

# ACM ICPC TEAM REFERENCE

## 2010 WORLD FINALS

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### 1. CONFIGURATION FILES AND SCRIPTS

#### 1.1. .emacs. Hash: c4c6b75b731e46e642e98db153594c25

```
(global-font-lock-mode t)
(setq transient-mark-mode t)
(require 'font-lock)
(require_ 'paren)
```

```
(global-set-key [f5] 'cxx-compile)
(set-input-mode_nil_nil_1)
(fset_ 'yes-or-no-p 'y-or-n-p)
```

```
(require_ 'cc-mode)
(defun cxx-compile ()
  (interactive)
  (progn
    (save-buffer)
    (compile (concat "g++-g_-O2_-o_" (substring buffer-file-name 0 -4)
```

```
buffer-file-name))
)
)

(add-hook 'c++-mode-hook_ (lambda () (c-set-style "stroustrup")))
```

## 1.2. Hash generator. Hash: 0d22aecd779fc370b30a2c628aff517c

```
#!/bin/sh
```

```
sed ':a;N;$!ba;s/[_\n\t]//g' | md5sum | cut -d'_' -f1
```

## 2. GRAPH ALGORITHMS

### 2.1. Dijkstra's algorithm. Hash: c182c6dfdc4334cb79c7721ae6e88a98

```
int dist[MAXV], last_edge[MAXV], d_visited[MAXV];
int prev_edge[MAXE], weight[MAXE], adj[MAXE];
int nedges;
priority_queue<pair<int, int> > d_q;

void d_init() {
  nedges = 0;
  memset(last_edge, -1, sizeof last_edge);
}

void d_edge(int v, int w, int eweight) {
  prev_edge[nedges] = last_edge[v];
  weight[nedges] = eweight;
  adj[nedges] = w;
  last_edge[v] = nedges++;
}
```

```
void dijkstra(int s, int num_nodes = MAXV) {
  memset(dist, 0x3f, sizeof dist);
  memset(d_visited, 0, sizeof d_visited);
  d_q.push(make_pair(dist[s] = 0, s));

  while(!d_q.empty()) {
    int v = d_q.top().second; d_q.pop();
    if(d_visited[v]) continue; d_visited[v] = true;

    for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
      int w = adj[i], new_dist = dist[v] + weight[i];
      if(new_dist < dist[w])
        d_q.push(make_pair(-(dist[w] = new_dist), w));
    }
  }
}
```

### 2.2. Tarjan's SCC algorithm. Hash: f98d9589db68c8f1e8274cf53eb7f3bf

```
int lowest[MAXV], num[MAXV], visited[MAXV], comp[MAXV];
int prev_edge[MAXE], last_edge[MAXV], adj[MAXE], nedges;
int cur_num, cur_comp;
stack<int> visiting;

int t_init() {
  memset(last_edge, -1, sizeof last_edge);
```

```
nedges = 0;
}

void t_edge(int v, int w) {
  prev_edge[nedges] = last_edge[v];
  adj[nedges] = w;
  last_edge[v] = nedges++;
```

```

}

int tarjan_dfs(int v) {
    lowest[v] = num[v] = cur_num++;
    visiting.push(v);

    visited[v] = 1;
    for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
        int w = adj[i];
        if(visited[w] == 0) lowest[v] = min(lowest[v], tarjan_dfs(w));
        else if(visited[w] == 1) lowest[v] = min(lowest[v], num[w]);
    }

    if(lowest[v] == num[v]) {
        int last = -1;
        while(last != v) {
            comp[last = visiting.top()] = cur_comp;
            visited[last] = 2;
        }
    }
}

```

### 2.3. Dinic's algorithm. Hash: 4dd537effe7e233681c099912397839a

```

int last_edge[MAXV], cur_edge[MAXV], dist[MAXV];
int prev_edge[MAXE], cap[MAXE], flow[MAXE], adj[MAXE];
int nedges;

void d_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
}

void d_edge(int v, int w, int capacity, bool r = false) {
    prev_edge[nedges] = last_edge[v];
    cap[nedges] = capacity;
    adj[nedges] = w;
    flow[nedges] = 0;
    last_edge[v] = nedges++;
}

if(!r) d_edge(w, v, 0, true);
}

bool d_auxflow(int source, int sink) {
    queue<int> q;
    q.push(source);

    memset(dist, -1, sizeof dist);
}

```

```

        visiting.pop();
    }
    cur_comp++;
}

return lowest[v];
}

void tarjan_scc(int num_v = MAXV) {
    visiting = stack<int>();
    memset(visited, 0, sizeof visited);
    cur_num = cur_comp = 0;

    for(int i = 0; i < num_v; i++)
        if(!visited[i])
            tarjan_dfs(i);
}

```

```

dist[source] = 0;
memcpy(cur_edge, last_edge, sizeof last_edge);

while(!q.empty()) {
    int v = q.front(); q.pop();
    for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
        if(cap[i] - flow[i] == 0) continue;

        if(dist[adj[i]] == -1) {
            dist[adj[i]] = dist[v] + 1;
            q.push(adj[i]);

            if(adj[i] == sink) return true;
        }
    }
}

return false;
}

inline int rev(int i) { return i ^ 1; }

int d_augmenting(int v, int sink, int c) {
    if(v == sink) return c;
}

```

```

for(int& i = cur_edge[v]; i != -1; i = prev_edge[i]) {
    if(cap[i] - flow[i] == 0 || dist[adj[i]] != dist[v] + 1)
        continue;

    int val;
    if(val = d_augmenting(adj[i], sink, min(c, cap[i] - flow[i]))) {
        flow[i] += val;
        flow[rev(i)] -= val;
        return val;
    }
}

