# ACM ICPC TEAM REFERENCE 2010 WORLD FINALS

# Team Anuncie Aqui Universidade Federal de Sergipe

#### 1. Configuration files and scripts

1.1. **.emacs.** Hash: c4c6b75b731e46e642e98db153594c25

```
(global-font-lock-mode t)
(setq transient-mark-mode t)
(require 'font-lock)
(require_'paren)
(global-set-key [f5] 'cxx-compile)
(set-input-mode_nil_nil_1)
(fset_'yes-or-no-p 'y-or-n-p)
(require_'cc-mode)
(defun cxx-compile()
```

1.2. **Hash generator.** Hash: 0d22aecd779fc370b30a2c628aff517c

#!/bin/sh

sed ':a;N;\$!ba;s/[\_\n\t]//g' | md5sum | cut -d'\_' -f1

1.3. **Solution template.** Hash: 6d62780682c9ea96d2e5daec770800bf

```
#include <iostream>
#include <cstdio>
#include <algorithm>
#include <vector>
#include <set>
#include <queue>
#include <map>
```

```
#include <utility>
#include <cstring>
#include <cstdlib>
#include <cmath>

using namespace std;
```

```
typedef double TYPE;
const TYPE EPS = 1e-9;
inline int sgn(TYPE a) { return a > EPS ? 1 : (a < -EPS ? -1 : 0); }
inline int cmp(TYPE a, TYPE b) { return sgn(a - b); }</pre>
```

#### 2. Graph algorithms

#### 2.1. **Tarjan's SCC algorithm.** Hash: f98d9589db68c8f1e8274cf53eb7f3bf

```
int lowest[MAXV], num[MAXV], visited[MAXV], comp[MAXV];
int prev_edge[MAXE], last_edge[MAXV], adj[MAXE], nedges;
int cur_num, cur_comp;
stack<int> visiting;
int t_init() {
   memset(last_edge, -1, sizeof last_edge);
   nedges = 0;
void t_edge(int v, int w) {
  prev_edge[nedges] = last_edge[v];
   adj[nedges] = w;
   last_edge[v] = nedges++;
int tarjan_dfs(int v) {
  lowest[v] = num[v] = cur_num++;
  visiting.push(v);
   visited[v] = 1;
   for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
      int w = adj[i];
      if(visited[w] == 0) lowest[v] = min(lowest[v], tarjan_dfs(w));
      else if(visited[w] == 1) lowest[v] = min(lowest[v], num[w]);
```

# 2.2. **Dinic's algorithm.** Hash: 4dd537effe7e233681c099912397839a

```
int last_edge[MAXV], cur_edge[MAXV], dist[MAXV];
int prev_edge[MAXE], cap[MAXE], flow[MAXE], adj[MAXE];
int nedges;
void d_init() {
```

```
if(lowest[v] == num[v]) {
      int last = -1;
      while(last != v) {
         comp[last = visiting.top()] = cur_comp;
        visited[last] = 2;
         visiting.pop();
      cur_comp++;
   return lowest[v];
void tarjan_scc(int num_v = MAXV) {
  visiting = stack<int>();
  memset(visited, 0, sizeof visited);
  cur_num = cur_comp = 0;
   for (int i = 0; i < num_v; i++)</pre>
      if(!visited[i])
         tarjan_dfs(i);
  memset(last_edge, -1, sizeof last_edge);
```

void d\_edge(int v, int w, int capacity, bool r = false) {

```
prev_edge[nedges] = last_edge[v];
   cap[nedges] = capacity;
   adj[nedges] = w;
   flow[nedges] = 0;
  last_edge[v] = nedges++;
   if(!r) d_edge(w, v, 0, true);
bool d auxflow(int source, int sink) {
   queue<int> q;
   q.push(source);
   memset(dist, -1, sizeof dist);
   dist[source] = 0;
   memcpy(cur_edge, last_edge, sizeof last_edge);
   while(!q.empty()) {
      int v = q.front(); q.pop();
      for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
         if(cap[i] - flow[i] == 0) continue;
         if(dist[adj[i]] == -1) {
            dist[adj[i]] = dist[v] + 1;
            q.push(adj[i]);
            if(adj[i] == sink) return true;
   return false;
```

# 2.3. Busacker-Gowen's algorithm. Hash: 6933692fe046f78da13b05166c7e6d23

```
int dist[MAXV], last_edge[MAXV], d_visited[MAXV], bg_prev[MAXV], pot[MAXV],
    capres[MAXV];
int prev_edge[MAXE], adj[MAXE], cap[MAXE], cost[MAXE], flow[MAXE];

int nedges;
priority_queue<pair<int, int> > d_q;

inline void bg_edge(int v, int w, int capacity, int cst, bool r = false) {
    prev_edge[nedges] = last_edge[v];
    adj[nedges] = w;
```

```
inline int rev(int i) { return i ^ 1; }
int d_augmenting(int v, int sink, int c) {
  if(v == sink) return c;
   for(int& i = cur_edge[v]; i != -1; i = prev_edge[i]) {
     if(cap[i] - flow[i] == 0 || dist[adj[i]] != dist[v] + 1)
        continue;
      int val;
     if(val = d_augmenting(adj[i], sink, min(c, cap[i] - flow[i]))) {
        flow[i] += val;
        flow[rev(i)] -= val;
         return val;
   return 0;
int dinic(int source, int sink) {
   int ret = 0;
  while(d_auxflow(source, sink)) {
     int flow:
     while(flow = d_augmenting(source, sink, 0x3f3f3f3f))
        ret += flow:
   return ret;
```

```
cap[nedges] = capacity;
flow[nedges] = 0;
cost[nedges] = cst;
last_edge[v] = nedges++;

if(!r) bg_edge(w, v, 0, -cost, true);
}
inline int rev(int i) { return i ^ 1; }
inline int from(int i) { return adj[rev(i)]; }
```

```
inline void bg_init() {
   nedges = 0;
  memset(last_edge, -1, sizeof last_edge);
  memset(pot, 0, sizeof pot);
void bg_dijkstra(int s, int num_nodes = MAXV) {
  memset(dist, 0x3f, sizeof dist);
  memset (d visited, 0, sizeof d visited);
   d_q.push(make_pair(dist[s] = 0, s));
   capres[s] = 0x3f3f3f3f;
   while(!d_q.empty()) {
      int v = d_q.top().second; d_q.pop();
      if(d_visited[v]) continue; d_visited[v] = true;
      for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
         if(cap[i] - flow[i] == 0) continue;
         int w = adj[i], new_dist = dist[v] + cost[i] + pot[v] - pot[w];
         if(new dist < dist[w]) {</pre>
            d_q.push(make_pair(-(dist[w] = new_dist), w));
            bq_prev[w] = rev(i);
            capres[w] = min(capres[v], cap[i] - flow[i]);
```

