ACM ICPC Team Reference

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Contents

1. Configuration files and scripts

1.1. .emacs. Hash: c62e934956fb568d3e909ce92ec379e8

```
(global-font-lock-mode t)
(setq transient-mark-mode t)
(global-set-key [f5] 'cxx-compile)

(defun cxx-compile()
  (interactive)
  (progn
    (save-buffer)
    (compile (concat "g++ -g -O2 -o " (substring buffer-file-name 0 -4)
                     buffer-file-name))
  )
)

(add-hook 'c++-mode-hook '(lambda () (c-set-style "stroustrup")))
```

1.2. .vimrc. Hash: c1e8578e5f779285977a53cce7a48031

```
syn on
filetype on
filetype plugin on
filetype indent on
colorscheme koehler

set number
set shiftwidth=4

set ts=4

imap <C-Space> <C-P>
set cinkeys=0{,0},0),0#,!<Tab>,;,:,o,O,e
set indentkeys=!<Tab>,o,O

runtime mswin.vim
```

1.3. Hash generator. Hash: 0d22aecd779fc370b30a2c628aff517c

```
#!/bin/sh

sed ':a;N;$!ba;s/[ \n\t]//g' | md5sum | cut -d' ' -f1
```

1.4. Solution template. Hash: 91b0fffaa0504c01fe4cc05bc08561d0

```cpp
#include <iostream>
#include <cstdio>
#include <algorithm>
#include <vector>
#include <set>
#include <queue>
#include <map>
#include <utility>
#include <cstring>
#include <cstdlib>
#include <cmath>
#include <cassert>

using namespace std;

typedef double TYPE;
const TYPE EPS = 1e-9;
const TYPE INF = 1e9;

inline int sgn(TYPE a) { return a > EPS ? 1 : (a < -EPS ? -1 : 0); }
inline int cmp(TYPE a, TYPE b) { return sgn(a - b); }

int main() {
    return 0;
}
```

2. Graph algorithms

2.1. Tarjan's SCC algorithm. Hash: f98d9589db68c8f1e8274cf53eb7f3bf

```
int lowest[MAXV], num[MAXV], visited[MAXV], comp[MAXV];
int prev_edge[MAXE], last_edge[MAXV], adj[MAXE], nedges;
int cur_num, cur_comp;
stack<int> visiting;

int t_init() {
    memset(last_edge, -1, sizeof last_edge);
    nedges = 0;
}

void t_edge(int v, int w) {
    prev_edge[nedges] = last_edge[v];
    adj[nedges] = w;
    last_edge[v] = nedges++;
}

int tarjan_dfs(int v) {
    lowest[v] = num[v] = cur_num++;
    visiting.push(v);

    visited[v] = 1;
    for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
        int w = adj[i];
        if(visited[w] == 0) lowest[v] = min(lowest[v], tarjan_dfs(w));
        else if(visited[w] == 1) lowest[v] = min(lowest[v], num[w]);
```

```
    }

    if(lowest[v] == num[v]) {
        int last = -1;
        while(last != v) {
            comp[last = visiting.top()] = cur_comp;
            visited[last] = 2;
            visiting.pop();
        }
        cur_comp++;
    }

    return lowest[v];
}

void tarjan_scc(int num_v = MAXV) {
    visiting = stack<int>();
    memset(visited, 0, sizeof visited);
    cur_num = cur_comp = 0;

    for(int i = 0; i < num_v; i++)
        if(!visited[i])
            tarjan_dfs(i);
}
```

2.2. Dinic's maximum flow algorithm. Hash: 4dd537effe7e233681c099912397839a

```
int last_edge[MAXV], cur_edge[MAXV], dist[MAXV];
int prev_edge[MAXE], cap[MAXE], flow[MAXE], adj[MAXE];
int nedges;

void d_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
}

void d_edge(int v, int w, int capacity, bool r = false) {
    prev_edge[nedges] = last_edge[v];
    cap[nedges] = capacity;
```

```
    adj[nedges] = w;
    flow[nedges] = 0;
    last_edge[v] = nedges++;

    if(!r) d_edge(w, v, 0, true);
}

bool d_auxflow(int source, int sink) {
    queue<int> q;
    q.push(source);

    memset(dist, -1, sizeof dist);
```

```
    dist[source] = 0;
    memcpy(cur_edge, last_edge, sizeof last_edge);

    while(!q.empty()) {
        int v = q.front(); q.pop();
        for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
            if(cap[i] - flow[i] == 0) continue;

            if(dist[adj[i]] == -1) {
                dist[adj[i]] = dist[v] + 1;
                q.push(adj[i]);

                if(adj[i] == sink) return true;
            }
        }
    }

    return false;
}

inline int rev(int i) { return i ^ 1; }

int d_augmenting(int v, int sink, int c) {
    if(v == sink) return c;
```

```
    for(int& i = cur_edge[v]; i != -1; i = prev_edge[i]) {
        if(cap[i] - flow[i] == 0 || dist[adj[i]] != dist[v] + 1)
            continue;

        int val;
        if(val = d_augmenting(adj[i], sink, min(c, cap[i] - flow[i]))) {
            flow[i] += val;
            flow[rev(i)] -= val;
            return val;
        }
    }

    return 0;
}

int dinic(int source, int sink) {
    int ret = 0;
    while(d_auxflow(source, sink)) {
        int flow;
        while(flow = d_augmenting(source, sink, 0x3f3f3f3f))
            ret += flow;
    }

    return ret;
}
```

2.3. Successive shortest paths mincost maxflow algorithm. Hash: 6933692fe046f78da13b05166c7e6d23

```
int dist[MAXV], last_edge[MAXV], d_visited[MAXV], bg_prev[MAXV], pot[MAXV],
    capres[MAXV];
int prev_edge[MAXE], adj[MAXE], cap[MAXE], cost[MAXE], flow[MAXE];

int nedges;
priority_queue<pair<int, int> > d_q;

inline void bg_edge(int v, int w, int capacity, int cst, bool r = false) {
    prev_edge[nedges] = last_edge[v];
    adj[nedges] = w;
    cap[nedges] = capacity;
    flow[nedges] = 0;
    cost[nedges] = cst;
    last_edge[v] = nedges++;

    if(!r) bg_edge(w, v, 0, -cost, true);
}
```

```
inline int rev(int i) { return i ^ 1; }
inline int from(int i) { return adj[rev(i)]; }

inline void bg_init() {
    nedges = 0;
    memset(last_edge, -1, sizeof last_edge);
    memset(pot, 0, sizeof pot);
}

void bg_dijkstra(int s, int num_nodes = MAXV) {
    memset(dist, 0x3f, sizeof dist);
    memset(d_visited, 0, sizeof d_visited);
    d_q.push(make_pair(dist[s] = 0, s));
    capres[s] = 0x3f3f3f3f;

    while(!d_q.empty()) {
```

```
      int v = d_q.top().second; d_q.pop();
      if(d_visited[v]) continue; d_visited[v] = true;

      for(int i = last_edge[v]; i != -1; i = prev_edge[i]) {
         if(cap[i] - flow[i] == 0) continue;
         int w = adj[i], new_dist = dist[v] + cost[i] + pot[v] - pot[w];

         if(new_dist < dist[w]) {
            d_q.push(make_pair(-(dist[w] = new_dist), w));
            bg_prev[w] = rev(i);
            capres[w] = min(capres[v], cap[i] - flow[i]);
         }
      }
   }
}

pair<int, int> busacker_gowen(int src, int sink, int num_nodes = MAXV) {
   int retFlow = 0, retCost = 0;
```

```
   bg_dijkstra(src, num_nodes);
   while(dist[sink] < 0x3f3f3f3f) {
      int cur = sink;
      while(cur != src) {
         flow[bg_prev[cur]] -= capres[sink];
         flow[rev(bg_prev[cur])] += capres[sink];
         retCost += cost[rev(bg_prev[cur])] * capres[sink];
         cur = adj[bg_prev[cur]];
      }
      retFlow += capres[sink];

      for(int i = 0; i < MAXV; i++)
         pot[i] = min(pot[i] + dist[i], 0x3f3f3f3f);

      bg_dijkstra(src, num_nodes);
   }
   return make_pair(retFlow, retCost);
}
```

