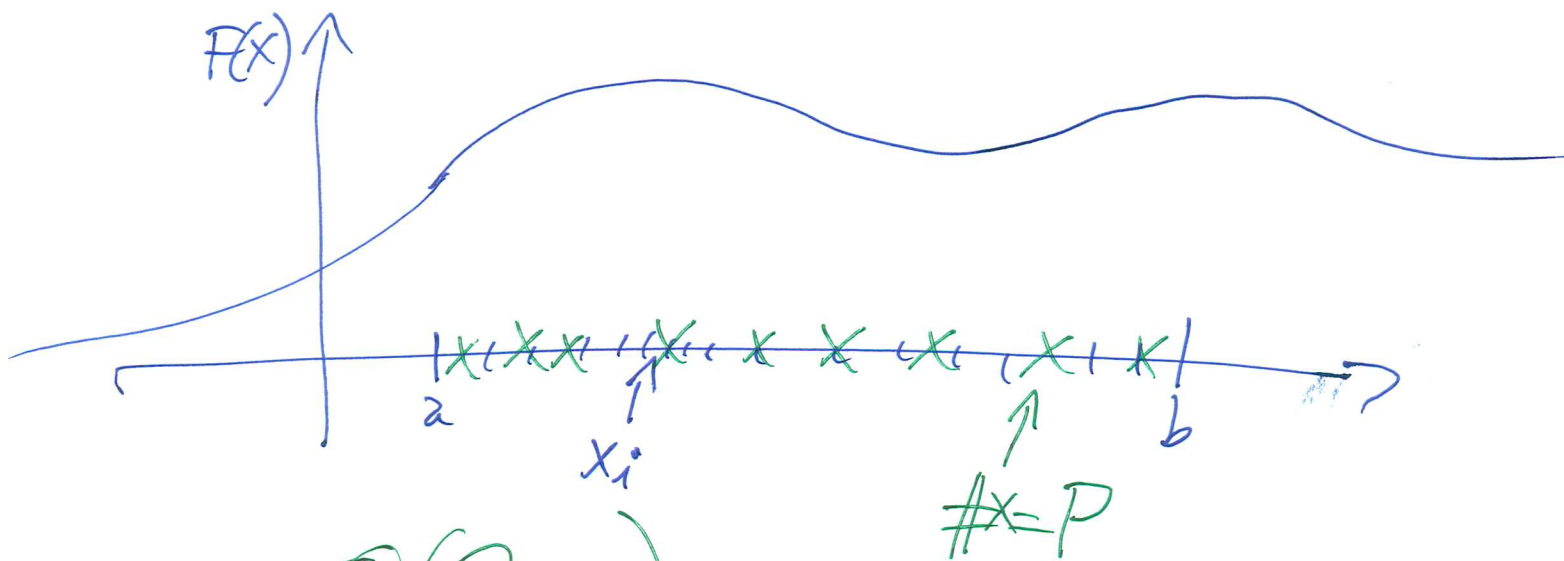
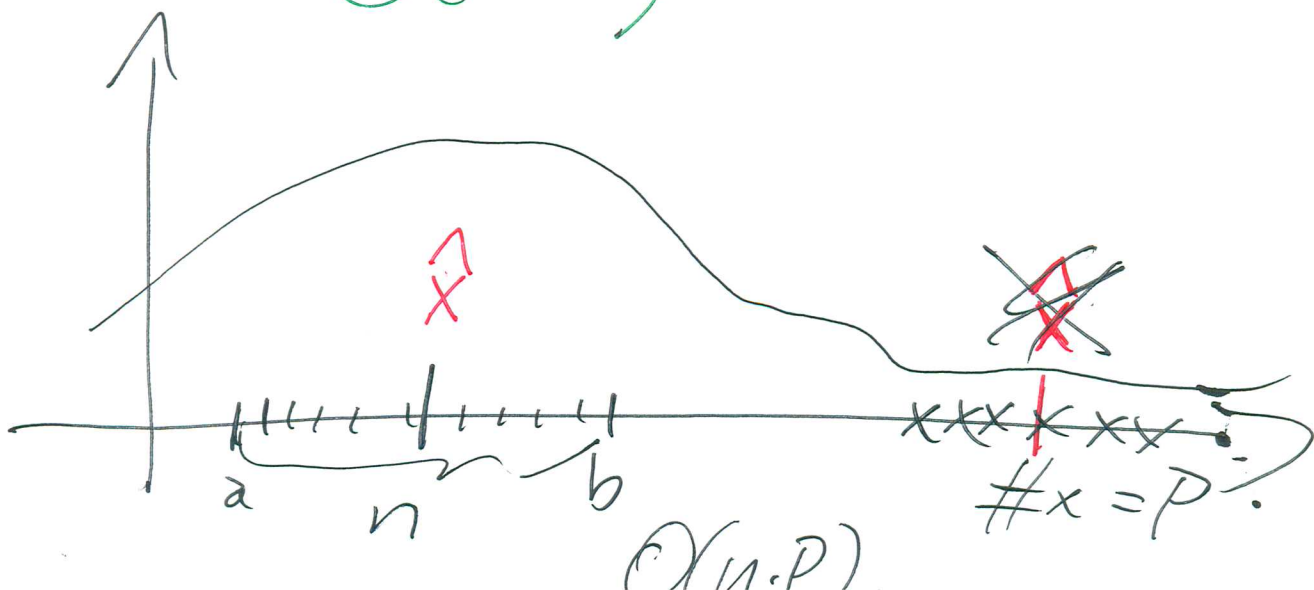