#### 2.4. **Gabow's algorithm.** Hash: 31f8b67cd2b16187c6733f42801ee2be

```
int prev_edge[MAXE], v[MAXE], w[MAXE], last_edge[MAXV];
int type[MAXV], label[MAXV], first[MAXV], mate[MAXV], nedges;
bool g_flag[MAXV], g_souter[MAXV];

void g_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
}

void g_edge(int a, int b) {
    prev_edge[nedges] = last_edge[a];
    v[nedges] = a;
    w[nedges] = b;
    last_edge[a] = nedges++;

    prev_edge[nedges] = last_edge[b];
```

```
pair<int, int> busacker_gowen(int src, int sink, int num_nodes = MAXV) {
   int retFlow = 0, retCost = 0;
  bg_dijkstra(src, num_nodes);
   while(dist[sink] < 0x3f3f3f3f) {</pre>
      int cur = sink;
      while(cur != src) {
         flow[bg_prev[cur]] -= capres[sink];
        flow[rev(bg_prev[cur])] += capres[sink];
         retCost += cost[rev(bg_prev[cur])] * capres[sink];
        cur = adj[bg_prev[cur]];
      retFlow += capres[sink];
      for(int i = 0; i < MAXV; i++)</pre>
         pot[i] = min(pot[i] + dist[i], 0x3f3f3f3f);
      bg_dijkstra(src, num_nodes);
   return make_pair(retFlow, retCost);
  v[nedges] = b;
   w[nedges] = a;
   last_edge[b] = nedges++;
void g_label(int v, int join, int edge, queue<int>& outer) {
  if(v == join) return;
  if(label[v] == -1) outer.push(v);
  label[v] = edge;
  type[v] = 1;
   first[v] = join;
  q_label(first[label[mate[v]]], join, edge, outer);
```

```
void q_augment(int _v, int _w) {
   int t = mate[_v];
  mate[\_v] = \_w;
   if(mate[t] != _v) return;
   if(label[_v] == -1) return;
   if(type[_v] == 0) {
      mate[t] = label[_v];
      g_augment(label[_v], t);
   else if(type[_v] == 1) {
      g_augment(v[label[_v]], w[label[_v]]);
      g_augment(w[label[_v]], v[label[_v]]);
int gabow(int n) {
   memset(mate, -1, sizeof mate);
  memset(first, -1, sizeof first);
   int u = 0, ret = 0;
   for (int z = 0; z < n; z++) {
      if (mate[z] != -1) continue;
      memset (label, -1, sizeof label);
      memset (type, -1, sizeof type);
      memset(g_souter, 0, sizeof g_souter);
      label[z] = -1; type[z] = 0;
      queue<int> outer;
      outer.push(z);
      bool done = false;
      while(!outer.empty()) {
         int x = outer.front(); outer.pop();
         if(g_souter[x]) continue;
         g_souter[x] = true;
         for(int i = last_edge[x]; i != -1; i = prev_edge[i]) {
            if (mate[w[i]] == -1 && w[i] != z) {
               mate[w[i]] = x;
```

```
g_augment(x, w[i]);
            ret++;
            done = true;
            break;
         if(type[w[i]] == -1) {
            int v = mate[w[i]];
            if(type[v] == -1) {
               type[v] = 0;
               label[v] = x;
               outer.push(v);
               first[v] = w[i];
            continue;
         int r = first[x], s = first[w[i]];
         if(r == s) continue;
         memset(g_flag, 0, sizeof g_flag);
         q_flaq[r] = q_flaq[s] = true;
         while(true) {
            if(s != -1) swap(r, s);
            r = first[label[mate[r]]];
            if(g_flag[r]) break; g_flag[r] = true;
         g_label(first[x], r, i, outer);
         g_label(first[w[i]], r, i, outer);
         for(int c = 0; c < n; c++)
           if(type[c] != -1 && first[c] != -1 && type[first[c]] != -1)
               first[c] = r;
      if(done) break;
return ret;
```

#### 3.1. **Fractions.** Hash: 379fd408c3007c650c022fd4adfeabbd

```
struct frac {
  long long num, den;

  frac() : num(0), den(1) { };
  frac(long long num, long long den) { set_val(num, den); }
  frac(long long num) : num(num), den(1) { };

  void set_val(long long _num, long long _den) {
    num = _num/__gcd(_num, _den);
    den = _den/__gcd(_num, _den);
    if(den < 0) { num *= -1; den *= -1; }
}

  void operator*=(frac f) { set_val(num * f.num, den * f.den); }
  void operator+=(frac f) { set_val(num * f.den + f.num * den, den * f.den); }
  void operator-=(frac f) { set_val(num * f.den - f.num * den, den * f.den); }
  void operator/=(frac f) { set_val(num * f.den, den * f.num); }
};

bool operator<(frac a, frac b) {</pre>
```

3.2. Chinese remainder theorem. Hash: 06b5ebd5c44c204a4b11bbb76d09023d

```
struct t {
   long long a, b; int g;
   t(long long a, long long b, int g) : a(a), b(b), g(g) { }
   t swap() { return t(b, a, g); }
};

t egcd(int p, int q) {
   if(q == 0) return t(1, 0, p);

   t t2 = egcd(q, p % q);
```