```

```

return 0;
}

int dinic(int source, int sink) {
    int ret = 0;
    while(d_auxflow(source, sink)) {
        int flow;
        while(flow = d_augmenting(source, sink, 0x3f3f3f3f))
            ret += flow;
    }

    return ret;
}

```

## 2.4. Busacker-Gowen's algorithm. Hash: 6933692fe046f78da13b05166c7e6d23

```

int dist[MAXV], last_edge[MAXV], d_visited[MAXV], bg_prev[MAXV], pot[MAXV],
    capres[MAXV];
int prev_edge[MAXE], adj[MAXE], cap[MAXE], cost[MAXE], flow[MAXE];

int nedges;
priority_queue<pair<int, int> > d_q;

inline void bg_edge(int v, int w, int capacity, int cst, bool r = false) {
    prev_edge[nedges] = last_edge[v];
    adj[nedges] = w;
    cap[nedges] = capacity;
    flow[nedges] = 0;
    cost[nedges] = cst;
    last_edge[v] = nedges++;

    if(!r) bg_edge(w, v, 0, -cost, true);
}

inline int rev(int i) { return i ^ 1; }
inline int from(int i) { return adj[rev(i)]; }

inline void bg_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
    memset(pot, 0, sizeof pot);
}

void bg_dijkstra(int s, int num_nodes = MAXV) {
    memset(dist, 0x3f, sizeof dist);

```

```

memset(d_visited, 0, sizeof d_visited);
d_q.push(make_pair(dist[s] = 0, s));
capres[s] = 0x3f3f3f3f;

while(!d_q.empty()) {
    int v = d_q.top().second; d_q.pop();
    if(d_visited[v]) continue; d_visited[v] = true;

    for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
        if(cap[i] - flow[i] == 0) continue;
        int w = adj[i], new_dist = dist[v] + cost[i] + pot[v] - pot[w];

        if(new_dist < dist[w]) {
            d_q.push(make_pair(-(dist[w] = new_dist), w));
            bg_prev[w] = rev(i);
            capres[w] = min(capres[v], cap[i] - flow[i]);
        }
    }
}

pair<int, int> busacker_gowen(int src, int sink, int num_nodes = MAXV) {
    int retFlow = 0, retCost = 0;

    bg_dijkstra(src, num_nodes);
    while(dist[sink] < 0x3f3f3f3f) {
        int cur = sink;
        while(cur != src) {
            flow[bg_prev[cur]] -= capres[sink];

```

```

        flow[rev(bg_prev[cur])] += capres[sink];
        retCost += cost[rev(bg_prev[cur])] * capres[sink];
        cur = adj[bg_prev[cur]];
    }
    retFlow += capres[sink];

    for(int i = 0; i < MAXV; i++)

```

## 2.5. Gabow's algorithm. Hash: 31f8b67cd2b16187c6733f42801ee2be

```

int prev_edge[MAXE], v[MAXE], w[MAXE], last_edge[MAXV];
int type[MAXV], label[MAXV], first[MAXV], mate[MAXV], nedges;
bool g_flag[MAXV], g_souter[MAXV];

void g_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
}

void g_edge(int a, int b) {
    prev_edge[nedges] = last_edge[a];
    v[nedges] = a;
    w[nedges] = b;
    last_edge[a] = nedges++;

    prev_edge[nedges] = last_edge[b];
    v[nedges] = b;
    w[nedges] = a;
    last_edge[b] = nedges++;
}

void g_label(int v, int join, int edge, queue<int>& outer) {
    if(v == join) return;
    if(label[v] == -1) outer.push(v);

    label[v] = edge;
    type[v] = 1;
    first[v] = join;

    g_label(first[label[mate[v]]], join, edge, outer);
}

void g_augment(int _v, int _w) {
    int t = mate[_v];
    mate[_v] = _w;

```

```

        pot[i] = min(pot[i] + dist[i], 0x3f3f3f3f);

        bg_dijkstra(src, num_nodes);
    }
    return make_pair(retFlow, retCost);
}

```

```

if(mate[t] != _v) return;
if(label[_v] == -1) return;

if(type[_v] == 0) {
    mate[t] = label[_v];
    g_augment(label[_v], t);
}
else if(type[_v] == 1) {
    g_augment(v[label[_v]], w[label[_v]]);
    g_augment(w[label[_v]], v[label[_v]]);
}
}

int gabow(int n) {
    memset(mate, -1, sizeof mate);
    memset(first, -1, sizeof first);

    int u = 0, ret = 0;
    for(int z = 0; z < n; z++) {
        if(mate[z] != -1) continue;

        memset(label, -1, sizeof label);
        memset(type, -1, sizeof type);
        memset(g_souter, 0, sizeof g_souter);

        label[z] = -1; type[z] = 0;

        queue<int> outer;
        outer.push(z);

        bool done = false;
        while(!outer.empty()) {
            int x = outer.front(); outer.pop();

```

```

    if(g_souter[x]) continue;
    g_souter[x] = true;

    for(int i = last_edge[x]; i != -1; i = prev_edge[i]) {
        if(mate[w[i]] == -1 && w[i] != z) {
            mate[w[i]] = x;
            g_augment(x, w[i]);
            ret++;

            done = true;
            break;
        }

        if(type[w[i]] == -1) {
            int v = mate[w[i]];
            if(type[v] == -1) {
                type[v] = 0;
                label[v] = x;
                outer.push(v);

                first[v] = w[i];
            }
            continue;
        }
    }
}

