\lambda_t^{\text{LOWREGIME}^1}\right) \quad (2.2)$$

$$yL_{t-1} = yL_t - \sigma (iL_{t-1} - \pi iL_t) + (yH_t - yL_t) \left(1 - pL_{ss} - \tau (-\pi iCB + \pi iL_t)^2\right) + \sigma (\pi iH_t - \pi iL_t) \left(1 - pL_{ss} - \tau (-\pi iCB + \pi iL_t)^2\right) \quad \left(\lambda_t^{\text{LOWREGIME}^2}\right) \quad (2.3)$$

## 2.2 First order conditions

$$\beta - \lambda_t^{\text{LOWREGIME}^{\text{UL}}} - \beta \left( 1 - pL_{ss} - \tau (-\pi CB + \pi L_{t-1})^2 \right) = 0 \quad (UL_t) \quad (2.4)$$

$$\pi CB - \pi L - \pi L_t + \lambda_t^{\text{LOWREGIME}^1} \left( \beta \left( pL_{ss} + \tau (-\pi CB + \pi L_t)^2 \right) - \beta \left( 1 - pL_{ss} - \tau (-\pi CB + \pi L_t)^2 \right) + 2\beta\tau\pi L_t (-\pi CB + \pi L_t) - 2\beta\tau (-\pi CB + \pi L_t) (\pi H_t - \pi L_t) \right) + \lambda_t^{\text{LOWREGIME}^2} \left( \sigma \right. \quad (2.5)$$

$$\lambda_t^{\text{LOWREGIME}^2} \left( pL_{ss} + \tau (-\pi CB + \pi L_t)^2 \right) - \kappa\theta^{-1}yL_t + E_t \left[ \lambda_{t+1}^{\text{LOWREGIME}^{\text{UL}}} \left( -\lambda_{t+1}^{\text{LOWREGIME}^2} + \kappa\lambda_{t+1}^{\text{LOWREGIME}^1} \right) \right] = 0 \quad (yL_t) \quad (2.6)$$

$$-\sigma E_t \left[ \lambda_{t+1}^{\text{LOWREGIME}^{\text{UL}}} \lambda_{t+1}^{\text{LOWREGIME}^2} \right] = 0 \quad (iL_t) \quad (2.7)$$

## 3 EXOG

### 3.1 Identities

$$\epsilon \pi i_t = e^{\epsilon_t^\pi + \phi \log \epsilon \pi i_{t-1}} \quad (3.1)$$

## 4 Equilibrium relationships (after reduction)

$$-\epsilon \pi i_t + e^{\epsilon_t^\pi + \phi \log \epsilon \pi i_{t-1}} = 0 \quad (4.1)$$

$$\lambda_t^{\text{HIGHREGIME}^2} \left( pH_{ss} + \tau (-\pi CB + \pi H_t)^2 \right) + \left( \beta - \beta \left( 1 - pH_{ss} - \tau (-\pi CB + \pi H_t)^2 \right) \right) E_t \left[ -\lambda_{t+1}^{\text{HIGHREGIME}^2} + \kappa\lambda_{t+1}^{\text{HIGHREGIME}^1} \right] - \kappa\theta^{-1}yH_t = 0 \quad (4.2)$$

$$\lambda_t^{\text{LOWREGIME}^2} \left( pL_{ss} + \tau (-\pi CB + \pi L_t)^2 \right) + \left( \beta - \beta \left( 1 - pL_{ss} - \tau (-\pi CB + \pi L_t)^2 \right) \right) E_t \left[ -\lambda_{t+1}^{\text{LOWREGIME}^2} + \kappa\lambda_{t+1}^{\text{LOWREGIME}^1} \right] - \kappa\theta^{-1}yL_t = 0 \quad (4.3)$$

$$-\pi H_{t-1} + \log \epsilon \pi i_{t-1} + \kappa yH_{t-1} + \beta \pi H_t \left( pH_{ss} + \tau (-\pi CB + \pi H_t)^2 \right) + \beta (-\pi H_t + \pi L_t) \left( 1 - pH_{ss} - \tau (-\pi CB + \pi H_t)^2 \right) = 0 \quad (4.4)$$

