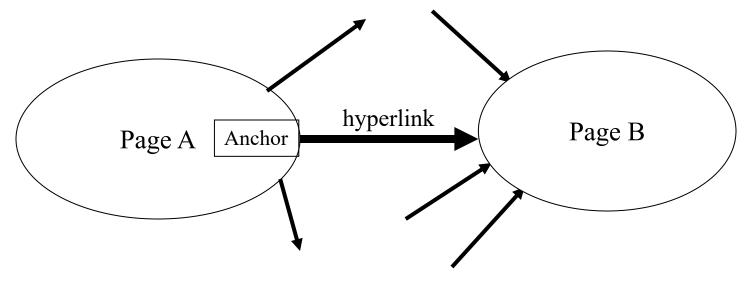
Introduction to Information Retrieval

Lecture 18: Link analysis

Today's lecture

- Anchor text
- Link analysis for ranking
 - Pagerank and variants

The Web as a Directed Graph



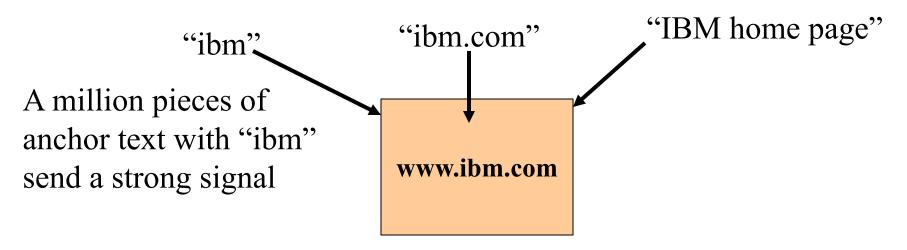
Assumption 1: A hyperlink between pages denotes author perceived relevance (quality signal)

Assumption 2: The text in the anchor of the hyperlink describes the target page (textual context)

Anchor Text

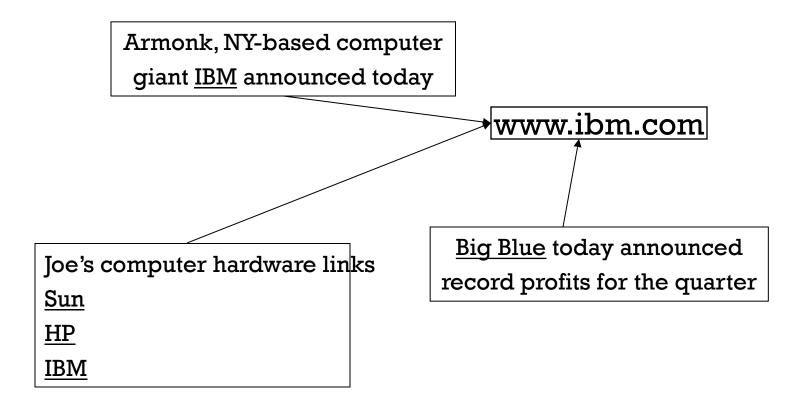
WWW Worm - McBryan [Mcbr94]

- For *ibm* how to distinguish between:
 - IBM's home page (mostly graphical)
 - IBM's copyright page (high term freq. for 'ibm')
 - Rival's spam page (arbitrarily high term freq.)



Indexing anchor text

 When indexing a document D, include anchor text from links pointing to D.



Indexing anchor text

- Can sometimes have unexpected side effects e.g.,
 evil empire.
- Can score anchor text with weight depending on the authority of the anchor page's website
 - E.g., if we were to assume that content from cnn.com or yahoo.com is authoritative, then trust the anchor text from them

Anchor Text

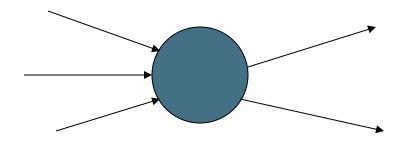
- Other applications
 - Weighting/filtering links in the graph
 - Generating page descriptions from anchor text

Citation Analysis

- Citation frequency
- Co-citation coupling frequency
 - Cocitations with a given author measures "impact"
 - Cocitation analysis
- Bibliographic coupling frequency
 - Articles that co-cite the same articles are related
- Citation indexing
 - Who is this author cited by? (Garfield 1972)
- Pagerank preview: Pinsker and Narin '60s

Query-independent ordering

- First generation: using link counts as simple measures of popularity.
- Two basic suggestions:
 - Undirected popularity:
 - Each page gets a score = the number of in-links plus the number of out-links (3+2=5).
 - Directed popularity:
 - Score of a page = number of its in-links (3).