```

```

    int r = first[x], s = first[w[i]];
    if(r == s) continue;

    memset(g_flag, 0, sizeof g_flag);
    g_flag[r] = g_flag[s] = true;

    while(true) {
        if(s != -1) swap(r, s);
        r = first[label[mate[r]]];
        if(g_flag[r]) break; g_flag[r] = true;
    }

    g_label(first[x], r, i, outer);
    g_label(first[w[i]], r, i, outer);

    for(int c = 0; c < n; c++)
        if(type[c] != -1 && first[c] != -1 && type[first[c]] != -1)
            first[c] = r;
    }
    if(done) break;
}
}
return ret;
}

```

### 3. MATH

#### 3.1. Fractions. Hash: 379fd408c3007c650c022fd4adfeabbd

```

struct frac {
    long long num, den;

    frac() : num(0), den(1) { };
    frac(long long num, long long den) { set_val(num, den); }
    frac(long long num) : num(num), den(1) { };

    void set_val(long long _num, long long _den) {
        num = _num/__gcd(_num, _den);
        den = _den/__gcd(_num, _den);
        if(den < 0) { num *= -1; den *= -1; }
    }

    void operator*=(frac f) { set_val(num * f.num, den * f.den); }
    void operator+=(frac f) { set_val(num * f.den + f.num * den, den * f.den); }
}

```

```

    void operator-=(frac f) { set_val(num * f.den - f.num * den, den * f.den); }
    void operator/=(frac f) { set_val(num * f.den, den * f.num); }
};

bool operator<(frac a, frac b) {
    if((a.den < 0) ^ (b.den < 0)) return a.num * b.den > b.num * a.den;
    return a.num * b.den < b.num * a.den;
}

std::ostream& operator<<(std::ostream& o, const frac f) {
    o << f.num << "/" << f.den;
    return o;
}

bool operator==(frac a, frac b) { return a.num * b.den == b.num * a.den; }

```

```

bool operator!=(frac a, frac b) { return !(a == b); }
bool operator<=(frac a, frac b) { return (a == b) || (a < b); }
bool operator>=(frac a, frac b) { return !(a < b); }
bool operator>(frac a, frac b) { return !(a <= b); }
frac operator/(frac a, frac b) { frac ret = a; ret /= b; return ret; }

```

```

frac operator*(frac a, frac b) { frac ret = a; ret *= b; return ret; }
frac operator+(frac a, frac b) { frac ret = a; ret += b; return ret; }
frac operator-(frac a, frac b) { frac ret = a; ret -= b; return ret; }
frac operator~(frac f) { return 0 - f; }

```

### 3.2. Chinese remainder theorem. Hash: 06b5ebd5c44c204a4b11bbb76d09023d

```

struct t {
    long long a, b; int g;
    t(long long a, long long b, int g) : a(a), b(b), g(g) { }
    t swap() { return t(b, a, g); }
};

t egcd(int p, int q) {
    if(q == 0) return t(1, 0, p);

    t t2 = egcd(q, p % q);

```

```

    t2.a -= t2.b * (p/q);
    return t2.swap();
}

int crt(int a, int p, int b, int q) {
    t t2 = egcd(p, q); t2.a %= p*q; t2.b %= p*q;
    assert(t2.g == 1);
    int ret = ((b * t2.a)%(p*q) * p + (a * t2.b)%(p*q) * q) % (p*q);
    return ret >= 0 ? ret : ret + p*q;
}

```

### 3.3. Longest increasing subsequence. Hash: 0f80b5d3af188d8bf4d1cbe45a76b46d

```

vector<int> lis(vector<int>& seq) {
    int smallest_end[seq.size()+1], prev[seq.size()];
    smallest_end[1] = seq[0];

    int sz = 1;
    for(int i = 1; i < seq.size(); i++) {
        int lo = 0, hi = sz;
        while(lo < hi) {
            int mid = (lo + hi + 1)/2;
            if(seq[smallest_end[mid]] <= seq[i])
                lo = mid;
            else
                hi = mid - 1;
        }
    }

```

```

    prev[i] = smallest_end[lo];
    if(lo == sz)
        smallest_end[++sz] = i;
    else if(seq[i] < seq[smallest_end[lo+1]])
        smallest_end[lo+1] = i;
}

vector<int> ret;
for(int cur = smallest_end[sz]; sz > 0; cur = prev[cur], sz--)
    ret.push_back(seq[cur]);
reverse(ret.begin(), ret.end());

return ret;
}

```

### 3.4. Simplex (Warsaw University). Hash: c687094970cf1953fd6f87a01adc6a95

```

const double EPS = 1e-9;
typedef long double T;
typedef vector<T> VT;

```

```

vector<VT> A;
VT b,c,res;
VI kt,N;

```

```

int m;
inline void pivot(int k,int l,int e){
    int x=kt[l]; T p=A[l][e];
    REP(i,k) A[l][i]/=p; b[l]/=p; N[e]=0;
    REP(i,m) if (i!=l) b[i]-=A[i][e]*b[l],A[i][x]=A[i][e]*-A[l][x];
    REP(j,k) if (N[j]){
        c[j]-=c[e]*A[l][j];
        REP(i,m) if (i!=l) A[i][j]-=A[i][e]*A[l][j];
    }
    kt[l]=e; N[x]=1; c[x]=c[e]*-A[l][x];
}

VT doit(int k){
    VT res; T best;
    while (1){
        int e=-1,l=-1; REP(i,k) if (N[i] && c[i]>EPS) {e=i; break;}
        if (e==-1) break;
        REP(i,m) if (A[i][e]>EPS && (l==-1 || best>b[i]/A[i][e]))
            best=b[i]/A[i][e];
        if (l==-1) /*ilimitado*/ return VT();
        pivot(k,l,e);
    }
}