3.3. Longest increasing subsequence. Hash: 0f80b5d3af188d8bf4d1cbe45a76b46d

```
vector<int> lis(vector<int>& seq) {
  int smallest_end[seq.size()+1], prev[seq.size()];
  smallest_end[1] = seq[0];

int sz = 1;
```

```
if((a.den < 0) ^ (b.den < 0)) return a.num * b.den > b.num * a.den;
return a.num * b.den < b.num * a.den;
}

std::ostream& operator<<(std::ostream& o, const frac f) {
    o << f.num << "/" << f.den;
    return o;
}

bool operator==(frac a, frac b) { return a.num * b.den == b.num * a.den; }
bool operator!=(frac a, frac b) { return !(a == b); }
bool operator<=(frac a, frac b) { return (a == b) || (a < b); }
bool operator>=(frac a, frac b) { return !(a <= b); }
bool operator>(frac a, frac b) { return !(a <= b); }
frac operator/(frac a, frac b) { frac ret = a; ret /= b; return ret; }
frac operator+(frac a, frac b) { frac ret = a; ret *= b; return ret; }
frac operator-(frac a, frac b) { frac ret = a; ret += b; return ret; }
frac operator-(frac a, frac b) { frac ret = a; ret -= b; return ret; }
frac operator-(frac f) { return 0 - f; }</pre>
```

```
t2.a -= t2.b * (p/q);
  return t2.swap();
}

int crt(int a, int p, int b, int q) {
  t t2 = egcd(p, q); t2.a %= p*q; t2.b %= p*q;
  assert(t2.g == 1);
  int ret = ((b * t2.a)%(p*q) * p + (a * t2.b)%(p*q) * q) % (p*q);
  return ret >= 0 ? ret : ret + p*q;
}
```

```
for (int i = 1; i < seq.size(); i++) {
  int lo = 0, hi = sz;
  while(lo < hi) {
    int mid = (lo + hi + 1)/2;
    if(seq[smallest_end[mid]] <= seq[i])</pre>
```

```
lo = mid;
else
    hi = mid - 1;
}

prev[i] = smallest_end[lo];
if(lo == sz)
    smallest_end[++sz] = i;
else if(seq[i] < seq[smallest_end[lo+1]])
    smallest_end[lo+1] = i;</pre>
```

vector<int> ret;
for(int cur = smallest\_end[sz]; sz > 0; cur = prev[cur], sz--)
 ret.push\_back(seq[cur]);
reverse(ret.begin(), ret.end());

return ret;
}

3.4. Simplex (Warsaw University). Hash: c687094970cf1953fd6f87a01adc6a95

```
const double EPS = 1e-9;
typedef long double T;
typedef vector<T> VT;
vector<VT> A;
VT b,c,res;
VI kt, N;
int m;
inline void pivot(int k, int 1, int e) {
    int x=kt[1]; T p=A[1][e];
     REP(i,k) A[1][i]/=p; b[1]/=p; N[e]=0;
     \label{eq:repair} \texttt{REP}\,(\texttt{i},\texttt{m}) \ \ \textbf{if} \ \ (\texttt{i}\,!\,=\!1) \ \ \texttt{b}\,[\texttt{i}\,]\,-\!\!=\!\!\texttt{A}\,[\texttt{i}\,]\,[\texttt{e}\,]\,\star\!\!>\!\!\texttt{b}\,[\texttt{1}\,]\,,\\ \texttt{A}\,[\texttt{i}\,]\,[\texttt{x}\,]\,=\!\!\texttt{A}\,[\texttt{i}\,]\,[\texttt{e}\,]\,\star\!\!-\!\!\texttt{A}\,[\texttt{1}\,]\,[\texttt{x}\,]\,;
    REP(j,k) if (N[j]) {
         c[j]-=c[e]*A[l][j];
         REP(i,m) if (i!=1) A[i][j]-=A[i][e]*A[1][j];
     kt[1]=e; N[x]=1; c[x]=c[e]*-A[1][x];
VT doit(int k) {
     VT res; T best;
     while (1) {
         int e=-1,1=-1; REP(i,k) if (N[i] && c[i]>EPS) {e=i; break;}
         if (e==-1) break;
         REP(i,m) if (A[i][e]>EPS && (l==-1 || best>b[i]/A[i][e]))
              best=b[ l=i ]/A[i][e];
```

if (l==-1) /\*ilimitado\*/ return VT(); pivot(k,l,e); res.resize(k,0); REP(i,m) res[kt[i]]=b[i]; return res; VT simplex(vector<VT> &AA, VT &bb, VT &cc) { int n=AA[0].size(),k; m=AA.size(); k=n+m+1; kt.resize(m); b=bb; c=cc; c.resize(n+m);  $A=AA; REP(i,m) \{ A[i].resize(k); A[i][n+i]=1; A[i][k-1]=-1; kt[i]=n+i; \}$ N=VI(k,1); REP(i,m) N[kt[i]]=0; int pos=min\_element(ALL(b))-b.begin(); if (b[pos]<-EPS) {</pre> c=VT(k,0); c[k-1]=-1; pivot(k,pos,k-1); res=doit(k); if (res[k-1]>EPS) /\*impossivel\*/ return VT(); REP(i,m) **if** (kt[i] == k-1) REP(j, k-1) if  $(N[j] \&\& (A[i][j] < -EPS || EPS < A[i][j])) {$ pivot(k,i,j); break; c=cc; c.resize(k,0); REP(i,m) REP(j,k) **if** (N[j]) c[j]-=c[kt[i]]\*A[i][j]; res=doit(k-1); if (!res.empty()) res.resize(n); return res;

3.5. **Romberg's method.** Hash: a85facba1eac60c8909b04b552bd2222

```
long double romberg(int a, int b, double(*func)(double)) {
   long double approx[2][50];
```

long double \*cur=approx[1], \*prev=approx[0];

```
prev[0] = 1/2.0 * (b-a) * (func(a) + func(b));
for(int it = 1; it < 25; it++, swap(cur, prev)) {
   if(it > 1 && cmp(prev[it-1], prev[it-2]) == 0)
      return prev[it-1];

cur[0] = 1/2.0 * prev[0];
   long double div = (b-a)/pow(2, it);
   for(long double sample = a + div; sample < b; sample += 2 * div)</pre>
```

3.6. Floyd's cycle detection algorithm. Hash: 4aaa3277ea9011cae6d9b1358521f02c

```
pair<int, int> floyd(int x0) {
  int t = f(x0), h = f(f(x0)), start = 0, length = 1;
  while(t != h)
      t = f(t), h = f(f(h));

h = t; t = x0;
  while(t != h)
      t = f(t), h = f(h), start++;
```