Query processing

- First retrieve all pages meeting the text query (say venture capital).
- Order these by their link popularity (either variant on the previous slide).
- More nuanced use link counts as a measure of static goodness (Lecture 7), combined with text match score

Spamming simple popularity

- Exercise: How do you spam each of the following heuristics so your page gets a high score?
- Each page gets a static score = the number of inlinks plus the number of out-links.
- 2. Static score of a page = number of its in-links.

Ideas of Pagerank

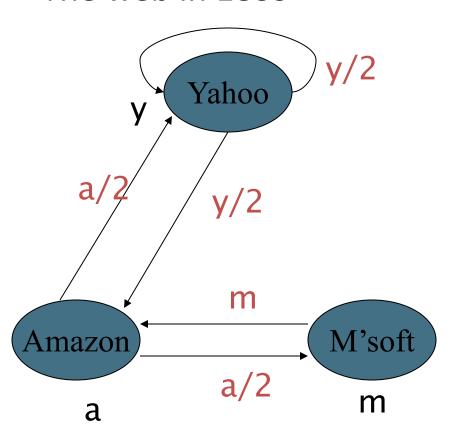
- Inlinks as votes
 - www.stanford.edu has 23,400 inlinks
 - www.joe-schmoe.com has 1 inlink
- Web pages are not equally "important"
 - www.joe-schmoe.com → p1
 - VS. <u>www.stanford.edu</u> → p2
- Are all inlinks equal?
 - Recursive question!

Pagerank scoring

- Imagine a browser doing a random walk on web pages:
 - Start at a random page
 - At each step, go out of the current page along one of the links on that page, equiprobably
- "In the steady state" each page has a long-term visit rate - use this as the page's score.

Example – the Simple "Flow" Model

The web in 1839



$$y = y/2 + a/2$$

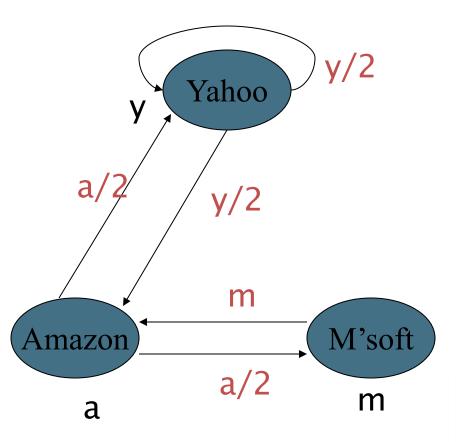
 $a = y/2 + m$
 $m = a/2$

Solving the flow equations

- 3 equations, 3 unknowns, no constants
 - No unique solution
 - All solutions equivalent modulo scale factor
- Additional constraint forces uniqueness
 - y+a+m = 1
 - y = 2/5, a = 2/5, m = 1/5
- Gaussian elimination method works for small examples, but we need a better method for large graphs

Example – the Simple "Flow" Model

The web in 1839



$$y_{new} = y_{old}/2 + a_{old}/2$$

 $a_{new} = y_{old}/2 + m_{old}$
 $m_{new} = a_{old}/2$
 $y = 1/3$ 1/3 5/12 ... 2/5
 $a = 1/3$ 1/2 1/3 ... 2/5

Matrix-based characterization of the computation is simpler and more useful for the general case.