2.4. **Gabow's general matching algorithm.** Hash: 31f8b67cd2b16187c6733f42801ee2be

```
int prev_edge[MAXE], v[MAXE], w[MAXE], last_edge[MAXV];
int type[MAXV], label[MAXV], first[MAXV], mate[MAXV], nedges;
bool g_flag[MAXV], g_souter[MAXV];

void g_init() {
   nedges = 0;
   memset(last_edge, -1, sizeof last_edge);
}

void g_edge(int a, int b) {
   prev_edge[nedges] = last_edge[a];
   v[nedges] = a;
   w[nedges] = b;
   last_edge[a] = nedges++;

   prev_edge[nedges] = last_edge[b];
   v[nedges] = b;
   w[nedges] = a;
   last_edge[b] = nedges++;
}

void g_label(int v, int join, int edge, queue<int>& outer) {
   if(v == join) return;
```

```
   if(label[v] == -1) outer.push(v);

   label[v] = edge;
   type[v] = 1;
   first[v] = join;

   g_label(first[label[mate[v]]], join, edge, outer);
}

void g_augment(int _v, int _w) {
   int t = mate[_v];
   mate[_v] = _w;

   if(mate[t] != _v) return;
   if(label[_v] == -1) return;

   if(type[_v] == 0) {
      mate[t] = label[_v];
      g_augment(label[_v], t);
   }
   else if(type[_v] == 1) {
      g_augment(v[label[_v]], w[label[_v]]);
      g_augment(w[label[_v]], v[label[_v]]);
```

```
        }
}

int gabow(int n) {
    memset(mate, -1, sizeof mate);
    memset(first, -1, sizeof first);

    int u = 0, ret = 0;
    for(int z = 0; z < n; z++) {
        if(mate[z] != -1) continue;

        memset(label, -1, sizeof label);
        memset(type, -1, sizeof type);
        memset(g_souter, 0, sizeof g_souter);

        label[z] = -1; type[z] = 0;

        queue<int> outer;
        outer.push(z);

        bool done = false;
        while(!outer.empty()) {
            int x = outer.front(); outer.pop();

            if(g_souter[x]) continue;
            g_souter[x] = true;

            for(int i = last_edge[x]; i != -1; i = prev_edge[i]) {
                if(mate[w[i]] == -1 && w[i] != z) {
                    mate[w[i]] = x;
                    g_augment(x, w[i]);
                    ret++;

                    done = true;
                    break;
                }
```

```
                if(type[w[i]] == -1) {
                    int v = mate[w[i]];
                    if(type[v] == -1) {
                        type[v] = 0;
                        label[v] = x;
                        outer.push(v);

                        first[v] = w[i];
                    }
                    continue;
                }

                int r = first[x], s = first[w[i]];
                if(r == s) continue;

                memset(g_flag, 0, sizeof g_flag);
                g_flag[r] = g_flag[s] = true;

                while(true) {
                    if(s != -1) swap(r, s);
                    r = first[label[mate[r]]];
                    if(g_flag[r]) break; g_flag[r] = true;
                }

                g_label(first[x], r, i, outer);
                g_label(first[w[i]], r, i, outer);

                for(int c = 0; c < n; c++)
                    if(type[c] != -1 && first[c] != -1 && type[first[c]] != -1)
                        first[c] = r;
            }
            if(done) break;
        }
    }
    return ret;
}
```

3. MATH

3.1. Fractions. Hash: 379fd408c3007c650c022fd4adfeabbd

```
struct frac {
    long long num, den;
```

```
    frac() : num(0), den(1) { };
    frac(long long num, long long den) { set_val(num, den); }
    frac(long long num) : num(num), den(1) { };
```

```cpp
    void set_val(long long _num, long long _den) {
        num = _num/__gcd(_num, _den);
        den = _den/__gcd(_num, _den);
        if(den < 0) { num *= -1; den *= -1; }
    }

    void operator*=(frac f) { set_val(num * f.num, den * f.den); }
    void operator+=(frac f) { set_val(num * f.den + f.num * den, den * f.den); }
    void operator-=(frac f) { set_val(num * f.den - f.num * den, den * f.den); }
    void operator/=(frac f) { set_val(num * f.den, den * f.num); }
};

bool operator<(frac a, frac b) {
    if((a.den < 0) ^ (b.den < 0)) return a.num * b.den > b.num * a.den;
    return a.num * b.den < b.num * a.den;
}
```

```cpp
std::ostream& operator<<(std::ostream& o, const frac f) {
    o << f.num << "/" << f.den;
    return o;
}

bool operator==(frac a, frac b) { return a.num * b.den == b.num * a.den; }
bool operator!=(frac a, frac b) { return !(a == b); }
bool operator<=(frac a, frac b) { return (a == b) || (a < b); }
bool operator>=(frac a, frac b) { return !(a < b); }
bool operator>(frac a, frac b) { return !(a <= b); }
frac operator/(frac a, frac b) { frac ret = a; ret /= b; return ret; }
frac operator*(frac a, frac b) { frac ret = a; ret *= b; return ret; }
frac operator+(frac a, frac b) { frac ret = a; ret += b; return ret; }
frac operator-(frac a, frac b) { frac ret = a; ret -= b; return ret; }
frac operator-(frac f) { return 0 - f; }
```

3.2. **Chinese remainder theorem.** Hash: 06b5ebd5c44c204a4b11bbb76d09023d

```cpp
struct t {
    long long a, b; int g;
    t(long long a, long long b, int g) : a(a), b(b), g(g) { }
    t swap() { return t(b, a, g); }
};

t egcd(int p, int q) {
    if(q == 0) return t(1, 0, p);

    t t2 = egcd(q, p % q);
```

```cpp
    t2.a -= t2.b * (p/q);
    return t2.swap();
}


int crt(int a, int p, int b, int q) {
    t t2 = egcd(p, q); t2.a %= p*q; t2.b %= p*q;
    assert(t2.g == 1);
    int ret = ((b * t2.a)%(p*q) * p + (a * t2.b)%(p*q) * q) % (p*q);
    return ret >= 0 ? ret : ret + p*q;
}
```

3.3. **Longest increasing subsequence.** Hash: 0f80b5d3af188d8bf4d1cbe45a76b46d

```cpp
vector<int> lis(vector<int>& seq) {
    int smallest_end[seq.size()+1], prev[seq.size()];
    smallest_end[1] = seq[0];

    int sz = 1;
    for(int i = 1; i < seq.size(); i++) {
        int lo = 0, hi = sz;
        while(lo < hi) {
            int mid = (lo + hi + 1)/2;
            if(seq[smallest_end[mid]] <= seq[i])
```

```cpp
                lo = mid;
            else
                hi = mid - 1;
        }

        prev[i] = smallest_end[lo];
        if(lo == sz)
            smallest_end[++sz] = i;
        else if(seq[i] < seq[smallest_end[lo+1]])
            smallest_end[lo+1] = i;
```

```
    }

    vector<int> ret;
    for(int cur = smallest_end[sz]; sz > 0; cur = prev[cur], sz--)
        ret.push_back(seq[cur]);
```

