(global-font-lock-mode t)

#!/bin/sh

(compile (concat "g++_-g_-O2_-o_" (file-name-sans-extension buffer-file-name)

sed ':a;N; $$!ba;s/[_\n\t]//g' \mid md5sum \mid cut -d'_' -f1$

ACM ICPC TEAM REFERENCE 2010 WORLD FINALS

Team Anuncie Aqui Universidade Federal de Sergipe

1. Configuration files and scripts

1.1. .emacs. Hash: b1040cede72bb06f9b3197eba2d833f5

```
(setq transient-mark-mode t)
                                                                                                     "_" buffer-file-name))
(global-set-key [f5] 'cxx-compile)
                                                                                       (add-hook 'c++-mode-hook (lambda () (c-set-style "stroustrup")
(defun cxx-compile()
 (interactive)
                                                                                                                 (flymake-mode t)))
  (save-buffer)
1.2. Makefile. Hash: 7381d22266f4ef5a9a601b80a76a956c
check-syntax:
                                                                                             q++ -Wall -fsyntax-only $(CHK_SOURCES)
1.3. .vimrc. Hash: da63747b3e94a58450094526d21a9e41
syn on
                                                                                       ab #i #include
set nocp number ai si ts=4 sts=4 sw=4
1.4. Hash generator. Hash: 0d22aecd779fc370b30a2c628aff517c
```

1.5. **Solution template.** Hash: 220ea9d23d25447636bd67aeaf899fee

```
#include <algorithm>
                                                                                            #include <set>
#include <cassert>
                                                                                            #include <sstream>
                                                                                            #include <string>
#include <cmath>
#include <cstdio>
                                                                                            #include <utility>
#include <cstdlib>
                                                                                            #include <vector>
#include <cstring>
#include <ctime>
                                                                                            using namespace std;
#include <iostream>
#include <map>
                                                                                            int main() {
#include <queue>
```

2. Graph algorithms

2.1. Tarjan's SCC algorithm. Hash: 3d598e293de54a302a6492c57304d745

```
int lowest[MAXV], num[MAXV], visited[MAXV], comp[MAXV];
int prev_edge[MAXE], last_edge[MAXV], adj[MAXE], nedges;
int cur_num, cur_comp;
stack<int> visiting;
void t_init() {
  memset(last_edge, -1, sizeof last_edge);
   nedges = 0;
void t_edge(int v, int w) {
  prev_edge[nedges] = last_edge[v];
   adj[nedges] = w;
   last_edge[v] = nedges++;
int tarjan_dfs(int v) {
   lowest[v] = num[v] = cur_num++;
   visiting.push(v);
   visited[v] = 1;
   for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
      int w = adj[i];
      if(visited[w] == 0) lowest[v] = min(lowest[v], tarjan_dfs(w));
      else if(visited[w] == 1) lowest[v] = min(lowest[v], num[w]);
```

```
if(lowest[v] == num[v]) {
    int last = -1;
    while(last != v) {
        comp[last = visiting.top()] = cur_comp;
        visited[last] = 2;
        visiting.pop();
    }
    ++cur_comp;
}

return lowest[v];

void tarjan_scc(int num_v = MAXV) {
    visiting = stack<int>();
    memset(visited, 0, sizeof visited);
    cur_num = cur_comp = 0;

for(int i = 0; i < num_v; ++i)
    if(!visited[i])
        tarjan_dfs(i);
}</pre>
```

2.2. Dinic's maximum flow algorithm. Hash: 3a41582d750893ec5cd598e8c9c0e2b2

```
int last_edge[MAXV], cur_edge[MAXV], dist[MAXV];
int prev_edge[MAXE], cap[MAXE], flow[MAXE], adj[MAXE];
int nedges;
void d_init() {
   nedges = 0;
   memset(last_edge, -1, sizeof last_edge);
void d_edge(int v, int w, int capacity, bool r = false) {
   prev_edge[nedges] = last_edge[v];
   cap[nedges] = capacity;
   adj[nedges] = w;
   flow[nedges] = 0;
  last_edge[v] = nedges++;
   if(!r) d_edge(w, v, 0, true);
bool d_auxflow(int source, int sink) {
   queue<int> q;
   q.push(source);
   memset(dist, -1, sizeof dist);
   dist[source] = 0;
   memcpy(cur_edge, last_edge, sizeof last_edge);
   while(!q.empty()) {
      int v = q.front(); q.pop();
      for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
         if(cap[i] - flow[i] == 0) continue;
         if(dist[adj[i]] == -1) {
            dist[adj[i]] = dist[v] + 1;
            q.push(adj[i]);
```

```
if(adj[i] == sink) return true;
   return false;
int d_augmenting(int v, int sink, int c) {
  if(v == sink) return c;
   for(int& i = cur_edge[v]; i != -1; i = prev_edge[i]) {
     if(cap[i] - flow[i] == 0 || dist[adj[i]] != dist[v] + 1)
        continue;
     int val;
     if(val = d_augmenting(adj[i], sink, min(c, cap[i] - flow[i]))) {
        flow[i] += val;
        flow[i^1] -= val;
         return val;
   return 0;
int dinic(int source, int sink) {
   int ret = 0;
  while(d_auxflow(source, sink)) {
     int flow;
      while(flow = d_augmenting(source, sink, 0x3f3f3f3f))
        ret += flow;
   return ret;
```

2.3. Successive shortest paths mincost maxflow algorithm. Hash: 1899233cb68a8d5f6e280654146e1747

```
int dist[MAXV], last_edge[MAXV], d_visited[MAXV], bg_prev[MAXV], pot[MAXV],
    capres[MAXV];
int prev_edge[MAXE], adj[MAXE], cap[MAXE], flow[MAXE];
```

```
int nedges;
priority_queue<pair<int, int> > d_q;
```

```
inline void bq_edge(int v, int w, int capacity, int cst, bool r = false) {
   prev_edge[nedges] = last_edge[v];
   adj[nedges] = w;
   cap[nedges] = capacity;
   flow[nedges] = 0;
   cost[nedges] = cst;
  last_edge[v] = nedges++;
  if(!r) bg_edge(w, v, 0, -cst, true);
inline int rev(int i) { return i ^ 1; }
inline int from(int i) { return adj[rev(i)]; }
inline void bg_init() {
  nedges = 0;
  memset(last_edge, -1, sizeof last_edge);
  memset(pot, 0, sizeof pot);
void bq_dijkstra(int s, int num_nodes = MAXV) {
  memset(dist, 0x3f, sizeof dist);
  memset(d_visited, 0, sizeof d_visited);
   d_q.push(make_pair(dist[s] = 0, s));
   capres[s] = 0x3f3f3f3f3f;
   while(!d_q.empty()) {
     int v = d_q.top().second; d_q.pop();
     if(d_visited[v]) continue; d_visited[v] = true;
      for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
         if(cap[i] - flow[i] == 0) continue;
```

```
int w = adj[i], new_dist = dist[v] + cost[i] + pot[v] - pot[w];
         if(new_dist < dist[w]) {</pre>
            d_q.push(make_pair(-(dist[w] = new_dist), w));
            bg_prev[w] = rev(i);
            capres[w] = min(capres[v], cap[i] - flow[i]);
pair<int, int> busacker gowen(int src, int sink, int num nodes = MAXV) {
   int ret_flow = 0, ret_cost = 0;
  bg_dijkstra(src, num_nodes);
   while(dist[sink] < 0x3f3f3f3f3f) {
      int cur = sink;
      while(cur != src) {
         flow[bq_prev[cur]] -= capres[sink];
         flow[rev(bq_prev[cur])] += capres[sink];
        ret_cost += cost[rev(bg_prev[cur])] * capres[sink];
        cur = adj[bq_prev[cur]];
      ret_flow += capres[sink];
      for (int i = 0; i < MAXV; ++i)
        pot[i] = min(pot[i] + dist[i], 0x3f3f3f3f);
      bg_dijkstra(src, num_nodes);
   return make_pair(ret_flow, ret_cost);
```