3.7. **Pollard's rho algorithm.** Hash: ad4ee1d4afc564b2c55f90d6269994c4

```
long long pollard_r, pollard_n;
inline long long f(long long val) { return (val*val + pollard_r) % pollard_n; }
inline long long myabs(long long a) { return a >= 0 ? a : -a; }

long long pollard(long long n) {
    srand(unsigned(time(0)));
    pollard_n = n;

    long long d = 1;
    do {
```

3.8. Miller-Rabin's algorithm. Hash: 3a5ca9acc192107c3eb9940088ad16c7

```
int fastpow(int base, int d, int n) {
  int ret = 1;
  for(long long pow = base; d > 0; d >>= 1, pow = (pow * pow) % n)
    if(d & 1)
       ret = (ret * pow) % n;
  return ret;
```

```
h = f(t);
while(t != h)
h = f(h), length++;
return make_pair(start, length);
}
```

```
d = 1;
pollard_r = rand() % n;

long long x = 2, y = 2;
while(d == 1)
    x = f(x), y = f(f(y)), d = __gcd(myabs(x-y), n);
} while(d == n);

return d;
}
```

```
bool miller_rabin(int n, int base) {
   if(n <= 1) return false;
   if(n % 2 == 0) return n == 2;</pre>
```

```
int s = 0, d = n - 1;
while(d % 2 == 0) d /= 2, s++;

int base_d = fastpow(base, d, n);
if(base_d == 1) return true;
int base_2r = base_d;

for(int i = 0; i < s; i++) {
    if(base_2r == 1) return false;
    if(base_2r == n - 1) return true;</pre>
```

3.9. Polynomials (PUC-Rio). Hash: d69d1ad494e487327d2338e69eccfa2f

```
typedef complex<double> cdouble;
int cmp(cdouble x, cdouble y = 0) {
  return cmp(abs(x), abs(y));
const int TAM = 200;
struct poly {
  cdouble poly[TAM]; int n;
  poly(int n = 0): n(n) { memset(p, 0, sizeof(p)); }
  cdouble& operator [](int i) { return p[i]; }
  poly operator ~() {
   poly r(n-1);
    for (int i = 1; i <= n; i++)</pre>
    r[i-1] = p[i] * cdouble(i);
    return r;
  pair<poly, cdouble> ruffini(cdouble z) {
    if (n == 0) return make_pair(poly(), 0);
    poly r(n-1);
    for (int i = n; i > 0; i--) r[i-1] = r[i] * z + p[i];
    return make_pair(r, r[0] * z + p[0]);
  cdouble operator ()(cdouble z) { return ruffini(z).second; }
  cdouble find_one_root(cdouble x) {
   poly p0 = *this, p1 = ~p0, p2 = ~p1;
    int m = 1000;
```

```
base_2r = (long long)base_2r * base_2r % n;
}

return false;
}

int isprime(int n) {
   return miller_rabin(n, 2) && miller_rabin(n, 7) && miller_rabin(n, 61);
}
```

```
while (m--) {
     cdouble y0 = p0(x);
     if (cmp(y0) == 0) break;
     cdouble G = p1(x) / y0;
     cdouble H = G * G - p2(x) - y0;
     cdouble R = sqrt(cdouble(n-1) * (H * cdouble(n) - G * G));
     cdouble D1 = G + R, D2 = G - R;
     cdouble a = cdouble(n) / (cmp(D1, D2) > 0 ? D1 : D2);
     x -= a;
     if (cmp(a) == 0) break;
   return x;
  vector<cdouble> roots() {
   poly q = *this;
   vector<cdouble> r;
    while (q.n > 1) {
     cdouble z(rand() / double(RAND_MAX), rand() / double(RAND_MAX));
     z = q.find_one_root(z); z = find_one_root(z);
     q = q.ruffini(z).first;
     r.push_back(z);
    return r;
};
```

4. Geometry

#### 4.1. **Point class.** Hash: 66e85d5b140956c47aa31754eab18864

```
struct pt {
   TYPE x, y;
   pt(TYPE x = 0, TYPE y = 0) : x(x), y(y) { }
   bool operator== (pt p) { return cmp(x, p.x) == 0 \&\& cmp(y, p.y) == 0; }
   bool operator<(pt p) const {</pre>
      return cmp(x, p.x) ? cmp(x, p.x) < 0 : cmp(y, p.y) < 0;
   bool operator<=(pt p) { return *this < p || *this == p; }</pre>
   TYPE operator||(pt p) { return x*p.x + y*p.y; }
   TYPE operator%(pt p) { return x*p.y - y*p.x; }
   pt operator () { return pt(x, -y); }
   pt operator+(pt p) { return pt(x + p.x, y + p.y); }
   pt operator-(pt p) { return pt(x - p.x, y - p.y); }
   pt operator*(pt p) { return pt(x*p.x - y*p.y, x*p.y + y*p.x); }
   pt operator/(TYPE t) { return pt(x/t, y/t); }
   pt operator/(pt p) { return (*this * ~p)/(p||p); }
};
const pt I = pt(0,1);
```

# 4.2. Intersection primitives. Hash: ab780978106a5c062b8f7a129ebc9196

```
bool in_rect(pt a, pt b, pt c) {
   return sgn(c.x - min(a.x, b.x)) >= 0 && sgn(max(a.x, b.x) - c.x) >= 0 &&
        sgn(c.y - min(a.y, b.y)) >= 0 && sgn(max(a.y, b.y) - c.y) >= 0;
}
bool ps_isects(pt a, pt b, pt c) { return ccw(a,b,c) == 0 && in_rect(a,b,c); }

bool ss_isects(pt a, pt b, pt c, pt d) {
   if (ccw(a,b,c)*ccw(a,b,d) == -1 && ccw(c,d,a)*ccw(c,d,b) == -1) return true;
   return ps_isects(a, b, c) || ps_isects(a, b, d) ||
        ps_isects(c, d, a) || ps_isects(c, d, b);
}
```

