

ACM ICPC TEAM REFERENCE

2010 WORLD FINALS

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1. CONFIGURATION FILES AND SCRIPTS

1.1. **.emacs**. Hash: 11ccc2e5d31fb5624290adb958a589c5

```
(global-font-lock-mode t)
(setq transient-mark-mode t)

(global-set-key [f5] 'cxx-compile)
(require 'cc-mode)
(defun cxx-compile()
  (interactive)
```

```
(save-buffer)
(compile (concat "g++-g_-02_-o_" (file-name-sans-extension buffer-file-name)
  "_" buffer-file-name))
)

(add-hook 'c++-mode-hook '(lambda () (c-set-style "stroustrup")))
```

1.2. **.vimrc**. Hash: c1e8578e5f779285977a53cce7a48031

```
syn on
filetype on
filetype plugin on
filetype indent on
colorscheme koehler

set number
set shiftwidth=4
```

```
set ts=4

imap <C-Space> <C-P>
set cinkeys={,0},0),0#,!<Tab>,;,:,o,O,e
set indentkeys=!<Tab>,o,O

runtime mswin.vim
```

1.3. **Hash generator**. Hash: 0d22aecdd779fc370b30a2c628aff517c

```
#!/bin/sh
```

```
sed ' :a;N;$!ba;s/[_\n\t]//g' | md5sum | cut -d'_' -f1
```

1.4. Solution template. Hash: 91b0fffaa0504c01fe4cc05bc08561d0

```
#include <iostream>
#include <cstdio>
#include <algorithm>
#include <vector>
#include <set>
#include <queue>
#include <map>
#include <utility>
#include <cstring>
#include <cstdlib>
#include <cmath>
#include <cassert>
```

```
using namespace std;
```

```
typedef double TYPE;
const TYPE EPS = 1e-9;
const TYPE INF = 1e9;
```

```
inline int sgn(TYPE a) { return a > EPS ? 1 : (a < -EPS ? -1 : 0); }
inline int cmp(TYPE a, TYPE b) { return sgn(a - b); }
```

```
int main() {
    return 0;
}
```

2. GRAPH ALGORITHMS

2.1. Tarjan's SCC algorithm. Hash: f98d9589db68c8f1e8274cf53eb7f3bf

```
int lowest[MAXV], num[MAXV], visited[MAXV], comp[MAXV];
int prev_edge[MAXE], last_edge[MAXV], adj[MAXE], nedges;
int cur_num, cur_comp;
stack<int> visiting;
```

```
int t_init() {
    memset(last_edge, -1, sizeof last_edge);
    nedges = 0;
}
```

```
void t_edge(int v, int w) {
    prev_edge[nedges] = last_edge[v];
    adj[nedges] = w;
    last_edge[v] = nedges++;
}
```

```
int tarjan_dfs(int v) {
    lowest[v] = num[v] = cur_num++;
    visiting.push(v);

    visited[v] = 1;
    for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
        int w = adj[i];
        if(visited[w] == 0) lowest[v] = min(lowest[v], tarjan_dfs(w));
        else if(visited[w] == 1) lowest[v] = min(lowest[v], num[w]);
    }
```

```
    }

    if(lowest[v] == num[v]) {
        int last = -1;
        while(last != v) {
            comp[last = visiting.top()] = cur_comp;
            visited[last] = 2;
            visiting.pop();
        }
        cur_comp++;
    }
}
```

```
return lowest[v];
}
```

```
void tarjan_scc(int num_v = MAXV) {
    visiting = stack<int>();
    memset(visited, 0, sizeof visited);
    cur_num = cur_comp = 0;

    for(int i = 0; i < num_v; i++)
        if(!visited[i])
            tarjan_dfs(i);
}
```

2.2. Dinic's maximum flow algorithm. Hash: 4dd537effe7e233681c099912397839a

```

int last_edge[MAXV], cur_edge[MAXV], dist[MAXV];
int prev_edge[MAXE], cap[MAXE], flow[MAXE], adj[MAXE];
int nedges;

void d_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
}

void d_edge(int v, int w, int capacity, bool r = false) {
    prev_edge[nedges] = last_edge[v];
    cap[nedges] = capacity;
    adj[nedges] = w;
    flow[nedges] = 0;
    last_edge[v] = nedges++;
}

if(!r) d_edge(w, v, 0, true);
}

bool d_auxflow(int source, int sink) {
    queue<int> q;
    q.push(source);

    memset(dist, -1, sizeof dist);
    dist[source] = 0;
    memcpy(cur_edge, last_edge, sizeof last_edge);

    while(!q.empty()) {
        int v = q.front(); q.pop();
        for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
            if(cap[i] - flow[i] == 0) continue;

            if(dist[adj[i]] == -1) {
                dist[adj[i]] = dist[v] + 1;
                q.push(adj[i]);
            }

            if(adj[i] == sink) return true;
        }
    }
}

```

```

    }
}

return false;
}

inline int rev(int i) { return i ^ 1; }

int d_augmenting(int v, int sink, int c) {
    if(v == sink) return c;

    for(int& i = cur_edge[v]; i != -1; i = prev_edge[i]) {
        if(cap[i] - flow[i] == 0 || dist[adj[i]] != dist[v] + 1)
            continue;

        int val;
        if(val = d_augmenting(adj[i], sink, min(c, cap[i] - flow[i]))) {
            flow[i] += val;
            flow[rev(i)] -= val;
            return val;
        }
    }

    return 0;
}

int dinic(int source, int sink) {
    int ret = 0;
    while(d_auxflow(source, sink)) {
        int flow;
        while(flow = d_augmenting(source, sink, 0x3f3f3f3f))
            ret += flow;
    }

    return ret;
}

```

2.3. Successive shortest paths mincost maxflow algorithm. Hash: 6933692fe046f78da13b05166c7e6d23

```

int dist[MAXV], last_edge[MAXV], d_visited[MAXV], bg_prev[MAXV], pot[MAXV],
    capres[MAXV];

```

```

int prev_edge[MAXE], adj[MAXE], cap[MAXE], cost[MAXE], flow[MAXE];

```

```

int nedges;
priority_queue<pair<int, int> > d_q;

inline void bg_edge(int v, int w, int capacity, int cst, bool r = false) {
    prev_edge[nedges] = last_edge[v];
    adj[nedges] = w;
    cap[nedges] = capacity;
    flow[nedges] = 0;
    cost[nedges] = cst;
    last_edge[v] = nedges++;

    if(!r) bg_edge(w, v, 0, -cost, true);
}

inline int rev(int i) { return i ^ 1; }
inline int from(int i) { return adj[rev(i)]; }

inline void bg_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
    memset(pot, 0, sizeof pot);
}

void bg_dijkstra(int s, int num_nodes = MAXV) {
    memset(dist, 0x3f, sizeof dist);
    memset(d_visited, 0, sizeof d_visited);
    d_q.push(make_pair(dist[s] = 0, s));
    capres[s] = 0x3f3f3f3f;

    while(!d_q.empty()) {
        int v = d_q.top().second; d_q.pop();
        if(d_visited[v]) continue; d_visited[v] = true;

        for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {

```

```

            if(cap[i] - flow[i] == 0) continue;
            int w = adj[i], new_dist = dist[v] + cost[i] + pot[v] - pot[w];

            if(new_dist < dist[w]) {
                d_q.push(make_pair(-(dist[w] = new_dist), w));
                bg_prev[w] = rev(i);
                capres[w] = min(capres[v], cap[i] - flow[i]);
            }
        }
    }

pair<int, int> busacker_gowen(int src, int sink, int num_nodes = MAXV) {
    int retFlow = 0, retCost = 0;

    bg_dijkstra(src, num_nodes);
    while(dist[sink] < 0x3f3f3f3f) {
        int cur = sink;
        while(cur != src) {
            flow[bg_prev[cur]] -= capres[sink];
            flow[rev(bg_prev[cur])] += capres[sink];
            retCost += cost[rev(bg_prev[cur])] * capres[sink];
            cur = adj[bg_prev[cur]];
        }
        retFlow += capres[sink];

        for(int i = 0; i < MAXV; i++)
            pot[i] = min(pot[i] + dist[i], 0x3f3f3f3f);

        bg_dijkstra(src, num_nodes);
    }
    return make_pair(retFlow, retCost);
}