2.4. Gabow's general matching algorithm. Hash: 85de6860f6b8472baad4c5b063815b18

```
int prev_edge[MAXE], v[MAXE], w[MAXE], last_edge[MAXV];
int type[MAXV], label[MAXV], first[MAXV], mate[MAXV], nedges;
bool g_flag[MAXV], g_souter[MAXV];

void g_init() {
   nedges = 0;
   memset(last_edge, -1, sizeof last_edge);
}
```

```
void g_edge(int a, int b, bool rev = false) {
   prev_edge[nedges] = last_edge[a];
   v[nedges] = a;
   w[nedges] = b;
   last_edge[a] = nedges++;

   if(!rev) return g_edge(b, a, true);
}
```

```
void q_label(int v, int join, int edge, queue<int>& outer) {
   if(v == join) return;
  if(label[v] == -1) outer.push(v);
  label[v] = edge;
   type[v] = 1;
   first[v] = join;
   g_label(first[label[mate[v]]], join, edge, outer);
void g_augment(int _v, int _w) {
   int t = mate[_v];
  mate[\_v] = \_w;
   if(mate[t] != _v) return;
   if(label[_v] == -1) return;
   if(type[_v] == 0) {
      mate[t] = label[_v];
      g_augment(label[_v], t);
  } else if(type[_v] == 1) {
      g_augment(v[label[_v]], w[label[_v]]);
      q_augment(w[label[_v]], v[label[_v]]);
int gabow(int n) {
   memset(mate, -1, sizeof mate);
   memset(first, -1, sizeof first);
   int ret = 0;
   for (int z = 0; z < n; ++z) {
      if (mate[z] != -1) continue;
      memset (label, -1, sizeof label);
      memset(type, -1, sizeof type);
      memset(g_souter, 0, sizeof g_souter);
      label[z] = -1; type[z] = 0;
      queue<int> outer;
      outer.push(z);
      bool done = false;
      while(!outer.empty()) {
```

```
int x = outer.front(); outer.pop();
if(q_souter[x]) continue;
g_souter[x] = true;
for(int i = last_edge[x]; i != -1; i = prev_edge[i]) {
   if (mate[w[i]] == -1 && w[i] != z) {
      mate[w[i]] = x;
      g_augment(x, w[i]);
      ++ret;
      done = true;
      break;
   if(type[w[i]] == -1) {
      int v = mate[w[i]];
      if(type[v] == -1) {
         type[v] = 0;
         label[v] = x;
         outer.push(v);
         first[v] = w[i];
      continue;
   int r = first[x], s = first[w[i]];
   if(r == s) continue;
   memset(g_flag, 0, sizeof g_flag);
   g_flag[r] = g_flag[s] = true;
   while (r != -1 || s != -1)  {
      if(s != -1) swap(r, s);
      r = first[label[mate[r]]];
      if(r == -1) continue;
      if(g_flag[r]) break; g_flag[r] = true;
   g_label(first[x], r, i, outer);
   g_label(first[w[i]], r, i, outer);
   for(int c = 0; c < n; ++c)
      if(type[c] != -1 && first[c] != -1 && type[first[c]] != -1)
         first[c] = r;
```

```
}
if(done) break;

return ret;
}
```

3. Math

3.1. **Fractions.** Hash: 85739ae11b5b0351c0a9b5b6f813eaf8

```
struct frac {
  long long num, den;
  frac(long long num = 0, long long den = 1) { set_val(num, den); }

void set_val(long long _num, long long _den) {
    num = _num/__gcd(_num, _den);
    den = _den/__gcd(_num, _den);
    if(den < 0) { num *= -1; den *= -1; }
}

void operator*=(frac f) { set_val(num * f.num, den * f.den); }
  void operator+=(frac f) { set_val(num * f.den + f.num * den, den * f.den); }
  void operator-=(frac f) { set_val(num * f.den - f.num * den, den * f.den); }
  void operator/=(frac f) { set_val(num * f.den, den * f.num); }
};</pre>
```

```
bool operator==(frac a, frac b) { return a.num * b.den == b.num * a.den; }
bool operator!=(frac a, frac b) { return ! (a == b); }
bool operator<(frac a, frac b) { return a.num * b.den < b.num * a.den; }
bool operator<=(frac a, frac b) { return (a == b) || (a < b); }
bool operator>(frac a, frac b) { return !(a <= b); }
bool operator>=(frac a, frac b) { return !(a < b); }
frac operator/(frac a, frac b) { frac ret = a; ret /= b; return ret; }
frac operator*(frac a, frac b) { frac ret = a; ret += b; return ret; }
frac operator+(frac a, frac b) { frac ret = a; ret += b; return ret; }
frac operator-(frac a, frac b) { frac ret = a; ret -= b; return ret; }
frac operator-(frac a, frac b) { frac ret = a; ret -= b; return ret; }
frac operator-(frac a, frac b) { frac ret = a; ret -= b; return ret; }
frac operator-(frac f) { return 0 - f; }

std::ostream& operator<<(std::ostream& o, const frac f) {
    o << f.num << "/" << f.den;
    return o;
}</pre>
```

3.2. Chinese remainder theorem. Hash: 06b5ebd5c44c204a4b11bbb76d09023d

```
struct t {
   long long a, b; int g;
   t(long long a, long long b, int g) : a(a), b(b), g(g) { }
   t swap() { return t(b, a, g); }
};

t egcd(int p, int q) {
   if(q == 0) return t(1, 0, p);
   t t2 = egcd(q, p % q);
```

```
t2.a -= t2.b * (p/q);
  return t2.swap();
}

int crt(int a, int p, int b, int q) {
  t t2 = egcd(p, q); t2.a %= p*q; t2.b %= p*q;
  assert(t2.g == 1);
  int ret = ((b * t2.a) % (p*q) * p + (a * t2.b) % (p*q) * q) % (p*q);
  return ret >= 0 ? ret : ret + p*q;
}
```

3.3. Longest increasing subsequence. Hash: 8578a256b2926d8be6ace63e1ed4088c

```
vector<int> lis(vector<int>& seq) {
  int smallest_end[seq.size()+1], prev[seq.size()];
```

```
smallest\_end[1] = 0;
```

```
int sz = 1;
for(int i = 1; i < seq.size(); ++i) {
   int lo = 0, hi = sz;
   while(lo < hi) {
      int mid = (lo + hi + 1)/2;
      if(seq[smallest_end[mid]] <= seq[i])
            lo = mid;
      else
            hi = mid - 1;
   }
   prev[i] = smallest_end[lo];
   if(lo == sz)</pre>
```