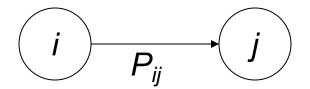
 $m = 1/3 \quad 1/6 \quad 1/4 \quad \dots 1/5$

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Markov chains

- A Markov chain consists of n states, plus an $n \times n$ transition probability matrix **P**.
- At each step, we are in exactly one of the states.
- For $1 \le i,j \le n$, the matrix entry P_{ij} tells us the probability of j being the next state, given we are currently in state i.



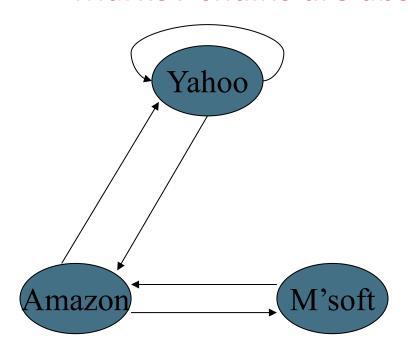


Markov chains

• Clearly, for all i, $\sum_{j=1}^{n} P_{ij} = 1.$

$$\sum_{i=1}^{n} P_{ij} = 1.$$

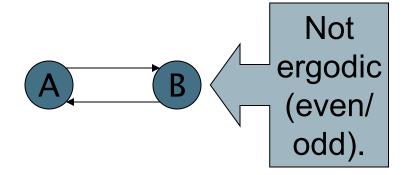
Markov chains are abstractions of random walks.



	У	a	m
y	1/2	1/2	0
a [1/2	0	1/2
m	0	1	0

Ergodic Markov chains

- A Markov chain is <u>ergodic</u> if
 - you have a path from any state to any other
 - For any start state, after a finite transient time T₀, the probability of being in any state at a fixed time T>T₀ is nonzero.



Ergodic Markov chains

- For any ergodic Markov chain, there is a unique long-term visit rate for each state.
 - Steady-state probability distribution.
- Over a long time-period, we visit each state in proportion to this rate.
- It doesn't matter where we start.

Probability vectors

- A probability (row) vector $\mathbf{x} = (x_1, ... x_n)$ tells us where the walk is at any point.
- E.g., (000...1...000) means we're in state i.
 1 i n

More generally, the vector $\mathbf{x} = (x_1, \dots x_n)$ means the walk is in state i with probability x_i .

$$\sum_{i=1}^{n} x_i = 1$$

Change in probability vector

- If the probability vector is $\mathbf{x} = (x_1, ... x_n)$ at this step, what is it at the next step?
- Recall that row *i* of the transition prob.
 Matrix P tells us where we go next from state *i*.
- So from x, our next state is distributed as xP.

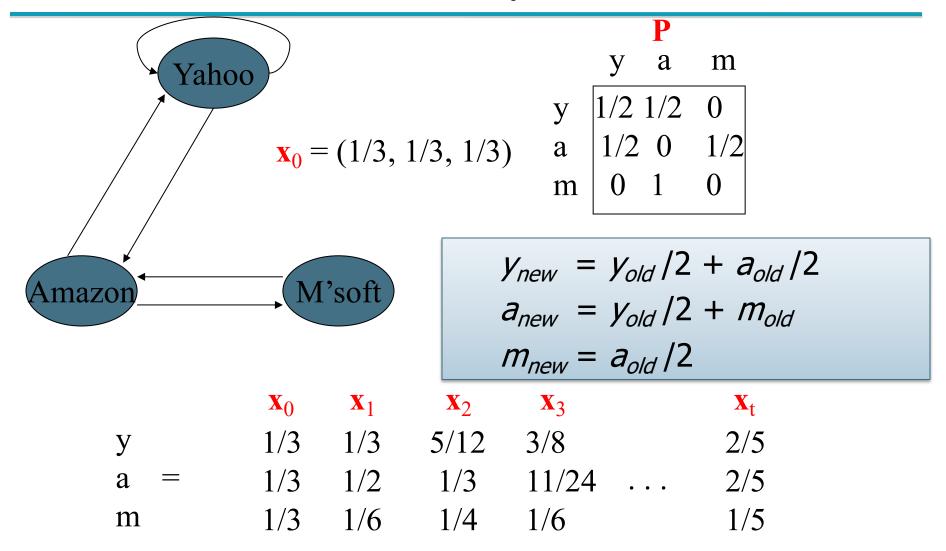
How do we compute this vector?