# 4.3. **Polygon primitives.** Hash: fba20bb1645bf37ab6c9b309d3850a7d

```
double p_area(vector<pt>& pol) {
  double ret = 0;
  for(int i = 0; i < pol.size(); i++)
    ret += pol[i] % pol[g_mod(i+1, pol.size())];
  return ret/2;</pre>
```

```
struct circle {
  pt c; TYPE r;
  circle(pt c, TYPE r) : c(c), r(r) { }
TYPE norm(pt a) { return a||a; }
TYPE abs(pt a) { return sgrt(a||a); }
TYPE dist(pt a, pt b) { return abs(a - b); }
TYPE area(pt a, pt b, pt c) { return (a-c)%(b-c); }
int ccw(pt a, pt b, pt c) { return sgn(area(a, b, c)); }
pt unit(pt a) { return a/abs(a); }
double arg(pt a) { return atan2(a.y, a.x); }
pt f_polar(TYPE mod, double ang) { return pt (mod * cos(ang), mod * sin(ang)); }
inline int q_mod(int i, int n) { if(i == n) return 0; return i; }
ostream& operator << (ostream& o, pt p) {
  return o << "(" << p.x << "," << p.v << ")";
pt parametric_isect(pt p, pt v, pt q, pt w) {
   double t = ((q-p)%w)/(v%w);
   return p + v*t;
pt ss_isect(pt p, pt q, pt r, pt s) {
  pt isect = parametric_isect(p, q-p, r, s-r);
  if(ps_isects(p, q, isect) && ps_isects(r, s, isect)) return isect;
   return pt (1/0.0, 1/0.0);
int point_polygon(pt p, vector<pt>& pol) {
  int n = pol.size(), count = 0;
```

```
for(int i = 0; i < n; i++) {
   int i1 = g_mod(i+1, n);
   if (ps_isects(pol[i], pol[i1], p)) return -1;
   else if(((sgn(pol[i].y - p.y) == 1) != (sgn(pol[i1].y - p.y) == 1)) &&</pre>
```

4.4. Miscellaneous primitives. Hash: be051245293a9db9c991d414c598e854

```
bool point_circle(pt p, circle c) {
   return cmp(abs(p - c.c), c.r) <= 0;
}

double ps_distance(pt p, pt a, pt b) {
   p = p - a; b = b - a;
   double coef = min(max((b||p)/(b||b), TYPE(0)), TYPE(1));
   return abs(p - b*coef);
}</pre>
```

4.5. Smallest enclosing circle. Hash: 4e41d94c106dee349b45ca542ff0a532

```
circle enclosing_circle(vector<pt>& pts) {
    srand(unsigned(time(0)));
    random_shuffle(pts.begin(), pts.end());

    circle c(pt(), -1);
    for(int i = 0; i < pts.size(); i++) {
        if(point_circle(pts[i], c)) continue;
        c = circle(pts[i], 0);
        for(int j = 0; j < i; j++) {
            if(point_circle(pts[j], c)) continue;
        }
        c = circle(pts[i], 0);
        continue;
        contin
```

4.6. Convex hull. Hash: a7f921d07f1b9b8a0053a0833329ddcf

```
pt pivot;
bool hull_comp(pt a, pt b) {
   int turn = ccw(a, b, pivot);
   return turn == 1 || (turn == 0 && cmp(norm(a), norm(b)) < 0);
}
vector<pt> hull(vector<pt> pts) {
   if(pts.size() <= 1) return pts;
   vector<pt> ret;
```

```
ccw(pol[i], p, pol[i1]) == sgn(pol[i].y - pol[i1].y)) count++;
  return count % 2;
pt circumcenter(pt a, pt b, pt c) {
  return parametric_isect((b+a)/2, (b-a)*I, (c+a)/2, (c-a)*I);
bool compy (pt a, pt b) {
   return cmp(a.y, b.y) ? cmp(a.y, b.y) < 0 : cmp(a.x, b.x) < 0;
bool compx(pt a, pt b) { return a < b; }</pre>
         c = circle((pts[i] + pts[j])/2, abs(pts[i] - pts[j])/2);
         for (int k = 0; k < j; k++) {
            if(point_circle(pts[k], c)) continue;
            pt center = circumcenter(pts[i], pts[j], pts[k]);
            c = circle(center, abs(center - pts[i])/2);
   return c;
   int mini = 0;
   for(int i = 1; i < pts.size(); i++)</pre>
     if(pts[i] < pts[mini])</pre>
         mini = i;
  pivot = pts[mini];
   swap(pts[0], pts[mini]);
   sort(pts.begin() + 1, pts.end(), hull_comp);
```

```
ret.push_back(pts[0]);
ret.push_back(pts[1]);
int sz = 2;

for(int i = 2; i < pts.size(); i++) {
    while(sz >= 2 && ccw(ret[sz-2], ret[sz-1], pts[i]) <= 0)</pre>
```

# 4.7. Closest pair of points. Hash: 3296fbf8040f9e70030bedeb852d21ac

```
pair<pt, pt> closest_points_rec(vector<pt>& px, vector<pt>& py) {
   pair<pt, pt> ret;
   double d;
   if(px.size() <= 3) {
      double best = 1e10;
      for(int i = 0; i < px.size(); i++)</pre>
         for(int j = i + 1; j < px.size(); j++)</pre>
            if(dist(px[i], px[j]) < best) {</pre>
                ret = make_pair(px[i], px[j]);
               best = dist(px[i], px[j]);
      return ret;
   pt split = px[(px.size() - 1)/2];
   vector<pt> qx, qy, rx, ry;
   for(int i = 0; i < px.size(); i++)</pre>
      if(px[i] <= split) qx.push_back(px[i]);</pre>
      else rx.push_back(px[i]);
   for(int i = 0; i < py.size(); i++)</pre>
      if(py[i] <= split) qy.push_back(py[i]);</pre>
      else ry.push_back(py[i]);
   ret = closest_points_rec(qx, qy);
   pair<pt, pt> rans = closest_points_rec(rx, ry);
   double delta = dist(ret.first, ret.second);
   if((d = dist(rans.first, rans.second)) < delta) {</pre>
```

```
ret.pop_back(), sz--;
      ret.push_back(pts[i]), sz++;
   return ret;
      delta = d;
      ret = rans;
   vector<pt> s;
   for(int i = 0; i < py.size(); i++)</pre>
      if (cmp (abs (py[i].x - split.x), delta) <= 0)</pre>
         s.push_back(py[i]);
   for(int i = 0; i < s.size(); i++)</pre>
      for(int j = 1; j <= 15 && i + j < s.size(); j++)</pre>
         if((d = dist(s[i], s[i+j])) < delta) {</pre>
            delta = d:
            ret = make_pair(s[i], s[i+j]);
   return ret;
pair<pt, pt> closest_points(vector<pt> pts) {
   if(pts.size() == 1) return make_pair(pt(-1e9, -1e9), pt(1e9, 1e9));
   sort(pts.begin(), pts.end());
   for(int i = 0; i + 1 < pts.size(); i++)</pre>
      if(pts[i] == pts[i+1])
         return make_pair(pts[i], pts[i+1]);
   vector<pt> py = pts;
   sort(py.begin(), py.end(), compy);
   return closest_points_rec(pts, py);
```