$$-\pi L_{t-1} + \log \epsilon \pi i_{t-1} + \kappa yL_{t-1} + \beta \pi L_t \left( pL_{ss} + \tau (-\pi CB + \pi L_t)^2 \right) + \beta (\pi H_t - \pi L_t) \left( 1 - pL_{ss} - \tau (-\pi CB + \pi L_t)^2 \right) = 0 \quad (4.5)$$

$$-yH_{t-1} + yH_t - \sigma (iH_{t-1} - \pi H_t) + (-yH_t + yL_t) \left( 1 - pH_{ss} - \tau (-\pi CB + \pi H_t)^2 \right) + \sigma (-\pi H_t + \pi L_t) \left( 1 - pH_{ss} - \tau (-\pi CB + \pi H_t)^2 \right) = 0 \quad (4.6)$$

$$-yL_{t-1} + yL_t - \sigma (iL_{t-1} - \pi L_t) + (yH_t - yL_t) \left( 1 - pL_{ss} - \tau (-\pi CB + \pi L_t)^2 \right) + \sigma (\pi H_t - \pi L_t) \left( 1 - pL_{ss} - \tau (-\pi CB + \pi L_t)^2 \right) = 0 \quad (4.7)$$

$$UH_t + 0.5 (\pi H_t - \pi CB + \pi H_t)^2 - \beta E_t [UH_{t+1}] - \beta (-E_t [UH_{t+1}] + E_t [UL_{t+1}]) \left( 1 - pH_{ss} - \tau (-\pi CB + \pi H_t)^2 \right) + 0.5\kappa\theta^{-1}yH_t^2 = 0 \quad (4.8)$$

$$UL_t + 0.5 (-\pi CB + \pi L_t + \pi L_t)^2 - \beta E_t [UL_{t+1}] - \beta (E_t [UH_{t+1}] - E_t [UL_{t+1}]) \left( 1 - pL_{ss} - \tau (-\pi CB + \pi L_t)^2 \right) + 0.5\kappa\theta^{-1}yL_t^2 = 0 \quad (4.9)$$

$$-\pi H_t + \pi CB - \pi H_t + \lambda_t^{\text{HIGHREGIME}^1} \left( \beta \left( pH_{ss} + \tau (-\pi CB + \pi H_t)^2 \right) - \beta \left( 1 - pH_{ss} - \tau (-\pi CB + \pi H_t)^2 \right) + 2\beta\tau\pi H_t (-\pi CB + \pi H_t) - 2\beta\tau (-\pi CB + \pi H_t) (-\pi H_t + \pi L_t) \right) + \lambda_t^{\text{HIGHREGIME}^2} \left( \sigma \right) \quad (4.10)$$

$$p\dot{t}CB - p\dot{t}L - p\dot{L}_t + \lambda_t^{\text{LOWREGIME}^1} \left( \beta \left( pL_{ss} + \tau (-p\dot{t}CB + p\dot{L}_t)^2 \right) - \beta \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_t)^2 \right) + 2\beta\tau p\dot{L}_t (-p\dot{t}CB + p\dot{L}_t) - 2\beta\tau (-p\dot{t}CB + p\dot{L}_t) (p\dot{H}_t - p\dot{L}_t) \right) + \lambda_t^{\text{LOWREGIME}^2} \left( \sigma \right. \\ \left. - \sigma \left( \beta - \beta \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_t)^2 \right) \right) \right) E_t \left[ \lambda_{t+1}^{\text{HIGHREGIME}^2} \right] = 0 \quad (4.11)$$

$$- \sigma \left( \beta - \beta \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_t)^2 \right) \right) E_t \left[ \lambda_{t+1}^{\text{HIGHREGIME}^2} \right] = 0 \quad (4.12)$$

$$- \sigma \left( \beta - \beta \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_t)^2 \right) \right) E_t \left[ \lambda_{t+1}^{\text{LOWREGIME}^2} \right] = 0 \quad (4.13)$$