- Let $\mathbf{a} = (a_1, \dots a_n)$ denote the row vector of steadystate probabilities.
- If our current position is described by a, then the next step is distributed as aP.
- But a is the steady state, so a=aP.
- Solving this matrix equation gives us a.
 - So a is the (left) eigenvector for P.
 - (Corresponds to the "principal" eigenvector of P with the largest eigenvalue.)
 - Transition probability matrices always have largest eigenvalue 1.

One way of computing a

- Recall, regardless of where we start, we eventually reach the steady state a.
- Start with any distribution (say $\mathbf{x} = (1/n, 1/n, ..., 1/n)$).
- After one step, we're at xP;
- after two steps at xP^2 , then xP^3 and so on.
- "Eventually" means for "large" k, $\mathbf{xP}^k = \mathbf{a}$.
- Algorithm: multiply x by increasing powers of P until the product looks stable.

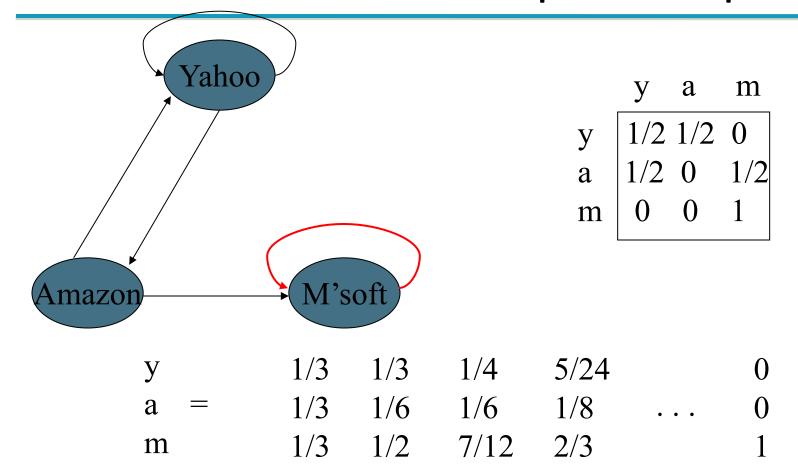
Power Iteration Example



Spider traps

- A group of pages is a spider trap if there are no links from within the group to outside the group
 - Random surfer gets trapped
- Spider traps violate the conditions needed for the random walk theorem

