## **Exercise 1**

- a) X Variable
- b)  $\lambda x \cdot x$  Abstraction
- c) (XQ.Z)Q Application
- d) λά. ②a Abstraction
- e)  $(\lambda n. n)$  Application
- f)  $\lambda z. (\lambda y. (\lambda x. x)y)z$  Abstraction
- g)  $(\lambda t. ((\lambda t. (\lambda t. t)t)t))$  Application

## Exercise 2

- a)  $\lambda x. x(\lambda z. z)$
- b)  $\lambda w. w(\lambda z. zx)$
- c)  $(f(\lambda x. yx)y(fy))$
- d)  $\lambda w. w(\lambda x. yx)y(fy)$

## Exercise 3

- a)  $(\lambda w. y)x 1$  redex
- b)  $(\lambda y. z)(\lambda x. x) 1$  redex
- c)  $\lambda w. w(\lambda x. xy) 1$  redex
- d)  $(\lambda x. xx)(\lambda x. x) 2$  redexes  $((\lambda y. y)(\lambda x. x))((\lambda y. y)(\lambda x. x))$
- e)  $(\lambda y. y)(\lambda y. y)(\lambda x. x) 1$  redex
- f)  $(\lambda x. xx)(\lambda x. xx)((\lambda y. y)(\lambda x. x)) 2$  redexes  $(\lambda x. xx)(\lambda x. xx)(\lambda x. xx)$

## **Exercise 4**

- a)  $M = (\lambda x. x)(\lambda x. x)$ 
  - $N = (\lambda y. \lambda x. x)x$
- b)  $M = ((\lambda x. x)(\lambda x. x))((\lambda y. x)(\lambda z. z))((\lambda x. xx)(\lambda z. z))$ 
  - $N = (\lambda x. x)((\lambda y. x)(\lambda z. z))((\lambda x. xx)(\lambda z. z))$
  - $P = ((\lambda x. x)(\lambda x. x))x((\lambda x. xx)(\lambda z. z))$
  - $Q = ((\lambda x. x)(\lambda x. x))((\lambda y. x)(\lambda z. z))((\lambda z. z)(\lambda z. z))$