3.4. Simplex (Warsaw University). Hash: c687094970cf1953fd6f87a01adc6a95

```
const double EPS = 1e-9;
typedef long double T;
typedef vector<T> VT;
vector<VT> A;
VT b,c,res;
VI kt.N:
int m;
inline void pivot(int k,int l,int e){
   int x=kt[1]; T p=A[1][e];
   REP(i,k) A[1][i]/=p; b[1]/=p; N[e]=0;
   REP(i,m) if (i!=1) b[i]-A[i][e]*b[1],A[i][x]-A[i][e]*-A[1][x];
   REP(j,k) if (N[j]){
     c[j] = c[e] *A[l][j];
      REP(i,m) if (i!=1) A[i][j]-=A[i][e]*A[1][j];
   kt[1]=e; N[x]=1; c[x]=c[e]*-A[1][x];
VT doit(int k) {
   VT res; T best;
   while (1) {
      int e=-1,1=-1; REP(i,k) if (N[i] && c[i]>EPS) {e=i; break;}
      if (e==-1) break;
      REP(i,m) if (A[i][e]>EPS && (l==-1 || best>b[i]/A[i][e]))
        best=b[ l=i ]/A[i][e];
```

```
smallest_end[++sz] = i;
else if(seq[i] < seq[smallest_end[lo+1]])
    smallest_end[lo+1] = i;
}

vector<int> ret;
for(int cur = smallest_end[sz]; sz > 0; cur = prev[cur], --sz)
    ret.push_back(seq[cur]);
reverse(ret.begin(), ret.end());

return ret;
}
```

```
if (l==-1) /*ilimitado*/ return VT();
      pivot(k,l,e);
   res.resize(k,0); REP(i,m) res[kt[i]]=b[i];
   return res;
VT simplex(vector<VT> &AA, VT &bb, VT &cc) {
   int n=AA[0].size(),k;
  m=AA.size(); k=n+m+1; kt.resize(m); b=bb; c=cc; c.resize(n+m);
  A=AA; REP(i,m) \{ A[i].resize(k); A[i][n+i]=1; A[i][k-1]=-1; kt[i]=n+i; \}
  N=VI(k,1); REP(i,m) N[kt[i]]=0;
  int pos=min_element(ALL(b))-b.begin();
  if (b[pos] <-EPS) {
      c=VT(k,0); c[k-1]=-1; pivot(k,pos,k-1); res=doit(k);
      if (res[k-1]>EPS) /*impossivel*/ return VT();
      REP(i,m) if (kt[i]==k-1)
        REP(j,k-1) if (N[j] && (A[i][j]<-EPS || EPS<A[i][j])){
            pivot(k,i,j); break;
      c=cc; c.resize(k,0); REP(i,m) REP(j,k) if (N[j]) c[j]-=c[kt[i]]*A[i][j];
   res=doit(k-1); if (!res.empty()) res.resize(n);
   return res;
```

3.5. Romberg's method. Hash: a50b581a5c45b3266a7b2d1e76d8e453

```
long double div = (b-a)/pow(2, it);
for(long double sample = a + div; sample < b; sample += 2 * div)
        cur[0] += div * func(a + sample);

for(int j = 1; j <= it; ++j)
        cur[j] = cur[j-1] + 1/(pow(4, it) - 1)*(cur[j-1] + prev[j-1]);
}
return prev[24];</pre>
```

3.6. Floyd's cycle detection algorithm. Hash: 97a42d1ac6750f912c5a06e04636c1db

```
pair<int, int> floyd(int x0) {
  int t = f(x0), h = f(f(x0)), start = 0, length = 1;
  while(t != h)
    t = f(t), h = f(f(h));

h = t; t = x0;
  while(t != h)
    t = f(t), h = f(h), ++start;
```

}

while(t != h)

h = f(h), ++length;

return make_pair(start, length);

h = f(t);

3.7. **Pollard's rho algorithm.** Hash: ad4ee1d4afc564b2c55f90d6269994c4

```
long long pollard_r, pollard_n;
inline long long f(long long val) { return (val*val + pollard_r) % pollard_n; }
inline long long myabs(long long a) { return a >= 0 ? a : -a; }

long long pollard(long long n) {
    srand(unsigned(time(0)));
    pollard_n = n;

    long long d = 1;
    do {
```

```
d = 1;
pollard_r = rand() % n;

long long x = 2, y = 2;
while(d == 1)
    x = f(x), y = f(f(y)), d = __gcd(myabs(x-y), n);
} while(d == n);

return d;
```

3.8. Miller-Rabin's algorithm. Hash: 5288cd2ac5d62a97ea1175eec20d0010

```
int fastpow(int base, int d, int n) {
   int ret = 1;
   for(long long pow = base; d > 0; d >>= 1, pow = (pow * pow) % n)
      if(d & 1)
        ret = (ret * pow) % n;
   return ret;
}

bool miller_rabin(int n, int base) {
   if(n <= 1) return false;
   if(n % 2 == 0) return n == 2;

   int s = 0, d = n - 1;
   while(d % 2 == 0) d /= 2, ++s;

   int base_d = fastpow(base, d, n);</pre>
```

3.9. Karatsuba's algorithm. Hash: baa2224f03b35ae422eed1c261dcf6b8

```
typedef vector<int> poly;

poly mult(const poly& p, const poly& q) {
   int sz = p.size(), half = sz/2;
   assert(sz == q.size() && !(sz&(sz-1)));

if(sz <= 64) {
   poly ret(2*sz);
   for(int i = 0; i < sz; i++)
        for(int j = 0; j < sz; j++)
        ret[i+j] += p[i] * q[j];
   return ret;
}

poly pl(p.begin(), p.begin() + half), p2(p.begin() + half, p.end());</pre>
```

```
if(base_2r == n - 1) return true;
      base_2r = (long long)base_2r * base_2r % n;
   return false;
bool isprime(int n) {
  if(n == 2 || n == 7 || n == 61) return true;
  return miller_rabin(n, 2) && miller_rabin(n, 7) && miller_rabin(n, 61);
  poly q1(q.begin(), q.begin() + half), q2(q.begin() + half, q.end());
  poly p1p2(half), q1q2(half);
  for(int i = 0; i < half; i++)</pre>
      p1p2[i] = p1[i] + p2[i], q1q2[i] = q1[i] + q2[i];
  poly low = mult(p1, q1), high = mult(p2, q2), mid = mult(p1p2, q1q2);
   for(int i = 0; i < sz; i++)</pre>
      mid[i] -= high[i] + low[i];
   low.resize(2*sz);
   for(int i = 0; i < sz; i++)</pre>
      low[i+half] += mid[i], low[i+sz] += high[i];
   return low;
```

3.10. Optimized sieve of Erathostenes. Hash: f61dff82d061bab316148816c3b7ac01

```
const unsigned MAX = 1000000020/60, MAX_S = sqrt(MAX/60);
unsigned w[16] = {1, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 49, 53, 59};
unsigned short composite[MAX];
```

```
vector<int> primes;

void sieve() {
   unsigned mod[16][16], di[16][16], num;
```

if(base_d == 1) return true;

for (int i = 0; i < s; ++i) {

if(base_2r == 1) return false;

int base_2r = base_d;

```
for(int i = 0; i < 16; i++)
    for(int j = 0; j < 16; j++) {
        di[i][j] = (w[i]*w[j])/60;
        mod[i][j] = lower_bound(w, w + 16, (w[i]*w[j])%60) - w;
    }

primes.push_back(2); primes.push_back(3); primes.push_back(5);

memset(composite, 0, sizeof composite);
for(unsigned i = 0; i < MAX; i++)
    for(int j = (i==0); j < 16; j++) {
        if(composite[i] & (1<<j)) continue;</pre>
```

3.11. Polynomials (PUC-Rio). Hash: d69d1ad494e487327d2338e69eccfa2f

```
typedef complex<double> cdouble;
int cmp(cdouble x, cdouble y = 0) {
   return cmp(abs(x), abs(y));
const int TAM = 200;
struct poly {
   cdouble poly[TAM]; int n;
   poly(int n = 0): n(n) { memset(p, 0, sizeof(p)); }
   cdouble& operator [](int i) { return p[i]; }
   poly operator ~() {
      poly r(n-1);
      for (int i = 1; i <= n; i++)</pre>
         r[i-1] = p[i] * cdouble(i);
      return r;
   pair<poly, cdouble> ruffini(cdouble z) {
      if (n == 0) return make_pair(poly(), 0);
      poly r(n-1);
      for (int i = n; i > 0; i--) r[i-1] = r[i] * z + p[i];
      return make_pair(r, r[0] * z + p[0]);
   cdouble operator ()(cdouble z) { return ruffini(z).second; }
   cdouble find_one_root(cdouble x) {
      poly p0 = *this, p1 = ~p0, p2 = ~p1;
      int m = 1000;
```

```
primes.push_back(num = 60*i + w[j]);

if(i > MAX_S) continue;
for(unsigned k = i, done = false; !done; k++)
    for(int 1 = (k==0); 1 < 16 && !done; 1++) {
        unsigned mult = k*num + i*w[1] + di[j][1];
        if(mult >= MAX) done = true;
        else composite[mult] |= 1<<mod[j][1];
    }
}</pre>
```

```
while (m--) {
         cdouble y0 = p0(x);
         if (cmp(y0) == 0) break;
         cdouble G = p1(x) / y0;
         cdouble H = G * G - p2(x) - y0;
         cdouble R = sqrt(cdouble(n-1) * (H * cdouble(n) - G * G));
        cdouble D1 = G + R, D2 = G - R;
        cdouble a = cdouble(n) / (cmp(D1, D2) > 0 ? D1 : D2);
        x -= a;
         if (cmp(a) == 0) break;
      return x;
  vector<cdouble> roots() {
     poly q = *this;
     vector<cdouble> r;
      while (q.n > 1) {
         cdouble z(rand() / double(RAND_MAX), rand() / double(RAND_MAX));
        z = q.find_one_root(z); z = find_one_root(z);
        q = q.ruffini(z).first;
        r.push_back(z);
      return r;
};
```