```

```

res.resize(k,0); REP(i,m) res[kt[i]]=b[i];
return res;
}

VT simplex(vector<VT> &AA,VT &bb,VT &cc){
    int n=AA[0].size(),k;
    m=AA.size(); k=n+m+1; kt.resize(m); b=bb; c=cc; c.resize(n+m);
    A=AA; REP(i,m){ A[i].resize(k); A[i][n+i]=1; A[i][k-1]=-1; kt[i]=n+i;}
    N=VI(k,1); REP(i,m) N[kt[i]]=0;
    int pos=min_element(ALL(b))-b.begin();
    if (b[pos]<-EPS){
        c=VT(k,0); c[k-1]=-1; pivot(k,pos,k-1); res=doit(k);
        if (res[k-1]>EPS) /*impossivel*/ return VT();
        REP(i,m) if (kt[i]==k-1)
            REP(j,k-1) if (N[j] && (A[i][j]<-EPS || EPS<A[i][j])){
                pivot(k,i,j); break;
            }
        c=cc; c.resize(k,0); REP(i,m) REP(j,k) if (N[j]) c[j]-=c[kt[i]]*A[i][j];
    }
    res=doit(k-1); if (!res.empty()) res.resize(n);
    return res;
}

```

### 3.5. Romberg's method. Hash: a85facba1eac60c8909b04b552bd2222

```

long double romberg(int a, int b, double(*func)(double))
{
    long double approx[2][50];
    long double *cur=approx[1], *prev=approx[0];

    prev[0] = 1/2.0 * (b-a) * (func(a) + func(b));
    for(int it = 1; it < 25; it++, swap(cur, prev)) {
        if(it > 1 && cmp(prev[it-1], prev[it-2]) == 0)
            return prev[it-1];

        cur[0] = 1/2.0 * prev[0];
    }
}

```

```

long double div = (b-a)/pow(2, it);
for(long double sample = a + div; sample < b; sample += 2 * div)
    cur[0] += div * func(a + sample);

for(int j = 1; j <= it; j++)
    cur[j] = cur[j-1] + 1/(pow(4, it) - 1)*(cur[j-1] + prev[j-1]);
}

return prev[24];
}

```

## 4. GEOMETRY

### 4.1. Point class. Hash: 385163b56d204afaf5acd511cf175606

```

typedef double TYPE;
const TYPE EPS = 1e-9;

```

```

inline int sgn(TYPE a) { return a > EPS ? 1 : (a < -EPS ? -1 : 0); }

```



```

inline int cmp(TYPE a, TYPE b) { return sgn(a - b); }

struct pt {
    TYPE x, y;
    pt(TYPE x = 0, TYPE y = 0) : x(x), y(y) { }

    bool operator==(pt p) { return cmp(x, p.x) == 0 && cmp(y, p.y) == 0; }
    bool operator<(pt p) const {
        return cmp(x, p.x) ? cmp(x, p.x) < 0 : cmp(y, p.y) < 0;
    }
    TYPE operator|(pt p) { return x*p.x + y*p.y; }
    TYPE operator%(pt p) { return x*p.y - y*p.x; }
    pt operator~() { return pt(x, -y); }
    pt operator+(pt p) { return pt(x + p.x, y + p.y); }
    pt operator-(pt p) { return pt(x - p.x, y - p.y); }
    pt operator*(pt p) { return pt(x*p.x - y*p.y, x*p.y + y*p.x); }
    pt operator/(TYPE t) { return pt(x/t, y/t); }
    pt operator/(pt p) { return (*this * ~p)/(p|p); }
};

```

#### 4.2. Primitives. Hash: 1b17ae7aac295409a56d2534a0507176

```

inline int g_mod(int i, int n) { if(i == n) return 0; return i; }
bool in_rect(pt a, pt b, pt c) {
    return sgn(c.x - min(a.x, b.x)) >= 0 && sgn(max(a.x, b.x) - c.x) >= 0 &&
        sgn(c.y - min(a.y, b.y)) >= 0 && sgn(max(a.y, b.y) - c.y) >= 0;
}
bool ps_isects(pt a, pt b, pt c) { return ccw(a,b,c) == 0 && in_rect(a,b,c); }

bool ss_isects(pt a, pt b, pt c, pt d) {
    if (ccw(a,b,c)*ccw(a,b,d) == -1 && ccw(c,d,a)*ccw(c,d,b) == -1) return true;
    return ps_isects(a, b, c) || ps_isects(a, b, d) ||
        ps_isects(c, d, a) || ps_isects(c, d, b);
}

double p_area(vector<pt>& pol) {
    double ret = 0;
    for(int i = 0; i < pol.size(); i++)
        ret += pol[i] % pol[g_mod(i+1, pol.size())];
    return ret/2;
}

int point_polygon(pt p, vector<pt>& pol) {
    int n = pol.size(), count = 0;

```

```

const pt I = pt(0,1);

struct circle {
    pt c; TYPE r;
    circle(pt c, TYPE r) : c(c), r(r) { }
};

TYPE norm(pt a) { return a|a; }
TYPE abs(pt a) { return sqrt(a|a); }
TYPE dist(pt a, pt b) { return abs(a - b); }
TYPE area(pt a, pt b, pt c) { return (a-c)%(b-c); }
int ccw(pt a, pt b, pt c) { return sgn(area(a, b, c)); }
pt unit(pt a) { return a/abs(a); }
double arg(pt a) { return atan2(a.y, a.x); }
pt f_polar(TYPE mod, double ang) { return pt(mod * cos(ang), mod * sin(ang)); }

ostream& operator<<(ostream& o, pt p) {
    return o << "(" << p.x << ", " << p.y << ")";
}