```

2.4. Gabow's general matching algorithm. Hash: 31f8b67cd2b16187c6733f42801ee2be

```

int prev_edge[MAXE], v[MAXE], w[MAXE], last_edge[MAXV];
int type[MAXV], label[MAXV], first[MAXV], mate[MAXV], nedges;
bool g_flag[MAXV], g_souter[MAXV];

void g_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
}

```

```

void g_edge(int a, int b) {
    prev_edge[nedges] = last_edge[a];
    v[nedges] = a;
    w[nedges] = b;
    last_edge[a] = nedges++;

    prev_edge[nedges] = last_edge[b];
}

```

```

    v[nedges] = b;
    w[nedges] = a;
    last_edge[b] = nedges++;
}

void g_label(int v, int join, int edge, queue<int>& outer) {
    if(v == join) return;
    if(label[v] == -1) outer.push(v);

    label[v] = edge;
    type[v] = 1;
    first[v] = join;

    g_label(first[label[mate[v]]], join, edge, outer);
}

void g_augment(int _v, int _w) {
    int t = mate[_v];
    mate[_v] = _w;

    if(mate[t] != _v) return;
    if(label[_v] == -1) return;

    if(type[_v] == 0) {
        mate[t] = label[_v];
        g_augment(label[_v], t);
    }
    else if(type[_v] == 1) {
        g_augment(v[label[_v]], w[label[_v]]);
        g_augment(w[label[_v]], v[label[_v]]);
    }
}

int gabow(int n) {
    memset(mate, -1, sizeof mate);
    memset(first, -1, sizeof first);

    int u = 0, ret = 0;
    for(int z = 0; z < n; z++) {
        if(mate[z] != -1) continue;

        memset(label, -1, sizeof label);
        memset(type, -1, sizeof type);
        memset(g_souter, 0, sizeof g_souter);

        label[z] = -1; type[z] = 0;

```

```

        queue<int> outer;
        outer.push(z);

        bool done = false;
        while(!outer.empty()) {
            int x = outer.front(); outer.pop();

            if(g_souter[x]) continue;
            g_souter[x] = true;

            for(int i = last_edge[x]; i != -1; i = prev_edge[i]) {
                if(mate[w[i]] == -1 && w[i] != z) {
                    mate[w[i]] = x;
                    g_augment(x, w[i]);
                    ret++;

                    done = true;
                    break;
                }
            }

            if(type[w[i]] == -1) {
                int v = mate[w[i]];
                if(type[v] == -1) {
                    type[v] = 0;
                    label[v] = x;
                    outer.push(v);

                    first[v] = w[i];
                }
                continue;
            }
        }

        int r = first[x], s = first[w[i]];
        if(r == s) continue;

        memset(g_flag, 0, sizeof g_flag);
        g_flag[r] = g_flag[s] = true;

        while(true) {
            if(s != -1) swap(r, s);
            r = first[label[mate[r]]];
            if(g_flag[r]) break; g_flag[r] = true;
        }

        g_label(first[x], r, i, outer);

```

```

        g_label(first[w[i]], r, i, outer);

    for(int c = 0; c < n; c++)
        if(type[c] != -1 && first[c] != -1 && type[first[c]] != -1)
            first[c] = r;
}

```

```

        if(done) break;
    }
}
return ret;
}

```

3. MATH

3.1. Fractions. Hash: 379fd408c3007c650c022fd4adfeabbd

```

struct frac {
    long long num, den;

    frac() : num(0), den(1) { };
    frac(long long num, long long den) { set_val(num, den); }
    frac(long long num) : num(num), den(1) { };

    void set_val(long long _num, long long _den) {
        num = _num/__gcd(_num, _den);
        den = _den/__gcd(_num, _den);
        if(den < 0) { num *= -1; den *= -1; }
    }

    void operator*=(frac f) { set_val(num * f.num, den * f.den); }
    void operator+=(frac f) { set_val(num * f.den + f.num * den, den * f.den); }
    void operator-=(frac f) { set_val(num * f.den - f.num * den, den * f.den); }
    void operator/=(frac f) { set_val(num * f.den, den * f.num); }
};

bool operator<(frac a, frac b) {

```

```

        if((a.den < 0) ^ (b.den < 0)) return a.num * b.den > b.num * a.den;
        return a.num * b.den < b.num * a.den;
    }

    std::ostream& operator<<(std::ostream& o, const frac f) {
        o << f.num << "/" << f.den;
        return o;
    }

    bool operator==(frac a, frac b) { return a.num * b.den == b.num * a.den; }
    bool operator!=(frac a, frac b) { return !(a == b); }
    bool operator<=(frac a, frac b) { return (a == b) || (a < b); }
    bool operator>=(frac a, frac b) { return !(a < b); }
    bool operator>(frac a, frac b) { return !(a <= b); }
    frac operator/(frac a, frac b) { frac ret = a; ret /= b; return ret; }
    frac operator*(frac a, frac b) { frac ret = a; ret *= b; return ret; }
    frac operator+(frac a, frac b) { frac ret = a; ret += b; return ret; }
    frac operator-(frac a, frac b) { frac ret = a; ret -= b; return ret; }
    frac operator-(frac f) { return 0 - f; }
}

```

3.2. Chinese remainder theorem. Hash: 06b5ebd5c44c204a4b11bbb76d09023d

```

struct t {
    long long a, b; int g;
    t(long long a, long long b, int g) : a(a), b(b), g(g) { }
    t swap() { return t(b, a, g); }
};

t egcd(int p, int q) {
    if(q == 0) return t(1, 0, p);

    t t2 = egcd(q, p % q);

```

```

    t2.a -= t2.b * (p/q);
    return t2.swap();
}

int crt(int a, int p, int b, int q) {
    t t2 = egcd(p, q); t2.a %= p*q; t2.b %= p*q;
    assert(t2.g == 1);
    int ret = ((b * t2.a)%(p*q) * p + (a * t2.b)%(p*q) * q) % (p*q);
    return ret >= 0 ? ret : ret + p*q;
}

```

3.3. Longest increasing subsequence. Hash: 0f80b5d3af188d8bf4d1cbe45a76b46d

```
vector<int> lis(vector<int>& seq) {
    int smallest_end[seq.size()+1], prev[seq.size()];
    smallest_end[1] = seq[0];

    int sz = 1;
    for(int i = 1; i < seq.size(); i++) {
        int lo = 0, hi = sz;
        while(lo < hi) {
            int mid = (lo + hi + 1)/2;
            if(seq[smallest_end[mid]] <= seq[i])
                lo = mid;
            else
                hi = mid - 1;
        }
    }
```

```
        prev[i] = smallest_end[lo];
        if(lo == sz)
            smallest_end[++sz] = i;
        else if(seq[i] < seq[smallest_end[lo+1]])
            smallest_end[lo+1] = i;
    }

    vector<int> ret;
    for(int cur = smallest_end[sz]; sz > 0; cur = prev[cur], sz--)
        ret.push_back(seq[cur]);
    reverse(ret.begin(), ret.end());

    return ret;
}
```

3.4. Simplex (Warsaw University). Hash: c687094970cf1953fd6f87a01adc6a95

```
const double EPS = 1e-9;
typedef long double T;
typedef vector<T> VT;
vector<VT> A;
VT b,c,res;
VI kt,N;
int m;
inline void pivot(int k,int l,int e){
    int x=kt[l]; T p=A[l][e];
    REP(i,k) A[l][i]/=p; b[l]/=p; N[e]=0;
    REP(i,m) if (i!=l) b[i]-=A[i][e]*b[l],A[i][x]=A[i][e]*-A[l][x];
    REP(j,k) if (N[j]){
        c[j]-=c[e]*A[l][j];
        REP(i,m) if (i!=l) A[i][j]-=A[i][e]*A[l][j];
    }
    kt[l]=e; N[x]=1; c[x]=c[e]*-A[l][x];
}

VT doit(int k){
    VT res; T best;
    while (1){
        int e=-1,l=-1; REP(i,k) if (N[i] && c[i]>EPS) {e=i; break;}
        if (e==-1) break;
        REP(i,m) if (A[i][e]>EPS && (l==-1 || best>b[i]/A[i][e]))
            best=b[i] l=i ]/A[i][e];
    }
```

```
        if (l==-1) /*ilimitado*/ return VT();
        pivot(k,l,e);
    }
    res.resize(k,0); REP(i,m) res[kt[i]]=b[i];
    return res;
}

VT simplex(vector<VT> &AA,VT &bb,VT &cc){
    int n=AA[0].size(),k;
    m=AA.size(); k=n+m+1; kt.resize(m); b=bb; c=cc; c.resize(n+m);
    A=AA; REP(i,m){ A[i].resize(k); A[i][n+i]=1; A[i][k-1]=-1; kt[i]=n+i;}
    N=VI(k,1); REP(i,m) N[kt[i]]=0;
    int pos=min_element(ALL(b))-b.begin();
    if (b[pos]<-EPS){
        c=VT(k,0); c[k-1]=-1; pivot(k,pos,k-1); res=doit(k);
        if (res[k-1]>EPS) /*impossivel*/ return VT();
        REP(i,m) if (kt[i]==k-1)
            REP(j,k-1) if (N[j] && (A[i][j]<-EPS || EPS<A[i][j])){
                pivot(k,i,j); break;
            }
        c=cc; c.resize(k,0); REP(i,m) REP(j,k) if (N[j]) c[j]-=c[kt[i]]*A[i][j];
    }
    res=doit(k-1); if (!res.empty()) res.resize(n);
    return res;
}
```