3.4. **Simplex (Warsaw University).** Hash: c687094970cf1953fd6f87a01adc6a95

```
const double EPS = 1e-9;
typedef long double T;
typedef vector<T> VT;
vector<VT> A;
VT b,c,res;
VI kt,N;
int m;
inline void pivot(int k,int l,int e){
    int x=kt[l]; T p=A[l][e];
    REP(i,k) A[l][i]/=p; b[l]/=p; N[e]=0;
    REP(i,m) if (i!=l) b[i]-=A[i][e]*b[l],A[i][x]=A[i][e]*-A[l][x];
    REP(j,k) if (N[j]){
        c[j]-=c[e]*A[l][j];
        REP(i,m) if (i!=l) A[i][j]-=A[i][e]*A[l][j];
    }
    kt[l]=e; N[x]=1; c[x]=c[e]*-A[l][x];
}

VT doit(int k){
    VT res; T best;
    while (1){
        int e=-1,l=-1; REP(i,k) if (N[i] && c[i]>EPS) {e=i; break;}
        if (e==-1) break;
        REP(i,m) if (A[i][e]>EPS && (l==-1 || best>b[i]/A[i][e]))
            best=b[ l=i ]/A[i][e];
```

```
        if (l==-1) /*ilimitado*/ return VT();
        pivot(k,l,e);
    }
    res.resize(k,0); REP(i,m) res[kt[i]]=b[i];
    return res;
}

VT simplex(vector<VT> &AA,VT &bb,VT &cc){
    int n=AA[0].size(),k;
    m=AA.size(); k=n+m+1; kt.resize(m); b=bb; c=cc; c.resize(n+m);
    A=AA; REP(i,m){ A[i].resize(k); A[i][n+i]=1; A[i][k-1]=-1; kt[i]=n+i;}
    N=VI(k,1); REP(i,m) N[kt[i]]=0;
    int pos=min_element(ALL(b))-b.begin();
    if (b[pos]<-EPS){
        c=VT(k,0); c[k-1]=-1; pivot(k,pos,k-1); res=doit(k);
        if (res[k-1]>EPS) /*impossivel*/ return VT();
        REP(i,m) if (kt[i]==k-1)
            REP(j,k-1) if (N[j] && (A[i][j]<-EPS || EPS<A[i][j])){
                pivot(k,i,j); break;
            }
        c=cc; c.resize(k,0); REP(i,m) REP(j,k) if (N[j]) c[j]-=c[kt[i]]*A[i][j];
    }
    res=doit(k-1); if (!res.empty()) res.resize(n);
    return res;
}
```

3.5. **Romberg's method.** Hash: a85facba1eac60c8909b04b552bd2222

```
long double romberg(int a, int b, double(*func)(double)) {
    long double approx[2][50];
    long double *cur=approx[1], *prev=approx[0];

    prev[0] = 1/2.0 * (b-a) * (func(a) + func(b));
    for(int it = 1; it < 25; it++, swap(cur, prev)) {
        if(it > 1 && cmp(prev[it-1], prev[it-2]) == 0)
```

```
            return prev[it-1];

        cur[0] = 1/2.0 * prev[0];
        long double div = (b-a)/pow(2, it);
        for(long double sample = a + div; sample < b; sample += 2 * div)
            cur[0] += div * func(a + sample);
```

```
    for(int j = 1; j <= it; j++)
        cur[j] = cur[j-1] + 1/(pow(4, it) - 1)*(cur[j-1] + prev[j-1]);
}
```

```
    return prev[24];
}
```

3.6. Floyd's cycle detection algorithm. Hash: 4aaa3277ea9011cae6d9b1358521f02c

```
pair<int, int> floyd(int x0) {
    int t = f(x0), h = f(f(x0)), start = 0, length = 1;
    while(t != h)
        t = f(t), h = f(f(h));

    h = t; t = x0;
    while(t != h)
        t = f(t), h = f(h), start++;
```

```
    h = f(t);
    while(t != h)
        h = f(h), length++;

    return make_pair(start, length);
}
```

3.7. Pollard's rho algorithm. Hash: ad4ee1d4afc564b2c55f90d6269994c4

```
long long pollard_r, pollard_n;

inline long long f(long long val) { return (val*val + pollard_r) % pollard_n; }
inline long long myabs(long long a) { return a >= 0 ? a : -a; }

long long pollard(long long n) {
    srand(unsigned(time(0)));
    pollard_n = n;

    long long d = 1;
    do {
```

```
        d = 1;
        pollard_r = rand() % n;

        long long x = 2, y = 2;
        while(d == 1)
            x = f(x), y = f(f(y)), d = __gcd(myabs(x-y), n);
    } while(d == n);

    return d;
}
```

3.8. Miller-Rabin's algorithm. Hash: e081ab82a09579a682aa62bee429c7f4

```
int fastpow(int base, int d, int n) {
    int ret = 1;
    for(long long pow = base; d > 0; d >>= 1, pow = (pow * pow) % n)
        if(d & 1)
            ret = (ret * pow) % n;
    return ret;
}

bool miller_rabin(int n, int base) {
    if(n <= 1) return false;
    if(n % 2 == 0) return n == 2;
```

```
    int s = 0, d = n - 1;
    while(d % 2 == 0) d /= 2, s++;

    int base_d = fastpow(base, d, n);
    if(base_d == 1) return true;
    int base_2r = base_d;

    for(int i = 0; i < s; i++) {
        if(base_2r == 1) return false;
        if(base_2r == n - 1) return true;
```

```
    base_2r = (long long)base_2r * base_2r % n;
  }

  return false;
}
```

```
bool isprime(int n) {
  return miller_rabin(n, 2) && miller_rabin(n, 7) && miller_rabin(n, 61);
}
```

3.9. **Polynomials (PUC-Rio).** Hash: d69d1ad494e487327d2338e69eccfa2f

```
typedef complex<double> cdouble;
int cmp(cdouble x, cdouble y = 0) {
  return cmp(abs(x), abs(y));
}
const int TAM = 200;
struct poly {
  cdouble poly[TAM]; int n;
  poly(int n = 0): n(n) { memset(p, 0, sizeof(p)); }
  cdouble& operator [](int i) { return p[i]; }
  poly operator ~() {
   poly r(n-1);
   for (int i = 1; i <= n; i++)
    r[i-1] = p[i] * cdouble(i);
   return r;
  }
  pair<poly, cdouble> ruffini(cdouble z) {
   if (n == 0) return make_pair(poly(), 0);
   poly r(n-1);
   for (int i = n; i > 0; i--) r[i-1] = r[i] * z + p[i];
   return make_pair(r, r[0] * z + p[0]);
  }
  cdouble operator ()(cdouble z) { return ruffini(z).second; }
  cdouble find_one_root(cdouble x) {
   poly p0 = *this, p1 = ~p0, p2 = ~p1;
   int m = 1000;
```

```
   while (m--) {
    cdouble y0 = p0(x);
    if (cmp(y0) == 0) break;
    cdouble G = p1(x) / y0;
    cdouble H = G * G - p2(x) - y0;
    cdouble R = sqrt(cdouble(n-1) * (H * cdouble(n) - G * G));
    cdouble D1 = G + R, D2 = G - R;
    cdouble a = cdouble(n) / (cmp(D1, D2) > 0 ? D1 : D2);
    x -= a;
    if (cmp(a) == 0) break;
   }
   return x;
  }
  vector<cdouble> roots() {
   poly q = *this;
   vector<cdouble> r;
   while (q.n > 1) {
    cdouble z(rand() / double(RAND_MAX), rand() / double(RAND_MAX));
    z = q.find_one_root(z); z = find_one_root(z);
    q = q.ruffini(z).first;
    r.push_back(z);
   }
   return r;
  }
};
```

4. GEOMETRY

4.1. **Point class.** Hash: 66e85d5b140956c47aa31754eab18864

```
struct pt {
  TYPE x, y;
  pt(TYPE x = 0, TYPE y = 0) : x(x), y(y) { }

  bool operator==(pt p) { return cmp(x, p.x) == 0 && cmp(y, p.y) == 0; }
```

```
  bool operator<(pt p) const {
    return cmp(x, p.x) ? cmp(x, p.x) < 0 : cmp(y, p.y) < 0;
  }
  bool operator<=(pt p) { return *this < p || *this == p; }
  TYPE operator||(pt p) { return x*p.x + y*p.y; }
```

```
   TYPE operator%(pt p) { return x*p.y - y*p.x; }
   pt operator~() { return pt(x, -y); }
   pt operator+(pt p) { return pt(x + p.x, y + p.y); }
   pt operator-(pt p) { return pt(x - p.x, y - p.y); }
   pt operator*(pt p) { return pt(x*p.x - y*p.y, x*p.y + y*p.x); }
   pt operator/(TYPE t) { return pt(x/t, y/t); }
   pt operator/(pt p) { return (*this * ~p)/(p||p); }
};
const pt I = pt(0,1);

struct circle {
   pt c; TYPE r;
   circle(pt c, TYPE r) : c(c), r(r) { }
};
```

```
TYPE norm(pt a) { return a||a; }
TYPE abs(pt a) { return sqrt(a||a); }
TYPE dist(pt a, pt b) { return abs(a - b); }
TYPE area(pt a, pt b, pt c) { return (a-c)%(b-c); }
int ccw(pt a, pt b, pt c) { return sgn(area(a, b, c)); }
pt unit(pt a) { return a/abs(a); }
double arg(pt a) { return atan2(a.y, a.x); }
pt f_polar(TYPE mod, double ang) { return pt(mod * cos(ang), mod * sin(ang)); }
inline int g_mod(int i, int n) { if(i == n) return 0; return i; }

ostream& operator<<(ostream& o, pt p) {
   return o << "(" << p.x << "," << p.y << ")";
}
```