## 5 Steady state relationships (after reduction)

$$-d\alpha p\dot{i}_{ss} + e^{\phi \log d\alpha p\dot{i}_{ss}} = 0 \quad (5.1)$$

$$\lambda_{ss}^{\text{HIGHREGIME}^2} \left( pH_{ss} + \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) + \left( \beta - \beta \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) \right) \left( -\lambda_{ss}^{\text{HIGHREGIME}^2} + \kappa \lambda_{ss}^{\text{HIGHREGIME}^1} \right) - \kappa \theta^{-1} yH_{ss} = 0 \quad (5.2)$$

$$\lambda_{ss}^{\text{LOWREGIME}^2} \left( pL_{ss} + \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) + \left( \beta - \beta \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) \right) \left( -\lambda_{ss}^{\text{LOWREGIME}^2} + \kappa \lambda_{ss}^{\text{LOWREGIME}^1} \right) - \kappa \theta^{-1} yL_{ss} = 0 \quad (5.3)$$

$$-p\dot{H}_{ss} + \log d\alpha p\dot{i}_{ss} + \kappa yH_{ss} + \beta p\dot{H}_{ss} \left( pH_{ss} + \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) + \beta (-p\dot{H}_{ss} + p\dot{L}_{ss}) \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) = 0 \quad (5.4)$$

$$-p\dot{L}_{ss} + \log d\alpha p\dot{i}_{ss} + \kappa yL_{ss} + \beta p\dot{L}_{ss} \left( pL_{ss} + \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) + \beta (p\dot{H}_{ss} - p\dot{L}_{ss}) \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) = 0 \quad (5.5)$$

$$(-yH_{ss} + yL_{ss}) \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) - \sigma (iH_{ss} - p\dot{H}_{ss}) + \sigma (-p\dot{H}_{ss} + p\dot{L}_{ss}) \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) = 0 \quad (5.6)$$

$$(yH_{ss} - yL_{ss}) \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) - \sigma (iL_{ss} - p\dot{L}_{ss}) + \sigma (p\dot{H}_{ss} - p\dot{L}_{ss}) \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) = 0 \quad (5.7)$$

$$UH_{ss} + 0.5 (p\dot{t}H - p\dot{t}CB + p\dot{H}_{ss})^2 - \beta UH_{ss} - \beta (-UH_{ss} + UL_{ss}) \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) + 0.5 \kappa \theta^{-1} yH_{ss}^2 = 0 \quad (5.8)$$

$$UL_{ss} + 0.5 (-p\dot{t}CB + p\dot{t}L + p\dot{L}_{ss})^2 - \beta UL_{ss} - \beta (UH_{ss} - UL_{ss}) \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) + 0.5 \kappa \theta^{-1} yL_{ss}^2 = 0 \quad (5.9)$$

$$-p\dot{t}H + p\dot{t}CB - p\dot{H}_{ss} - \lambda_{ss}^{\text{HIGHREGIME}^1} \left( \beta - \beta \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) \right) + \lambda_{ss}^{\text{HIGHREGIME}^1} \left( \beta \left( pH_{ss} + \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) - \beta \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) + 2\beta\tau p\dot{H}_{ss} (-p\dot{t}CB + p\dot{H}_{ss}) \right) \\ \quad (5.10)$$

$$p\dot{t}CB - p\dot{t}L - p\dot{L}_{ss} - \lambda_{ss}^{\text{LOWREGIME}^1} \left( \beta - \beta \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) \right) + \lambda_{ss}^{\text{LOWREGIME}^1} \left( \beta \left( pL_{ss} + \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) - \beta \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) + 2\beta\tau p\dot{L}_{ss} (-p\dot{t}CB + p\dot{L}_{ss}) \right) \\ \quad (5.11)$$

$$- \sigma \lambda_{ss}^{\text{HIGHREGIME}^2} \left( \beta - \beta \left( 1 - pH_{ss} - \tau (-p\dot{t}CB + p\dot{H}_{ss})^2 \right) \right) = 0 \quad (5.12)$$

$$- \sigma \lambda_{ss}^{\text{LOWREGIME}^2} \left( \beta - \beta \left( 1 - pL_{ss} - \tau (-p\dot{t}CB + p\dot{L}_{ss})^2 \right) \right) = 0 \quad (5.13)$$