3.5. Romberg's method. Hash: a85facba1eac60c8909b04b552bd2222

```
long double romberg(int a, int b, double(*func)(double)) {
    long double approx[2][50];
    long double *cur=approx[1], *prev=approx[0];

    prev[0] = 1/2.0 * (b-a) * (func(a) + func(b));
    for(int it = 1; it < 25; it++, swap(cur, prev)) {
        if(it > 1 && cmp(prev[it-1], prev[it-2]) == 0)
            return prev[it-1];

        cur[0] = 1/2.0 * prev[0];
```

```
        long double div = (b-a)/pow(2, it);
        for(long double sample = a + div; sample < b; sample += 2 * div)
            cur[0] += div * func(a + sample);

        for(int j = 1; j <= it; j++)
            cur[j] = cur[j-1] + 1/(pow(4, it) - 1)*(cur[j-1] + prev[j-1]);
    }

    return prev[24];
}
```

3.6. Floyd's cycle detection algorithm. Hash: 4aaa3277ea9011cae6d9b1358521f02c

```
pair<int, int> floyd(int x0) {
    int t = f(x0), h = f(f(x0)), start = 0, length = 1;
    while(t != h)
        t = f(t), h = f(f(h));

    h = t; t = x0;
    while(t != h)
        t = f(t), h = f(h), start++;
```

```
    h = f(t);
    while(t != h)
        h = f(h), length++;

    return make_pair(start, length);
}
```

3.7. Pollard's rho algorithm. Hash: ad4ee1d4afc564b2c55f90d6269994c4

```
long long pollard_r, pollard_n;

inline long long f(long long val) { return (val*val + pollard_r) % pollard_n; }
inline long long myabs(long long a) { return a >= 0 ? a : -a; }

long long pollard(long long n) {
    srand(unsigned(time(0)));
    pollard_n = n;

    long long d = 1;
    do {
```

```
        d = 1;
        pollard_r = rand() % n;

        long long x = 2, y = 2;
        while(d == 1)
            x = f(x), y = f(f(y)), d = __gcd(myabs(x-y), n);
    } while(d == n);

    return d;
}
```

3.8. Miller-Rabin's algorithm. Hash: ef42ec97d363aa518dc87efc6e7c1b8d

```
int fastpow(int base, int d, int n) {
```

```
    int ret = 1;
```



```

    for(long long pow = base; d > 0; d >= 1, pow = (pow * pow) % n)
        if(d & 1)
            ret = (ret * pow) % n;
    return ret;
}

bool miller_rabin(int n, int base) {
    if(n <= 1) return false;
    if(n % 2 == 0) return n == 2;

    int s = 0, d = n - 1;
    while(d % 2 == 0) d /= 2, s++;

    int base_d = fastpow(base, d, n);
    if(base_d == 1) return true;

```

```

    int base_2r = base_d;

    for(int i = 0; i < s; i++) {
        if(base_2r == 1) return false;
        if(base_2r == n - 1) return true;
        base_2r = (long long)base_2r * base_2r % n;
    }

    return false;
}

bool isprime(int n) {
    if(n == 2 || n == 7 || n == 61) return true;
    return miller_rabin(n, 2) && miller_rabin(n, 7) && miller_rabin(n, 61);
}

```

3.9. Polynomials (PUC-Rio). Hash: d69d1ad494e487327d2338e69eccfa2f

```

typedef complex<double> cdouble;
int cmp(cdouble x, cdouble y = 0) {
    return cmp(abs(x), abs(y));
}

const int TAM = 200;
struct poly {
    cdouble poly[TAM]; int n;
    poly(int n = 0): n(n) { memset(p, 0, sizeof(p)); }
    cdouble& operator [] (int i) { return p[i]; }
    poly operator ~() {
        poly r(n-1);
        for (int i = 1; i <= n; i++)
            r[i-1] = p[i] * cdouble(i);
        return r;
    }
}

pair<poly, cdouble> ruffini(cdouble z) {
    if (n == 0) return make_pair(poly(), 0);
    poly r(n-1);
    for (int i = n; i > 0; i--) r[i-1] = r[i] * z + p[i];
    return make_pair(r, r[0] * z + p[0]);
}

cdouble operator () (cdouble z) { return ruffini(z).second; }

cdouble find_one_root(cdouble x) {
    poly p0 = *this, p1 = ~p0, p2 = ~p1;
    int m = 1000;

```

```

    while (m--) {
        cdouble y0 = p0(x);
        if (cmp(y0) == 0) break;
        cdouble G = p1(x) / y0;
        cdouble H = G * G - p2(x) - y0;
        cdouble R = sqrt(cdouble(n-1) * (H * cdouble(n) - G * G));
        cdouble D1 = G + R, D2 = G - R;
        cdouble a = cdouble(n) / (cmp(D1, D2) > 0 ? D1 : D2);
        x -= a;
        if (cmp(a) == 0) break;
    }
    return x;
}

vector<cdouble> roots() {
    poly q = *this;
    vector<cdouble> r;
    while (q.n > 1) {
        cdouble z(rand() / double(RAND_MAX), rand() / double(RAND_MAX));
        z = q.find_one_root(z); z = find_one_root(z);
        q = q.ruffini(z).first;
        r.push_back(z);
    }
    return r;
}
};

```

4. GEOMETRY

4.1. Point class. Hash: 66e85d5b140956c47aa31754eab18864

```

struct pt {
    TYPE x, y;
    pt(TYPE x = 0, TYPE y = 0) : x(x), y(y) { }

    bool operator==(pt p) { return cmp(x, p.x) == 0 && cmp(y, p.y) == 0; }
    bool operator<(pt p) const {
        return cmp(x, p.x) ? cmp(x, p.x) < 0 : cmp(y, p.y) < 0;
    }
    bool operator<=(pt p) { return *this < p || *this == p; }
    TYPE operator||(pt p) { return x*p.x + y*p.y; }
    TYPE operator%(pt p) { return x*p.y - y*p.x; }
    pt operator~() { return pt(x, -y); }
    pt operator+(pt p) { return pt(x + p.x, y + p.y); }
    pt operator-(pt p) { return pt(x - p.x, y - p.y); }
    pt operator*(pt p) { return pt(x*p.x - y*p.y, x*p.y + y*p.x); }
    pt operator/(TYPE t) { return pt(x/t, y/t); }
    pt operator/(pt p) { return (*this * ~p)/(p||p); }
};
const pt I = pt(0,1);

```

4.2. Intersection primitives. Hash: ab780978106a5c062b8f7a129ebc9196

```

bool in_rect(pt a, pt b, pt c) {
    return sgn(c.x - min(a.x, b.x)) >= 0 && sgn(max(a.x, b.x) - c.x) >= 0 &&
        sgn(c.y - min(a.y, b.y)) >= 0 && sgn(max(a.y, b.y) - c.y) >= 0;
}
bool ps_isects(pt a, pt b, pt c) { return ccw(a,b,c) == 0 && in_rect(a,b,c); }

bool ss_isects(pt a, pt b, pt c, pt d) {
    if (ccw(a,b,c)*ccw(a,b,d) == -1 && ccw(c,d,a)*ccw(c,d,b) == -1) return true;
    return ps_isects(a, b, c) || ps_isects(a, b, d) ||
        ps_isects(c, d, a) || ps_isects(c, d, b);
}