```

```

for(int i = 0; i < n; i++) {
    int il = g_mod(i+1, n);
    if (ps_isects(pol[i], pol[il], p)) return -1;
    else if (((sgn(pol[i].y - p.y) == 1) != (sgn(pol[il].y - p.y) == 1)) &&
        ccw(pol[i], p, pol[il]) == sgn(pol[i].y - pol[il].y)) count++;
}
return count % 2;
}

bool point_circle(pt p, circle c) {
    return cmp(abs(p - c.c), c.r) <= 0;
}

pt parametric_isect(pt p, pt v, pt q, pt w) {
    double t = ((q-p)%w)/(v%w);
    return p + v*t;
}

pt ss_isect(pt p, pt q, pt r, pt s) {
    pt isect = parametric_isect(p, q-p, r, s-r);
    if(ps_isects(p, q, isect) && ps_isects(r, s, isect)) return isect;
    return pt(1/0.0, 1/0.0);
}

```

```
double ps_distance(pt p, pt a, pt b) {
    p = p - a; b = b - a;
    double coef = min(max((b||p)/(b||b), TYPE(0)), TYPE(1));
    return abs(p - b*coef);
}

pt circumcenter(pt a, pt b, pt c) {
```

#### 4.3. Smallest enclosing circle. Hash: 4e41d94c106dee349b45ca542ff0a532

```
circle enclosing_circle(vector<pt>& pts)
{
    srand(unsigned(time(0)));
    random_shuffle(pts.begin(), pts.end());

    circle c(pt(), -1);
    for(int i = 0; i < pts.size(); i++) {
        if(point_circle(pts[i], c)) continue;
        c = circle(pts[i], 0);
        for(int j = 0; j < i; j++) {
            if(point_circle(pts[j], c)) continue;
```

#### 4.4. Convex hull. Hash: a7f921d07f1b9b8a0053a0833329ddcf

```
pt pivot;

bool hull_comp(pt a, pt b) {
    int turn = ccw(a, b, pivot);
    return turn == 1 || (turn == 0 && cmp(norm(a), norm(b)) < 0);
}

vector<pt> hull(vector<pt> pts) {
    if(pts.size() <= 1) return pts;
    vector<pt> ret;

    int mini = 0;
    for(int i = 1; i < pts.size(); i++)
        if(pts[i] < pts[mini])
            mini = i;
```

```
        return parametric_isect((b+a)/2, (b-a)*I, (c+a)/2, (c-a)*I);
    }

    bool compy(pt a, pt b) {
        return cmp(a.y, b.y) ? cmp(a.y, b.y) < 0 : cmp(a.x, b.x) < 0;
    }
    bool compx(pt a, pt b) { return a < b; }
```

```
        c = circle((pts[i] + pts[j])/2, abs(pts[i] - pts[j])/2);
        for(int k = 0; k < j; k++) {
            if(point_circle(pts[k], c)) continue;
            pt center = circumcenter(pts[i], pts[j], pts[k]);
            c = circle(center, abs(center - pts[i])/2);
        }
    }
    return c;
}
```

```
    pivot = pts[mini];
    swap(pts[0], pts[mini]);
    sort(pts.begin() + 1, pts.end(), hull_comp);

    ret.push_back(pts[0]);
    ret.push_back(pts[1]);
    int sz = 2;

    for(int i = 2; i < pts.size(); i++) {
        while(sz >= 2 && ccw(ret[sz-2], ret[sz-1], pts[i]) <= 0)
            ret.pop_back(), sz--;
        ret.push_back(pts[i]), sz++;
    }

    return ret;
}
```

## 4.5. Kd-tree. Hash: a6e0d07a83dde3bc241f10b0f75abdc0

```

int tree[4*MAXSZ];
TYPE split[4*MAXSZ];
vector<pt> pts;

void kd_recurse(int root, int left, int right, bool x) {
    if(left == right) {
        tree[root] = left;
        return;
    }

    int mid = (right+left)/2;
    nth_element(pts.begin() + left, pts.begin() + mid,
        pts.begin() + right + 1, x ? compx : compy);
    split[root] = x ? pts[mid].x : pts[mid].y;

    kd_recurse(2*root+1, left, mid, !x);
    kd_recurse(2*root+2, mid+1, right, !x);
}

void kd_build() {
    memset(tree, -1, sizeof tree);
    kd_recurse(0, 0, pts.size() - 1, true);
}

int kd_query(int root, int a, int b, int c, int d, bool x) {
    if(tree[root] != -1)
        return a <= pts[tree[root]].x && pts[tree[root]].x <= b &&
            c <= pts[tree[root]].y && pts[tree[root]].y <= d;
}

```

```

int ret = 0, l, r;
if(x) l = a, r = b;
else l = c, r = d;

if(l <= split[root]) ret += kd_query(2*root + 1, a, b, c, d, !x);
if(split[root] <= r) ret += kd_query(2*root + 2, a, b, c, d, !x);

return ret;
}

pt kd_neighbor(int root, pt a, bool x) {
    if(tree[root] != -1)
        return a == pts[tree[root]] ? pt(2e9, 2e9) : pts[tree[root]];

    TYPE num = x ? a.x : a.y;
    int term = num <= split[root] ? 1 : 2;
    pt ret;

    TYPE d = norm(a - (ret = kd_neighbor(2*root + term, a, !x)));
    if((split[root] - num)*(split[root] - num) < d) {
        pt ret2 = kd_neighbor(2*root + 3 - term, a, !x);
        if(norm(a - ret2) < d)
            ret = ret2;
    }

    return ret;
}

```

## 4.6. Range tree. Hash: 06e46c5eab58c9fb1332ed9998c017c1

```

vector<pt> pts, tree[MAXSZ];
vector<TYPE> xs;
vector<int> lnk[MAXSZ][2];

int rt_recurse(int root, int left, int right) {
    if(left == right) {
        vector<pt>::iterator it;
        it = lower_bound(pts.begin(), pts.end(), pt(xs[left], -1e9));
        for(; it != pts.end() && it->x == xs[left]; it++)
            tree[root].push_back(*it);
    }
}