#### 4.8. **Kd-tree.** Hash: a6e0d07a83dde3bc241f10b0f75abdc0

```
int tree[4*MAXSZ];
TYPE split[4*MAXSZ];
vector<pt> pts;
void kd_recurse(int root, int left, int right, bool x) {
   if(left == right) {
      tree[root] = left;
      return;
   int mid = (right+left)/2;
   nth_element(pts.begin() + left, pts.begin() + mid,
            pts.begin() + right + 1, x ? compx : compy);
   split[root] = x ? pts[mid].x : pts[mid].y;
   kd_recurse(2*root+1, left, mid, !x);
   kd_recurse(2*root+2, mid+1, right, !x);
void kd build() {
   memset (tree, -1, sizeof tree);
   kd_recurse(0, 0, pts.size() - 1, true);
int kd_query(int root, int a, int b, int c, int d, bool x) {
  if(tree[root] != -1)
      return a <= pts[tree[root]].x && pts[tree[root]].x <= b &&</pre>
           c <= pts[tree[root]].y && pts[tree[root]].y <= d;</pre>
```

# 4.9. Range tree. Hash: 06e46c5eab58c9fb1332ed9998c017c1

```
vector<pt> pts, tree[MAXSZ];
vector<TYPE> xs;
vector<int> lnk[MAXSZ][2];

int rt_recurse(int root, int left, int right) {
   if(left == right) {
      vector<pt>::iterator it;
      it = lower_bound(pts.begin(), pts.end(), pt(xs[left], -le9));
      for(; it != pts.end() && it->x == xs[left]; it++)
            tree[root].push_back(*it);
```

```
int ret = 0, 1, r;
  if(x) 1 = a, r = b;
   else 1 = c, r = d;
  if(1 \le split[root]) ret += kd_query(2*root + 1, a, b, c, d, !x);
  if(split[root] <= r) ret += kd_query(2*root + 2, a, b, c, d, !x);
   return ret;
pt kd_neighbor(int root, pt a, bool x) {
  if(tree[root] != -1)
      return a == pts[tree[root]] ? pt(2e9, 2e9) : pts[tree[root]];
  TYPE num = x ? a.x : a.y;
  int term = num <= split[root] ? 1 : 2;</pre>
  pt ret:
  TYPE d = norm(a - (ret = kd_neighbor(2*root + term, a, !x)));
  if((split[root] - num) * (split[root] - num) < d) {</pre>
      pt ret2 = kd_neighbor(2*root + 3 - term, a, !x);
      if(norm(a - ret2) < d)
         ret = ret2;
   return ret;
      sort(tree[root].begin(), tree[root].end(), compy);
      return tree[root].size();
  int mid = (left + right)/2, cl = 2*root + 1, cr = cl + 1;
   int sz1 = rt_recurse(cl, left, mid);
  int sz2 = rt_recurse(cr, mid + 1, right);
  int l = 0, r = 0, llink = 0, rlink = 0; pt last;
  while(1 < sz1 || r < sz2) {
      if(r == sz2 || (1 < sz1 && tree[c1][1].y <= tree[cr][r].y))</pre>
```

```
int pos1 = -1, int posr = -1) {
if (root == 0 \&\& pos == -1)
   pos = lower_bound(tree[0].begin(), tree[0].end(), c, compy)
      - tree[0].begin();
int ret = 0;
if(a <= xs[l] && xs[r] <= b) {</pre>
   while(pos < tree[root].size() && tree[root][pos].y <= d)</pre>
      ret++, pos++;
   return ret;
if(pos >= tree[root].size()) return 0;
int mid = (1 + r)/2;
if(a <= xs[mid])</pre>
   ret += rt_query(2*root+1, 1, mid, a, b, c, d, lnk[root][0][pos]);
if(xs[mid+1] <= b)
   ret += rt_query(2*root+2, mid+1, r, a, b, c, d, lnk[root][1][pos]);
return ret;
```

#### 5. Data structures

#### 5.1. **Treap.** Hash: 2199b72803301716616a462d9d5e9a66

```
treap* find(treap* t, TYPE val) {
   if(!t) return NULL;
   if(val == t->value) return t;

   if(val < t->value) return find(t->left, val);
   if(val > t->value) return find(t->right, val);
}

void rotate_to_right(treap* &t) {
   treap* n = t->left;
   t->left = n->right;
   n->right = t;
   t = n;
}

void rotate_to_left(treap* &t) {
   treap* n = t->right;
   t->right = n->left;
   t->right = n->left;
```

```
n\rightarrow left = t;
   t = n;
void fix_augment(treap* t) {
   if(!t) return;
   t->sons = (t->left ? t->left->sons + 1 : 0) +
      (t->right ? t->right->sons + 1 : 0);
void insert(treap* &t, TYPE val) {
   if(!t)
      t = new treap(val);
   else
      insert(val <= t->value ? t->left : t->right, val);
   if(t->left && t->left->priority > t->priority)
      rotate_to_right(t);
   else if(t->right && t->right->priority > t->priority)
      rotate_to_left(t);
   fix_augment(t->left); fix_augment(t->right); fix_augment(t);
```