```

4.3. Polygon primitives. Hash: fba20bb1645bf37ab6c9b309d3850a7d

```

double p_area(vector<pt>& pol) {
    double ret = 0;
    for(int i = 0; i < pol.size(); i++)

```

```

struct circle {
    pt c; TYPE r;
    circle(pt c, TYPE r) : c(c), r(r) { }
};

TYPE norm(pt a) { return a||a; }
TYPE abs(pt a) { return sqrt(a||a); }
TYPE dist(pt a, pt b) { return abs(a - b); }
TYPE area(pt a, pt b, pt c) { return (a-c)%(b-c); }
int ccw(pt a, pt b, pt c) { return sgn(area(a, b, c)); }
pt unit(pt a) { return a/abs(a); }
double arg(pt a) { return atan2(a.y, a.x); }
pt f_polar(TYPE mod, double ang) { return pt(mod * cos(ang), mod * sin(ang)); }
inline int g_mod(int i, int n) { if(i == n) return 0; return i; }

ostream& operator<<(ostream& o, pt p) {
    return o << "(" << p.x << "," << p.y << ")";
}

```

```

pt parametric_isect(pt p, pt v, pt q, pt w) {
    double t = ((q-p)%w)/(v%w);
    return p + v*t;
}

pt ss_isect(pt p, pt q, pt r, pt s) {
    pt isect = parametric_isect(p, q-p, r, s-r);
    if(ps_isects(p, q, isect) && ps_isects(r, s, isect)) return isect;
    return pt(1/0.0, 1/0.0);
}

```

```

    ret += pol[i] % pol[g_mod(i+1, pol.size())];
    return ret/2;
}

```

```
int point_polygon(pt p, vector<pt>& pol) {
    int n = pol.size(), count = 0;

    for(int i = 0; i < n; i++) {
        int il = g_mod(i+1, n);
```

```
        if (ps_isects(pol[i], pol[il], p)) return -1;
        else if (((sgn(pol[i].y - p.y) == 1) != (sgn(pol[il].y - p.y) == 1)) &&
            ccw(pol[i], p, pol[il]) == sgn(pol[i].y - pol[il].y)) count++;
    }
    return count % 2;
}
```

4.4. Miscellaneous primitives. Hash: be051245293a9db9c991d414c598e854

```
bool point_circle(pt p, circle c) {
    return cmp(abs(p - c.c), c.r) <= 0;
}

double ps_distance(pt p, pt a, pt b) {
    p = p - a; b = b - a;
    double coef = min(max((b||p)/(b||b), TYPE(0)), TYPE(1));
    return abs(p - b*coef);
}
```

```
pt circumcenter(pt a, pt b, pt c) {
    return parametric_isect((b+a)/2, (b-a)*I, (c+a)/2, (c-a)*I);
}

bool compy(pt a, pt b) {
    return cmp(a.y, b.y) ? cmp(a.y, b.y) < 0 : cmp(a.x, b.x) < 0;
}

bool compx(pt a, pt b) { return a < b; }
```

4.5. Smallest enclosing circle. Hash: 4e41d94c106dee349b45ca542ff0a532

```
circle enclosing_circle(vector<pt>& pts) {
    srand(unsigned(time(0)));
    random_shuffle(pts.begin(), pts.end());

    circle c(pt(), -1);
    for(int i = 0; i < pts.size(); i++) {
        if(point_circle(pts[i], c)) continue;
        c = circle(pts[i], 0);
        for(int j = 0; j < i; j++) {
            if(point_circle(pts[j], c)) continue;
```

```
        c = circle((pts[i] + pts[j])/2, abs(pts[i] - pts[j])/2);
        for(int k = 0; k < j; k++) {
            if(point_circle(pts[k], c)) continue;
            pt center = circumcenter(pts[i], pts[j], pts[k]);
            c = circle(center, abs(center - pts[i])/2);
        }
    }
    return c;
}
```

4.6. Convex hull. Hash: a7f921d07f1b9b8a0053a0833329ddcf

```
pt pivot;

bool hull_comp(pt a, pt b) {
    int turn = ccw(a, b, pivot);
    return turn == 1 || (turn == 0 && cmp(norm(a), norm(b)) < 0);
}

vector<pt> hull(vector<pt> pts) {
```

```
    if(pts.size() <= 1) return pts;
    vector<pt> ret;

    int mini = 0;
    for(int i = 1; i < pts.size(); i++)
        if(pts[i] < pts[mini])
            mini = i;
```

```

pivot = pts[mini];
swap(pts[0], pts[mini]);
sort(pts.begin() + 1, pts.end(), hull_comp);

ret.push_back(pts[0]);
ret.push_back(pts[1]);
int sz = 2;

```

```

for(int i = 2; i < pts.size(); i++) {
    while(sz >= 2 && ccw(ret[sz-2], ret[sz-1], pts[i]) <= 0)
        ret.pop_back(), sz--;
    ret.push_back(pts[i]), sz++;
}

return ret;
}

```

4.7. Closest pair of points. Hash: 251ad75a3af2d531a0cbb4e8138d3aef

```

pair<pt, pt> closest_points_rec(vector<pt>& px, vector<pt>& py) {
    pair<pt, pt> ret;
    double d;

    if(px.size() <= 3) {
        double best = 1e10;
        for(int i = 0; i < px.size(); i++)
            for(int j = i + 1; j < px.size(); j++)
                if(dist(px[i], px[j]) < best) {
                    ret = make_pair(px[i], px[j]);
                    best = dist(px[i], px[j]);
                }

        return ret;
    }

    pt split = px[(px.size() - 1)/2];
    vector<pt> qx, qy, rx, ry;
    for(int i = 0; i < px.size(); i++)
        if(px[i] <= split) qx.push_back(px[i]);
        else rx.push_back(px[i]);

    for(int i = 0; i < py.size(); i++)
        if(py[i] <= split) qy.push_back(py[i]);
        else ry.push_back(py[i]);

    ret = closest_points_rec(qx, qy);
    pair<pt, pt> rans = closest_points_rec(rx, ry);
    double delta = dist(ret.first, ret.second);

    if((d = dist(rans.first, rans.second)) < delta) {

```

```

        delta = d;
        ret = rans;
    }

    vector<pt> s;
    for(int i = 0; i < py.size(); i++)
        if(cmp(abs(py[i].x - split.x), delta) <= 0)
            s.push_back(py[i]);

    for(int i = 0; i < s.size(); i++)
        for(int j = i + 1; j <= 15 && i + j < s.size(); j++)
            if((d = dist(s[i], s[j])) < delta) {
                delta = d;
                ret = make_pair(s[i], s[j]);
            }

    return ret;
}

pair<pt, pt> closest_points(vector<pt> pts) {
    if(pts.size() == 1) return make_pair(pt(-INF, -INF), pt(INF, INF));

    sort(pts.begin(), pts.end());
    for(int i = 0; i + 1 < pts.size(); i++)
        if(pts[i] == pts[i+1])
            return make_pair(pts[i], pts[i+1]);

    vector<pt> py = pts;
    sort(py.begin(), py.end(), compy);
    return closest_points_rec(pts, py);
}

```

4.8. Kd-tree. Hash: de78e67c89c057ba920d2060641a7f48

```

int tree[4*MAXSZ], val[4*MAXSZ];
TYPE split[4*MAXSZ];
vector<pt> pts;

void kd_recurse(int root, int left, int right, bool x) {
    if(left == right) {
        tree[root] = left;
        val[root] = 1;
        return;
    }

    int mid = (right+left)/2;
    nth_element(pts.begin() + left, pts.begin() + mid,
        pts.begin() + right + 1, x ? compx : compy);
    split[root] = x ? pts[mid].x : pts[mid].y;

    kd_recurse(2*root+1, left, mid, !x);
    kd_recurse(2*root+2, mid+1, right, !x);

    val[root] = val[2*root+1] + val[2*root+2];
}

void kd_build() {
    memset(tree, -1, sizeof tree);
    kd_recurse(0, 0, pts.size() - 1, true);
}

int kd_query(int root, TYPE a, TYPE b, TYPE c, TYPE d, TYPE ca = -INF,
    TYPE cb = INF, TYPE cc = -INF, TYPE cd = INF, bool x) {
    if(a <= ca && cb <= b && c <= cc && cd <= d) {
        return val[root];
    }

    if(tree[root] != -1)
        return a <= pts[tree[root]].x && pts[tree[root]].x <= b &&
            c <= pts[tree[root]].y && pts[tree[root]].y <= d ? val[root] : 0;
}