```

```

sort(tree[root].begin(), tree[root].end(), compy);
return tree[root].size();
}

int mid = (left + right)/2, cl = 2*root + 1, cr = cl + 1;
int sz1 = rt_recurse(cl, left, mid);
int sz2 = rt_recurse(cr, mid + 1, right);

int l = 0, r = 0, llink = 0, rlink = 0; pt last;
while(l < sz1 || r < sz2) {
    if(r == sz2 || (l < sz1 && tree[cl][l].y <= tree[cr][r].y))

```

```

        tree[root].push_back(last = tree[cl][l++]);
    else tree[root].push_back(last = tree[cr][r++]);

    while(llink < tree[cl].size() && compy(tree[cl][llink].y, last))
        llink++;
    while(rlink < tree[cr].size() && compy(tree[cr][rlink].y, last))
        rlink++;

    lnk[root][0].push_back(llink);
    lnk[root][1].push_back(rlink);
}

return tree[root].size();
}

void rt_build() {
    sort(pts.begin(), pts.end());
    for(int i = 0; i < pts.size(); i++) xs.push_back(pts[i].x);
    rt_recurse(0, 0, xs.size() - 1);
}

int rt_query(int root, int l, int r, int a, int b, int c, int d,

```

```

        int posl = -1, int posr = -1) {
    if(root == 0 && pos == -1)
        pos = lower_bound(tree[0].begin(), tree[0].end(), c, compy)
            - tree[0].begin();

    int ret = 0;
    if(a <= xs[l] && xs[r] <= b) {
        while(pos < tree[root].size() && tree[root][pos].y <= d)
            ret++, pos++;
        return ret;
    }
    if(pos >= tree[root].size()) return 0;

    int mid = (l + r)/2;
    if(a <= xs[mid])
        ret += rt_query(2*root+1, l, mid, a, b, c, d, lnk[root][0][pos]);
    if(xs[mid+1] <= b)
        ret += rt_query(2*root+2, mid+1, r, a, b, c, d, lnk[root][1][pos]);

    return ret;
}

```

## 5. DATA STRUCTURES

### 5.1. Treap. Hash: 2199b72803301716616a462d9d5e9a66

```

typedef int TYPE;

class treap {
public:
    treap *left, *right;
    int priority, sons;
    TYPE value;

    treap(TYPE value) : left(NULL), right(NULL), value(value), sons(0) {
        priority = rand();
    }

    ~treap() {
        if(left) delete left;
        if(right) delete right;
    }
};

```

```

treap* find(treap* t, TYPE val) {
    if(!t) return NULL;
    if(val == t->value) return t;

    if(val < t->value) return find(t->left, val);
    if(val > t->value) return find(t->right, val);
}

void rotate_to_right(treap* &t) {
    treap* n = t->left;
    t->left = n->right;
    n->right = t;
    t = n;
}

void rotate_to_left(treap* &t) {
    treap* n = t->right;
    t->right = n->left;

```

```

    n->left = t;
    t = n;
}

void fix_augment(treap* t) {
    if(!t) return;
    t->sons = (t->left ? t->left->sons + 1 : 0) +
        (t->right ? t->right->sons + 1 : 0);
}

void insert(treap* &t, TYPE val) {
    if(!t)
        t = new treap(val);
    else
        insert(val <= t->value ? t->left : t->right, val);

    if(t->left && t->left->priority > t->priority)
        rotate_to_right(t);
    else if(t->right && t->right->priority > t->priority)
        rotate_to_left(t);

    fix_augment(t->left); fix_augment(t->right); fix_augment(t);
}

```

```

}

inline int p(treap* t) {
    return t ? t->priority : -1;
}

void erase(treap* &t, TYPE val) {
    if(!t) return;

    if(t->value != val)
        erase(val < t->value ? t->left : t->right, val);
    else {
        if(!t->left && !t->right)
            delete t, t = NULL;
        else {
            p(t->left) < p(t->right) ? rotate_to_left(t) : rotate_to_right(t);
            erase(t, val);
        }
    }

    fix_augment(t->left); fix_augment(t->right); fix_augment(t);
}

```

## 5.2. Heap. Hash: e334218955a73d1286ad0fc19e84b642

```

struct heap {
    int heap[MAXV][2], v2n[MAXV];
    int size;

    void init(int sz) __attribute__((always_inline)) {
        memset(v2n, -1, sizeof(int) * sz);
        size = 0;
    }

    void swap(int& a, int& b) __attribute__((always_inline)) {
        int temp = a;
        a = b;
        b = temp;
    }

    void s(int a, int b) __attribute__((always_inline)) {
        swap(v2n[heap[a][1]], v2n[heap[b][1]]);
        swap(heap[a][0], heap[b][0]);
        swap(heap[a][1], heap[b][1]);
    }
}

```

```

int extract_min() {
    int ret = heap[0][1];
    s(0, --size);

    int cur = 0, next = 2;
    while(next < size) {
        if(heap[next][0] > heap[next - 1][0])
            next--;
        if(heap[next][0] >= heap[cur][0])
            break;

        s(next, cur);
        cur = next;
        next = 2*cur + 2;
    }
    if(next == size && heap[next - 1][0] < heap[cur][0])
        s(next - 1, cur);

    return ret;
}

```

```

}

void decrease_key(int vertex, int new_value) __attribute__((always_inline))
{
    if(v2n[vertex] == -1) {
        v2n[vertex] = size;
        heap[size++][1] = vertex;
    }

    heap[v2n[vertex]][0] = new_value;

```

```

    int cur = v2n[vertex];
    while(cur >= 1) {
        int parent = (cur - 1)/2;
        if(new_value >= heap[parent][0])
            break;

        s(cur, parent);
        cur = parent;
    }
}
};