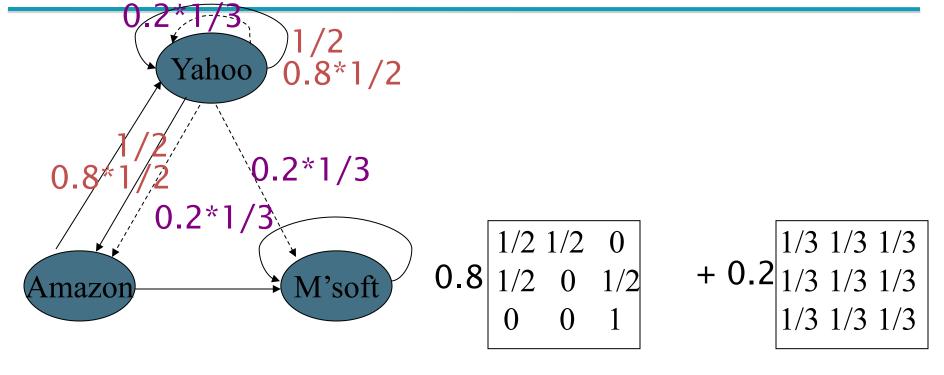
Microsoft becomes a spider trap



Random teleports

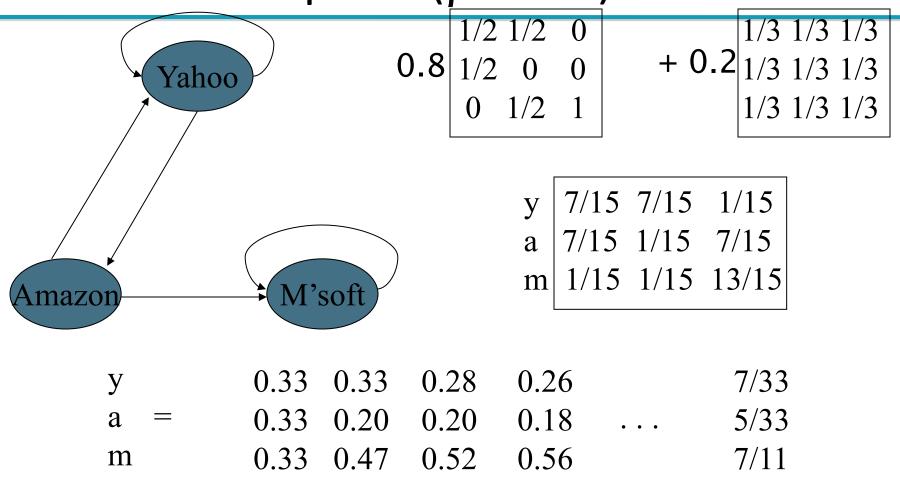
- The Google solution for spider traps
- At each time step, the random surfer has two options:
 - With probability β , follow a link at random
 - With probability 1- β , jump to some page uniformly at random
 - Common values for β are in the range 0.8 to 0.9
- Surfer will teleport out of spider trap within a few time steps

Random teleports ($\beta = 0.8$)



y 7/15 7/15 1/15 a 7/15 1/15 7/15 m 1/15 1/15 13/15

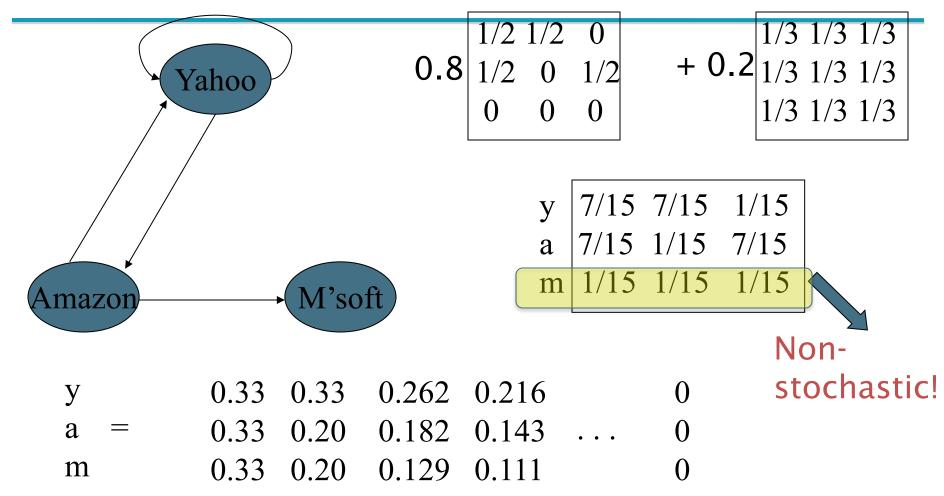
Random teleports ($\beta = 0.8$)



Dead ends

- Pages with no outlinks are "dead ends" for the random surfer
 - Nowhere to go on next step
- Especially common for Web Search Engines
 - URLs that have not yet been crawled

Microsoft becomes a dead end



Dealing with dead-ends

- Teleport
 - Follow random teleport links with probability 1.0 from dead-ends
 - Adjust matrix accordingly
 - How?
- (Suggested by Google) prune and propagate
 - Preprocess the graph to eliminate dead-ends
 - Might require multiple passes
 - Compute page rank on reduced graph
 - Approximate values for deadends by propagating values from reduced graph

Q: Why approximate values and why errors are insignificant?