4. Geometry

4.1. **Point class.** Hash: 4a0fc00fd27520d94e04b2fc6c05ed73

```
typedef double TYPE;
const TYPE EPS = 1e-9, INF = 1e9;
inline int sgn(TYPE a) { return a > EPS ? 1 : (a < -EPS ? -1 : 0); }</pre>
inline int cmp(TYPE a, TYPE b) { return sgn(a - b); }
struct pt {
   TYPE x, v;
   pt(TYPE x = 0, TYPE y = 0) : x(x), y(y) { }
   bool operator== (pt p) { return cmp(x, p.x) == 0 \&\& cmp(y, p.y) == 0; }
   bool operator<(pt p) const {</pre>
      return cmp(x, p.x) ? cmp(x, p.x) < 0 : cmp(y, p.y) < 0;
  bool operator<=(pt p) { return *this < p || *this == p; }</pre>
   TYPE operator | (pt p) { return x*p.x + y*p.y; }
   TYPE operator%(pt p) { return x*p.y - y*p.x; }
   pt operator () { return pt(x, -y); }
   pt operator+(pt p) { return pt(x + p.x, y + p.y); }
   pt operator-(pt p) { return pt(x - p.x, y - p.y); }
   pt operator*(pt p) { return pt(x*p.x - y*p.y, x*p.y + y*p.x); }
   pt operator/(TYPE t) { return pt(x/t, y/t); }
```

4.2. Intersection primitives. Hash: ab780978106a5c062b8f7a129ebc9196

4.3. Polygon primitives. Hash: 621a339a657d07de8f651d55e13d988b

```
double p_signedarea(vector<pt>& pol) {
   double ret = 0;
```

```
pt operator/(pt p) { return (*this * ~p)/(p||p); }
};
const pt I = pt(0,1);
struct circle {
  pt c; TYPE r;
  circle(pt c, TYPE r) : c(c), r(r) { }
TYPE norm(pt a) { return a | |a; }
TYPE abs(pt a) { return sqrt(a||a); }
TYPE dist(pt a, pt b) { return abs(a - b); }
TYPE area(pt a, pt b, pt c) { return (a-c)%(b-c); }
int ccw(pt a, pt b, pt c) { return sqn(area(a, b, c)); }
pt unit(pt a) { return a/abs(a); }
double arg(pt a) { return atan2(a.y, a.x); }
pt f_polar(TYPE mod, double ang) { return pt (mod * cos(ang), mod * sin(ang)); }
inline int q_mod(int i, int n) { if(i == n) return 0; return i; }
ostream& operator<<(ostream& o, pt p) {
  return o << "(" << p.x << "," << p.y << ")";
pt parametric_isect(pt p, pt v, pt q, pt w) {
   double t = ((q-p)%w)/(v%w);
   return p + v*t;
pt ss_isect(pt p, pt q, pt r, pt s) {
  pt isect = parametric_isect(p, q-p, r, s-r);
  if(ps_isects(p, q, isect) && ps_isects(r, s, isect)) return isect;
   return pt (1/0.0, 1/0.0);
  for(int i = 0; i < pol.size(); ++i)</pre>
      ret += pol[i] % pol[q_mod(i+1, pol.size())];
```

```
return ret/2;
}
int point_polygon(pt p, vector<pt>& pol) {
   int n = pol.size(), count = 0;
   for(int i = 0; i < n; ++i) {</pre>
```

4.4. **Miscellaneous primitives.** Hash: be051245293a9db9c991d414c598e854

```
bool point_circle(pt p, circle c) {
    return cmp(abs(p - c.c), c.r) <= 0;
}

double ps_distance(pt p, pt a, pt b) {
    p = p - a; b = b - a;
    double coef = min(max((b||p)/(b||b), TYPE(0)), TYPE(1));
    return abs(p - b*coef);
}</pre>
```

4.5. Smallest enclosing circle. Hash: 00dd4dbd6779989a64c1e935443a1d80

```
circle enclosing_circle(vector<pt>& pts) {
    srand(unsigned(time(0)));
    random_shuffle(pts.begin(), pts.end());

circle c(pt(), -1);
    for(int i = 0; i < pts.size(); ++i) {
        if(point_circle(pts[i], c)) continue;
        c = circle(pts[i], 0);
        for(int j = 0; j < i; ++j) {
            if(point_circle(pts[j], c)) continue;
        }
}</pre>
```

4.6. Convex hull. Hash: 2b14ae1a97e5ff686efb4d7e0e7ca78a

```
pt pivot;

bool hull_comp(pt a, pt b) {
   int turn = ccw(a, b, pivot);
   return turn == 1 || (turn == 0 && cmp(norm(a-pivot), norm(b-pivot)) < 0);
}</pre>
```

```
int i1 = q_mod(i+1, n);
      if (ps_isects(pol[i], pol[i1], p)) return -1;
      else if(((sgn(pol[i].y - p.y) == 1) != (sgn(pol[i1].y - p.y) == 1)) &&
            ccw(pol[i], p, pol[i1]) == sgn(pol[i].y - pol[i1].y)) ++count;
   return count % 2;
pt circumcenter(pt a, pt b, pt c) {
   return parametric_isect((b+a)/2, (b-a)*I, (c+a)/2, (c-a)*I);
bool compy (pt a, pt b) {
  return cmp(a.y, b.y) ? cmp(a.y, b.y) < 0 : cmp(a.x, b.x) < 0;
bool compx(pt a, pt b) { return a < b; }</pre>
         c = circle((pts[i] + pts[j])/2, abs(pts[i] - pts[j])/2);
         for (int k = 0; k < j; ++k) {
            if(point_circle(pts[k], c)) continue;
            pt center = circumcenter(pts[i], pts[j], pts[k]);
            c = circle(center, abs(center - pts[i])/2);
   return c;
vector<pt> hull(vector<pt> pts) {
  if(pts.size() <= 1) return pts;</pre>
  vector<pt> ret;
  int mini = 0;
   for(int i = 1; i < pts.size(); ++i)</pre>
      if(pts[i] < pts[mini])</pre>
```

```
mini = i;

pivot = pts[mini];
swap(pts[0], pts[mini]);
sort(pts.begin() + 1, pts.end(), hull_comp);

ret.push_back(pts[0]);
ret.push_back(pts[1]);
int sz = 2;
```