```

4.9. Range tree. Hash: ef9df10aeb8ecbb4a515100657f2468a

```

vector<pt> pts, tree[MAXSZ];
vector<TYPE> xs;
vector<int> lnk[MAXSZ][2];

```

```

int ret = 0;
if(x) {
    if(a <= split[root])
        ret += kd_query(2*root+1, a, b, c, d, ca, split[root], cc, cd, !x);
    if(split[root] <= b)
        ret += kd_query(2*root+2, a, b, c, d, split[root], cb, cc, cd, !x);
}
else {
    if(c <= split[root])
        ret += kd_query(2*root+1, a, b, c, d, ca, cb, cc, split[root], !x);
    if(split[root] <= d)
        ret += kd_query(2*root+2, a, b, c, d, ca, cb, split[root], cd, !x);
}
return ret;
}

pt kd_neighbor(int root, pt a, bool x) {
    if(tree[root] != -1)
        return a == pts[tree[root]] ? pt(2e9, 2e9) : pts[tree[root]];

    TYPE num = x ? a.x : a.y;
    int term = num <= split[root] ? 1 : 2;
    pt ret;

    TYPE d = norm(a - (ret = kd_neighbor(2*root + term, a, !x)));
    if((split[root] - num)*(split[root] - num) < d) {
        pt ret2 = kd_neighbor(2*root + 3 - term, a, !x);
        if(norm(a - ret2) < d)
            ret = ret2;
    }

    return ret;
}

```

```

int rt_recurse(int root, int left, int right) {
    if(left == right) {
        vector<pt>::iterator it;
        it = lower_bound(pts.begin(), pts.end(), pt(xs[left], -INF));
    }
}

```

```

    for(; it != pts.end() && it->x == xs[left]; it++)
        tree[root].push_back(*it);

    sort(tree[root].begin(), tree[root].end(), compy);
    return tree[root].size();
}

int mid = (left + right)/2, cl = 2*root + 1, cr = cl + 1;
int sz1 = rt_recurse(cl, left, mid);
int sz2 = rt_recurse(cr, mid + 1, right);

int l = 0, r = 0, llink = 0, rlink = 0; pt last;
while(l < sz1 || r < sz2) {
    if(r == sz2 || (l < sz1 && compy(tree[cl][l], tree[cr][r])))
        tree[root].push_back(last = tree[cl][l++]);
    else tree[root].push_back(last = tree[cr][r++]);

    while(llink < tree[cl].size() && compy(tree[cl][llink], last))
        llink++;
    while(rlink < tree[cr].size() && compy(tree[cr][rlink], last))
        rlink++;

    lnk[root][0].push_back(llink);
    lnk[root][1].push_back(rlink);
}

lnk[root][0].push_back(tree[cl].size());
lnk[root][1].push_back(tree[cr].size());

return tree[root].size();

```

```

}

void rt_build() {
    sort(pts.begin(), pts.end());
    for(int i = 0; i < pts.size(); i++) xs.push_back(pts[i].x);
    rt_recurse(0, 0, xs.size() - 1);
}

int rt_query(int root, int l, int r, TYPE a, TYPE b, TYPE c, TYPE d,
             int posl = -1, int posr = -1) {
    if(root == 0 && posl == -1) {
        posl = lower_bound(tree[0].begin(), tree[0].end(), pt(a, c), compy)
            - tree[0].begin();
        posr = upper_bound(tree[0].begin(), tree[0].end(), pt(b, d), compy)
            - tree[0].begin();
    }

    if(a <= xs[l] && xs[r] <= b)
        return posr - posl;
    if(posl >= tree[root].size()) return 0;

    int mid = (l + r)/2, ret = 0;
    if(a <= xs[mid])
        ret += rt_query(2*root+1, l, mid, a, b, c, d,
                       lnk[root][0][posl], lnk[root][0][posr]);
    if(xs[mid+1] <= b)
        ret += rt_query(2*root+2, mid+1, r, a, b, c, d,
                       lnk[root][1][posl], lnk[root][1][posr]);
    return ret;
}

```

5. DATA STRUCTURES

5.1. Treap. Hash: 2199b72803301716616a462d9d5e9a66

```

typedef int TYPE;

class treap {
public:
    treap *left, *right;
    int priority, sons;
    TYPE value;

    treap(TYPE value) : left(NULL), right(NULL), value(value), sons(0) {
        priority = rand();
    }

```

```

    }

    ~treap() {
        if(left) delete left;
        if(right) delete right;
    }
};

treap* find(treap* t, TYPE val) {
    if(!t) return NULL;

```

```

    if(val == t->value) return t;

    if(val < t->value) return find(t->left, val);
    if(val > t->value) return find(t->right, val);
}

void rotate_to_right(treap* &t) {
    treap* n = t->left;
    t->left = n->right;
    n->right = t;
    t = n;
}

void rotate_to_left(treap* &t) {
    treap* n = t->right;
    t->right = n->left;
    n->left = t;
    t = n;
}

void fix_augment(treap* t) {
    if(!t) return;
    t->sons = (t->left ? t->left->sons + 1 : 0) +
        (t->right ? t->right->sons + 1 : 0);
}

void insert(treap* &t, TYPE val) {
    if(!t)
        t = new treap(val);
    else

```

```

        insert(val <= t->value ? t->left : t->right, val);

    if(t->left && t->left->priority > t->priority)
        rotate_to_right(t);
    else if(t->right && t->right->priority > t->priority)
        rotate_to_left(t);

    fix_augment(t->left); fix_augment(t->right); fix_augment(t);
}

inline int p(treap* t) {
    return t ? t->priority : -1;
}

void erase(treap* &t, TYPE val) {
    if(!t) return;

    if(t->value != val)
        erase(val < t->value ? t->left : t->right, val);
    else {
        if(!t->left && !t->right)
            delete t, t = NULL;
        else {
            p(t->left) < p(t->right) ? rotate_to_left(t) : rotate_to_right(t);
            erase(t, val);
        }
    }

    fix_augment(t->left); fix_augment(t->right); fix_augment(t);
}

```

5.2. Heap. Hash: e334218955a73d1286ad0fc19e84b642

```

struct heap {
    int heap[MAXV][2], v2n[MAXV];
    int size;

    void init(int sz) __attribute__((always_inline)) {
        memset(v2n, -1, sizeof(int) * sz);
        size = 0;
    }

    void swap(int& a, int& b) __attribute__((always_inline)) {
        int temp = a;
        a = b;

```

```

        b = temp;
    }

    void s(int a, int b) __attribute__((always_inline)) {
        swap(v2n[heap[a][1]], v2n[heap[b][1]]);
        swap(heap[a][0], heap[b][0]);
        swap(heap[a][1], heap[b][1]);
    }

    int extract_min() {
        int ret = heap[0][1];
        s(0, --size);

```

```

int cur = 0, next = 2;
while(next < size) {
    if(heap[next][0] > heap[next - 1][0])
        next--;
    if(heap[next][0] >= heap[cur][0])
        break;

    s(next, cur);
    cur = next;
    next = 2*cur + 2;
}
if(next == size && heap[next - 1][0] < heap[cur][0])
    s(next - 1, cur);

return ret;
}

void decrease_key(int vertex, int new_value) __attribute__((always_inline))

```

```

{
    if(v2n[vertex] == -1) {
        v2n[vertex] = size;
        heap[size++][1] = vertex;
    }

    heap[v2n[vertex]][0] = new_value;

    int cur = v2n[vertex];
    while(cur >= 1) {
        int parent = (cur - 1)/2;
        if(new_value >= heap[parent][0])
            break;

        s(cur, parent);
        cur = parent;
    }
}
};