## 6 Parameter settings

$$\beta = 0.99 \tag{6.1}$$

$$\kappa = 0.2465 \tag{6.2}$$

$$\phi = 0.95 \tag{6.3}$$

$$pitH = 0 \tag{6.4}$$

$$pitCB = 0 \tag{6.5}$$

$$pitL = 2 \tag{6.6}$$

$$pHss = 0.99 \tag{6.7}$$

$$pLss = 0.99 \tag{6.8}$$

$$\sigma = 1 \tag{6.9}$$

$$\tau = 0.01 \tag{6.10}$$

$$\theta = 6 \tag{6.11}$$

## 7 Steady-state values

	Steady-state value
$\epsilon \pi$	1
$iH$	-0.0149
$iL$	-1.5222
$\lambda^{\text{HIGHREGIME}^1}$	0.0103
$\lambda^{\text{HIGHREGIME}^2}$	0
$\lambda^{\text{LOWREGIME}^1}$	0.0152
$\lambda^{\text{LOWREGIME}^2}$	0
$\pi H$	-2e-04
$\pi L$	-1.5036
$yH$	0.0604
$yL$	0.0913
$UH$	-16.4635
$UL$	-33.0857

## 8 The solution of the 1st order perturbation

Matrix  $P$

$$\begin{matrix}
 & \epsilon \pi_{t-1} & iH_{t-1} & iL_{t-1} & \pi H_{t-1} & \pi L_{t-1} & yH_{t-1} & yL_{t-1} \\
 \begin{matrix} \epsilon \pi_t \\ iH_t \\ iL_t \\ \pi H_t \\ \pi L_t \\ yH_t \\ yL_t \end{matrix} & \begin{pmatrix} 0.95 & 0 & 0 & 0 & 0 & 0 & 0 \\ -848.7704 & -1.911 & 2.0657 & 0.0579 & -5.8446 & -13.4357 & 0.2113 \\ -7.7526 & -3e-04 & -1.8409 & 0 & 4.8756 & -0.0019 & -0.1833 \\ -6739.446 & 0 & 0 & 1.0306 & -91.6514 & -101.197 & 1.3713 \\ -0.6098 & 0 & 0 & 0 & 0.9053 & -1e-04 & -0.0135 \\ 16.9118 & 0.2489 & -0.2515 & -0.0026 & 0.24 & 1.264 & -0.0187 \\ 10.4862 & 0.002 & 16.4684 & 0 & -15.5666 & 0.0103 & 1.2203 \end{pmatrix}
 \end{matrix}$$

Matrix  $Q$

$$\begin{matrix}
 & \epsilon^\pi \\
 \begin{matrix} \epsilon \pi \\ iH \\ iL \\ \pi H \\ \pi L \\ yH \\ yL \end{matrix} & \begin{pmatrix} 1 \\ -495.6617 \\ -4.6907 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}
 \end{matrix}$$

Matrix  $R$

$$\begin{matrix}
 & \epsilon \pi_{t-1} & iH_{t-1} & iL_{t-1} & \pi H_{t-1} & \pi L_{t-1} & yH_{t-1} & yL_{t-1} \\
 \begin{matrix} \lambda_t^{\text{HIGHREGIME}^1} \\ \lambda_t^{\text{HIGHREGIME}^2} \\ \lambda_t^{\text{LOWREGIME}^1} \\ \lambda_t^{\text{LOWREGIME}^2} \\ UH_t \\ UL_t \end{matrix} & \begin{pmatrix} -462.4401 & -0.5903 & 1.1272 & 0.0389 & -5.9375 & -6.2186 & 0.1564 \\ 0.8172 & 0.0017 & -0.0027 & -1e-04 & 0.0104 & 0.0129 & -3e-04 \\ -350.1771 & -0.0115 & -44.8291 & 7e-04 & 301.0756 & -0.1149 & -7.1927 \\ 0.9313 & 0 & 0.194 & 0 & -0.6719 & 4e-04 & 0.0217 \\ 0.0112 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0.0083 & 0 & 0 & 0 & -7e-04 & 0 & 0 \end{pmatrix}
 \end{matrix}$$