4.2. Intersection primitives. Hash: ab780978106a5c062b8f7a129ebc9196

```
bool in_rect(pt a, pt b, pt c) {
   return sgn(c.x - min(a.x, b.x)) >= 0 && sgn(max(a.x, b.x) - c.x) >= 0 &&
          sgn(c.y - min(a.y, b.y)) >= 0 && sgn(max(a.y, b.y) - c.y) >= 0;
}
bool ps_isects(pt a, pt b, pt c) { return ccw(a,b,c) == 0 && in_rect(a,b,c); }

bool ss_isects(pt a, pt b, pt c, pt d) {
   if (ccw(a,b,c)*ccw(a,b,d) == -1 && ccw(c,d,a)*ccw(c,d,b) == -1) return true;
   return ps_isects(a, b, c) || ps_isects(a, b, d) ||
          ps_isects(c, d, a) || ps_isects(c, d, b);
}
```

```
pt parametric_isect(pt p, pt v, pt q, pt w) {
   double t = ((q-p)%w)/(v%w);
   return p + v*t;
}

pt ss_isect(pt p, pt q, pt r, pt s) {
   pt isect = parametric_isect(p, q-p, r, s-r);
   if(ps_isects(p, q, isect) && ps_isects(r, s, isect)) return isect;
   return pt(1/0.0, 1/0.0);
}
```

4.3. Polygon primitives. Hash: fba20bb1645bf37ab6c9b309d3850a7d

```
double p_area(vector<pt>& pol) {
   double ret = 0;
   for(int i = 0; i < pol.size(); i++)
      ret += pol[i] % pol[g_mod(i+1, pol.size())];
   return ret/2;
}

int point_polygon(pt p, vector<pt>& pol) {
   int n = pol.size(), count = 0;
```

```
   for(int i = 0; i < n; i++) {
      int i1 = g_mod(i+1, n);
      if (ps_isects(pol[i], pol[i1], p)) return -1;
      else if(((sgn(pol[i].y - p.y) == 1) != (sgn(pol[i1].y - p.y) == 1)) &&
         ccw(pol[i], p, pol[i1]) == sgn(pol[i].y - pol[i1].y)) count++;
   }
   return count % 2;
}
```

4.4. Miscellaneous primitives. Hash: be051245293a9db9c991d414c598e854

```cpp
bool point_circle(pt p, circle c) {
    return cmp(abs(p - c.c), c.r) <= 0;
}

double ps_distance(pt p, pt a, pt b) {
    p = p - a; b = b - a;
    double coef = min(max((b||p)/(b||b), TYPE(0)), TYPE(1));
    return abs(p - b*coef);
}
```

```cpp
pt circumcenter(pt a, pt b, pt c) {
    return parametric_isect((b+a)/2, (b-a)*I, (c+a)/2, (c-a)*I);
}

bool compy(pt a, pt b) {
    return cmp(a.y, b.y) ? cmp(a.y, b.y) < 0 : cmp(a.x, b.x) < 0;
}
bool compx(pt a, pt b) { return a < b; }
```

4.5. Smallest enclosing circle. Hash: 4e41d94c106dee349b45ca542ff0a532

```cpp
circle enclosing_circle(vector<pt>& pts) {
    srand(unsigned(time(0)));
    random_shuffle(pts.begin(), pts.end());

    circle c(pt(), -1);
    for(int i = 0; i < pts.size(); i++) {
        if(point_circle(pts[i], c)) continue;
        c = circle(pts[i], 0);
        for(int j = 0; j < i; j++) {
            if(point_circle(pts[j], c)) continue;
```

```cpp
            c = circle((pts[i] + pts[j])/2, abs(pts[i] - pts[j])/2);
            for(int k = 0; k < j; k++) {
                if(point_circle(pts[k], c)) continue;
                pt center = circumcenter(pts[i], pts[j], pts[k]);
                c = circle(center, abs(center - pts[i])/2);
            }
        }
    }
    return c;
}
```

4.6. Convex hull. Hash: a7f921d07f1b9b8a0053a0833329ddcf

```cpp
pt pivot;

bool hull_comp(pt a, pt b) {
    int turn = ccw(a, b, pivot);
    return turn == 1 || (turn == 0 && cmp(norm(a), norm(b)) < 0);
}

vector<pt> hull(vector<pt> pts) {
    if(pts.size() <= 1) return pts;
    vector<pt> ret;

    int mini = 0;
    for(int i = 1; i < pts.size(); i++)
        if(pts[i] < pts[mini])
            mini = i;
```

```cpp
    pivot = pts[mini];
    swap(pts[0], pts[mini]);
    sort(pts.begin() + 1, pts.end(), hull_comp);

    ret.push_back(pts[0]);
    ret.push_back(pts[1]);
    int sz = 2;

    for(int i = 2; i < pts.size(); i++) {
        while(sz >= 2 && ccw(ret[sz-2], ret[sz-1], pts[i]) <= 0)
            ret.pop_back(), sz--;
        ret.push_back(pts[i]), sz++;
    }

    return ret;
}
```

4.7. **Closest pair of points.** Hash: 251ad75a3af2d531a0cbb4e8138d3aef

```cpp
pair<pt, pt> closest_points_rec(vector<pt>& px, vector<pt>& py) {
    pair<pt, pt> ret;
    double d;

    if(px.size() <= 3) {
        double best = 1e10;
        for(int i = 0; i < px.size(); i++)
            for(int j = i + 1; j < px.size(); j++)
                if(dist(px[i], px[j]) < best) {
                    ret = make_pair(px[i], px[j]);
                    best = dist(px[i], px[j]);
                }

        return ret;
    }

    pt split = px[(px.size() - 1)/2];
    vector<pt> qx, qy, rx, ry;
    for(int i = 0; i < px.size(); i++)
        if(px[i] <= split) qx.push_back(px[i]);
        else rx.push_back(px[i]);

    for(int i = 0; i < py.size(); i++)
        if(py[i] <= split) qy.push_back(py[i]);
        else ry.push_back(py[i]);

    ret = closest_points_rec(qx, qy);
    pair<pt, pt> rans = closest_points_rec(rx, ry);
    double delta = dist(ret.first, ret.second);

    if((d = dist(rans.first, rans.second)) < delta) {
```

```cpp
        delta = d;
        ret = rans;
    }

    vector<pt> s;
    for(int i = 0; i < py.size(); i++)
        if(cmp(abs(py[i].x - split.x), delta) <= 0)
            s.push_back(py[i]);

    for(int i = 0; i < s.size(); i++)
        for(int j = 1; j <= 15 && i + j < s.size(); j++)
            if((d = dist(s[i], s[i+j])) < delta) {
                delta = d;
                ret = make_pair(s[i], s[i+j]);
            }

    return ret;
}

pair<pt, pt> closest_points(vector<pt> pts) {
    if(pts.size() == 1) return make_pair(pt(-INF, -INF), pt(INF, INF));

    sort(pts.begin(), pts.end());
    for(int i = 0; i + 1 < pts.size(); i++)
        if(pts[i] == pts[i+1])
            return make_pair(pts[i], pts[i+1]);

    vector<pt> py = pts;
    sort(py.begin(), py.end(), compy);
    return closest_points_rec(pts, py);
}
```