```

5.3. Big numbers (PUC-Rio). Hash: a7d74e7158634f9201c19235badd3364

```

const int DIG = 4;
const int BASE = 10000; // BASE**3 < 2**51
const int TAM = 2048;

struct bigint {
    int v[TAM], n;
    bigint(int x = 0): n(1) {
        memset(v, 0, sizeof(v));
        v[n++] = x; fix();
    }
    bigint(char *s): n(1) {
        memset(v, 0, sizeof(v));
        int sign = 1;
        while (*s && !isdigit(*s)) if (*s++ == '-') sign *= -1;
        char *t = strdup(s), *p = t + strlen(t);
        while (p > t) {
            *p = 0; p = max(t, p - DIG);
            sscanf(p, "%d", &v[n]);
            v[n++] *= sign;
        }
        free(t); fix();
    }
    bigint& fix(int m = 0) {

```

```

        n = max(m, n);
        int sign = 0;
        for (int i = 1, e = 0; i <= n || e && (n = i); i++) {
            v[i] += e; e = v[i] / BASE; v[i] %= BASE;
            if (v[i]) sign = (v[i] > 0) ? 1 : -1;
        }

        for (int i = n - 1; i > 0; i--)
            if (v[i] * sign < 0) { v[i] += sign * BASE; v[i+1] -= sign; }
        while (n && !v[n]) n--;
        return *this;
    }

    int cmp(const bigint& x = 0) const {
        int i = max(n, x.n), t = 0;
        while (1) if ((t = ::cmp(v[i], x.v[i])) || i-- == 0) return t;
    }
    bool operator <(const bigint& x) const { return cmp(x) < 0; }
    bool operator ==(const bigint& x) const { return cmp(x) == 0; }
    bool operator !=(const bigint& x) const { return cmp(x) != 0; }

    operator string() const {
        ostringstream s; s << v[n];

```



```

    for (int i = n - 1; i > 0; i--) {
        s.width(DIG); s.fill('0'); s << abs(v[i]);
    }
    return s.str();
}

friend ostream& operator <<(ostream& o, const bigint& x) {
    return o << (string) x;
}

bigint& operator +=(const bigint& x) {
    for (int i = 1; i <= x.n; i++) v[i] += x.v[i];
    return fix(x.n);
}

bigint operator +(const bigint& x) { return bigint(*this) += x; }
bigint& operator +=(const bigint& x) {
    for (int i = 1; i <= x.n; i++) v[i] += x.v[i];
    return fix(x.n);
}

bigint operator -(const bigint& x) { return bigint(*this) -= x; }
bigint operator -() { bigint r = 0; return r -= *this; }

void ams(const bigint& x, int m, int b) { // *this += (x * m) << b;
    for (int i = 1, e = 0; (i <= x.n || e) && (n = i + b); i++) {
        v[i+b] += x.v[i] * m + e; e = v[i+b] / BASE; v[i+b] %= BASE;
    }
}

bigint operator *(const bigint& x) const {
    bigint r;
    for (int i = 1; i <= n; i++) r.ams(x, v[i], i-1);
    return r;
}

bigint& operator *=(const bigint& x) { return *this = *this * x; }
// cmp(x / y) == cmp(x) * cmp(y); cmp(x % y) == cmp(x);
bigint div(const bigint& x) {
    if (x == 0) return 0;

```

```

    bigint q; q.n = max(n - x.n + 1, 0);
    int d = x.v[x.n] * BASE + x.v[x.n-1];
    for (int i = q.n; i > 0; i--) {
        int j = x.n + i - 1;
        q.v[i] = int((v[j] * double(BASE) + v[j-1]) / d);
        ams(x, -q.v[i], i-1);
        if (i == 1 || j == 1) break;
        v[j-1] += BASE * v[j]; v[j] = 0;
    }
    fix(x.n); return q.fix();
}

bigint& operator /=(const bigint& x) { return *this = div(x); }
bigint& operator %=(const bigint& x) { div(x); return *this; }
bigint operator /(const bigint& x) { return bigint(*this).div(x); }
bigint operator %(const bigint& x) { return bigint(*this) %= x; }
bigint pow(int x) {
    if (x < 0) return (*this == 1 || *this == -1) ? pow(-x) : 0;
    bigint r = 1;
    for (int i = 0; i < x; i++) r *= *this;
    return r;
}

bigint root(int x) {
    if (cmp() == 0 || cmp() < 0 && x % 2 == 0) return 0;
    if (*this == 1 || x == 1) return *this;
    if (cmp() < 0) return -(*this).root(x);
    bigint a = 1, d = *this;

    while (d != 1) {
        bigint b = a + (d /= 2);
        if (cmp(b.pow(x)) >= 0) { d += 1; a = b; }
    }
    return a;
}
};

```

6. STRING ALGORITHMS

6.1. Manber-Myers' algorithm. Hash: b32cb670595bef320decbbced7420bb8

```

int pos[MAXSZ], prm[MAXSZ], cnt[MAXSZ];
bool bh[MAXSZ + 1], b2h[MAXSZ];
int blast[256], bprev[MAXSZ];
int mm_segtree[4*MAXSZ];
string mm_s;

```

```

inline void regen_pos(int sz) {
    for(int i = 0; i < sz; i++)
        pos[prm[i]] = i;
}

inline void bubbleupbucket(int index) {

```

```

    if(index < 0) return;

    int& prm_ext = prm[index];
    cnt[prm_ext]++;
    prm_ext += cnt[prm_ext] - 1;
    b2h[prm_ext] = true;
}

void updatetree(int root, int l, int r, int pos, int val) {
    if(l == r) { mm_segtree[root] = val; return; }

    int m = (l + r + 1)/2;
    if(pos < m) updatetree(2*root + 1, l, m - 1, pos, val);
    else updatetree(2*root + 2, m, r, pos, val);

    mm_segtree[root] = min(mm_segtree[2*root + 1], mm_segtree[2*root + 2]);
}

int querytree(int root, int l, int r, int begin, int end) {
    if(begin == l && end == r) return mm_segtree[root];

    int m = (l + r + 1)/2;
    if(begin < m && end < m)
        return querytree(2*root + 1, l, m - 1, begin, end);
    else if(begin >= m && end >= m)
        return querytree(2*root + 2, m, r, begin, end);
    else return min(querytree(2*root + 1, l, m - 1, begin, m - 1),
        querytree(2*root + 2, m, r, m, end));
}

void mm_build(string s) {
    mm_s = s;
    memset(blast, -1, sizeof blast);
    memset(bh, 0, sizeof(bool) * s.size());
    memset(mm_segtree, 0x3f, sizeof(int) * 4 * s.size());
    updatetree(0, 0, s.size() - 1, s.size() - 1, 0);

    for(int i = 0; i < s.size(); i++) {
        bprev[i] = blast[s[i]];
        blast[s[i]] = i;
    }
    int let_count = 0;
    for(int i = 0; i < 256; i++) {
        if(blast[i] != -1) {
            bh[let_count] = true;
            if(let_count > 0)

```

```

                updatetree(0, 0, s.size() - 1, let_count - 1, 0);
        }
        for(int j = blast[i]; j != -1; j = bprev[j])
            prm[j] = let_count++;
    }
    regen_pos(s.size());
    bh[s.size()] = true;

    for(int st = 1; st < s.size(); st *= 2) {
        memset(cnt, 0, sizeof(int) * s.size());
        memset(b2h, 0, sizeof(bool) * s.size());

        for(int bl = 0, br = 0; br < s.size(); bl = br++)
            for(; !bh[br]; br++)
                prm[pos[br]] = bl;

        bubbleupbucket(s.size() - st);
        for(int bl = 0, br = 0; br < s.size(); bl = br) {
            bubbleupbucket(pos[bl] - st);
            for(br++; !bh[br]; br++)
                bubbleupbucket(pos[br] - st);

            for(int i = bl; i < br; i++) {
                if(pos[i] - st < 0) continue;
                int prm_ext = prm[pos[i] - st];
                if(b2h[prm_ext])
                    for(int j = prm_ext + 1; !bh[j] && b2h[j]; j++)
                        b2h[j] = false;
            }
        }

        regen_pos(s.size());
        for(int i = 0; i < s.size(); i++)
            if(!bh[i] && b2h[i]) {
                bh[i] = true;
                if(pos[i - 1] + st < s.size() && pos[i] + st < s.size()) {
                    int m = min(prm[pos[i - 1] + st], prm[pos[i] + st]);
                    int M = max(prm[pos[i - 1] + st], prm[pos[i] + st]);
                    updatetree(0, 0, s.size() - 1, i - 1,
                        st + querytree(0, 0, s.size() - 1, m, M - 1));
                }
                else
                    updatetree(0, 0, s.size() - 1, i - 1, st);
            }
    }
}