## Matrix $S$

$$\begin{matrix} & \epsilon^\pi \\ \lambda^{\text{HIGHREGIME}^1} & \left( \begin{matrix} -220.5089 \\ 0.4387 \\ -152.9985 \\ 0.497 \\ 0.0111 \\ 0.0083 \end{matrix} \right) \\ \lambda^{\text{HIGHREGIME}^2} & \\ \lambda^{\text{LOWREGIME}^1} & \\ \lambda^{\text{LOWREGIME}^2} & \\ UH & \\ UL & \end{matrix}$$

## 9 Model statistics

### 9.1 Basic statistics

	Steady-state value	Std. dev.	Variance	Loglin
$etapi$	1	0.1303	0.017	Y
$iH$	-0.0149	49.8555	2485.5672	Y
$iL$	-1.5222	0.4746	0.2253	Y
$\lambda^{\text{HIGHREGIME}^1}$	0.0103	24.2739	589.2208	Y
$\lambda^{\text{HIGHREGIME}^2}$	0	0.0423	0.0018	N
$\lambda^{\text{LOWREGIME}^1}$	0.0152	17.4504	304.515	Y
$\lambda^{\text{LOWREGIME}^2}$	0	0.0479	0.0023	N
$pH$	-2e-04	666.7814	444597.4198	Y
$pL$	-1.5036	0.0585	0.0034	Y
$yH$	0.0604	11.3389	128.5701	Y
$yL$	0.0913	7.201	51.8548	Y
$UH$	-16.4635	0.0015	0	Y
$UL$	-33.0857	0.0011	0	Y

### 9.2 Correlation matrix

	$etapi$	$iH$	$iL$	$\lambda^{\text{HIGHREGIME}^1}$	$\lambda^{\text{HIGHREGIME}^2}$	$\lambda^{\text{LOWREGIME}^1}$	$\lambda^{\text{LOWREGIME}^2}$	$pH$	$pL$
$etapi$	1	-0.32	-0.312	-0.861	0.436	-0.836	0.436	-0.52	-0.51
$iH$		1	0.999	0.583	-0.985	0.556	-0.985	-0.294	-0.29
$iL$			1	0.563	-0.979	0.533	-0.979	-0.324	-0.33
$\lambda^{\text{HIGHREGIME}^1}$				1	-0.71	0.997	-0.71	0.565	0.557
$\lambda^{\text{HIGHREGIME}^2}$					1	-0.689	1	0.125	0.131
$\lambda^{\text{LOWREGIME}^1}$						1	-0.689	0.606	0.602
$\lambda^{\text{LOWREGIME}^2}$							1	0.125	0.131
$pH$								1	0.997
$pL$									1
$yH$									
$yL$									
$UH$									
$UL$									

### 9.3 Cross correlations with the reference variable ( $iH$ )

	$\sigma[\cdot]$ rel. to $\sigma[iH]$	$iH_{t-5}$	$iH_{t-4}$	$iH_{t-3}$	$iH_{t-2}$	$iH_{t-1}$	$iH_t$	$iH_{t+1}$	$iH_{t+2}$	$iH_{t+3}$	$iH_{t+4}$
$\epsilon\alpha\pi_t$	0.003	0.108	0.145	0.195	0.275	0.43	-0.32	-0.269	-0.222	-0.178	-0.139
$iH_t$	1	-0.032	-0.041	-0.058	-0.095	-0.186	1	-0.186	-0.095	-0.058	-0.041
$iL_t$	0.01	-0.032	-0.041	-0.057	-0.094	-0.183	0.999	-0.224	-0.09	-0.05	-0.035
$\lambda_t^{\text{HIGHREGIME}^1}$	0.487	-0.09	-0.116	-0.155	-0.224	-0.369	0.583	0.449	0.18	0.069	0.02
$\lambda_t^{\text{HIGHREGIME}^2}$	0.001	0.044	0.056	0.078	0.122	0.228	-0.985	0.047	0.046	0.044	0.041
$\lambda_t^{\text{LOWREGIME}^1}$	0.35	-0.087	-0.112	-0.15	-0.217	-0.358	0.556	0.517	0.156	0.044	0.004
$\lambda_t^{\text{LOWREGIME}^2}$	0.001	0.044	0.056	0.078	0.122	0.228	-0.985	0.047	0.046	0.044	0.041
$\pi H_t$	13.374	-0.053	-0.066	-0.083	-0.112	-0.167	-0.294	0.835	0.283	0.072	-0.009
$\pi L_t$	0.001	-0.052	-0.066	-0.084	-0.113	-0.17	-0.299	0.871	0.227	0.039	-0.016
$yH_t$	0.227	-0.077	-0.102	-0.135	-0.181	-0.26	-0.418	0.542	0.299	0.186	0.124
$yL_t$	0.144	-0.077	-0.102	-0.135	-0.182	-0.261	-0.421	0.556	0.279	0.174	0.122
$UH_t$	0	0.108	0.144	0.194	0.275	0.43	-0.313	-0.315	-0.197	-0.168	-0.135
$UL_t$	0	0.108	0.144	0.194	0.274	0.428	-0.301	-0.299	-0.226	-0.176	-0.135