Pagerank summary

- Preprocessing:
 - Given graph of links, build matrix P.
 - From it compute a.
 - **a** is the principle eigen vector of a matrix $\tilde{\mathbf{P}}$

$$\tilde{\mathbf{P}} = (1 - \beta)\mathbf{P} + \beta\mathbf{T}, \qquad \mathbf{T}_{i,j} = \frac{1}{n}$$

- The entry a_i is a number between 0 and 1: the pagerank of page i.
- Query processing:
 - Retrieve pages meeting query.
 - Rank them by their pagerank.
 - Order is query-independent.

The reality

- Pagerank is used in google, but is hardly the full story of ranking
 - Many sophisticated features are used
 - Some address specific query classes
 - Machine learned ranking (Lecture 15) heavily used
- Pagerank still very useful for things like crawl policy

Pagerank: Issues and Variants

- How realistic is the random surfer model?
 - (Does it matter?)
 - What if we modeled the back button?
 - Surfer behavior sharply skewed towards short paths
 - Search engines, bookmarks & directories make jumps nonrandom.
- Biased Surfer Models
 - Weight edge traversal probabilities based on match with topic/query (non-uniform edge selection)
 - Bias jumps to pages on topic (e.g., based on personal bookmarks & categories of interest)

Topic Specific Pagerank

- Goal pagerank values that depend on query topic
- Conceptually, we use a random surfer who teleports, with say 10% probability, using the following rule:

only randomly teleport to a subset of pages

- Selects a topic (say, one of the 16 top level ODP categories) based on a query & user -specific distribution over the categories
- Teleport to a page uniformly at random within the chosen topic
- Sounds hard to implement: can't compute PageRank at query time!

Topic Specific Pagerank

- Offline:Compute pagerank for individual topics
 - Query independent as before
 - Each page has multiple pagerank scores one for each ODP category, with teleportation only to that category
- Online: Query context classified into (distribution of weights over) topics
 - Generate a dynamic pagerank score for each page weighted sum of topicspecific pageranks

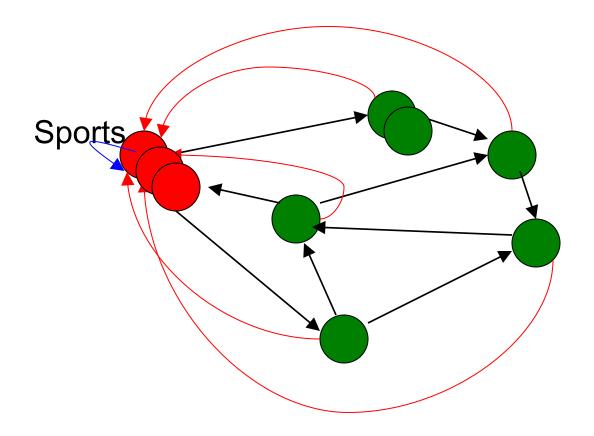
Influencing PageRank ("Personalization")

- Input:
 - Web graph W
 - Influence vector v over pages of a topic

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\mathbf{v}: (page \rightarrow degree of influence)
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- Output:
 - Rank vector \mathbf{r} : (page \rightarrow page importance wrt \mathbf{v})
- $\mathbf{r} = PR(W, \mathbf{v})$

Non-uniform Teleportation



Teleport with 10% probability to a Sports page

Interpretation of Composite Score

Given a set of personalization vectors {v_j}

$$PR(W, \sum_{j} [w_{j} \cdot \mathbf{v}_{j}]) = \sum_{j} [w_{j} \cdot PR(W, \mathbf{v}_{j})]$$

Given a user's preferences over topics, express as a combination of the "basis" vectors \mathbf{v}_i

PageRank as a Linear System [Jeh & Widom, KDD 2003] [Optional]