# 5.2. **Heap.** Hash: e334218955a73d1286ad0fc19e84b642

```
struct heap {
   int heap[MAXV][2], v2n[MAXV];
   int size;

void init(int sz) __attribute__((always_inline)) {
      memset(v2n, -1, sizeof(int) * sz);
      size = 0;
   }

void swap(int& a, int& b) __attribute__((always_inline)) {
    int temp = a;
      a = b;
      b = temp;
   }

void s(int a, int b) __attribute__((always_inline)) {
    swap(v2n[heap[a][1]], v2n[heap[b][1]]);
    swap(heap[a][0], heap[b][0]);
    swap(heap[a][1], heap[b][1]);
}
```

```
inline int p(treap* t) {
   return t ? t->priority : -1;
void erase(treap* &t, TYPE val) {
  if(!t) return;
   if(t->value != val)
      erase(val < t->value ? t->left : t->right, val);
      if(!t->left && !t->right)
         delete t, t = NULL;
      else {
         p(t->left) < p(t->right) ? rotate_to_left(t) : rotate_to_right(t);
         erase(t, val);
   fix_augment(t->left); fix_augment(t->right); fix_augment(t);
  int extract_min() {
      int ret = heap[0][1];
      s(0, --size);
      int cur = 0, next = 2;
      while(next < size) {</pre>
         if(heap[next][0] > heap[next - 1][0])
            next--;
         if(heap[next][0] >= heap[cur][0])
            break;
         s(next, cur);
         cur = next;
         next = 2*cur + 2;
      if (next == size && heap[next - 1][0] < heap[cur][0])</pre>
         s(next - 1, cur);
      return ret:
```

```
void decrease_key(int vertex, int new_value) __attribute__((always_inline))
{
   if(v2n[vertex] == -1) {
      v2n[vertex] = size;
      heap[size++][1] = vertex;
   }
   heap[v2n[vertex]][0] = new_value;
```

#### 5.3. Big numbers (PUC-Rio). Hash: a7d74e7158634f9201c19235badd3364

```
const int DIG = 4;
const int BASE = 10000; // BASE**3 < 2**51</pre>
const int TAM = 2048;
struct bigint {
 int v[TAM], n;
 bigint (int x = 0): n(1) {
  memset(v, 0, sizeof(v));
  v[n++] = x; fix();
 bigint (char *s): n(1) {
  memset(v, 0, sizeof(v));
  int sign = 1;
   while (*s && !isdigit(*s)) if (*s++ == '-') sign *= -1;
   char *t = strdup(s), *p = t + strlen(t);
   while (p > t) {
    *p = 0; p = max(t, p - DIG);
    sscanf(p, "%d", &v[n]);
    v[n++] \star = sign;
   free(t); fix();
 bigint& fix(int m = 0) {
  n = max(m, n);
   int sign = 0;
   for (int i = 1, e = 0; i <= n || e && (n = i); i++) {</pre>
    v[i] += e; e = v[i] / BASE; v[i] %= BASE;
    if (v[i]) sign = (v[i] > 0) ? 1 : -1;
   for (int i = n - 1; i > 0; i--)
```

```
int cur = v2n[vertex];
while(cur >= 1) {
    int parent = (cur - 1)/2;
    if(new_value >= heap[parent][0])
        break;

    s(cur, parent);
    cur = parent;
}
};
```

```
if (v[i] * sign < 0) { v[i] += sign * BASE; v[i+1] -= sign; }</pre>
 while (n && !v[n]) n--;
 return *this;
int cmp(const bigint& x = 0) const {
 int i = max(n, x.n), t = 0;
 while (1) if ((t = ::cmp(v[i], x.v[i])) || i-- == 0) return t;
bool operator <(const bigint& x) const { return cmp(x) < 0; }</pre>
bool operator == (const bigint& x) const { return cmp(x) == 0; }
bool operator !=(const bigint& x) const { return cmp(x) != 0; }
operator string() const {
 ostringstream s; s << v[n];
 for (int i = n - 1; i > 0; i--) {
  s.width(DIG); s.fill('0'); s << abs(v[i]);
 return s.str();
friend ostream& operator <<(ostream& o, const bigint& x) {</pre>
 return o << (string) x;</pre>
bigint& operator += (const bigint& x) {
 for (int i = 1; i <= x.n; i++) v[i] += x.v[i];</pre>
 return fix(x.n);
bigint operator +(const bigint& x) { return bigint(*this) += x; }
bigint& operator -= (const bigint& x) {
 for (int i = 1; i <= x.n; i++) v[i] -= x.v[i];
```

```
return fix(x.n);
bigint operator -(const bigint& x) { return bigint(*this) -= x; }
bigint operator -() { bigint r = 0; return r -= *this; }
void ams(const bigint& x, int m, int b) { // *this += (x * m) << b;</pre>
 for (int i = 1, e = 0; (i <= x.n || e) && (n = i + b); i++) {
  v[i+b] += x.v[i] * m + e; e = v[i+b] / BASE; v[i+b] %= BASE;
bigint operator *(const bigint& x) const {
 bigint r;
 for (int i = 1; i <= n; i++) r.ams(x, v[i], i-1);</pre>
 return r;
bigint& operator *=(const bigint& x) { return *this = *this * x; }
// cmp(x / y) == cmp(x) * cmp(y); cmp(x % y) == cmp(x);
bigint div(const bigint& x) {
 if (x == 0) return 0;
 bigint q; q.n = max(n - x.n + 1, 0);
 int d = x.v[x.n] * BASE + x.v[x.n-1];
 for (int i = q.n; i > 0; i--) {
  int j = x.n + i - 1;
  q.v[i] = int((v[j] * double(BASE) + v[j-1]) / d);
   ams (x, -q.v[i], i-1);
  if (i == 1 || j == 1) break;
  v[j-1] += BASE * v[j]; v[j] = 0;
```

```
fix(x.n); return q.fix();
 bigint& operator /=(const bigint& x) { return *this = div(x); }
 bigint& operator %=(const bigint& x) { div(x); return *this; }
 bigint operator /(const bigint& x) { return bigint(*this).div(x); }
 bigint operator %(const bigint& x) { return bigint(*this) %= x; }
 bigint pow(int x) {
  if (x < 0) return (*this == 1 || *this == -1) ? pow(-x) : 0;</pre>
  bigint r = 1;
   for (int i = 0; i < x; i++) r *= *this;</pre>
   return r;
 bigint root(int x) {
  if (cmp() == 0 || cmp() < 0 && x % 2 == 0) return 0;</pre>
   if (*this == 1 || x == 1) return *this;
  if (cmp() < 0) return -(-*this).root(x);</pre>
  bigint a = 1, d = *this;
   while (d != 1) {
    bigint b = a + (d /= 2);
    if (cmp(b.pow(x)) >= 0) \{ d += 1; a = b; \}
   return a:
};
```