Hola Hola
 Hola

$$F(x) = \sum_{i=1}^n y_i \cdot \frac{\sin(x - x_i)}{x - x_i}$$



$$O(P \cdot n) \\ \rightarrow O(n^2)$$



(1)

$$F(x) = \sum_{i=1}^n y_i \cdot \frac{\sin(x - x_i)}{x - x_i}$$

$$\sin(x - x_i) = \sin(x) \cdot \cos(x_i) - \cos(x) \cdot \sin(x_i)$$

$$F(x) = \sum_{i=1}^n y_i \cdot \frac{(\sin(x) \cdot \cos(x_i) - \cos(x) \cdot \sin(x_i))}{x - x_i}$$

$$= \sin(x) \cdot \sum_{i=1}^n \frac{y_i \cdot \cos(x_i)}{x - x_i} - \cos(x) \cdot \sum_{i=1}^n \frac{y_i \cdot \sin(x_i)}{x - x_i}$$

$$\frac{1}{x - x_i} = \text{"Natalia"} = \frac{1}{x} \cdot \frac{1}{1 - \frac{x_i}{x}}$$

$$= \frac{1}{x} \cdot \sum_{j=0}^{\infty} \left(\frac{x_i}{x}\right)^j$$

$$\left| \frac{x_i}{x} \right| < 1$$

$$\frac{1}{x - \cancel{x} + \hat{x} - x_i} = \frac{1}{x - \hat{x}} \cdot \frac{1}{1 - \frac{x_i - \hat{x}}{x - \hat{x}}}$$

$$\frac{|x_i - \hat{x}|}{|x - \hat{x}|} < 1 \Leftrightarrow |x_i - \hat{x}| < |x - \hat{x}| \quad (\Sigma)$$

$$\frac{1}{\cancel{x} - x_i} = \frac{1}{x - \hat{x}} \cdot \frac{1}{1 - \frac{x_i - \hat{x}}{x - \hat{x}}}$$

$$= \frac{1}{x - \hat{x}} \cdot \sum_{j=0}^{\infty} \frac{(x_i - \hat{x})^j}{(x - \hat{x})^j}$$

$$= \sum_{j=0}^{\infty} \frac{(x_i - \hat{x})^j}{(x - \hat{x})^{j+1}}$$

$$F(x) = \sin(x) \cdot \sum_{i=1}^n \frac{y_i \cdot \cos(x_i)}{x - x_i} - \cos(x) \cdot \sum_{i=1}^n \frac{y_i \cdot \sin(x_i)}{x - x_i}$$

~~$\sin(x)$~~

$$\sum_{i=1}^n \frac{y_i \cdot \cos(x_i)}{x - x_i} = \sum_{i=1}^n y_i \cdot \cos(x_i) \cdot \frac{1}{x - x_i}$$

$$= \sum_{i=1}^n y_i \cdot \cos(x_i) \cdot \sum_{j=0}^{\infty} \frac{(x_i - \hat{x})^j}{(x - \hat{x})^{j+1}}$$

$$F(x) = \sin(x) \cdot \sum_{i=1}^n y_i \cdot \cos(x_i) \cdot \sum_{j=0}^{\infty} \frac{(x_i - \bar{x})^j}{(x - \bar{x})^{j+1}}$$

$$- \cos(x) \cdot \sum_{i=1}^n y_i \cdot \sin(x_i) \cdot \sum_{j=0}^{\infty} \frac{(x_i - \bar{x})^j}{(x - \bar{x})^{j+1}}$$

$$= \sin(x) \cdot \sum_{j=0}^{\infty} \frac{1}{(x - \bar{x})^{j+1}} \cdot \sum_{i=1}^n y_i \cdot \cos(x_i) \cdot (x_i - \bar{x})^j$$

$$- \cos(x) \cdot \sum_{j=0}^{\infty} \frac{1}{(x - \bar{x})^{j+1}} \cdot \sum_{i=1}^n y_i \cdot \sin(x_i) \cdot (x_i - \bar{x})^j$$

$$= \sin(x) \cdot \sum_{j=0}^{\infty} \frac{a_j}{(x - \bar{x})^{j+1}} - \cos(x) \cdot \sum_{j=0}^{\infty} \frac{b_j}{(x - \bar{x})^{j+1}}$$

$$\approx \sin(x) \sum_{j=0}^m \frac{a_j}{(x - \bar{x})^{j+1}} - \cos(x) \cdot \sum_{j=0}^m \frac{b_j}{(x - \bar{x})^{j+1}}$$

$$\textcircled{1} \quad O(n) + O(1)$$

$$O(n \cdot P)$$

$$\textcircled{P} \quad O(n) + O(P)$$