```

```

inline int lcp(string& s1, int p1, string& s2, int p2) {
    int limit = min(s1.size() - p1, s2.size() - p2), i;
    for(i = 0; i < limit; i++) if(s1[p1 + i] != s2[p2 + i]) break;
    return i;
}

pair<bool, int> mm_find(string s) {
    int l = lcp(mm_s, pos[0], s, 0);
    int r = lcp(mm_s, pos[mm_s.size() - 1], s, 0);

    if(l == s.size() || s[l] < mm_s[pos[0] + 1])
        return make_pair(l == s.size(), pos[0]);
    else if(r == s.size() || s[r] > mm_s[pos[mm_s.size() - 1] + r])
        return make_pair(r == s.size(), pos[mm_s.size() - 1]);

    int low = 0, high = mm_s.size() - 1, next, st_n = 0, c_lcp;
    while(high - low > 1) {
        int mid = (low + high)/2;
        c_lcp = max(l, r);
        st_n = 2*st_n + 1 + (l < r);

```

```

        if(mm_segtree[st_n] >= c_lcp)
            next = c_lcp + lcp(mm_s, pos[mid] + c_lcp, s, c_lcp);
        else
            next = mm_segtree[st_n];

        if(next == s.size())
            return make_pair(true, pos[mid]);
        else if(s[next] > mm_s[pos[mid] + next]) {
            low = mid;
            l = next;
        }
        else {
            high = mid;
            r = next;
        }
    }

    return make_pair(false, pos[high]);
}

```

6.2. Morris-Pratt's algorithm. Hash: ace505eff2be640ff01d7c48b2b7d12f

```

int pi[MAXSZ], res[MAXSZ], nres;

void morris_pratt(string text, string pattern) {
    nres = 0;
    pi[0] = -1;
    for(int i = 1; i < pattern.size(); i++) {
        pi[i] = pi[i-1];
        while(pi[i] >= 0 && pattern[pi[i] + 1] != pattern[i])
            pi[i] = pi[pi[i]];
        if(pattern[pi[i] + 1] == pattern[i]) pi[i]++;
    }
}

```

```

int k = 0; //k + 1 eh o tamanho do match atual
for(int i = 0; i < text.size(); i++) {
    while(k >= 0 && pattern[k + 1] != text[i])
        k = pi[k];
    if(pattern[k + 1] == text[i]) k++;
    if(k + 1 == pattern.size()) {
        res[nres++] = i;
        k = pi[k];
    }
}
}

```

6.3. Aho-Corasick's algorithm (UFPE). Hash: 273f4391174d22898bfe3f2415f95915

```

struct No {
    int fail;
    vector< pair<int,int> > out; // num e tamanho do padrao
    //bool marc; // p/ decisao
}

```

```

map<char, int> lista;
int next; // aponta para o proximo sufixo que tenha out.size > 0
};
No arvore[1000003]; // quantida maxima de nos

```

```
//bool encontrado[1005]; // quantidade maxima de padroes, p/ decisao
int qtdNos, qtdPadroes;
```

```
// Funcao para inicializar
```

```
void inic() {
    arvore[0].fail = -1;
    arvore[0].lista.clear();
    arvore[0].out.clear();
    arvore[0].next = -1;
    qtdNos = 1;
    qtdPadroes = 0;
    //arvore[0].marc = false; // p/ decisao
    //memset(encontrado, false, sizeof(encontrado)); // p/ decisao
}
```

```
// Funcao para adicionar um padrao
```

```
void adicionar(char *padrao) {
    int no = 0, len = 0;
    for (int i = 0 ; padrao[i] ; i++, len++) {
        if (arvore[no].lista.find(padrao[i]) == arvore[no].lista.end()) {
            arvore[qtdNos].lista.clear(); arvore[qtdNos].out.clear();
            //arvore[qtdNos].marc = false; // p/ decisao
            arvore[no].lista[padrao[i]] = qtdNos;
            no = qtdNos++;
        } else no = arvore[no].lista[padrao[i]];
    }
    arvore[no].out.push_back(pair<int,int>(qtdPadroes++,len));
}
```

```
// Ativar Aho-corasick, ajustando funcoes de falha
```

```
void ativar() {
    int no,v,f,w;
    queue<int> fila;
    for (map<char,int>::iterator it = arvore[0].lista.begin();
        it != arvore[0].lista.end() ; it++) {
        arvore[no = it->second].fail = 0;
        arvore[no].next = arvore[0].out.size() ? 0 : -1;
        fila.push(no);
    }
    while (!fila.empty()) {
        no = fila.front(); fila.pop();
```

```
for (map<char,int>::iterator it=arvore[no].lista.begin();
    it!=arvore[no].lista.end(); it++) {
    char c = it->first;
    v = it->second;
    fila.push(v);
    f = arvore[no].fail;
    while (arvore[f].lista.find(c) == arvore[f].lista.end()) {
        if (f == 0) { arvore[0].lista[c] = 0; break; }
        f = arvore[f].fail;
    }
    w = arvore[f].lista[c];
    arvore[v].fail = w;
    arvore[v].next = arvore[w].out.size() ? w : arvore[w].next;
}
}
```

```
// Buscar padroes no aho-corasick
```

```
void buscar(char *input) {
    int v, no = 0;
    for (int i = 0 ; input[i] ; i++) {
        while (arvore[no].lista.find(input[i]) == arvore[no].lista.end()) {
            if (no == 0) { arvore[0].lista[input[i]] = 0; break; }
            no = arvore[no].fail;
        }
        v = no = arvore[no].lista[input[i]];
        // marcar os encontrados
        while (v != -1 /* && !arvore[v].marc */) { // p/ decisao
            //arvore[v].marc = true; // p/ decisao: nao continua a lista
            for (int k = 0 ; k < arvore[v].out.size() ; k++) {
                //encontrado[arvore[v].out[k].first] = true; // p/ decisao
                printf("Padrao_%d_na_posicao_%d\n", arvore[v].out[k].first,
                    i-arvore[v].out[k].second+1);
            }
            v = arvore[v].next;
        }
    }
    // for (int i = 0 ; i < qtdPadroes ; i++)
    //printf("%s\n", encontrado[i]?"y":"n"); // p/ decisao
}
```

7. USEFUL MATHEMATICAL FACTS

7.1. Prime counting function ($\pi(x)$). The prime counting function is asymptotic to $\frac{x}{\log x}$, by the prime number theorem.

x	10	10 ²	10 ³	10 ⁴	10 ⁵	10 ⁶	10 ⁷	10 ⁸
$\pi(x)$	4	25	168	1.229	9.592	78.498	664.579	5.761.455

7.2. Partition function. The partition function $p(x)$ counts show many ways there are to write the integer x as a sum of integers.

x	36	37	38	39	40	41	42
p(x)	17.977	21.637	26.015	31.185	37.338	44.583	53.174
x	43	44	45	46	47	100	
p(x)	63.261	75.175	89.134	105.558	125.754	190.569.292	

7.3. Catalan numbers. Catalan numbers are defined by the recurrence:

$$C_{n+1} = \sum_{i=0}^n C_i C_{n-i}$$

A closed formula for Catalan numbers is:

$$C_n = \frac{1}{n+1} \binom{2n}{n} = \binom{2n}{n} - \binom{2n}{n+1}$$

7.4. Stirling numbers of the first kind. These are the number of permutations of I_n with exactly k disjoint cycles. They obey the recurrence:

$$\begin{bmatrix} n \\ k \end{bmatrix} = (n-1) \begin{bmatrix} n-1 \\ k \end{bmatrix} + \begin{bmatrix} n-1 \\ k-1 \end{bmatrix}$$

7.5. Stirling numbers of the second kind. These are the number of ways to partition I_n into exactly k sets. They obey the recurrence:

$$\begin{Bmatrix} n \\ k \end{Bmatrix} = k \begin{Bmatrix} n-1 \\ k \end{Bmatrix} + \begin{Bmatrix} n-1 \\ k-1 \end{Bmatrix}$$

A “closed” formula for it is:

$$\begin{Bmatrix} n \\ k \end{Bmatrix} = \frac{1}{k!} \sum_{j=0}^k (-1)^{k-j} \binom{k}{j} j^n$$

7.6. Bell numbers. These count the number of ways to partition I_n into subsets. They obey the recurrence:

$$\mathcal{B}_{n+1} = \sum_{k=0}^n \binom{n}{k} \mathcal{B}_k$$

x	5	6	7	8	9	10	11	12
\mathcal{B}_x	52	203	877	4.140	21.147	115.975	678.570	4.213.597

7.7. Turán’s theorem. No graph with n vertices that is K_{r+1} -free can have more edges than the Turán graph: A k -partite complete graph with sets of size as equal as possible.