4.7. Closest pair of points. Hash: d704271ff258aac5dad13bb04cf0cfb6

```
pair<pt, pt> closest_points_rec(vector<pt>& px, vector<pt>& py) {
   pair<pt, pt> ret;
   double d;
   if(px.size() <= 3) {
      double best = 1e10;
      for(int i = 0; i < px.size(); ++i)</pre>
         for (int j = i + 1; j < px.size(); ++j)</pre>
            if(dist(px[i], px[j]) < best) {</pre>
                ret = make_pair(px[i], px[j]);
               best = dist(px[i], px[j]);
      return ret;
   pt split = px[(px.size() - 1)/2];
   vector<pt> qx, qy, rx, ry;
   for(int i = 0; i < px.size(); ++i)</pre>
      if(px[i] <= split) qx.push_back(px[i]);</pre>
      else rx.push_back(px[i]);
   for(int i = 0; i < pv.size(); ++i)</pre>
      if(py[i] <= split) qy.push_back(py[i]);</pre>
      else ry.push_back(py[i]);
   ret = closest_points_rec(qx, qy);
   pair<pt, pt> rans = closest_points_rec(rx, ry);
   double delta = dist(ret.first, ret.second);
   if((d = dist(rans.first, rans.second)) < delta) {</pre>
```

```
for(int i = 2; i < pts.size(); ++i) {</pre>
      while (sz \ge 2 \&\& ccw(ret[sz-2], ret[sz-1], pts[i]) \le 0)
         ret.pop_back(), --sz;
      ret.push_back(pts[i]), ++sz;
   return ret;
      delta = d;
      ret = rans;
   vector<pt> s;
   for(int i = 0; i < py.size(); ++i)</pre>
      if(cmp(abs(py[i].x - split.x), delta) <= 0)</pre>
         s.push_back(py[i]);
   for(int i = 0; i < s.size(); ++i)</pre>
      for(int j = 1; j <= 7 && i + j < s.size(); ++j)</pre>
         if((d = dist(s[i], s[i+j])) < delta) {
            delta = d;
            ret = make_pair(s[i], s[i+j]);
   return ret;
pair<pt, pt> closest_points(vector<pt> pts) {
   if(pts.size() == 1) return make_pair(pt(-INF, -INF), pt(INF, INF));
   sort(pts.begin(), pts.end());
   for(int i = 0; i + 1 < pts.size(); ++i)</pre>
      if(pts[i] == pts[i+1])
         return make_pair(pts[i], pts[i+1]);
   vector<pt> py = pts;
   sort(py.begin(), py.end(), compy);
   return closest_points_rec(pts, py);
```

4.8. **Kd-tree.** Hash: 181bc30d9b4f2bfc8c42ca71101934ba

```
int tree[4*MAXSZ], val[4*MAXSZ];
TYPE split[4*MAXSZ];
vector<pt> pts;
void kd_recurse(int root, int left, int right, bool x) {
   if(left == right) {
      tree[root] = left;
      val[root] = 1;
      return;
   int mid = (right+left)/2;
   nth_element(pts.begin() + left, pts.begin() + mid,
            pts.begin() + right + 1, x ? compx : compy);
   split[root] = x ? pts[mid].x : pts[mid].y;
   kd_recurse(2*root+1, left, mid, !x);
   kd_recurse(2*root+2, mid+1, right, !x);
   val[root] = val[2*root+1] + val[2*root+2];
void kd_build() {
   memset (tree, -1, sizeof tree);
   kd_recurse(0, 0, pts.size() - 1, true);
int kd_query(int root, TYPE a, TYPE b, TYPE c, TYPE d, TYPE ca = -INF,
          TYPE cb = INF, TYPE cc = -INF, TYPE cd = INF, bool x = true) {
   if(a <= ca && cb <= b && c <= cc && cd <= d)</pre>
      return val[root];
   if(tree[root] != -1)
      return a <= pts[tree[root]].x && pts[tree[root]].x <= b &&</pre>
```

4.9. Range tree. Hash: fe56bcb0195f42e56d89dc8e2015a9d6

```
vector<pt> pts, tree[MAXSZ];
vector<TYPE> xs;
vector<int> lnk[MAXSZ][2];
bool compy(pt a, pt b) { return cmp(a.y, b.y) < 0; }</pre>
```

```
c <= pts[tree[root]].y && pts[tree[root]].y <= d ? val[root] : 0;</pre>
   int ret = 0;
   if(x) {
      if(a <= split[root])</pre>
         ret += kd_{query}(2*root+1, a, b, c, d, ca, split[root], cc, cd, !x);
      if(split[root] <= b)</pre>
         ret += kd_{query}(2*root+2, a, b, c, d, split[root], cb, cc, cd, !x);
   } else {
      if(c <= split[root])</pre>
         ret += kd_query(2*root+1, a, b, c, d, ca, cb, cc, split[root], !x);
      if(split[root] <= d)</pre>
         ret += kd_query(2*root+2, a, b, c, d, ca, cb, split[root], cd, !x);
   return ret;
pt kd_neighbor(int root, pt a, bool x) {
   if(tree[root] != -1)
      return a == pts[tree[root]] ? pt(INF, INF) : pts[tree[root]];
   TYPE num = x ? a.x : a.y;
   int term = num <= split[root] ? 1 : 2;</pre>
   pt ret;
   TYPE d = norm(a - (ret = kd_neighbor(2*root + term, a, !x)));
   if((split[root] - num) * (split[root] - num) < d) {</pre>
      pt ret2 = kd_neighbor(2*root + 3 - term, a, !x);
      if(norm(a - ret2) < d)
         ret = ret2;
   return ret;
int rt_recurse(int root, int left, int right) {
   lnk[root][0].clear(); lnk[root][1].clear(); tree[root].clear();
```

if(left == right) {

```
vector<pt>::iterator it;
   it = lower_bound(pts.begin(), pts.end(), pt(xs[left], -INF));
   for(; it != pts.end() && cmp(it->x, xs[left]) == 0; ++it)
      tree[root].push_back(*it);
   return tree[root].size();
int mid = (left + right)/2, cl = 2*root + 1, cr = cl + 1;
int sz1 = rt_recurse(c1, left, mid);
int sz2 = rt recurse(cr, mid + 1, right);
lnk[root][0].reserve(sz1+sz2+1);
lnk[root][1].reserve(sz1+sz2+1);
tree[root].reserve(sz1+sz2);
int l = 0, r = 0, llink = 0, rlink = 0; pt last;
while(1 < sz1 || r < sz2) {
   if(r == sz2 || (1 < sz1 && compy(tree[c1][1], tree[cr][r])))</pre>
      tree[root].push_back(last = tree[cl][l++]);
   else tree[root].push_back(last = tree[cr][r++]);
   while(llink < szl && compy(tree[cl][llink], last))</pre>
      ++llink:
   while(rlink < sz2 && compy(tree[cr][rlink], last))</pre>
      ++rlink:
   lnk[root][0].push_back(llink);
   lnk[root][1].push_back(rlink);
lnk[root][0].push_back(tree[cl].size());
lnk[root][1].push_back(tree[cr].size());
```

```
return tree[root].size();
void rt_build() {
   sort(pts.begin(), pts.end());
  xs.clear();
   for(int i = 0; i < pts.size(); ++i) xs.push_back(pts[i].x);</pre>
  xs.erase(unique(xs.begin(), xs.end()), xs.end());
   rt_recurse(0, 0, xs.size() - 1);
int rt_query(int root, int 1, int r, TYPE a, TYPE b, TYPE c, TYPE d,
          int pos1 = -1, int posr = -1) {
  if(root == 0 && posl == -1) {
      posl = lower_bound(tree[0].begin(), tree[0].end(), pt(a, c), compy)
         - tree[0].begin();
      posr = upper_bound(tree[0].begin(), tree[0].end(), pt(b, d), compy)
         - tree[0].begin();
  if(posl == posr) return 0;
   if(a <= xs[1] && xs[r] <= b)
      return posr - posl;
  int mid = (1+r)/2, ret = 0;
  if(cmp(a, xs[mid]) <= 0)
      ret += rt_query(2*root+1, 1, mid, a, b, c, d,
                  lnk[root][0][posl], lnk[root][0][posr]);
  if(cmp(xs[mid+1], b) <= 0)
      ret += rt_query(2*root+2, mid+1, r, a, b, c, d,
                  lnk[root][1][posl], lnk[root][1][posr]);
   return ret;
```