4.8. **Kd-tree.** Hash: de78e67c89c057ba920d2060641a7f48

```cpp
int tree[4*MAXSZ], val[4*MAXSZ];
TYPE split[4*MAXSZ];
vector<pt> pts;

void kd_recurse(int root, int left, int right, bool x) {
    if(left == right) {
        tree[root] = left;
        val[root] = 1;
```

```cpp
        return;
    }

    int mid = (right+left)/2;
    nth_element(pts.begin() + left, pts.begin() + mid,
            pts.begin() + right + 1, x ? compx : compy);
    split[root] = x ? pts[mid].x : pts[mid].y;
```

```
    kd_recurse(2*root+1, left, mid, !x);
    kd_recurse(2*root+2, mid+1, right, !x);

    val[root] = val[2*root+1] + val[2*root+2];
}

void kd_build() {
    memset(tree, -1, sizeof tree);
    kd_recurse(0, 0, pts.size() - 1, true);
}

int kd_query(int root, TYPE a, TYPE b, TYPE c, TYPE d, TYPE ca = -INF,
             TYPE cb = INF, TYPE cc = -INF, TYPE cd = INF, bool x) {
    if(a <= ca && cb <= b && c <= cc && cd <= d)
        return val[root];

    if(tree[root] != -1)
        return a <= pts[tree[root]].x && pts[tree[root]].x <= b &&
            c <= pts[tree[root]].y && pts[tree[root]].y <= d ? val[root] : 0;

    int ret = 0;
    if(x) {
        if(a <= split[root])
            ret += kd_query(2*root+1, a, b, c, d, ca, split[root], cc, cd, !x);
        if(split[root] <= b)
            ret += kd_query(2*root+2, a, b, c, d, split[root], cb, cc, cd, !x);
    }
```

```
    else {
        if(c <= split[root])
            ret += kd_query(2*root+1, a, b, c, d, ca, cb, cc, split[root], !x);
        if(split[root] <= d)
            ret += kd_query(2*root+2, a, b, c, d, ca, cb, split[root], cd, !x);
    }
    return ret;
}

pt kd_neighbor(int root, pt a, bool x) {
    if(tree[root] != -1)
        return a == pts[tree[root]] ? pt(2e9, 2e9) : pts[tree[root]];

    TYPE num = x ? a.x : a.y;
    int term = num <= split[root] ? 1 : 2;
    pt ret;

    TYPE d = norm(a - (ret = kd_neighbor(2*root + term, a, !x)));
    if((split[root] - num)*(split[root] - num) < d) {
        pt ret2 = kd_neighbor(2*root + 3 - term, a, !x);
        if(norm(a - ret2) < d)
            ret = ret2;
    }

    return ret;
}
```

4.9. **Range tree.** Hash: ef9df10aeb8ecbb4a515100657f2468a

```
vector<pt> pts, tree[MAXSZ];
vector<TYPE> xs;
vector<int> lnk[MAXSZ][2];

int rt_recurse(int root, int left, int right) {
    if(left == right) {
        vector<pt>::iterator it;
        it = lower_bound(pts.begin(), pts.end(), pt(xs[left], -INF));
        for(; it != pts.end() && it->x == xs[left]; it++)
            tree[root].push_back(*it);

        sort(tree[root].begin(), tree[root].end(), compy);
        return tree[root].size();
    }
```

```
    int mid = (left + right)/2, cl = 2*root + 1, cr = cl + 1;
    int sz1 = rt_recurse(cl, left, mid);
    int sz2 = rt_recurse(cr, mid + 1, right);

    int l = 0, r = 0, llink = 0, rlink = 0; pt last;
    while(l < sz1 || r < sz2) {
        if(r == sz2 || (l < sz1 && compy(tree[cl][l], tree[cr][r])))
            tree[root].push_back(last = tree[cl][l++]);
        else tree[root].push_back(last = tree[cr][r++]);

        while(llink < tree[cl].size() && compy(tree[cl][llink], last))
            llink++;
        while(rlink < tree[cr].size() && compy(tree[cr][rlink], last))
            rlink++;
```

```
        lnk[root][0].push_back(llink);
        lnk[root][1].push_back(rlink);
    }

    lnk[root][0].push_back(tree[cl].size());
    lnk[root][1].push_back(tree[cr].size());

    return tree[root].size();
}


void rt_build() {
    sort(pts.begin(), pts.end());
    for(int i = 0; i < pts.size(); i++) xs.push_back(pts[i].x);
    rt_recurse(0, 0, xs.size() - 1);
}

int rt_query(int root, int l, int r, TYPE a, TYPE b, TYPE c, TYPE d,
          int posl = -1, int posr = -1) {
    if(root == 0 && posl == -1) {
```

```
        posl = lower_bound(tree[0].begin(), tree[0].end(), pt(a, c), compy)
            - tree[0].begin();
        posr = upper_bound(tree[0].begin(), tree[0].end(), pt(b, d), compy)
            - tree[0].begin();
    }

    if(a <= xs[l] && xs[r] <= b)
        return posr - posl;
    if(posl >= tree[root].size()) return 0;

    int mid = (l + r)/2, ret = 0;
    if(a <= xs[mid])
        ret += rt_query(2*root+1, l, mid, a, b, c, d,
                lnk[root][0][posl], lnk[root][0][posr]);
    if(xs[mid+1] <= b)
        ret += rt_query(2*root+2, mid+1, r, a, b, c, d,
                lnk[root][1][posl], lnk[root][1][posr]);
    return ret;
}
```

5. Data structures

5.1. **Treap.** Hash: 2199b72803301716616a462d9d5e9a66

```
typedef int TYPE;

class treap {
public:
    treap *left, *right;
    int priority, sons;
    TYPE value;

    treap(TYPE value) : left(NULL), right(NULL), value(value), sons(0) {
        priority = rand();
    }

    ~treap() {
        if(left) delete left;
        if(right) delete right;
    }
};

treap* find(treap* t, TYPE val) {
    if(!t) return NULL;
    if(val == t->value) return t;
```

```
    if(val < t->value) return find(t->left, val);
    if(val > t->value) return find(t->right, val);
}

void rotate_to_right(treap* &t) {
    treap* n = t->left;
    t->left = n->right;
    n->right = t;
    t = n;
}

void rotate_to_left(treap* &t) {
    treap* n = t->right;
    t->right = n->left;
    n->left = t;
    t = n;
}

void fix_augment(treap* t) {
    if(!t) return;
```

```
    t->sons = (t->left ? t->left->sons + 1 : 0) +
        (t->right ? t->right->sons + 1 : 0);
}

void insert(treap* &t, TYPE val) {
    if(!t)
        t = new treap(val);
    else
        insert(val <= t->value ? t->left : t->right, val);

    if(t->left && t->left->priority > t->priority)
        rotate_to_right(t);
    else if(t->right && t->right->priority > t->priority)
        rotate_to_left(t);

    fix_augment(t->left); fix_augment(t->right); fix_augment(t);
}

inline int p(treap* t) {
```

```
    return t ? t->priority : -1;
}

void erase(treap* &t, TYPE val) {
    if(!t) return;

    if(t->value != val)
        erase(val < t->value ? t->left : t->right, val);
    else {
        if(!t->left && !t->right)
            delete t, t = NULL;
        else {
            p(t->left) < p(t->right) ? rotate_to_left(t) : rotate_to_right(t);
            erase(t, val);
        }
    }

    fix_augment(t->left); fix_augment(t->right); fix_augment(t);
}
```