```

### 5.3. Big numbers (PUC-Rio). Hash: a7d74e7158634f9201c19235badd3364

```

const int DIG = 4;
const int BASE = 10000; // BASE**3 < 2**51
const int TAM = 2048;

struct bigint {
    int v[TAM], n;
    bigint(int x = 0): n(1) {
        memset(v, 0, sizeof(v));
        v[n++] = x; fix();
    }
    bigint(char *s): n(1) {
        memset(v, 0, sizeof(v));
        int sign = 1;
        while (*s && !isdigit(*s)) if (*s++ == '-') sign *= -1;
        char *t = strdup(s), *p = t + strlen(t);
        while (p > t) {
            *p = 0; p = max(t, p - DIG);
            sscanf(p, "%d", &v[n]);
            v[n++] *= sign;
        }
        free(t); fix();
    }
    bigint& fix(int m = 0) {
        n = max(m, n);
        int sign = 0;
        for (int i = 1, e = 0; i <= n || e && (n = i); i++) {
            v[i] += e; e = v[i] / BASE; v[i] %= BASE;
            if (v[i]) sign = (v[i] > 0) ? 1 : -1;
        }

        for (int i = n - 1; i > 0; i--)

```

```

        if (v[i] * sign < 0) { v[i] += sign * BASE; v[i+1] -= sign; }
        while (n && !v[n]) n--;
        return *this;
    }

    int cmp(const bigint& x = 0) const {
        int i = max(n, x.n), t = 0;
        while (1) if ((t = ::cmp(v[i], x.v[i])) || i-- == 0) return t;
    }
    bool operator <(const bigint& x) const { return cmp(x) < 0; }
    bool operator ==(const bigint& x) const { return cmp(x) == 0; }
    bool operator !=(const bigint& x) const { return cmp(x) != 0; }

    operator string() const {
        ostringstream s; s << v[n];
        for (int i = n - 1; i > 0; i--) {
            s.width(DIG); s.fill('0'); s << abs(v[i]);
        }
        return s.str();
    }
    friend ostream& operator <<(ostream& o, const bigint& x) {
        return o << (string) x;
    }

    bigint& operator +=(const bigint& x) {
        for (int i = 1; i <= x.n; i++) v[i] += x.v[i];
        return fix(x.n);
    }
    bigint operator +(const bigint& x) { return bigint(*this) += x; }
    bigint& operator -=(const bigint& x) {
        for (int i = 1; i <= x.n; i++) v[i] -= x.v[i];

```

```

    return fix(x.n);
}
bigint operator -(const bigint& x) { return bigint(*this) -= x; }
bigint operator -() { bigint r = 0; return r -= *this; }
void ams(const bigint& x, int m, int b) { // *this += (x * m) << b;
    for (int i = 1, e = 0; (i <= x.n || e) && (n = i + b); i++) {
        v[i+b] += x.v[i] * m + e; e = v[i+b] / BASE; v[i+b] %= BASE;
    }
}
bigint operator *(const bigint& x) const {
    bigint r;
    for (int i = 1; i <= n; i++) r.ams(x, v[i], i-1);
    return r;
}
bigint& operator *=(const bigint& x) { return *this = *this * x; }
// cmp(x / y) == cmp(x) * cmp(y); cmp(x % y) == cmp(x);
bigint div(const bigint& x) {
    if (x == 0) return 0;
    bigint q; q.n = max(n - x.n + 1, 0);
    int d = x.v[x.n] * BASE + x.v[x.n-1];
    for (int i = q.n; i > 0; i--) {
        int j = x.n + i - 1;
        q.v[i] = int((v[j] * double(BASE) + v[j-1]) / d);
        ams(x, -q.v[i], i-1);
        if (i == 1 || j == 1) break;
        v[j-1] += BASE * v[j]; v[j] = 0;
    }
}

```

```

    }
    fix(x.n); return q.fix();
}
bigint& operator /=(const bigint& x) { return *this = div(x); }
bigint& operator %=(const bigint& x) { div(x); return *this; }
bigint operator /(const bigint& x) { return bigint(*this).div(x); }
bigint operator %(const bigint& x) { return bigint(*this) %= x; }
bigint pow(int x) {
    if (x < 0) return (*this == 1 || *this == -1) ? pow(-x) : 0;
    bigint r = 1;
    for (int i = 0; i < x; i++) r *= *this;
    return r;
}
bigint root(int x) {
    if (cmp() == 0 || cmp() < 0 && x % 2 == 0) return 0;
    if (*this == 1 || x == 1) return *this;
    if (cmp() < 0) return -(*this).root(x);
    bigint a = 1, d = *this;
    while (d != 1) {
        bigint b = a + (d /= 2);
        if (cmp(b.pow(x)) >= 0) { d += 1; a = b; }
    }
    return a;
}
};

```

## 6. STRING ALGORITHMS

### 6.1. Manber-Myers' algorithm. Hash: b32cb670595bef320decbceed7420bb8

```

int pos[MAXSZ], prm[MAXSZ], cnt[MAXSZ];
bool bh[MAXSZ + 1], b2h[MAXSZ];
int blast[256], bprev[MAXSZ];
int mm_segtree[4*MAXSZ];
string mm_s;

inline void regen_pos(int sz) {
    for(int i = 0; i < sz; i++)
        pos[prm[i]] = i;
}

inline void bubbleupbucket(int index) {
    if(index < 0) return;
}