### 9.4 Autocorrelations

	Lag 1	Lag 2	Lag 3	Lag 4	Lag 5
$\epsilon\alpha\pi$	0.713	0.471	0.271	0.11	-0.016
$iH$	-0.186	-0.095	-0.058	-0.041	-0.032
$iL$	-0.221	-0.089	-0.049	-0.035	-0.028
$\lambda^{\text{HIGHREGIME}^1}$	0.525	0.133	-0.031	-0.102	-0.132
$\lambda^{\text{HIGHREGIME}^2}$	-0.074	-0.071	-0.066	-0.06	-0.054
$\lambda^{\text{LOWREGIME}^1}$	0.534	0.08	-0.064	-0.114	-0.131
$\lambda^{\text{LOWREGIME}^2}$	-0.074	-0.071	-0.066	-0.06	-0.054
$\pi H$	0.28	0.008	-0.089	-0.119	-0.121
$\pi L$	0.204	-0.024	-0.086	-0.1	-0.098
$yH$	0.535	0.281	0.123	0.016	-0.059
$yL$	0.517	0.281	0.133	0.029	-0.048
$UH$	0.713	0	0	0	0
$UL$	0	0	0	0	0

## 10 Impulse response functions

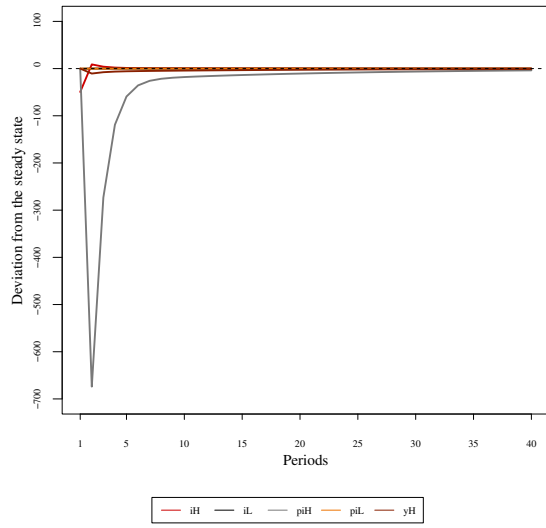


Figure 1: Impulse responses ( $iH, iL, \pi H, \pi L, yH$ ) to  $\epsilon^\pi$  shock

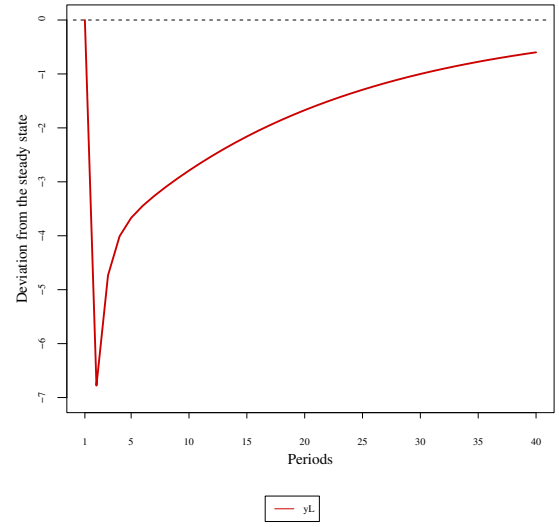


Figure 2: Impulse response ( $yL$ ) to  $\epsilon^\pi$  shock