5.2. **Heap.** Hash: e334218955a73d1286ad0fc19e84b642

```
struct heap {
    int heap[MAXV][2], v2n[MAXV];
    int size;

    void init(int sz) __attribute__((always_inline)) {
        memset(v2n, -1, sizeof(int) * sz);
        size = 0;
    }

    void swap(int& a, int& b) __attribute__((always_inline)) {
        int temp = a;
        a = b;
        b = temp;
    }

    void s(int a, int b) __attribute__((always_inline)) {
        swap(v2n[heap[a][1]], v2n[heap[b][1]]);
        swap(heap[a][0], heap[b][0]);
        swap(heap[a][1], heap[b][1]);
    }

    int extract_min() {
        int ret = heap[0][1];
```

```
        s(0, --size);

        int cur = 0, next = 2;
        while(next < size) {
            if(heap[next][0] > heap[next - 1][0])
                next--;
            if(heap[next][0] >= heap[cur][0])
                break;

            s(next, cur);
            cur = next;
            next = 2*cur + 2;
        }
        if(next == size && heap[next - 1][0] < heap[cur][0])
            s(next - 1, cur);

        return ret;
    }

    void decrease_key(int vertex, int new_value) __attribute__((always_inline))
    {
        if(v2n[vertex] == -1) {
         v2n[vertex] = size;
```

```
   heap[size++][1] = vertex;
  }

  heap[v2n[vertex]][0] = new_value;

  int cur = v2n[vertex];
  while(cur >= 1) {
    int parent = (cur - 1)/2;
```

```
       if(new_value >= heap[parent][0])
          break;

       s(cur, parent);
       cur = parent;
    }
  }
};
```

5.3. **Big numbers (PUC-Rio).** Hash: a7d74e7158634f9201c19235badd3364

```
const int DIG = 4;
const int BASE = 10000; // BASE**3 < 2**51
const int TAM = 2048;

struct bigint {
 int v[TAM], n;
 bigint(int x = 0): n(1) {
   memset(v, 0, sizeof(v));
   v[n++] = x; fix();
 }
 bigint(char *s): n(1) {
   memset(v, 0, sizeof(v));
   int sign = 1;
   while (*s && !isdigit(*s)) if (*s++ == '-') sign *= -1;
   char *t = strdup(s), *p = t + strlen(t);
   while (p > t) {
     *p = 0; p = max(t, p - DIG);
     sscanf(p, "%d", &v[n]);
     v[n++] *= sign;
   }
   free(t); fix();
 }
 bigint& fix(int m = 0) {
   n = max(m, n);
   int sign = 0;
   for (int i = 1, e = 0; i <= n || e && (n = i); i++) {
     v[i] += e; e = v[i] / BASE; v[i] %= BASE;
     if (v[i]) sign = (v[i] > 0) ? 1 : -1;
   }

   for (int i = n - 1; i > 0; i--)
     if (v[i] * sign < 0) { v[i] += sign * BASE; v[i+1] -= sign; }
   while (n && !v[n]) n--;
   return *this;
```

```
 }

 int cmp(const bigint& x = 0) const {
   int i = max(n, x.n), t = 0;
   while (1) if ((t = ::cmp(v[i], x.v[i])) || i-- == 0) return t;
 }
 bool operator <(const bigint& x) const { return cmp(x) < 0; }
 bool operator ==(const bigint& x) const { return cmp(x) == 0; }
 bool operator !=(const bigint& x) const { return cmp(x) != 0; }

 operator string() const {
   ostringstream s; s << v[n];
   for (int i = n - 1; i > 0; i--) {
     s.width(DIG); s.fill('0'); s << abs(v[i]);
   }
   return s.str();
 }
 friend ostream& operator <<(ostream& o, const bigint& x) {
   return o << (string) x;
 }

 bigint& operator +=(const bigint& x) {
   for (int i = 1; i <= x.n; i++) v[i] += x.v[i];
   return fix(x.n);
 }
 bigint operator +(const bigint& x) { return bigint(*this) += x; }
 bigint& operator -=(const bigint& x) {
   for (int i = 1; i <= x.n; i++) v[i] -= x.v[i];
   return fix(x.n);
 }
 bigint operator -(const bigint& x) { return bigint(*this) -= x; }
 bigint operator -() { bigint r = 0; return r -= *this; }
 void ams(const bigint& x, int m, int b) { // *this += (x * m) << b;
   for (int i = 1, e = 0; (i <= x.n || e) && (n = i + b); i++) {
```

```
   v[i+b] += x.v[i] * m + e; e = v[i+b] / BASE; v[i+b] %= BASE;
  }
 }
 bigint operator *(const bigint& x) const {
  bigint r;
  for (int i = 1; i <= n; i++) r.ams(x, v[i], i-1);
  return r;
 }
 bigint& operator *=(const bigint& x) { return *this = *this * x; }
 // cmp(x / y) == cmp(x) * cmp(y); cmp(x % y) == cmp(x);
 bigint div(const bigint& x) {
  if (x == 0) return 0;
  bigint q; q.n = max(n - x.n + 1, 0);
  int d = x.v[x.n] * BASE + x.v[x.n-1];
  for (int i = q.n; i > 0; i--) {
   int j = x.n + i - 1;
   q.v[i] = int((v[j] * double(BASE) + v[j-1]) / d);
   ams(x, -q.v[i], i-1);
   if (i == 1 || j == 1) break;
   v[j-1] += BASE * v[j]; v[j] = 0;
  }
  fix(x.n); return q.fix();
 }
```

```
  bigint& operator /=(const bigint& x) { return *this = div(x); }
  bigint& operator %=(const bigint& x) { div(x); return *this; }
  bigint operator /(const bigint& x) { return bigint(*this).div(x); }
  bigint operator %(const bigint& x) { return bigint(*this) %= x; }
  bigint pow(int x) {
   if (x < 0) return (*this == 1 || *this == -1) ? pow(-x) : 0;
   bigint r = 1;
   for (int i = 0; i < x; i++) r *= *this;
   return r;
  }
  bigint root(int x) {
   if (cmp() == 0 || cmp() < 0 && x % 2 == 0) return 0;
   if (*this == 1 || x == 1) return *this;
   if (cmp() < 0) return -(-*this).root(x);
   bigint a = 1, d = *this;

   while (d != 1) {
    bigint b = a + (d /= 2);
    if (cmp(b.pow(x)) >= 0) { d += 1; a = b; }
   }
   return a;
  }
};
```