```

```

int& prm_ext = prm[index];
cnt[prm_ext]++;
prm_ext += cnt[prm_ext] - 1;
b2h[prm_ext] = true;
}

void updatetree(int root, int l, int r, int pos, int val) {
    if(l == r) { mm_segtree[root] = val; return; }

    int m = (l + r + 1)/2;
    if(pos < m) updatetree(2*root + 1, l, m - 1, pos, val);
    else updatetree(2*root + 2, m, r, pos, val);

    mm_segtree[root] = min(mm_segtree[2*root + 1], mm_segtree[2*root + 2]);
}

```

```

}

int querytree(int root, int l, int r, int begin, int end) {
    if(begin == l && end == r) return mm_segtree[root];

    int m = (l + r + 1)/2;
    if(begin < m && end < m)
        return querytree(2*root + 1, l, m - 1, begin, end);
    else if(begin >= m && end >= m)
        return querytree(2*root + 2, m, r, begin, end);
    else return min(querytree(2*root + 1, l, m - 1, begin, m - 1),
        querytree(2*root + 2, m, r, m, end));
}

void mm_build(string s) {
    mm_s = s;
    memset(blast, -1, sizeof blast);
    memset(bh, 0, sizeof(bool) * s.size());
    memset(mm_segtree, 0x3f, sizeof(int) * 4 * s.size());
    updatetree(0, 0, s.size() - 1, s.size() - 1, 0);

    for(int i = 0; i < s.size(); i++) {
        bprev[i] = blast[s[i]];
        blast[s[i]] = i;
    }
    int let_count = 0;
    for(int i = 0; i < 256; i++) {
        if(blast[i] != -1) {
            bh[let_count] = true;
            if(let_count > 0)
                updatetree(0, 0, s.size() - 1, let_count - 1, 0);
        }
        for(int j = blast[i]; j != -1; j = bprev[j])
            prm[j] = let_count++;
    }
    regen_pos(s.size());
    bh[s.size()] = true;

    for(int st = 1; st < s.size(); st *= 2) {
        memset(cnt, 0, sizeof(int) * s.size());
        memset(b2h, 0, sizeof(bool) * s.size());

        for(int bl = 0, br = 0; br < s.size(); bl = br++)
            for(; !bh[br]; br++)
                prm[pos[br]] = bl;
    }
}

```

```

bubbleupbucket(s.size() - st);
for(int bl = 0, br = 0; br < s.size(); bl = br) {
    bubbleupbucket(pos[bl] - st);
    for(br++; !bh[br]; br++)
        bubbleupbucket(pos[br] - st);

    for(int i = bl; i < br; i++) {
        if(pos[i] - st < 0) continue;
        int prm_ext = prm[pos[i] - st];
        if(b2h[prm_ext])
            for(int j = prm_ext + 1; !bh[j] && b2h[j]; j++)
                b2h[j] = false;
    }
}

regen_pos(s.size());
for(int i = 0; i < s.size(); i++)
    if(!bh[i] && b2h[i]) {
        bh[i] = true;
        if(pos[i - 1] + st < s.size() && pos[i] + st < s.size()) {
            int m = min(prm[pos[i - 1] + st], prm[pos[i] + st]);
            int M = max(prm[pos[i - 1] + st], prm[pos[i] + st]);
            updatetree(0, 0, s.size() - 1, i - 1,
                st + querytree(0, 0, s.size() - 1, m, M - 1));
        }
        else
            updatetree(0, 0, s.size() - 1, i - 1, st);
    }
}

inline int lcp(string& s1, int p1, string& s2, int p2) {
    int limit = min(s1.size() - p1, s2.size() - p2), i;
    for(i = 0; i < limit; i++) if(s1[p1 + i] != s2[p2 + i]) break;
    return i;
}

pair<bool, int> mm_find(string s) {
    int l = lcp(mm_s, pos[0], s, 0);
    int r = lcp(mm_s, pos[mm_s.size() - 1], s, 0);

    if(l == s.size() || s[l] < mm_s[pos[0] + 1])
        return make_pair(l == s.size(), pos[0]);
    else if(r == s.size() || s[r] > mm_s[pos[mm_s.size() - 1] + r])
        return make_pair(r == s.size(), pos[mm_s.size() - 1]);
}

```



```

int low = 0, high = mm_s.size() - 1, next, st_n = 0, c_lcp;
while(high - low > 1) {
    int mid = (low + high)/2;
    c_lcp = max(l, r);
    st_n = 2*st_n + 1 + (l < r);

    if(mm_segtree[st_n] >= c_lcp)
        next = c_lcp + lcp(mm_s, pos[mid] + c_lcp, s, c_lcp);
    else
        next = mm_segtree[st_n];

    if(next == s.size())
        return make_pair(true, pos[mid]);

```

```

    else if(s[next] > mm_s[pos[mid] + next]) {
        low = mid;
        l = next;
    }
    else {
        high = mid;
        r = next;
    }
}

return make_pair(false, pos[high]);
}

```

## 6.2. Morris-Pratt's algorithm. Hash: ace505eff2be640ff01d7c48b2b7d12f

```

int pi[MAXSZ], res[MAXSZ], nres;

void morris_pratt(string text, string pattern) {
    nres = 0;
    pi[0] = -1;
    for(int i = 1; i < pattern.size(); i++) {
        pi[i] = pi[i-1];
        while(pi[i] >= 0 && pattern[pi[i] + 1] != pattern[i])
            pi[i] = pi[pi[i]];
        if(pattern[pi[i] + 1] == pattern[i]) pi[i]++;
    }
}

```

```

int k = 0; //k + 1 eh o tamanho do match atual
for(int i = 0; i < text.size(); i++) {
    while(k >= 0 && pattern[k + 1] != text[i])
        k = pi[k];
    if(pattern[k + 1] == text[i]) k++;
    if(k + 1 == pattern.size()) {
        res[nres++] = i;
        k = pi[k];
    }
}
}

```