5. Data structures

5.1. **Treap.** Hash: 2199b72803301716616a462d9d5e9a66

```
typedef int TYPE;

class treap {
public:
    treap *left, *right;
    int priority, sons;
    TYPE value;
```

```
treap(TYPE value) : left(NULL), right(NULL), value(value), sons(0) {
   priority = rand();
}

*treap() {
   if(left) delete left;
```

```
if(right) delete right;
};
treap* find(treap* t, TYPE val) {
   if(!t) return NULL;
   if(val == t->value) return t;
   if(val < t->value) return find(t->left, val);
   if(val > t->value) return find(t->right, val);
void rotate_to_right(treap* &t) {
   treap* n = t->left;
   t \rightarrow left = n \rightarrow right;
   n->right = t;
   t = n;
void rotate_to_left(treap* &t) {
   treap* n = t->right;
   t->right = n->left;
   n->left = t;
   t = n;
void fix_augment(treap* t) {
   if(!t) return;
   t\rightarrowsons = (t\rightarrow)left ? t\rightarrowleft->sons + 1 : 0) +
       (t->right ? t->right->sons + 1 : 0);
void insert(treap* &t, TYPE val) {
```

5.2. **Heap.** Hash: e334218955a73d1286ad0fc19e84b642

```
struct heap {
   int heap[MAXV][2], v2n[MAXV];
   int size;

void init(int sz) __attribute__((always_inline)) {
     memset(v2n, -1, sizeof(int) * sz);
     size = 0;
}
```

```
if(!t)
      t = new treap(val);
      insert(val <= t->value ? t->left : t->right, val);
  if(t->left && t->left->priority > t->priority)
     rotate_to_right(t);
   else if(t->right && t->right->priority > t->priority)
     rotate_to_left(t);
   fix_augment(t->left); fix_augment(t->right); fix_augment(t);
inline int p(treap* t) {
   return t ? t->priority : -1;
void erase(treap* &t, TYPE val) {
  if(!t) return;
  if(t->value != val)
     erase(val < t->value ? t->left : t->right, val);
  else {
     if(!t->left && !t->right)
        delete t, t = NULL;
        p(t->left) < p(t->right) ? rotate_to_left(t) : rotate_to_right(t);
         erase(t, val);
   fix_augment(t->left); fix_augment(t->right); fix_augment(t);
   void swap(int& a, int& b) __attribute__((always_inline)) {
     int temp = a;
     a = b;
     b = temp;
  void s(int a, int b) __attribute__((always_inline)) {
      swap(v2n[heap[a][1]], v2n[heap[b][1]]);
      swap(heap[a][0], heap[b][0]);
```

```
swap(heap[a][1], heap[b][1]);
int extract_min() {
   int ret = heap[0][1];
   s(0, --size);
   int cur = 0, next = 2;
   while(next < size) {</pre>
      if(heap[next][0] > heap[next - 1][0])
         next--;
      if(heap[next][0] >= heap[cur][0])
         break;
      s(next, cur);
      cur = next;
      next = 2*cur + 2;
   if (next == size && heap[next - 1][0] < heap[cur][0])</pre>
      s(next - 1, cur);
   return ret;
```

5.3. Big numbers (PUC-Rio). Hash: a7d74e7158634f9201c19235badd3364

```
const int DIG = 4;
const int BASE = 10000; // BASE**3 < 2**51</pre>
const int TAM = 2048;
struct bigint {
   int v[TAM], n;
  bigint(int x = 0): n(1) {
      memset(v, 0, sizeof(v));
      v[n++] = x; fix();
  bigint(char *s): n(1) {
      memset(v, 0, sizeof(v));
      int sign = 1;
      while (*s && !isdigit(*s)) if (*s++ == '-') sign *= -1;
      char *t = strdup(s), *p = t + strlen(t);
      while (p > t) {
         \star p = 0; p = max(t, p - DIG);
         sscanf(p, "%d", &v[n]);
         v[n++] \star = sign;
```

```
void decrease_key(int vertex, int new_value) __attribute__((always_inline))
{
    if(v2n[vertex] == -1) {
        v2n[vertex] = size;
        heap[size++][1] = vertex;
}

    heap[v2n[vertex]][0] = new_value;

    int cur = v2n[vertex];
    while(cur >= 1) {
        int parent = (cur - 1)/2;
        if(new_value >= heap[parent][0])
            break;

        s(cur, parent);
        cur = parent;
    }
};
```

```
free(t); fix();
}
bigint& fix(int m = 0) {
    n = max(m, n);
    int sign = 0;
    for (int i = 1, e = 0; i <= n || e && (n = i); i++) {
        v[i] += e; e = v[i] / BASE; v[i] %= BASE;
        if (v[i]) sign = (v[i] > 0) ? 1 : -1;
}

for (int i = n - 1; i > 0; i--)
        if (v[i] * sign < 0) { v[i] += sign * BASE; v[i+1] -= sign; }
    while (n && !v[n]) n--;
    return *this;
}

int cmp(const bigint& x = 0) const {
    int i = max(n, x.n), t = 0;
    while (1) if ((t = ::cmp(v[i], x.v[i])) || i-- == 0) return t;
}</pre>
```

```
bool operator <(const bigint& x) const { return cmp(x) < 0; }</pre>
bool operator == (const bigint& x) const { return cmp(x) == 0; }
bool operator !=(const bigint& x) const { return cmp(x) != 0; }
operator string() const {
   ostringstream s; s << v[n];
   for (int i = n - 1; i > 0; i--) {
      s.width(DIG); s.fill('0'); s << abs(v[i]);
   return s.str();
friend ostream& operator <<(ostream& o, const bigint& x) {</pre>
   return o << (string) x;</pre>
bigint& operator += (const bigint& x) {
   for (int i = 1; i <= x.n; i++) v[i] += x.v[i];</pre>
   return fix(x.n);
bigint operator +(const bigint& x) { return bigint(*this) += x; }
bigint& operator -= (const bigint& x) {
   for (int i = 1; i <= x.n; i++) v[i] -= x.v[i];</pre>
   return fix(x.n);
bigint operator - (const bigint & x) { return bigint (*this) -= x; }
bigint operator -() { bigint r = 0; return r -= *this; }
void ams(const bigint x, int m, int b) { //* *this += (x * m) << b;}
   for (int i = 1, e = 0; (i \le x, n \mid \mid e) && (n = i + b); i++) {
      v[i+b] += x.v[i] * m + e; e = v[i+b] / BASE; v[i+b] %= BASE;
bigint operator *(const bigint& x) const {
   bigint r;
   for (int i = 1; i <= n; i++) r.ams(x, v[i], i-1);</pre>
   return r;
bigint& operator *=(const bigint& x) { return *this = *this * x; }
```

```
// cmp(x/y) == cmp(x) * cmp(y); cmp(x % y) == cmp(x);
  bigint div(const bigint& x) {
      if (x == 0) return 0;
      bigint q; q.n = max(n - x.n + 1, 0);
      int d = x.v[x.n] * BASE + x.v[x.n-1];
      for (int i = q.n; i > 0; i--) {
         int j = x.n + i - 1;
         q.v[i] = int((v[j] * double(BASE) + v[j-1]) / d);
         ams (x, -q.v[i], i-1);
         if (i == 1 || i == 1) break;
         v[j-1] += BASE * v[j]; v[j] = 0;
      fix(x.n); return q.fix();
  bigint& operator /=(const bigint& x) { return *this = div(x); }
   bigint& operator %=(const bigint& x) { div(x); return *this; }
   bigint operator / (const bigint & x) { return bigint (*this).div(x); }
   bigint operator %(const bigint& x) { return bigint(*this) %= x; }
   bigint pow(int x) {
      if (x < 0) return (*this == 1 | | *this == -1) ? pow(-x) : 0;
      bigint r = 1;
      for (int i = 0; i < x; i++) r *= *this;</pre>
      return r;
  bigint root(int x) {
      if (cmp() == 0 | | cmp() < 0 && x % 2 == 0) return 0;</pre>
      if (*this == 1 || x == 1) return *this;
      if (cmp() < 0) return -(-*this).root(x);</pre>
      bigint a = 1, d = *this;
      while (d != 1) {
         bigint b = a + (d /= 2);
         if (cmp(b.pow(x)) >= 0) { d += 1; a = b; }
      return a;
};
```