7.8. Generating functions. A list of generating functions for useful sequences:

$(1, 1, 1, 1, 1, \dots)$	$\frac{1}{1-z}$
$(1, -1, 1, -1, 1, \dots)$	$\frac{1}{1+z}$
$(1, 0, 1, 0, 1, 0, \dots)$	$\frac{1}{1-z^2}$
$(1, 0, \dots, 0, 1, 0, 1, 0, \dots, 0, 1, 0, \dots)$	$\frac{1}{1-z^2}$
$(1, 2, 3, 4, 5, 6, \dots)$	$\frac{1}{(1-z)^2}$
$(1, \binom{m+1}{m}, \binom{m+2}{m}, \binom{m+3}{m}, \dots)$	$\frac{1}{(1-z)^{m+1}}$
$(1, c, \binom{c+1}{2}, \binom{c+2}{3}, \dots)$	$\frac{1}{(1-z)^c}$
$(1, c, c^2, c^3, \dots)$	$\frac{1}{1-cz}$
$(0, 1, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \dots)$	$\ln \frac{1}{1-z}$

A neat manipulation trick is:

$$\frac{1}{1-z} G(z) = \sum_n \sum_{k \leq n} g_k z^n$$

7.9. Polyominoes. How many free (rotation, reflection), one-sided (rotation) and fixed n -ominoes are there?

n	3	4	5	6	7	8	9	10
free	2	5	12	35	108	369	1.285	4.655
one-sided	2	7	18	60	196	704	2.500	9.189
fixed	6	19	63	216	760	2.725	9.910	36.446

7.10. The twelvefold way (from Stanley). How many functions $f: N \rightarrow X$ are there?

N	X	Any f	Injective	Surjective
dist.	dist.	x^n	$(x)_n$	$x! \begin{Bmatrix} n \\ x \end{Bmatrix}$
indist.	dist.	$\binom{x+n-1}{n}$	$\binom{x}{n}$	$\binom{n-1}{n-x}$
dist.	indist.	$\begin{Bmatrix} n \\ 1 \end{Bmatrix} + \dots + \begin{Bmatrix} n \\ x \end{Bmatrix}$	$[n \leq x]$	$\begin{Bmatrix} n \\ k \end{Bmatrix}$
indist.	indist.	$p_1(n) + \dots + p_x(n)$	$[n \leq x]$	$p_x(n)$

Where $\begin{pmatrix} a \\ b \end{pmatrix} = \frac{1}{b!} (a)_b$ and $p_x(n)$ is the number of ways to partition the integer n using x summands.

7.11. Common integral substitutions. And finally, a list of common substitutions:

$\int F(\sqrt{ax+b})dx$	$u = \sqrt{ax+b}$	$\frac{2}{a} \int uF(u)du$
$\int F(\sqrt{a^2-x^2})dx$	$x = a \sin u$	$a \int F(a \cos u) \cos u du$
$\int F(\sqrt{x^2+a^2})dx$	$x = a \tan u$	$a \int F(a \sec u) \sec^2 u du$
$\int F(\sqrt{x^2-a^2})dx$	$x = a \sec u$	$a \int F(a \tan u) \sec u \tan u du$
$\int F(e^{ax})dx$	$u = e^{ax}$	$\frac{1}{a} \int \frac{F(u)}{u} du$
$\int F(\ln x)dx$	$u = \ln x$	$\int F(u)e^u du$

7.12. Table of non-trigonometric integrals. Some useful integrals are:

$\int \frac{dx}{x^2+a^2}$	$\frac{1}{a} \arctan \frac{x}{a}$
$\int \frac{dx}{x^2-a^2}$	$\frac{1}{2a} \ln \frac{x-a}{x+a}$
$\int \frac{dx}{a^2-x^2}$	$\frac{1}{2a} \ln \frac{a+x}{a-x}$
$\int \frac{dx}{\sqrt{a^2-x^2}}$	$\arcsin \frac{x}{a}$
$\int \frac{dx}{\sqrt{x^2-a^2}}$	$\ln(u + \sqrt{x^2-a^2})$
$\int \frac{dx}{x\sqrt{x^2-a^2}}$	$\frac{1}{a} \operatorname{arcsec} \left \frac{u}{a} \right $
$\int \frac{dx}{x\sqrt{x^2+a^2}}$	$-\frac{1}{a} \ln \left(\frac{a+\sqrt{x^2+a^2}}{x} \right)$
$\int \frac{dx}{x\sqrt{a^2-x^2}}$	$-\frac{1}{a} \ln \left(\frac{a+\sqrt{a^2-x^2}}{x} \right)$

7.13. Table of trigonometric integrals. A list of common and not-so-common trigonometric integrals:

$\int \tan x dx$	$-\ln \cos x $
$\int \cot x dx$	$\ln \sin x $
$\int \sec x dx$	$\ln \sec x + \tan x $
$\int \csc x dx$	$\ln \csc x - \cot x $
$\int \sec^2 x dx$	$\tan x$
$\int \csc^2 x dx$	$\cot x$
$\int \sin^n x dx$	$-\frac{\sin^{n-1} x \cos x}{n} + \frac{n-1}{n} \int \sin^{n-2} x dx$
$\int \cos^n x dx$	$\frac{\cos^{n-1} x \sin x}{n} + \frac{n-1}{n} \int \cos^{n-2} x dx$
$\int \arcsin x dx$	$x \arcsin x + \sqrt{1-x^2}$
$\int \arccos x dx$	$x \arccos x - \sqrt{1-x^2}$
$\int \arctan x dx$	$x \arctan x - \frac{1}{2} \ln 1-x^2 $

ACM ICPC TEAM REFERENCE - CONTENTS

Team Anuncie Aqui
Universidade Federal de Sergipe

CONTENTS		
1. Configuration files and scripts	1	
1.1. .emacs	1	
1.2. .vimrc	1	
1.3. Hash generator	1	
1.4. Solution template	2	
2. Graph algorithms	2	
2.1. Tarjan's SCC algorithm	2	
2.2. Dinic's maximum flow algorithm	3	
2.3. Successive shortest paths mincost maxflow algorithm	3	
2.4. Gabow's general matching algorithm	4	
3. Math	6	
3.1. Fractions	6	
3.2. Chinese remainder theorem	6	
3.3. Longest increasing subsequence	7	
3.4. Simplex (Warsaw University)	7	
3.5. Romberg's method	8	
3.6. Floyd's cycle detection algorithm	8	
3.7. Pollard's rho algorithm	8	
3.8. Miller-Rabin's algorithm	8	
3.9. Polynomials (PUC-Rio)	9	
4. Geometry	10	
4.1. Point class	10	
4.2. Intersection primitives	10	
4.3. Polygon primitives	10	
4.4. Miscellaneous primitives	11	
4.5. Smallest enclosing circle	11	
4.6. Convex hull	11	
4.7. Closest pair of points	12	
4.8. Kd-tree	13	
4.9. Range tree	13	
5. Data structures	14	
5.1. Treap	14	
5.2. Heap	15	
5.3. Big numbers (PUC-Rio)	16	
6. String algorithms	17	
6.1. Manber-Myers' algorithm	17	
6.2. Morris-Pratt's algorithm	19	
6.3. Aho-Corasick's algorithm (UFPE)	19	
7. Useful mathematical facts	21	
7.1. Prime counting function ($\pi(x)$)	21	
7.2. Partition function	21	
7.3. Catalan numbers	21	
7.4. Stirling numbers of the first kind	21	
7.5. Stirling numbers of the second kind	21	
7.6. Bell numbers	21	
7.7. Turán's theorem	21	
7.8. Generating functions	21	
7.9. Polyominoes	22	
7.10. The twelvefold way (from Stanley)	22	
7.11. Common integral substitutions	22	
7.12. Table of non-trigonometric integrals	22	
7.13. Table of trigonometric integrals	22	