- Preference vectors u → specifies the random teleport probability distribution
 - A column vector of n dimensions (n: # of vertices in G)
 - sum up to 1.0
- Personalized pagerank vector v → steady-state distribution over the vertices in G
 - Also a column vector of n dimensions
- v is determined by u via a linear system

$$\mathbf{v} = (1 - \beta)\mathbf{P}^{\top}\mathbf{v} + \beta\mathbf{u}$$

Linearity of PageRank

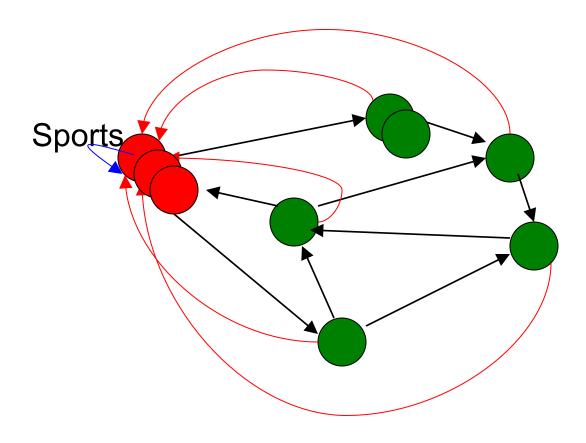
• For two preference vectors $\mathbf{u_1}$ and $\mathbf{u_2}$, let $\mathbf{v_1}$ and $\mathbf{v_2}$ be the corresponding personalized page rank vectors, then we can prove that

$$\lambda \mathbf{v}_1 + (1 - \lambda)\mathbf{v}_2 = (1 - \beta)\mathbf{P}^{\top}(\lambda \mathbf{v}_1 + (1 - \lambda)\mathbf{v}_2) + \beta(\lambda \mathbf{u}_1 + (1 - \lambda)\mathbf{u}_2)$$

Implication:

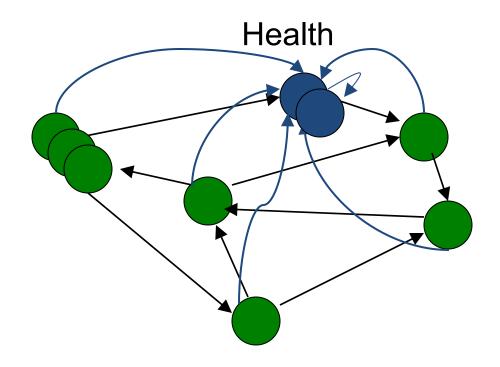
 Personalized pagerank vectors induced by a linear combination of preference vectors can be computed as the same linear combination of corresponding personalized pagerank vectors.

Interpretation



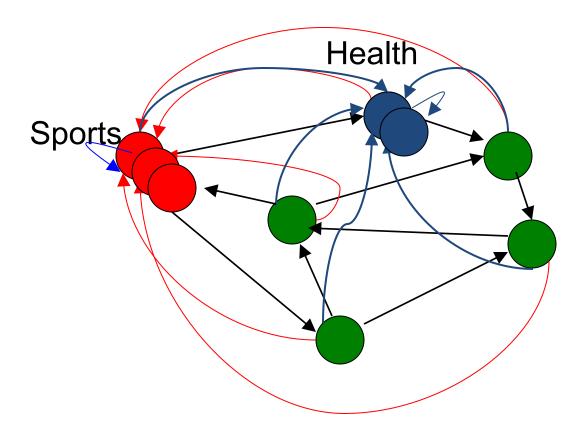
10% Sports teleportation

Interpretation



10% Health teleportation

Interpretation



 $pr = (0.9 PR_{sports} + 0.1 PR_{health})$ gives you: 9% sports teleportation, 1% health teleportation

Resources

- IIR Chap 21
- http://www2004.org/proceedings/docs/1p309.pdf
- http://www2004.org/proceedings/docs/1p595.pdf
- http://www2003.org/cdrom/papers/refereed/p270/ kamvar-270-xhtml/index.html
- http://www2003.org/cdrom/papers/refereed/p641/ xhtml/p641-mccurley.html
- Glen Jeh and Jennifer Widom: sScaling Personalized Web Search. KDD 2003.