# 6. String algorithms

# 6.1. Manber-Myers' algorithm. Hash: b32cb670595bef320decbceed7420bb8

```
int pos[MAXSZ], prm[MAXSZ], cnt[MAXSZ];
bool bh[MAXSZ + 1], b2h[MAXSZ];
int blast[256], bprev[MAXSZ];
int mm_segtree[4*MAXSZ];
string mm_s;

inline void regen_pos(int sz) {
   for(int i = 0; i < sz; i++)
        pos[prm[i]] = i;
}

inline void bubbleupbucket(int index) {
   if(index < 0) return;</pre>
```

```
int& prm_ext = prm[index];
cnt[prm_ext]++;
prm_ext += cnt[prm_ext] - 1;
b2h[prm_ext] = true;
}

void updatetree(int root, int 1, int r, int pos, int val) {
   if(1 == r) { mm_segtree[root] = val; return; }

   int m = (1 + r + 1)/2;
   if(pos < m) updatetree(2*root + 1, 1, m - 1, pos, val);
   else updatetree(2*root + 2, m, r, pos, val);

mm_segtree[root] = min(mm_segtree[2*root + 1], mm_segtree[2*root + 2]);</pre>
```

```
int querytree(int root, int 1, int r, int begin, int end) {
   if(begin == 1 && end == r) return mm segtree[root];
  int m = (1 + r + 1)/2;
  if(begin < m && end < m)</pre>
      return querytree(2*root + 1, 1, m - 1, begin, end);
   else if(begin >= m && end >= m)
      return querytree(2*root + 2, m, r, begin, end);
   else return min(querytree(2*root + 1, 1, m - 1, begin, m - 1),
               querytree(2*root + 2, m, r, m, end));
void mm_build(string s) {
  mm s = s;
  memset(blast, -1, sizeof blast);
  memset(bh, 0, sizeof(bool) * s.size());
  memset(mm_segtree, 0x3f, sizeof(int) * 4 * s.size());
   updatetree(0, 0, s.size() - 1, s.size() - 1, 0);
   for(int i = 0; i < s.size(); i++) {</pre>
      bprev[i] = blast[s[i]];
     blast[s[i]] = i;
   int let_count = 0;
   for (int i = 0; i < 256; i++) {
     if(blast[i] != -1) {
        bh[let_count] = true;
         if(let count > 0)
            updatetree(0, 0, s.size() - 1, let_count - 1, 0);
      for(int j = blast[i]; j != -1; j = bprev[j])
         prm[j] = let_count++;
   regen pos(s.size());
  bh[s.size()] = true;
   for (int st = 1; st < s.size(); st \star= 2) {
      memset(cnt, 0, sizeof(int) * s.size());
      memset(b2h, 0, sizeof(bool) * s.size());
      for(int bl = 0, br = 0; br < s.size(); bl = br++)</pre>
         for(; !bh[br]; br++)
            prm[pos[br]] = bl;
```

```
bubbleupbucket(s.size() - st);
      for(int bl = 0, br = 0; br < s.size(); bl = br) {</pre>
         bubbleupbucket(pos[bl] - st);
         for (br++; !bh[br]; br++)
            bubbleupbucket(pos[br] - st);
         for(int i = bl; i < br; i++) {</pre>
            if(pos[i] - st < 0) continue;</pre>
            int prm_ext = prm[pos[i] - st];
            if(b2h[prm ext])
               for(int j = prm_ext + 1; !bh[j] && b2h[j]; j++)
                  b2h[j] = false;
      regen_pos(s.size());
      for(int i = 0; i < s.size(); i++)</pre>
         if(!bh[i] && b2h[i]) {
            bh[i] = true;
            if(pos[i - 1] + st < s.size() && pos[i] + st < s.size()) {</pre>
               int m = min(prm[pos[i - 1] + st], prm[pos[i] + st]);
               int M = max(prm[pos[i - 1] + st], prm[pos[i] + st]);
               updatetree(0, 0, s.size() - 1, i - 1,
                          st + querytree(0, 0, s.size() - 1, m, M - 1));
            else
               updatetree(0, 0, s.size() - 1, i - 1, st);
inline int lcp(string& s1, int p1, string& s2, int p2) {
   int limit = min(s1.size() - p1, s2.size() - p2), i;
   for(i = 0; i < limit; i++) if(s1[p1 + i] != s2[p2 + i]) break;</pre>
   return i;
pair<bool, int> mm_find(string s) {
   int 1 = 1cp(mm s, pos[0], s, 0);
   int r = lcp(mm_s, pos[mm_s.size() - 1], s, 0);
   if(1 == s.size() || s[1] < mm_s[pos[0] + 1])</pre>
      return make_pair(l == s.size(), pos[0]);
   else if (r == s.size() \mid \mid s[r] > mm_s[pos[mm_s.size() - 1] + r])
      return make_pair(r == s.size(), pos[mm_s.size() - 1]);
```

```
int low = 0, high = mm_s.size() - 1, next, st_n = 0, c_lcp;
while(high - low > 1) {
   int mid = (low + high)/2;
   c_lcp = max(l, r);
   st_n = 2*st_n + 1 + (1 < r);

if(mm_segtree[st_n] >= c_lcp)
        next = c_lcp + lcp(mm_s, pos[mid] + c_lcp, s, c_lcp);
else
        next = mm_segtree[st_n];

if(next == s.size())
   return make_pair(true, pos[mid]);
```

# 6.2. Morris-Pratt's algorithm. Hash: ace505eff2be640ff01d7c48b2b7d12f

```
int pi[MAXSZ], res[MAXSZ], nres;

void morris_pratt(string text, string pattern) {
    nres = 0;
    pi[0] = -1;
    for(int i = 1; i < pattern.size(); i++) {
        pi[i] = pi[i-1];
        while(pi[i] >= 0 && pattern[pi[i] + 1] != pattern[i])
            pi[i] = pi[pi[i]];
    if(pattern[pi[i] + 1] == pattern[i]) pi[i]++;
    }
```

```
else if(s[next] > mm_s[pos[mid] + next]) {
    low = mid;
    l = next;
}
else {
    high = mid;
    r = next;
}
return make_pair(false, pos[high]);
```

```
int k = 0; //k + 1 eh o tamanho do match atual
for(int i = 0; i < text.size(); i++) {
    while(k >= 0 && pattern[k + 1] != text[i])
        k = pi[k];
    if(pattern[k + 1] == text[i]) k++;
    if(k + 1 == pattern.size()) {
        res[nres++] = i;
        k = pi[k];
    }
}
```