6. String algorithms

6.1. **Manber-Myers' algorithm.** Hash: b32cb670595bef320decbceed7420bb8

```
int pos[MAXSZ], prm[MAXSZ], cnt[MAXSZ];
bool bh[MAXSZ + 1], b2h[MAXSZ];
int blast[256], bprev[MAXSZ];
int mm_segtree[4*MAXSZ];
string mm_s;

inline void regen_pos(int sz) {
   for(int i = 0; i < sz; i++)
      pos[prm[i]] = i;
}

inline void bubbleupbucket(int index) {
   if(index < 0) return;

   int& prm_ext = prm[index];
   cnt[prm_ext]++;
   prm_ext += cnt[prm_ext] - 1;
```

```
   b2h[prm_ext] = true;
}

void updatetree(int root, int l, int r, int pos, int val) {
   if(l == r) { mm_segtree[root] = val; return; }

   int m = (l + r + 1)/2;
   if(pos < m) updatetree(2*root + 1, l, m - 1, pos, val);
   else updatetree(2*root + 2, m, r, pos, val);

   mm_segtree[root] = min(mm_segtree[2*root + 1], mm_segtree[2*root + 2]);
}

int querytree(int root, int l, int r, int begin, int end) {
   if(begin == l && end == r) return mm_segtree[root];

   int m = (l + r + 1)/2;
```

```
    if(begin < m && end < m)
        return querytree(2*root + 1, l, m - 1, begin, end);
    else if(begin >= m && end >= m)
        return querytree(2*root + 2, m, r, begin, end);
    else return min(querytree(2*root + 1, l, m - 1, begin, m - 1),
                    querytree(2*root + 2, m, r, m, end));
}

void mm_build(string s) {
    mm_s = s;
    memset(blast, -1, sizeof blast);
    memset(bh, 0, sizeof(bool) * s.size());
    memset(mm_segtree, 0x3f, sizeof(int) * 4 * s.size());
    updatetree(0, 0, s.size() - 1, s.size() - 1, 0);

    for(int i = 0; i < s.size(); i++) {
        bprev[i] = blast[s[i]];
        blast[s[i]] = i;
    }
    int let_count = 0;
    for(int i = 0; i < 256; i++) {
        if(blast[i] != -1) {
            bh[let_count] = true;
            if(let_count > 0)
                updatetree(0, 0, s.size() - 1, let_count - 1, 0);
        }
        for(int j = blast[i]; j != -1; j = bprev[j])
            prm[j] = let_count++;
    }
    regen_pos(s.size());
    bh[s.size()] = true;

    for(int st = 1; st < s.size(); st *= 2) {
        memset(cnt, 0, sizeof(int) * s.size());
        memset(b2h, 0, sizeof(bool) * s.size());

        for(int bl = 0, br = 0; br < s.size(); bl = br++)
            for(; !bh[br]; br++)
                prm[pos[br]] = bl;

        bubbleupbucket(s.size() - st);
        for(int bl = 0, br = 0; br < s.size(); bl = br) {
            bubbleupbucket(pos[bl] - st);
            for(br++; !bh[br]; br++)
                bubbleupbucket(pos[br] - st);
```

```
            for(int i = bl; i < br; i++) {
                if(pos[i] - st < 0) continue;
                int prm_ext = prm[pos[i] - st];
                if(b2h[prm_ext])
                    for(int j = prm_ext + 1; !bh[j] && b2h[j]; j++)
                        b2h[j] = false;
            }
        }

        regen_pos(s.size());
        for(int i = 0; i < s.size(); i++)
            if(!bh[i] && b2h[i]) {
                bh[i] = true;
                if(pos[i - 1] + st < s.size() && pos[i] + st < s.size()) {
                    int m = min(prm[pos[i - 1] + st], prm[pos[i] + st]);
                    int M = max(prm[pos[i - 1] + st], prm[pos[i] + st]);
                    updatetree(0, 0, s.size() - 1, i - 1,
                               st + querytree(0, 0, s.size() - 1, m, M - 1));
                }
                else
                    updatetree(0, 0, s.size() - 1, i - 1, st);
            }
    }
}

inline int lcp(string& s1, int p1, string& s2, int p2) {
    int limit = min(s1.size() - p1, s2.size() - p2), i;
    for(i = 0; i < limit; i++) if(s1[p1 + i] != s2[p2 + i]) break;
    return i;
}

pair<bool, int> mm_find(string s) {
    int l = lcp(mm_s, pos[0], s, 0);
    int r = lcp(mm_s, pos[mm_s.size() - 1], s, 0);

    if(l == s.size() || s[l] < mm_s[pos[0] + l])
        return make_pair(l == s.size(), pos[0]);
    else if(r == s.size() || s[r] > mm_s[pos[mm_s.size() - 1] + r])
        return make_pair(r == s.size(), pos[mm_s.size() - 1]);

    int low = 0, high = mm_s.size() - 1, next, st_n = 0, c_lcp;
    while(high - low > 1) {
        int mid = (low + high)/2;
        c_lcp = max(l, r);
        st_n = 2*st_n + 1 + (l < r);
```

```
    if(mm_segtree[st_n] >= c_lcp)                                                              }
        next = c_lcp + lcp(mm_s, pos[mid] + c_lcp, s, c_lcp);                              else {
    else                                                                                       high = mid;
        next = mm_segtree[st_n];                                                               r = next;
                                                                                           }
    if(next == s.size())                                                                }
        return make_pair(true, pos[mid]);
    else if(s[next] > mm_s[pos[mid] + next]) {                                       return make_pair(false, pos[high]);
        low = mid;                                                               }
        l = next;
```

6.2. **Morris-Pratt's algorithm.** Hash: ace505eff2be640ff01d7c48b2b7d12f

```
int pi[MAXSZ], res[MAXSZ], nres;                                                 int k = 0; //k + 1 eh o tamanho do match atual
                                                                                 for(int i = 0; i < text.size(); i++) {
void morris_pratt(string text, string pattern) {                                   while(k >= 0 && pattern[k + 1] != text[i])
 nres = 0;                                                                            k = pi[k];
 pi[0] = -1;                                                                        if(pattern[k + 1] == text[i]) k++;
 for(int i = 1; i < pattern.size(); i++) {                                         if(k + 1 == pattern.size()) {
   pi[i] = pi[i-1];                                                                  res[nres++] = i;
   while(pi[i] >= 0 && pattern[pi[i] + 1] != pattern[i])                             k = pi[k];
       pi[i] = pi[pi[i]];                                                           }
   if(pattern[pi[i] + 1] == pattern[i]) pi[i]++;                                  }
 }                                                                             }
```

6.3. **Aho-Corasick's algorithm (UFPE).** Hash: 273f4391174d22898bfe3f2415f95915

```
struct No {                                                                      arvore[0].out.clear();
    int fail;                                                                     arvore[0].next = -1;
    vector< pair<int,int> > out; // num e tamanho do padrao                       qtdNos = 1;
    //bool marc; // p/ decisao                                                    qtdPadroes = 0;
    map<char, int> lista;                                                         //arvore[0].marc = false; // p/ decisao
    int next; // aponta para o proximo sufixo que tenha out.size > 0              //memset(encontrado, false, sizeof(encontrado)); // p/ decisao
};                                                                           }
No arvore[1000003]; // quantida maxima de nos
//bool encontrado[1005]; // quantidade maxima de padroes, p/ decisao          // Funcao para adicionar um padrao
int qtdNos, qtdPadroes;                                                       void adicionar(char *padrao) {
                                                                                 int no = 0, len = 0;
// Funcao para inicializar                                                        for (int i = 0 ; padrao[i] ; i++, len++) {
void inic() {                                                                         if (arvore[no].lista.find(padrao[i]) == arvore[no].lista.end()) {
    arvore[0].fail = -1;                                                                  arvore[qtdNos].lista.clear(); arvore[qtdNos].out.clear();
    arvore[0].lista.clear();                                                              //arvore[qtdNos].marc = false; // p/ decisao
```

```
            arvore[no].lista[padrao[i]] = qtdNos;
            no = qtdNos++;
        } else no = arvore[no].lista[padrao[i]];
    }
    arvore[no].out.push_back(pair<int,int>(qtdPadroes++,len));
}

// Ativar Aho-corasick, ajustando funcoes de falha
void ativar() {
    int no,v,f,w;
    queue<int> fila;
    for (map<char,int>::iterator it = arvore[0].lista.begin();
         it != arvore[0].lista.end() ; it++) {
        arvore[no = it->second].fail = 0;
        arvore[no].next = arvore[0].out.size() ? 0 : -1;
        fila.push(no);
    }
    while (!fila.empty()) {
        no = fila.front(); fila.pop();
        for (map<char,int>::iterator it=arvore[no].lista.begin();
             it!=arvore[no].lista.end(); it++) {
            char c = it->first;
            v = it->second;
            fila.push(v);
            f = arvore[no].fail;
            while (arvore[f].lista.find(c) == arvore[f].lista.end()) {
                if (f == 0) { arvore[0].lista[c] = 0; break; }
                f = arvore[f].fail;
            }
            w = arvore[f].lista[c];
```

```
            arvore[v].fail = w;
            arvore[v].next = arvore[w].out.size() ? w : arvore[w].next;
        }
    }
}

// Buscar padroes no aho-corasik
void buscar(char *input) {
    int v, no = 0;
    for (int i = 0 ; input[i] ; i++) {
        while (arvore[no].lista.find(input[i]) == arvore[no].lista.end()) {
            if (no == 0) { arvore[0].lista[input[i]] = 0; break; }
            no = arvore[no].fail;
        }
        v = no = arvore[no].lista[input[i]];
        // marcar os encontrados
        while (v != -1 /* && !arvore[v].marc */ ) { // p/ decisao
            //arvore[v].marc = true; // p/ decisao: nao continua a lista
            for (int k = 0 ; k < arvore[v].out.size() ; k++) {
                //encontrado[arvore[v].out[k].first] = true; // p/ decisao
                printf("Padrao %d na posicao %d\n", arvore[v].out[k].first,
                       i-arvore[v].out[k].second+1);
            }
            v = arvore[v].next;
        }
    }
    // for (int i = 0 ; i < qtdPadroes ; i++)
    //printf("%s\n", encontrado[i]?"y":"n"); // p/ decisao
}
```

