



# **Exploratory Data Analysis**











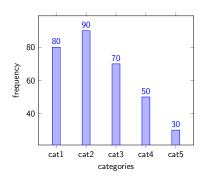








### Graphical analysis categorical attribute



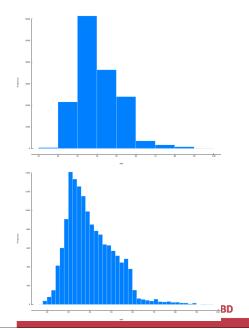
$$f_h = \frac{e_h}{m} = \frac{card\{i \in \mathcal{M} : x_i = cat_h\}}{m}$$

for large samples

$$f_h \approx P(x = cat_h)$$

**BABD** 

## Graphical analysis numerical attribute



### Central tendency

Mean:

$$\bar{x} = \frac{1}{m} \sum_{i=1}^{m} x_i$$

Median:

$$x^{\text{med}} = x_{(m+1)/2}, \qquad x^{\text{med}} = (x_{m/2} + x_{m/2+1})/2$$

- Mode
- Midrange:

$$x^{\mathsf{midr}} = (x_{\mathsf{max}} + x_{\mathsf{min}})/2$$

► Geometric mean=

$$\bar{\mu}_{\mathsf{geom}} = \sqrt[m]{\prod_{i}^{m} x_i}$$

### Measure of dispersion - numerical

Range:

$$x_{\text{max}} - x_{\text{min}}$$

Mean absolute deviation :

$$MAD = \frac{1}{m} \sum_{i=1}^{m} |x_i - \bar{m}u|$$

Sample variance:

$$\bar{\sigma}^2 = \frac{1}{m-1} \sum_{i=1}^m (x_i - \bar{\mu})^2$$

Sample standard deviation :

$$\bar{\sigma} = \sqrt{\bar{\sigma}^2}$$

Coefficient of Variation:

$$extit{CV} = 100 rac{\sigma}{\mu}$$

## Measure of dispersion - categorical

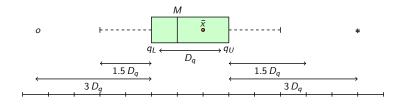
► Gini index:

$$Gini = 1 - \sum_{h=1}^{H} f_h^2 \qquad \in [0, (H-1)/H]$$

**▶** Entropy index:

$$Entropy = -\sum_{h=1}^{H} f_h \log_2 f_h \qquad \in [0, log_2 H]$$

### Box-plot



- $D_q = q_U q_L = q_{0.75} q_{0.25}$
- ightharpoonup internal lower edge=  $q_L 1.5 D_q$
- ightharpoonup external lower edge=  $q_L 3 D_q$

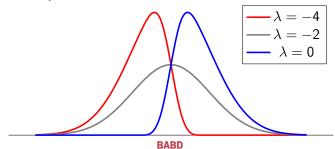
#### Measure relative location

- **Mead-Mean**: Mean of values between  $q_L$  and  $q_U$
- **Trimmed-Mean**: Mean of values between  $q_p$  and  $q_{(1-p)}$
- **Winsorized-Mean**: Map values smaller (bigger) than  $q_p(q_{(1-p)})$  to  $q_p(q_{(1-p)})$  and then compute the mean

### Asymmetry

$$\bar{\mu}_3 = \frac{1}{m} \sum_{i=1}^m (x_i - \bar{\mu})^3$$
, Skewness  $= I_{as} = \frac{\bar{\mu}_3}{\bar{\sigma}^3}$ 

- $ightharpoonup I_{as} > 0$  right asymmetry
- $ightharpoonup I_{as} < 0$  left asymmetry
- $I_{as} > 0$  symmetric

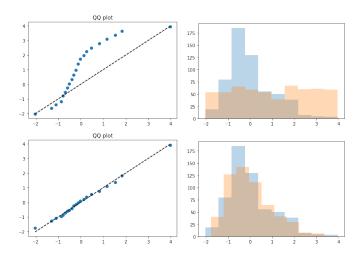


### Empirical density

$$\bar{\mu}_4 = \frac{1}{m} \sum_{i=1}^{m} (x_i - \bar{\mu})^4, \quad \text{Kurtosis} = I_{kurt} = \frac{\bar{\mu}_4}{\bar{\sigma}^4} - 3$$

- $I_{kurt} > 0$  Hypernormal
- ► *I<sub>kurt</sub>* < 0 Hyponormal
- $I_{kurt} > 0$  Normal

## QQ-plots



#### Measure of correlation

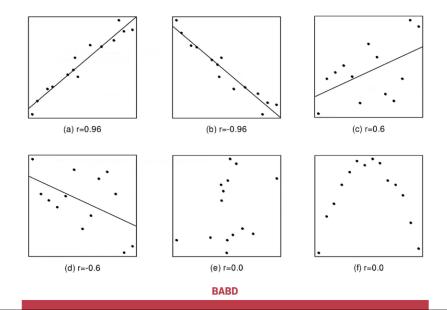
Sample covariance:

$$cov(a_j, a_k) = \frac{1}{m-2} \sum_{i=1}^{m} (x_{ij} - \bar{\mu}_j)(x_{ik} - \bar{\mu}_k)$$

Sample LINEAR correlation:

$$r_{jk} = \frac{cov(a_j, a_k)}{\bar{\sigma}_i \, \bar{\sigma}_i} \qquad \in [-1, 1]$$

#### **Linear Correlation**



#### Correlation on categorical attributes

#### **Contingency tables**

		family		
area		0	1	totale
1		2	4	6 ( <i>f</i> <sub>1</sub>
2		4	2	6
3		2	5	7
4		3	3	6
	totale	11 (g1)	14 (g <sub>2</sub> )	25

#### Two attributes are independent if

$$\frac{t_{r1}}{g_1} = \frac{t_{r2}}{g_2} \qquad r = 1, 2, \dots, J$$