6. String algorithms

6.1. Kärkkäinen-Sanders' suffix array algorithm. Hash: f52d447fe031ca31834ce0b3c4c828f9

```
bool k_cmp(int a1, int b1, int a2, int b2, int a3 = 0, int b3 = 0) {
   return a1 != b1 ? a1 < b1 : (a2 != b2 ? a2 < b2 : a3 < b3);
}
int bucket[MAXSZ+1], tmp[MAXSZ];
template<class T> void k_radix(T keys, int *in, int *out,
```

```
int off, int n, int k) {
   memset(bucket, 0, sizeof(int) * (k+1));
   for (int j = 0; j < n; j++)</pre>
      bucket[keys[in[j]+off]]++;
   for (int j = 0, sum = 0; j \le k; j++)
      sum += bucket[j], bucket[j] = sum - bucket[j];
   for(int j = 0; j < n; j++)
      out[bucket[keys[in[j]+off]]++] = in[j];
int m0[MAXSZ/3+1];
vector<int> k_rec(const vector<int>& v, int k) {
   int n = v.size()-3, sz = (n+2)/3, sz2 = sz + n/3;
   if(n < 2) return vector<int>(n);
   vector<int> sub(sz2+3);
   for (int i = 1, j = 0; j < sz2; i += i%3, j++)
      sub[j] = i;
   k_radix(v.begin(), &sub[0], tmp, 2, sz2, k);
   k radix(v.begin(), tmp, &sub[0], 1, sz2, k);
   k_radix(v.begin(), &sub[0], tmp, 0, sz2, k);
   int last[3] = \{-1, -1, -1\}, unique = 0;
   for(int i = 0; i < sz2; i++) {</pre>
      bool diff = false;
      for(int j = 0; j < 3; last[j] = v[tmp[i]+j], j++)</pre>
         diff |= last[j] != v[tmp[i]+j];
      unique += diff;
      if(tmp[i]%3 == 1) sub[tmp[i]/3] = unique;
      else sub[tmp[i]/3 + sz] = unique;
   vector<int> rec;
   if(unique < sz2) {</pre>
      rec = k_rec(sub, unique);
      rec.resize(sz2+sz);
      for(int i = 0; i < sz2; i++) sub[rec[i]] = i+1;</pre>
   } else {
      rec.resize(sz2+sz);
      for(int i = 0; i < sz2; i++) rec[sub[i]-1] = i;</pre>
   for (int i = 0, j = 0; j < sz; i++)
```

```
if(rec[i] < sz)</pre>
         tmp[j++] = 3*rec[i];
   k_{radix}(v.begin(), tmp, m0, 0, sz, k);
   for (int i = 0; i < sz2; i++)
      rec[i] = rec[i] < sz ? 3*rec[i] + 1 : 3*(rec[i] - sz) + 2;
   int prec = sz2-1, p0 = sz-1, pret = sz2+sz-1;
   while(prec >= 0 && p0 >= 0)
      if(rec[prec]%3 == 1 && k_cmp(v[m0[p0]], v[rec[prec]],
                            sub[m0[p0]/3], sub[rec[prec]/3+sz]) | |
        rec[prec] %3 == 2 \&\& k\_cmp(v[m0[p0]], v[rec[prec]],
                            v[m0[p0]+1], v[rec[prec]+1],
                            sub[m0[p0]/3+sz], sub[rec[prec]/3+1])
         rec[pret--] = rec[prec--];
      else
         rec[pret--] = m0[p0--];
  if(p0 >= 0) memcpy(&rec[0], m0, sizeof(int) * (p0+1));
  if(n%3==1) rec.erase(rec.begin());
   return rec;
vector<int> karkkainen(const string& s) {
   int n = s.size(), cnt = 1;
  vector<int> v(n + 3);
   for(int i = 0; i < n; i++) v[i] = i;</pre>
  k_radix(s.begin(), &v[0], tmp, 0, n, 256);
   for (int i = 0; i < n; cnt += (i+1 < n && s[tmp[i+1]] != s[tmp[i]]), i++)
     v[tmp[i]] = cnt;
   return k_rec(v, cnt);
vector<int> lcp(const string& s, const vector<int>& sa) {
   int n = sa.size();
  vector<int> prm(n), ans(n-1);
   for(int i = 0; i < n; i++) prm[sa[i]] = i;</pre>
   for (int h = 0, i = 0; i < n; i++)</pre>
      if(prm[i]) {
         int j = sa[prm[i]-1], ij = max(i, j);
         while (ij + h < n \&\& s[i+h] == s[j+h]) h++;
         ans[prm[i]-1] = h;
         if(h) h--;
```

return ans;

6.2. Morris-Pratt's algorithm. Hash: 0234dfb6e26b39d35704838d84f1e86e

```
int pi[MAXSZ], res[MAXSZ], nres;

void morris_pratt(string text, string pattern) {
    nres = 0;
    pi[0] = -1;
    for(int i = 1; i < pattern.size(); ++i) {
        pi[i] = pi[i-1];
        while(pi[i] >= 0 && pattern[pi[i] + 1] != pattern[i])
            pi[i] = pi[pi[i]];
        if(pattern[pi[i] + 1] == pattern[i]) ++pi[i];
    }
}
```

```
int k = -1; //k + 1 eh o tamanho do match atual
for(int i = 0; i < text.size(); ++i) {
    while(k >= 0 && pattern[k + 1] != text[i])
        k = pi[k];
    if(pattern[k + 1] == text[i]) ++k;
    if(k + 1 == pattern.size()) {
        res[nres++] = i - k;
        k = pi[k];
    }
}
```

6.3. Aho-Corasick's algorithm (UFPE). Hash: 273f4391174d22898bfe3f2415f95915

```
struct No {
   int fail;
   vector< pair<int,int> > out; // num e tamanho do padrao
   //bool marc; // p/ decisao
  map<char, int> lista;
   int next; // aponta para o proximo sufixo que tenha out.size > 0
};
No arvore[1000003]; // quantida maxima de nos
//bool encontrado[1005]; // quantidade maxima de padroes, p/ decisao
int qtdNos, qtdPadroes;
// Funcao para inicializar
void inic() {
   arvore[0].fail = -1;
   arvore[0].lista.clear();
   arvore[0].out.clear();
   arvore[0].next = -1;
   qtdNos = 1;
   qtdPadroes = 0;
   //arvore[0].marc = false; // p/ decisao
   //memset(encontrado, false, sizeof(encontrado)); // p/ decisao
// Funcao para adicionar um padrao
```

```
void adicionar(char *padrao) {
  int no = 0, len = 0;
   for (int i = 0 ; padrao[i] ; i++, len++) {
      if (arvore[no].lista.find(padrao[i]) == arvore[no].lista.end()) {
         arvore[gtdNos].lista.clear(); arvore[gtdNos].out.clear();
         //arvore[gtdNos].marc = false; // p/ decisao
        arvore[no].lista[padrao[i]] = qtdNos;
         no = qtdNos++;
      } else no = arvore[no].lista[padrao[i]];
   arvore[no].out.push_back(pair<int,int>(qtdPadroes++,len));
// Ativar Aho-corasick, ajustando funcoes de falha
void ativar() {
   int no, v, f, w;
   queue<int> fila;
   for (map<char,int>::iterator it = arvore[0].lista.begin();
      it != arvore[0].lista.end(); it++) {
      arvore[no = it->second].fail = 0;
      arvore[no].next = arvore[0].out.size() ? 0 : -1;
      fila.push(no);
   while (!fila.empty()) {
```

```
no = fila.front(); fila.pop();
      for (map<char,int>::iterator it=arvore[no].lista.begin();
         it!=arvore[no].lista.end(); it++) {
         char c = it->first;
         v = it->second;
         fila.push(v);
         f = arvore[no].fail;
         while (arvore[f].lista.find(c) == arvore[f].lista.end()) {
            if (f == 0) { arvore[0].lista[c] = 0; break; }
            f = arvore[f].fail;
         w = arvore[f].lista[c];
         arvore[v].fail = w;
         arvore[v].next = arvore[w].out.size() ? w : arvore[w].next;
// Buscar padroes no aho-corasik
void buscar(char *input) {
   int v, no = 0;
```

7. Useful mathematical facts

7.1. Prime counting function $(\pi(x))$. The prime counting function is asymptotic to $\frac{x}{\log x}$, by the prime number theorem.