7. Useful mathematical facts

7.1. Prime counting function ($\pi(x)$).
The prime counting function is asymptotic to $\frac{x}{\log x}$, by the prime number theorem.

x	10	10^2	10^3	10^4	10^5	10^6	10^7	10^8
$\pi(x)$	4	25	168	1.229	9.592	78.498	664.579	5.761.455

7.2. Partition function.
The partition function $p(x)$ counts show many ways there are to write the integer x as a sum of integers.

x	36	37	38	39	40	41	42
p(x)	17.977	21.637	26.015	31.185	37.338	44.583	53.174
x	43	44	45	46	47	100	
p(x)	63.261	75.175	89.134	105.558	125.754	190.569.292	

7.3. Catalan numbers.
Catalan numbers are defined by the recurrence:

$$C_{n+1} = \sum_{i=0}^{n} C_i C_{n-i}$$

A closed formula for Catalan numbers is:

$$C_n = \frac{1}{n+1}\binom{2n}{n} = \binom{2n}{n} - \binom{2n}{n+1}$$

7.4. Stirling numbers of the first kind.
These are the number of permutations of I_n with exactly k disjoint cycles. They obey the recurrence:

$$\begin{bmatrix} n \\ k \end{bmatrix} = (n-1)\begin{bmatrix} n-1 \\ k \end{bmatrix} + \begin{bmatrix} n-1 \\ k-1 \end{bmatrix}$$

7.5. Stirling numbers of the second kind.
These are the number of ways to partition I_n into exactly k sets. They obey the recurrence:

$$\begin{Bmatrix} n \\ k \end{Bmatrix} = k\begin{Bmatrix} n-1 \\ k \end{Bmatrix} + \begin{Bmatrix} n-1 \\ k-1 \end{Bmatrix}$$

A "closed" formula for it is:

$$\begin{Bmatrix} n \\ k \end{Bmatrix} = \frac{1}{k!}\sum_{j=0}^{k}(-1)^{k-j}\binom{k}{j}j^n$$

7.6. Bell numbers.
These count the number of ways to partition I_n into subsets. They obey the recurrence:

$$\mathcal{B}_{n+1} = \sum_{k=0}^{n}\binom{n}{k}\mathcal{B}_k$$

x	5	6	7	8	9	10	11	12
$\mathcal{B}_x$	52	203	877	4.140	21.147	115.975	678.570	4.213.597

7.7. Turán's theorem.
No graph with n vertices that is K_{r+1}-free can have more edges than the Turán graph: A k-partite complete graph with sets of size as equal as possible.

7.8. Generating functions.
A list of generating functions for useful sequences:

$(1, 1, 1, 1, 1, 1, \ldots)$	$\frac{1}{1-z}$
$(1, -1, 1, -1, 1, -1, \ldots)$	$\frac{1}{1+z}$
$(1, 0, 1, 0, 1, 0, \ldots)$	$\frac{1}{1-z^2}$
$(1, 0, \ldots, 0, 1, 0, 1, 0, \ldots, 0, 1, 0, \ldots)$	$\frac{1}{1-z^2}$
$(1, 2, 3, 4, 5, 6, \ldots)$	$\frac{1}{(1-z)^2}$
$(1, \binom{m+1}{m}, \binom{m+2}{m}, \binom{m+3}{m}, \ldots)$	$\frac{1}{(1-z)^{m+1}}$
$(1, c, \binom{c+1}{2}, \binom{c+2}{3}, \ldots)$	$\frac{1}{(1-z)^c}$
$(1, c, c^2, c^3, \ldots)$	$\frac{1}{1-cz}$
$(0, 1, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \ldots)$	$\ln\frac{1}{1-z}$

A neat manipulation trick is:

$$\frac{1}{1-z}G(z) = \sum_n \sum_{k \leq n} g_k z^n$$

7.9. Polyominoes. How many free (rotation, reflection), one-sided (rotation) and fixed n-ominoes are there?

n	3	4	5	6	7	8	9	10
free	2	5	12	35	108	369	1.285	4.655
one-sided	2	7	18	60	196	704	2.500	9.189
fixed	6	19	63	216	760	2.725	9.910	36.446

7.10. The twelvefold way (from Stanley). How many functions $f \colon N \to X$ are there?

N	X	Any f	Injective	Surjective
dist.	dist.	x^n	$(x)_n$	$x!\{{n \atop x}\}$
indist.	dist.	$\binom{x+n-1}{n}$	$\binom{x}{n}$	$\binom{n-1}{n-x}$
dist.	indist.	$\{{n \atop 1}\} + \ldots + \{{n \atop x}\}$	$[n \le x]$	$\{{n \atop k}\}$
indist.	indist.	$p_1(n) + \ldots p_x(n)$	$[n \le x]$	$p_x(n)$

Where $\binom{a}{b} = \frac{1}{b!}(a)_b$ and $p_x(n)$ is the number of ways to partition the integer n using x summands.

7.11. Common integral substitutions. And finally, a list of common substitutions:

$\int F(\sqrt{ax+b})dx$	$u = \sqrt{ax+b}$	$\frac{2}{a}\int uF(u)du$
$\int F(\sqrt{a^2-x^2})dx$	$x = a\sin u$	$a\int F(a\cos u)\cos u\,du$
$\int F(\sqrt{x^2+a^2})dx$	$x = a\tan u$	$a\int F(a\sec u)\sec^2 u\,du$
$\int F(\sqrt{x^2-a^2})dx$	$x = a\sec u$	$a\int F(a\tan u)\sec u\tan u\,du$
$\int F(e^{ax})dx$	$u = e^{ax}$	$\frac{1}{a}\int \frac{F(u)}{u}du$
$\int F(\ln x)dx$	$u = \ln x$	$\int F(u)e^u du$

7.12. Table of non-trigonometric integrals. Some useful integrals are:

$\int \frac{dx}{x^2+a^2}$	$\frac{1}{a}\arctan\frac{x}{a}$
$\int \frac{dx}{x^2-a^2}$	$\frac{1}{2a}\ln\frac{x-a}{x+a}$
$\int \frac{dx}{a^2-x^2}$	$\frac{1}{2a}\ln\frac{a+x}{a-x}$
$\int \frac{dx}{\sqrt{a^2-x^2}}$	$\arcsin\frac{x}{a}$
$\int \frac{dx}{\sqrt{x^2-a^2}}$	$\ln\left(u+\sqrt{x^2-a^2}\right)$
$\int \frac{dx}{x\sqrt{x^2-a^2}}$	$\frac{1}{a}\operatorname{arcsec}\left|\frac{u}{a}\right|$
$\int \frac{dx}{x\sqrt{x^2+a^2}}$	$-\frac{1}{a}\ln\left(\frac{a+\sqrt{x^2+a^2}}{x}\right)$
$\int \frac{dx}{x\sqrt{a^2+x^2}}$	$-\frac{1}{a}\ln\left(\frac{a+\sqrt{a^2-x^2}}{x}\right)$

7.13. Table of trigonometric integrals. A list of common and not-so-common trigonometric integrals:

$\int \tan x\,dx$	$-\ln|\cos x|$
$\int \cot x\,dx$	$\ln|\sin x|$
$\int \sec x\,dx$	$\ln|\sec x + \tan x|$
$\int \csc x\,dx$	$\ln|\csc x - \cot x|$
$\int \sec^2 x\,dx$	$\tan x$
$\int \csc^2 x\,dx$	$\cot x$
$\int \sin^n x\,dx$	$\frac{-\sin^{n-1}x\cos x}{n} + \frac{n-1}{n}\int \sin^{n-2}x\,dx$
$\int \cos^n x\,dx$	$\frac{\cos^{n-1}x\sin x}{n} + \frac{n-1}{n}\int \cos^{n-2}x\,dx$
$\int \arcsin x\,dx$	$x\arcsin x + \sqrt{1-x^2}$
$\int \arccos x\,dx$	$x\arccos x - \sqrt{1-x^2}$
$\int \arctan x\,dx$	$x\arctan x - \frac{1}{2}\ln|1-x^2|$