	X	10	10^{2}	10^{3}	10^{4}	10^{5}	10^{6}	10^{7}	10^{8}
Ì	$\pi(x)$	4	25	168	1.229	9.592	78.498	664.579	5.761.455

7.2. Partition function. The partition function p(x) counts show many ways there are to write the integer x as a sum of integers.

X	36	37	38	39	40	41	42
p(x)	17.977	21.637	26.015	31.185	37.338	44.583	53.174
X	43	44	45	46	47	100	
p(x)	63.261	75.175	89.134	105.558	125.754	190.569.292	

7.3. Catalan numbers. Catalan numbers are defined by the recurrence:

$$C_{n+1} = \sum_{i=0}^{n} C_i C_{n-i}$$

A closed formula for Catalan numbers is:

$$C_n = \frac{1}{n+1} \binom{2n}{n} = \binom{2n}{n} - \binom{2n}{n+1}$$

7.4. Stirling numbers of the first kind. These are the number of permutations of I_n with exactly k disjoint cycles. They obey the recurrence:

7.5. Stirling numbers of the second kind. These are the number of ways to partition I_n into exactly k sets. They obey the recurrence:

$${n \brace k} = k {n-1 \brace k} + {n-1 \brace k-1}$$

A "closed" formula for it is:

$${n \brace k} = \frac{1}{k!} \sum_{j=0}^{k} (-1)^{k-j} {k \choose j} j^n$$

7.6. **Bell numbers.** These count the number of ways to partition I_n into subsets. They obey the recurrence:

$$\mathcal{B}_{n+1} = \sum_{k=0}^{n} \binom{n}{k} \mathcal{B}_k$$

X	5	6	7	8	9	10	11	12
\mathcal{B}_x	52	203	877	4.140	21.147	115.975	678.570	4.213.597

- 7.7. **Turán's theorem.** No graph with n vertices that is K_{r+1} -free can have more edges than the Turán graph: A k-partite complete graph with sets of size as equal as possible.
- 7.8. **Generating functions.** A list of generating functions for useful sequences:

$(1,1,1,1,1,1,\ldots)$	$\frac{1}{1-z}$
$(1,-1,1,-1,1,-1,\ldots)$	$\frac{1}{1+z}$
$(1,0,1,0,1,0,\ldots)$	$\frac{1}{1-z^2}$
$(1,0,\ldots,0,1,0,1,0,\ldots,0,1,0,\ldots)$	$\frac{1}{1-z^2}$
$(1,2,3,4,5,6,\ldots)$	$\frac{1}{(1-z)^2}$
$(1, \binom{m+1}{m}, \binom{m+2}{m}, \binom{m+3}{m}, \ldots)$	$\frac{1}{(1-z)^{m+1}}$
$(1,c,\binom{c+1}{2},\binom{c+2}{3},\ldots)$	$\frac{1}{(1-z)^c}$
$(1,c,c^2,c^3,\ldots)$	$\frac{1}{1-cz}$
$(0,1,\frac{1}{2},\frac{1}{3},\frac{1}{4},\ldots)$	$\ln \frac{1}{1-z}$

A neat manipulation trick is:

$$\frac{1}{1-z}G(z) = \sum_{n} \sum_{k \le n} g_k z^n$$

7.9. **Polyominoes.** How many free (rotation, reflection), one-sided (rotation) and fixed *n*-ominoes are there?

	n	3	4	5	6	7	8	9	10
	free	2	5	12	35	108	369	1.285	4.655
	one-sided	2	7	18	60	196	704	2.500	9.189
Ì	fixed	6	19	63	216	760	2.725	9.910	36.446

7.10. The twelvefold way (from Stanley). How many functions $f \colon N \to X$ are there?

N	X	Any f	Injective	Surjective
dist.	dist.	x^n	$(x)_n$	$x!\binom{n}{x}$
indist.	dist.	$\binom{x+n-1}{n}$	$\binom{x}{n}$	$\binom{n-1}{n-x}$
dist.	indist.	$\binom{n}{1} + \ldots + \binom{n}{x}$	$[n \leq x]$	$\binom{n}{k}$
indist.	indist.	$p_1(n) + \dots p_x(n)$	$[n \leq x]$	$p_x(n)$

Where $\binom{a}{b} = \frac{1}{b!}(a)_b$ and $p_x(n)$ is the number of ways to partition the integer n using x summands.

7.11. **Common integral substitutions.** And finally, a list of common substitutions:

$\int F(\sqrt{ax+b})dx$	$u = \sqrt{ax + b}$	$\frac{2}{a}\int uF(u)du$
$\int F(\sqrt{a^2-x^2})dx$	$x = a\sin u$	$a \int F(a\cos u)\cos u du$
$\int F(\sqrt{x^2+a^2})dx$	$x = a \tan u$	$a \int F(a \sec u) \sec^2 u du$
$\int F(\sqrt{x^2 - a^2})dx$	$x = a \sec u$	$a \int F(a \tan u) \sec u \tan u du$
$\int F(e^{ax})dx$	$u = e^{ax}$	$\frac{1}{a}\int \frac{F(u)}{u}du$
$\int F(\ln x)dx$	$u = \ln x$	$\int F(u)e^udu$

7.12. Table of non-trigonometric integrals. Some useful integrals are:

$\frac{1}{a} \arctan \frac{x}{a}$
$\frac{1}{2a} \ln \frac{x-a}{x+a}$
$\frac{1}{2a} \ln \frac{a+x}{a-x}$
$\arcsin \frac{x}{a}$
$\ln\left(u+\sqrt{x^2-a^2}\right)$
$\frac{1}{a}\operatorname{arcsec}\left \frac{u}{a}\right $
$-\frac{1}{a}\ln\left(\frac{a+\sqrt{x^2+a^2}}{x}\right)$
$-\frac{1}{a}\ln\left(\frac{a+\sqrt{a^2-x^2}}{x}\right)$

7.13. **Table of trigonometric integrals.** A list of common and not-so-common trigonometric integrals:

$\int \tan x dx$	$-\ln \cos x $
$\int \cot x dx$	$\ln \sin x $
$\int \sec x dx$	$\ln \sec x + \tan x $
$\int \csc x dx$	$\ln \csc x - \cot x $
$\int \sec^2 x dx$	$\tan x$
$\int \csc^2 x dx$	$\cot x$
$\int \sin^n x dx$	$\frac{-\sin^{n-1}x\cos x}{n} + \frac{n-1}{n}\int \sin^{n-2}x dx$
$\int \cos^n x dx$	$\frac{\cos^{n-1}x\sin x}{n} + \frac{n-1}{n}\int \cos^{n-2}x dx$
$\int \arcsin x dx$	$x \arcsin x + \sqrt{1 - x^2}$
$\int \arccos x dx$	$x \arccos x - \sqrt{1 - x^2}$
$\int \arctan x dx$	$x\arctan x - \frac{1}{2}\ln 1 - x^2 $

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